

10-418 / 10-618 Machine Learning for Structured Data

MACHINE LEARNING DEPARTMENT

Machine Learning Department School of Computer Science Carnegie Mellon University

Convolutional Neural Networks

Matt Gormley Lecture 16 Oct. 21, 2019

Reminders

- Homework 3: Structured SVM
 - Out: Tue, Oct. 18
 - Due: Mon, Nov. 4 at 11:59pm
- Midterm Exam Viewing
- Midsemester Grades

aka. Max-Margin Markov Networks (M³Ns)

STRUCTURED SVM

Structured Perceptron

Whiteboard

- Warmup: Binary SVM
- Warmup: Binary SVM Hinge Loss
- Structured Large Margin
- Structured Hinge Loss
- Gradient of Structured Hinge Loss
- SGD for Structured SVM
- Loss Augmented MAP Inference

Max vs "Soft-Max" Margin



SVMs:

$$\min_{\mathbf{w}} k ||\mathbf{w}||^2 - \sum_{i} \left(\mathbf{w}^{\top} \mathbf{f}_i(\mathbf{y}^i) - \max_{\mathbf{y}} \left(\mathbf{w}^{\top} \mathbf{f}_i(\mathbf{y}) + \ell_i(\mathbf{y}) \right) \right)$$

Hard (Penalized) Margin

Maxent:

$$\min_{\mathbf{w}} \ k||w||^2 - \sum_i \left(\mathbf{w}^\top \mathbf{f}_i(\mathbf{y}^i) - \log \sum_{\mathbf{y}} \exp \left(\mathbf{w}^\top \mathbf{f}_i(\mathbf{y}) \right) \right)$$
Soft Margin

- Very similar! Both try to make the true score better than a function of the other scores.
 - The SVM tries to beat the augmented runner-up
 - The maxent classifier tries to beat the "soft-max"

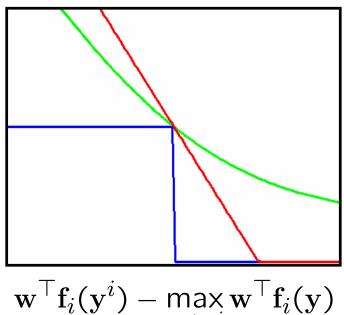
Hinge Loss



Consider the per-instance SVM objective:

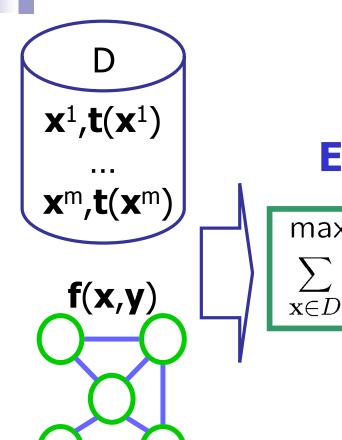
$$\min_{\mathbf{w}} k ||\mathbf{w}||^2 - \sum_{i} \left(\mathbf{w}^{\top} \mathbf{f}_i(\mathbf{y}^i) - \max_{\mathbf{y}} \left[\mathbf{w}^{\top} \mathbf{f}_i(\mathbf{y}) + \ell_i(\mathbf{y}) \right] \right)$$

- This is called the "hinge loss"
 - Upper bounds zero-one loss
 - Unlike maxent / log loss, you stop gaining objective once the true label wins by enough
 - You can start from here and derive the SVM objective



$$\mathbf{w}^{\top}\mathbf{f}_{i}(\mathbf{y}^{i}) - \max_{\mathbf{y} \neq \mathbf{y}^{i}} \mathbf{w}^{\top}\mathbf{f}_{i}(\mathbf{y})$$

Max (Conditional) Likelihood



Estimation

 $\begin{aligned} & \mathsf{maximize_w} \\ & \sum_{\mathbf{x} \in D} \mathsf{log}\, P_{\mathbf{w}}(\mathbf{t}(\mathbf{x}) \mid \mathbf{x}) \end{aligned}$

Classification

 $\mathsf{arg}\,\mathsf{max}_{\mathbf{y}}\mathbf{w}^{\top}\mathbf{f}(\mathbf{x},\mathbf{y})$

$$\log P_{\mathbf{w}}(\mathbf{y} \mid \mathbf{x}) = \mathbf{w}^{\top} \mathbf{f}(\mathbf{x}, \mathbf{y}) - \log Z_{\mathbf{w}}(\mathbf{x})$$

Don't need to learn entire distribution!

Structured SVM

The original name for Structured SVM:

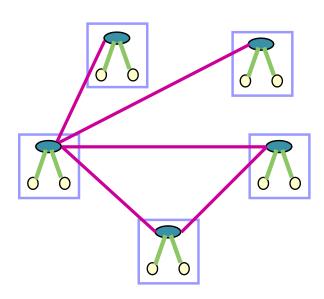
- Max-Margin Markov Networks
- abbreviated as M³Ns

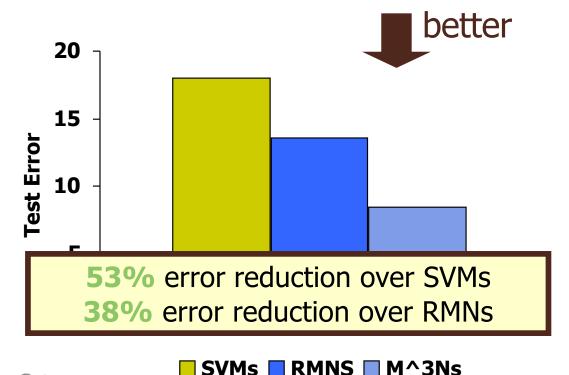
Results: Handwriting Recognition

quadratic cubic raw ror (average per-character) Length: ~8 chars 30 pixels kernel kernel Letter: 16x8 pixels 10-fold Train/Test 25 . better 5000/50000 letters 20 600/6000 words 15 Models: Multiclass-SVMs* **CRFs** 45% error reduction over linear CRFs M³ nets 33% error reduction over multiclass SVMs 0 + MC-SVMs **CRFs** M³ nets

Results: Hypertext Classification

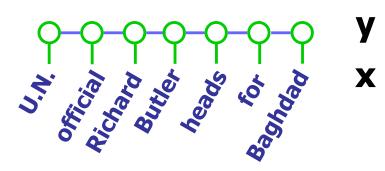
- WebKB dataset
 - Four CS department websites: 1300 pages/3500 links
 - Classify each page: faculty, course, student, project, other
 - Train on three universities/test on fourth
- Inference: loopy belief propagation
- Learning: relaxed dual





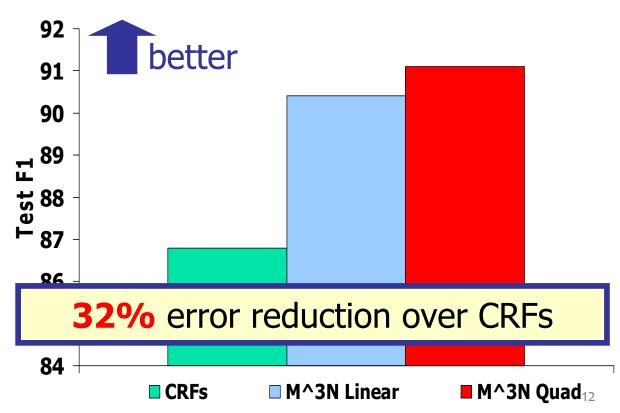
Named Entity Recognition

- Locate and classify named entities in sentences:
 - 4 categories: organization, person, location, misc.
 - e.g. "U.N. official Richard Butler heads for Baghdad".
- CoNLL 03 data set (200K words train, 50K words test)

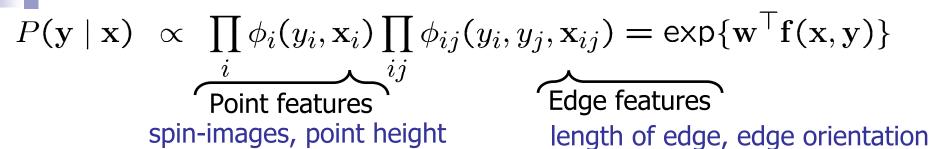


 $y_i = org/per/loc/misc/none$

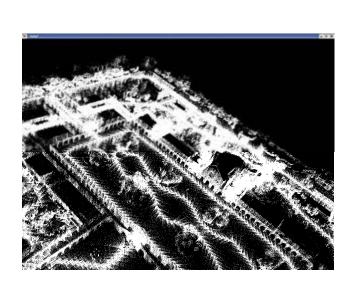
$$f(y_i, x) = [..., I(y_i = \text{org}, x_i = \text{``U.N.''}), I(y_i = \text{per}, x_i = \text{capitalized}), I(y_i = \text{loc}, x_i = \text{known city}), ...,]$$

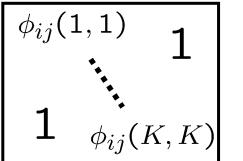


Associative Markov networks

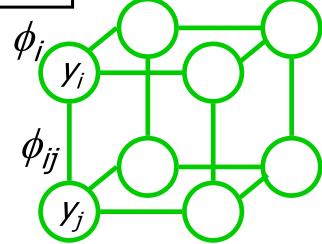


"associative" $\phi_{ij}(y_i, y_j) =$

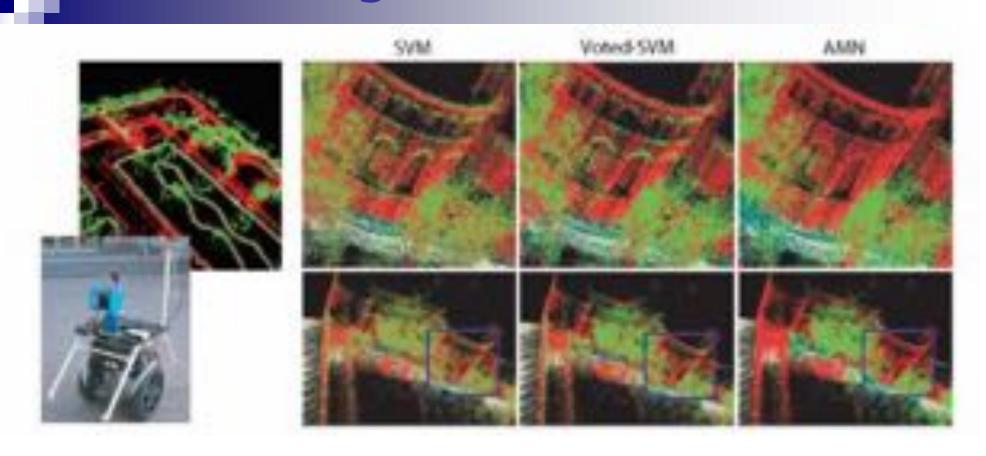








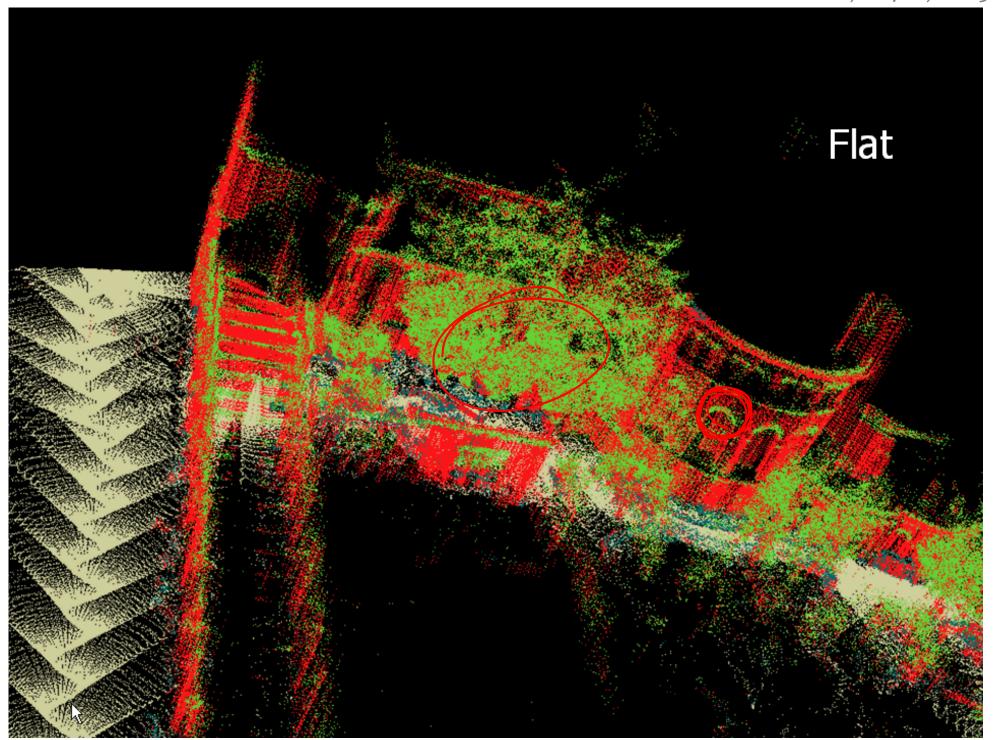
Max-margin AMNs results



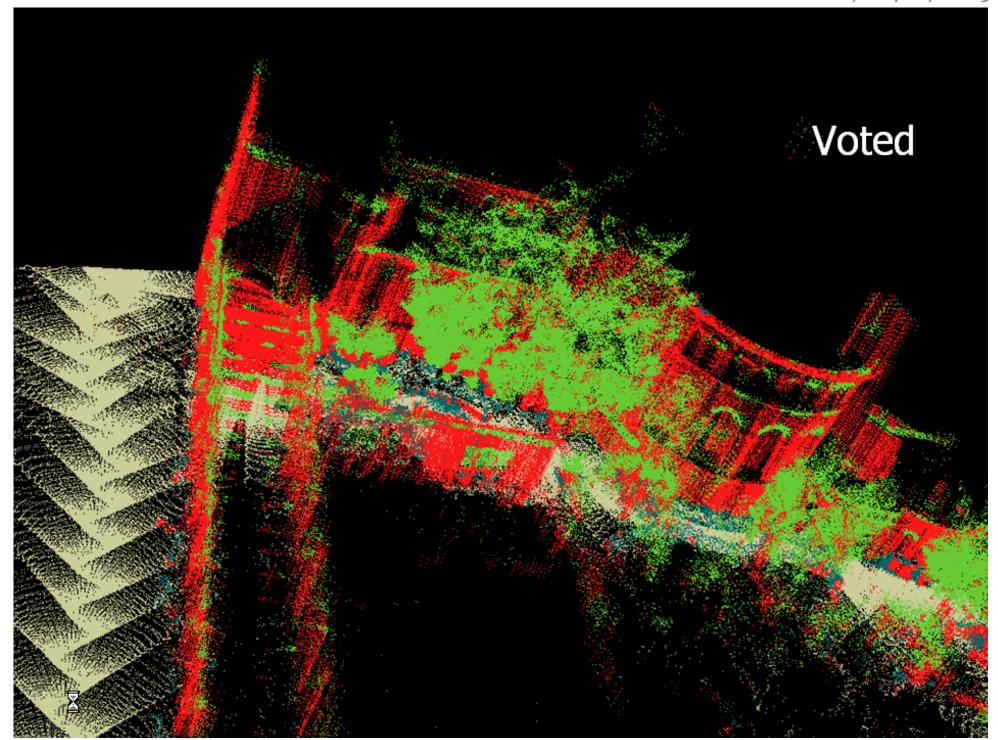
Label: ground, building, tree, shrub

Training: 30 thousand points Testing: 3 million points

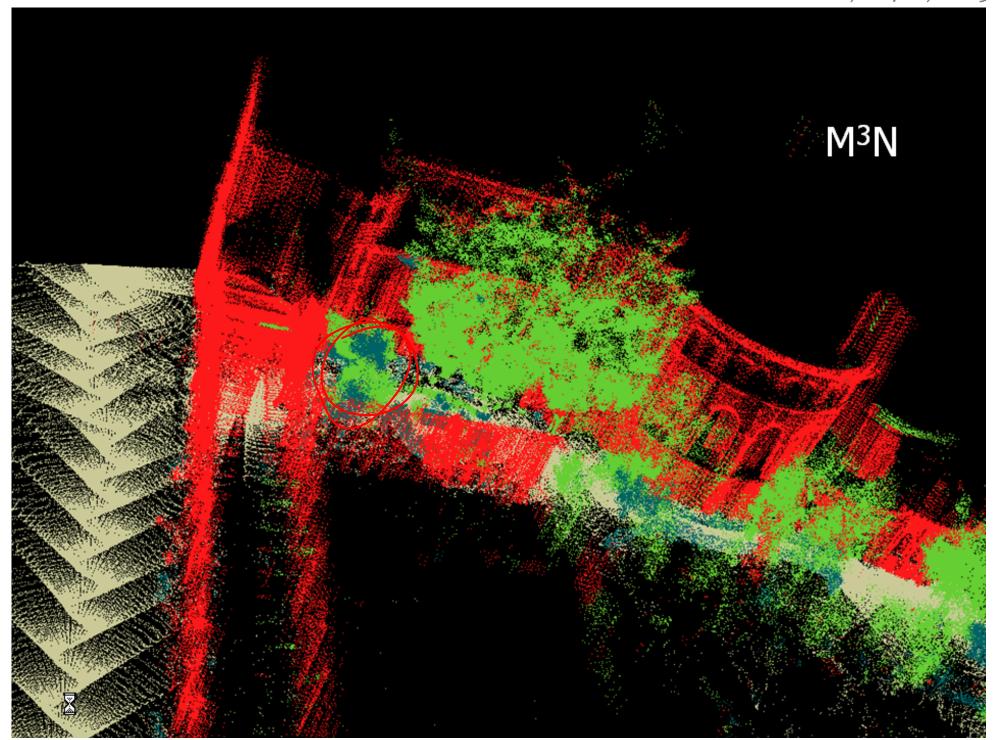
Slide from Guestrin, 10-701, 2005



Slide from Guestrin, 10-701, 2005



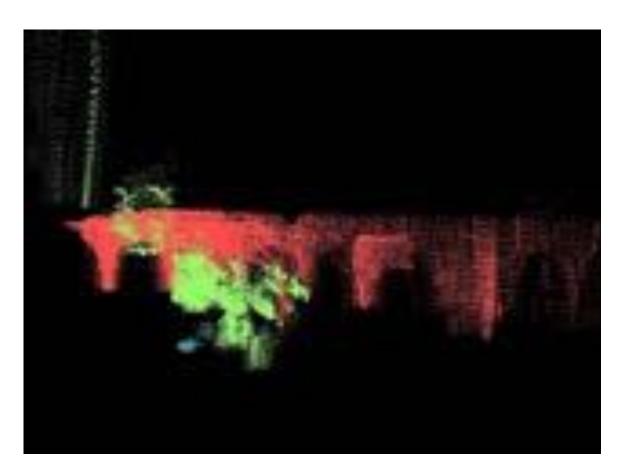
Slide from Guestrin, 10-701, 2005



Segmentation results

Hand labeled 180K test points

Model	Accuracy
SVM	68%
V-SVM	73%
M ³ N	93%



CNNs Outline

Background: Computer Vision

- Image Classification
- ILSVRC 2010 2016
- Traditional Feature Extraction Methods
- Convolution as Feature Extraction

Convolutional Neural Networks (CNNs)

- Learning Feature Abstractions
- Common CNN Layers:
 - Convolutional Layer
 - Max-Pooling Layer
 - Fully-connected Layer (w/tensor input)
 - Softmax Layer
 - ReLU Layer
- Background: Subgradient
- Architecture: LeNet
- Architecture: AlexNet
- Architecture: ResNet

Training a CNN

- SGD for CNNs
- Backpropagation for CNNs

BACKGROUND: COMPUTER VISION

Example: Image Classification

- ImageNet LSVRC-2011 contest:
 - Dataset: 1.2 million labeled images, 1000 classes
 - Task: Given a new image, label it with the correct class
 - Multiclass classification problem
- Examples from http://image-net.org/

THE RESERVE AND ADDRESS OF THE PARTY NAMED IN

and fundation resided as usings





Abertio	ment against the continues of the continues of the detect of
11 000	print, here party, so pint, so print (1)
1.000	ge (1)
- bund	No.
0.000	in protein years (1)
more I	ATT.
pond	er (II)
Sealer	70
1000	(0)
1 phorse	BH ERREY!
1 - W	KORK, Universities, unarioral (b)
1.00	Patrollerisks (71)
	NAMES OF THE PARTY
	Patricul, Prentration (1798)
	ME (87)
	Shouldest Motor and Ampliest May and It!
	and (T)
	56-33
	-typine (II)
	ngelikt(t)
	test of preside (5)
	Some fit
	Attended you architecture. Architecture introduction
	Mark (I)
	BAYL TAKKETS (II)
	entreering (ID)
	rame, sons sen. Representate (16)
	Committee, committee from Spring Spring (SS)

deal of grey, region, representative (46)



SHOW MARKET A LABOR TRAVELLE

German inis, Iris kochii

the of northern tray having less bloc purple foreign protein to tail smaller than the permantial







Complete Co. banders (M) DAYS (SI Cultivative by best (SC) MMP (54) promptor, exergence alone (2) distributed places (TE other (CTV) STREET THE - secondly priest, Spreams priest (1888) (aniuhyre 10) desirt plant, samplique, samplique plant, sampliée, sampliée innergity by temporary of print (ST Marks plan, sizer plan, furnishing huttighors (last [11] Total Our plant (TD) bullmar joint (175) 1 allegations alone (CT) FE. Say, Start St. St., Mark T. St., L'1911 1. Secretary via (4): Foreston etc. orin, tip germatica foreston, tro Services in personal filt. Commercial and house the Salmariam Ph., Wo. Judicip. (III) SHOP SHARE YELD AND Indiana ne (C) BASE WELLIS STREET, CO. stretching tries, affektion, alphabet cries, solvening affekting Person Inc. he person (in) unition into patient larg, purpose notice flag, int proach

depart one, commel you are contracted.

Mod Tell, the representati (III)









the hand in the course of

Court, courtyard

An exact whethy or parity increased to early or business. "The forces was last properly an inner count"

165

52.614 200000



States a heavy the sales of sales a state of

4 Imagetes 2011 Rel tension (SESE):

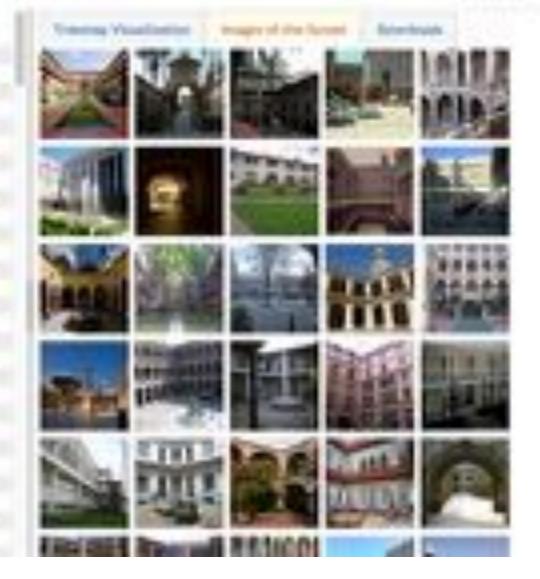
- pract, form, pract the LANSES
- geological formation, formation (175)
- HARMAN BURN (7.51E)
- I work where stills.
- within, whose cratery
- removements representation (3484)
 - printing contrictor (140%)
 - I strack harger, report shed (2)
 - after (10)
 - grounds, policylarity (7.5
 - 448 DEL

3-mm-(546)

- Andre 1773
- sultreture (C)
 - brouger date (f)
- MATERIAL
- front/od any linearlest rest: (C)
- Sulpan (1)
- sharped, sprohypry, leaves (5)
- Week (95)
- pomer, more (II)

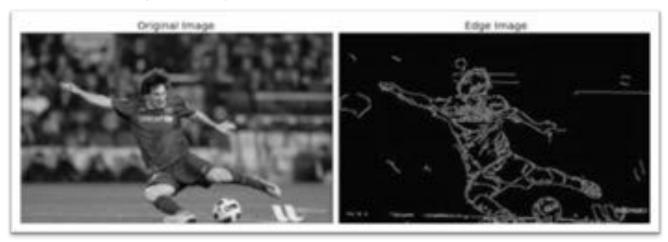
MAY, IMPROPERTY.

- photo-
- B080-31
- preser (2)
- 3: Sold Mark (Cit)
- THROAT ID-
- married RES

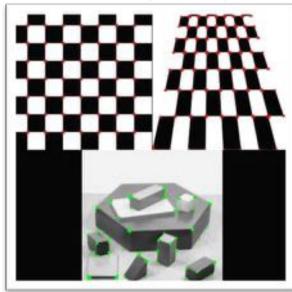


Feature Engineering for CV

Edge detection (Canny)

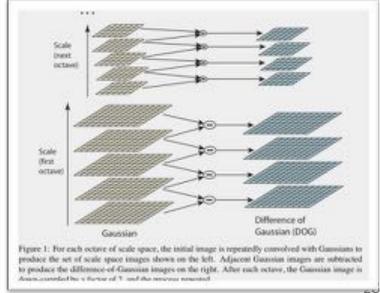


Corner Detection (Harris)



Scale Invariant Feature Transform (SIFT)





Figures from http://opencv.org

Figure from Lowe (1999) and Lowe (2004)

Example: Image Classification

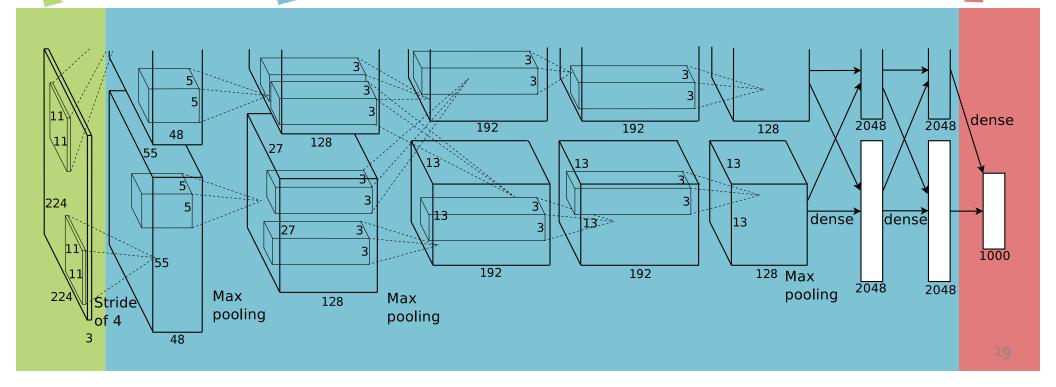
CNN for Image Classification

(Krizhevsky, Sutskever & Hinton, 2012) 15.3% error on ImageNet LSVRC-2012 contest

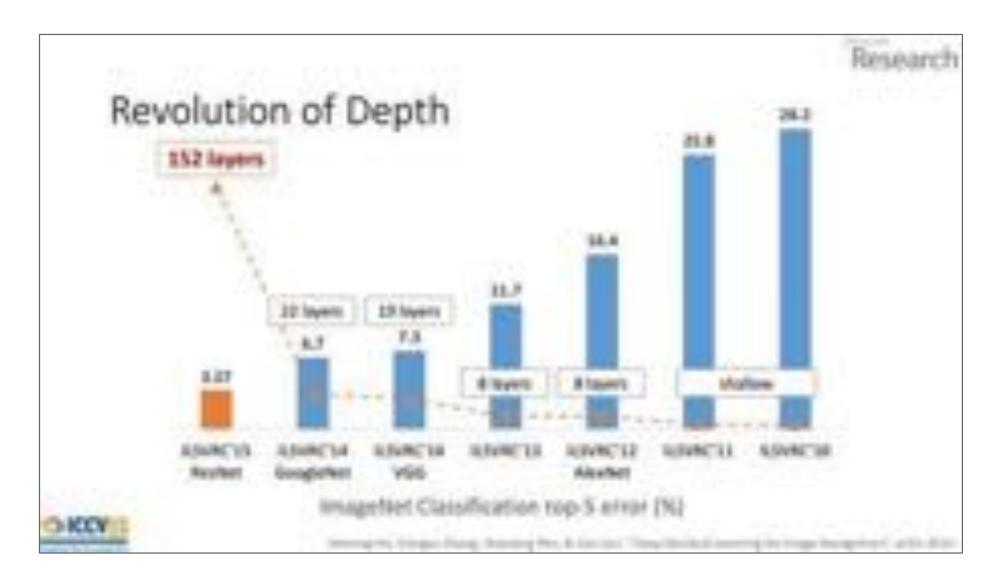
Input image (pixels)

- Five convolutional layers (w/max-pooling)
- Three fully connected layers

1000-way softmax



CNNs for Image Recognition



CONVOLUTION

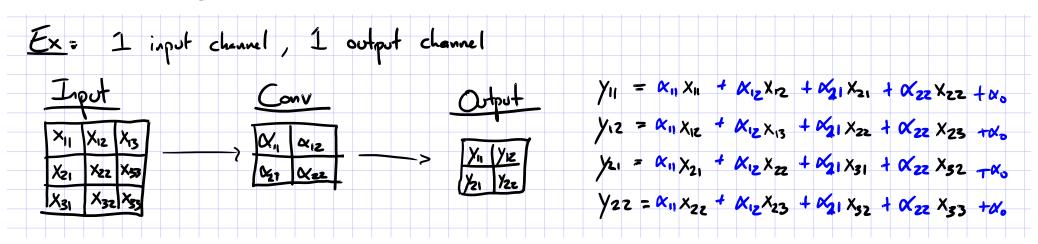
What's a convolution?

Basic idea:

- Pick a 3x3 matrix F of weights
- Slide this over an image and compute the "inner product" (similarity) of F and the corresponding field of the image, and replace the pixel in the center of the field with the output of the inner product operation

Key point:

- Different convolutions extract different types of low-level "features" from an image
- All that we need to vary to generate these different features is the weights of F



A **convolution matrix** is used in image processing for tasks such as edge detection, blurring, sharpening, etc.

Input Image

0	0	0	0	0	0	0
0	1	1	1	1	1	0
0	1	0	0	1	0	0
0	1	0	1	0	0	0
0	1	1	0	0	0	0
0	1	0	0	0	0	0
0	0	0	0	0	0	0

Convolution

0	0	0
0	1	1
О	1	0

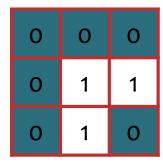
1	1	1	1	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	0	0	0	0

A **convolution matrix** is used in image processing for tasks such as edge detection, blurring, sharpening, etc.

Input Image

0	0	0	0	0	0	0
0	1	1	1	1	1	0
0	1	0	0	1	0	0
0	1	0	1	0	0	0
0	1	1	0	0	0	0
0	1	0	0	0	0	0
0	0	0	0	0	0	0



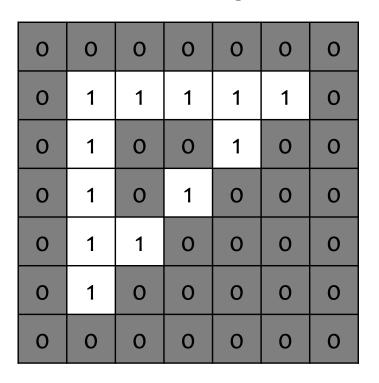


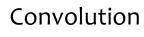
Convolved Image

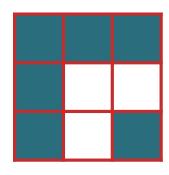
3	2	2	3	1
2	0	2	1	0
2	2	1	0	0
3	1	0	0	0
1	0	0	0	0

A **convolution matrix** is used in image processing for tasks such as edge detection, blurring, sharpening, etc.

Input Image



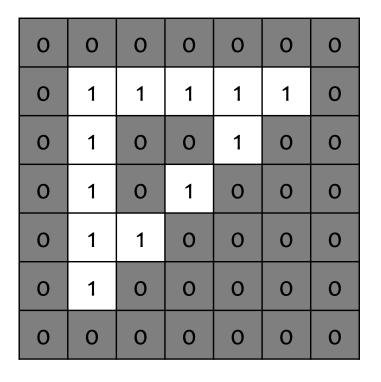




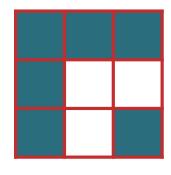
3	2	2	3	1
2	0	2	1	0
2	2	1	0	0
3	1	0	0	0
1	0	0	0	0

A **convolution matrix** is used in image processing for tasks such as edge detection, blurring, sharpening, etc.

Input Image



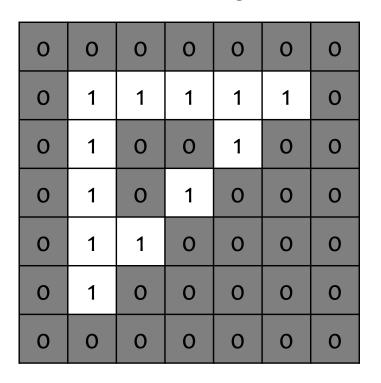




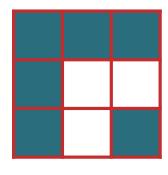
3	2	2	3	1
2	0	2	1	0
2	2	1	0	0
3	1	0	0	0
1	0	0	0	0

A **convolution matrix** is used in image processing for tasks such as edge detection, blurring, sharpening, etc.

Input Image



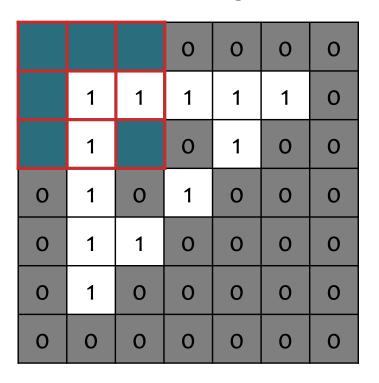


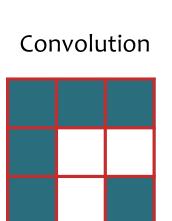


3	2	2	3	1
2	0	2	1	0
2	2	1	0	0
3	1	0	0	0
1	0	0	0	0

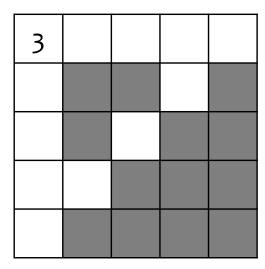
A **convolution matrix** is used in image processing for tasks such as edge detection, blurring, sharpening, etc.

Input Image



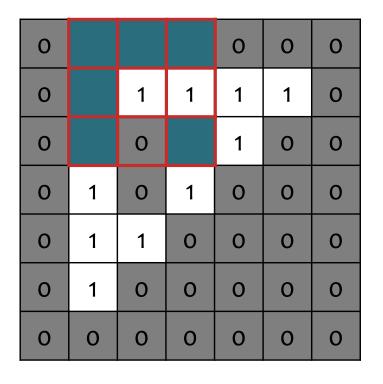




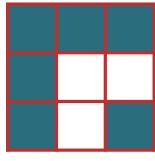


A **convolution matrix** is used in image processing for tasks such as edge detection, blurring, sharpening, etc.

Input Image





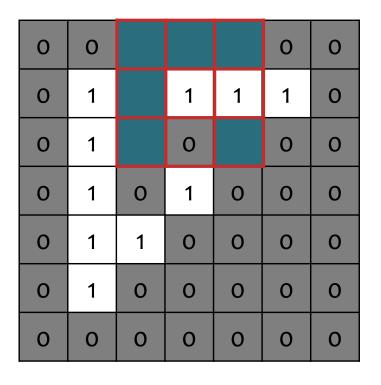


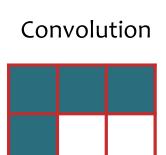
Convolved Image

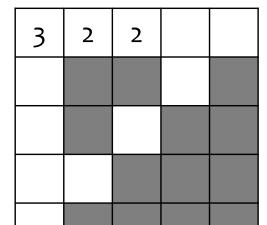
3	2		

A **convolution matrix** is used in image processing for tasks such as edge detection, blurring, sharpening, etc.

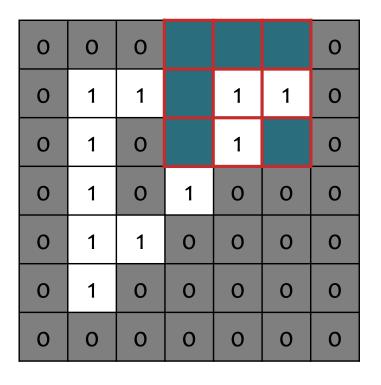
Input Image

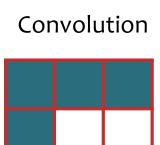




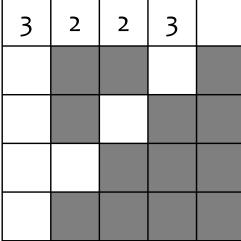


Input Image

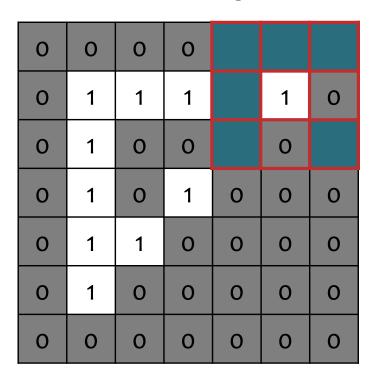


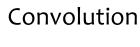


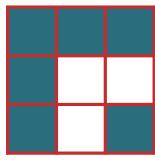
Convolved Image



Input Image



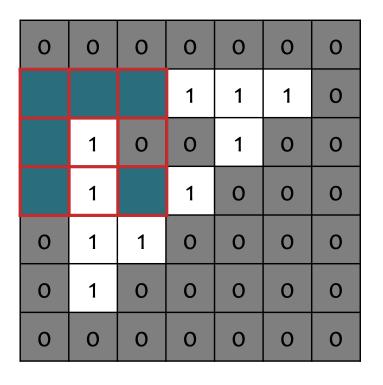




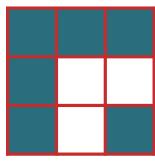
Convolved Image

3	2	2	3	1

Input Image



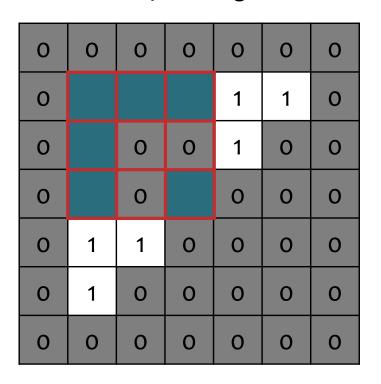




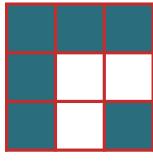
Convolved Image

3	2	2	3	1
2				

Input Image





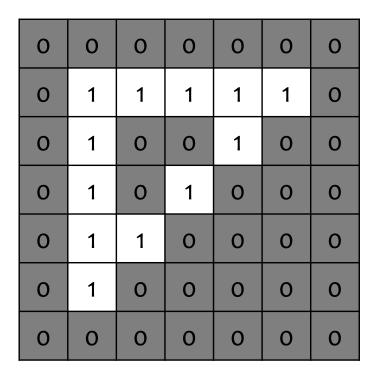


Convolved Image

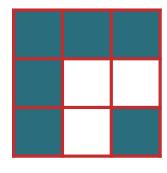
3	2	2	3	1
2	0			

A **convolution matrix** is used in image processing for tasks such as edge detection, blurring, sharpening, etc.

Input Image







3	2	2	3	1
2	0	2	1	0
2	2	1	0	0
3	1	0	0	0
1	0	0	0	0

Input Image

0	0	0	0	0	0	0
0	1	1	1	1	1	0
О	1	0	0	1	0	0
О	1	0	1	0	0	0
O	1	1	0	0	0	0
O	1	0	0	0	0	0
0	0	0	0	0	0	0

Identity Convolution

0	0	0
О	1	0
0	0	0

Convolved Image

1	1	1	1	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	0	0	0	0

A **convolution matrix** is used in image processing for tasks such as edge detection, blurring, sharpening, etc.

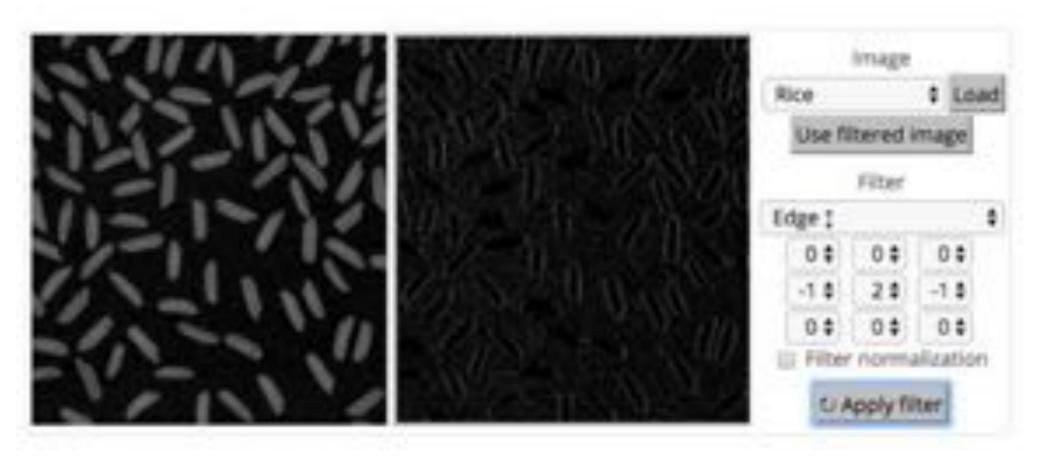
Input Image

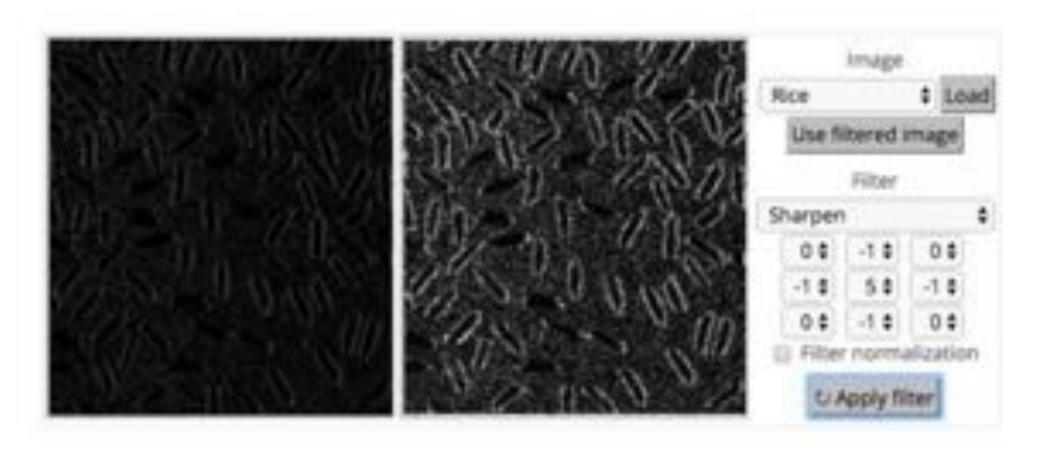
0	0	0	0	0	0	0
0	1	1	1	1	1	0
0	1	0	0	1	0	0
0	1	0	1	0	0	0
0	1	1	0	0	0	0
0	1	0	0	0	0	0
0	0	0	0	0	0	0

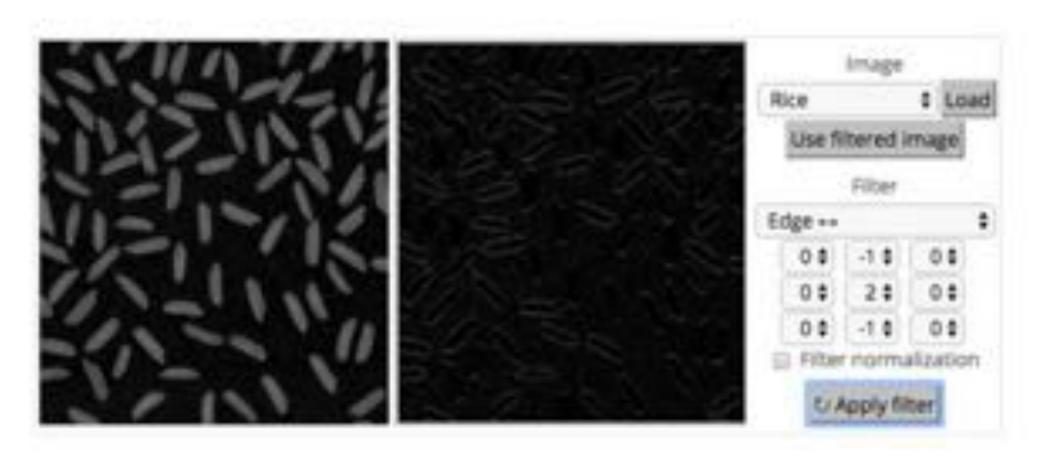
Blurring Convolution

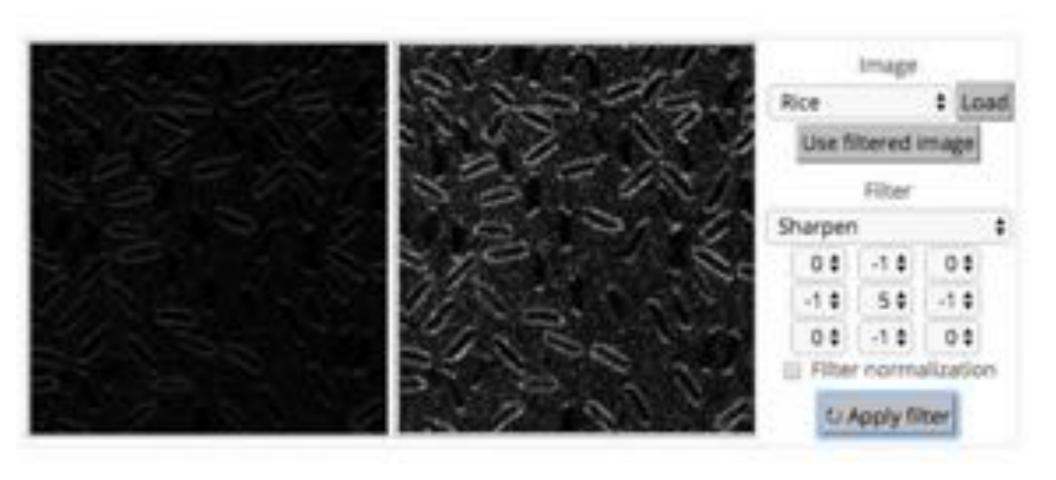
.1	.1	.1
.1	.2	.1
.1	.1	.1

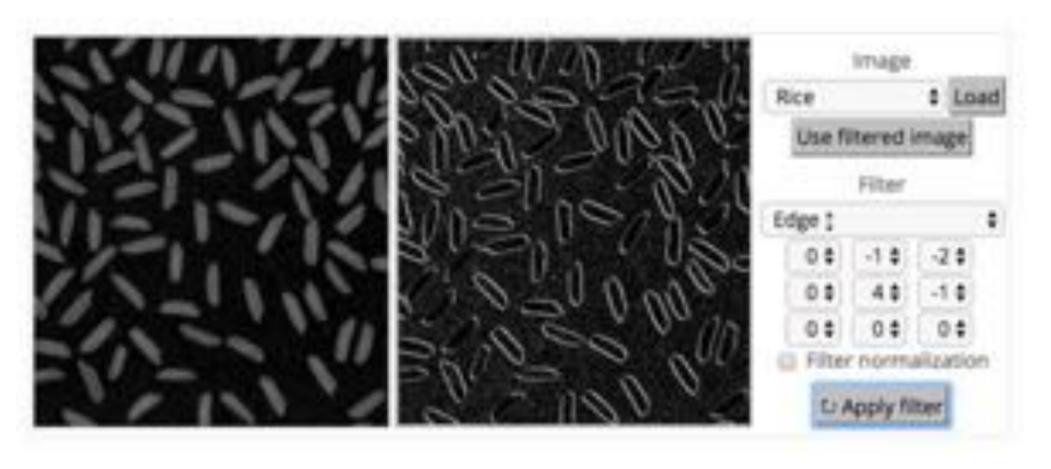
.4	.5	.5	.5	.4
.4	.2	•3	.6	.3
•5	.4	•4	.2	.1
.5	.6	.2	.1	0
.4	.3	.1	0	0

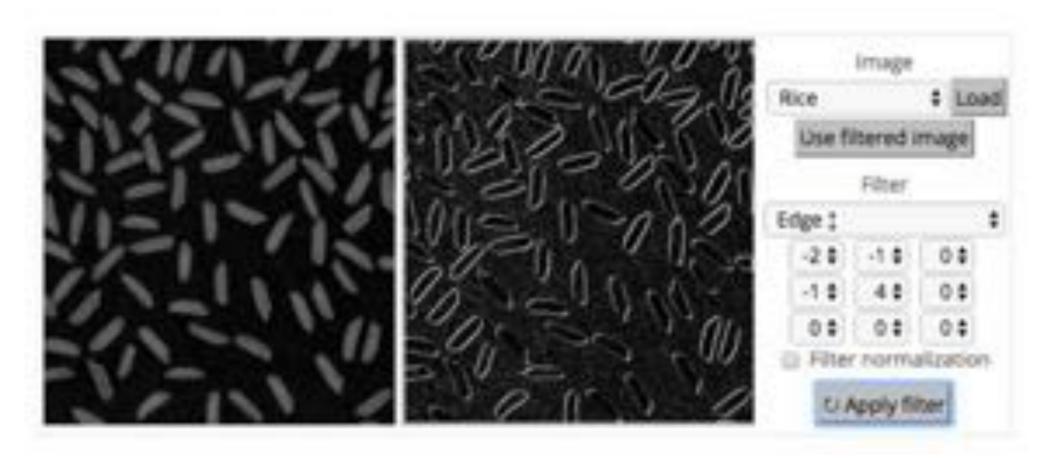










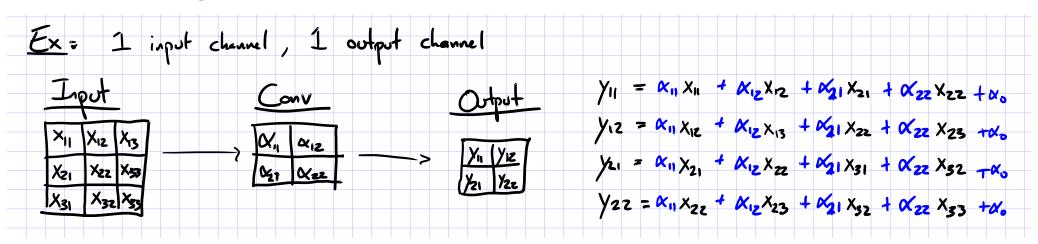


Basic idea:

- Pick a 3x3 matrix F of weights
- Slide this over an image and compute the "inner product" (similarity) of F and the corresponding field of the image, and replace the pixel in the center of the field with the output of the inner product operation

Key point:

- Different convolutions extract different types of low-level "features" from an image
- All that we need to vary to generate these different features is the weights of F

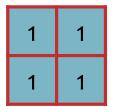


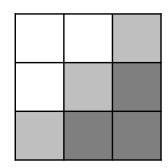
- Suppose we use a convolution with stride 2
- Only 9 patches visited in input, so only 9 pixels in output

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution



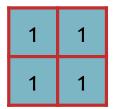


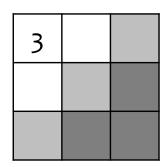
- Suppose we use a convolution with stride 2
- Only 9 patches visited in input, so only 9 pixels in output

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution



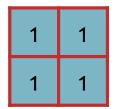


- Suppose we use a convolution with stride 2
- Only 9 patches visited in input, so only 9 pixels in output

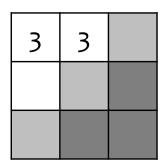
Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution



Convolved Image

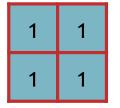


- Suppose we use a convolution with stride 2
- Only 9 patches visited in input, so only 9 pixels in output

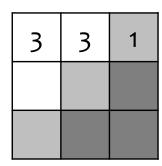
Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution



Convolved Image

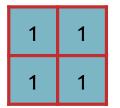


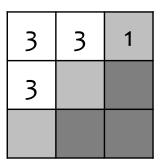
- Suppose we use a convolution with stride 2
- Only 9 patches visited in input, so only 9 pixels in output

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution



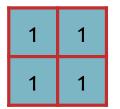


- Suppose we use a convolution with stride 2
- Only 9 patches visited in input, so only 9 pixels in output

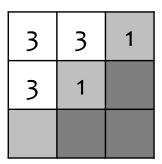
Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution



Convolved Image

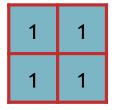


- Suppose we use a convolution with stride 2
- Only 9 patches visited in input, so only 9 pixels in output

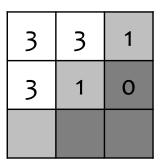
Input Image

1	1	1	1	1	0
1	0	0	1	0	О
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution



Convolved Image

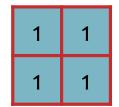


- Suppose we use a convolution with stride 2
- Only 9 patches visited in input, so only 9 pixels in output

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution



Convolved Image

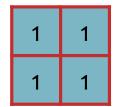
3	3	1
3	1	0
1		

- Suppose we use a convolution with stride 2
- Only 9 patches visited in input, so only 9 pixels in output

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution



Convolved Image

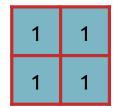
3	3	1
3	1	0
1	0	

- Suppose we use a convolution with stride 2
- Only 9 patches visited in input, so only 9 pixels in output

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution



3	3	1
3	1	0
1	0	0

CONVOLUTIONAL NEURAL NETS

A Recipe for Machine Learning

1. Given training data:

$$\{oldsymbol{x}_i, oldsymbol{y}_i\}_{i=1}^N$$

2. Choose each of these:

Decision function

$$\hat{\boldsymbol{y}} = f_{\boldsymbol{\theta}}(\boldsymbol{x}_i)$$

Loss function

$$\ell(\hat{m{y}},m{y}_i)\in\mathbb{R}$$

3. Define goal:

$$oldsymbol{ heta}^* = rg\min_{oldsymbol{ heta}} \sum_{i=1}^N \ell(f_{oldsymbol{ heta}}(oldsymbol{x}_i), oldsymbol{y}_i)$$

4. Train with SGD:

(take small steps opposite the gradient)

$$\boldsymbol{\theta}^{(t+1)} = \boldsymbol{\theta}^{(t)} - \eta_t \nabla \ell(f_{\boldsymbol{\theta}}(\boldsymbol{x}_i), \boldsymbol{y}_i)$$

A Recipe for Machine Learning

- Convolutional Neural Networks (CNNs) provide another form of decision function
 - Let's see what they look like...

 y_i

2. choose each of these:

Decision function

$$\hat{\boldsymbol{y}} = f_{\boldsymbol{\theta}}(\boldsymbol{x}_i)$$

Loss function

$$\ell(\hat{m{y}},m{y}_i)\in\mathbb{R}$$

Train with SGD:

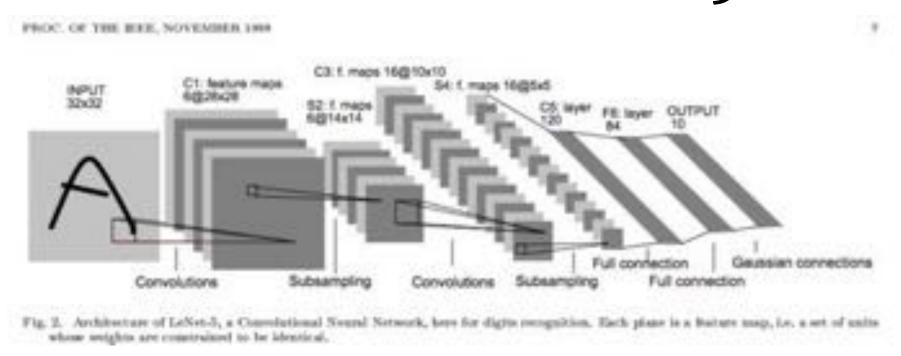
ke small steps
opposite the gradient)

$$oldsymbol{ heta}^{(t+1)} = oldsymbol{ heta}^{(t)} - \eta_t
abla \ell(f_{oldsymbol{ heta}}(oldsymbol{x}_i), oldsymbol{y}_i)$$

Convolutional Neural Network (CNN)

- Typical layers include:
 - Convolutional layer
 - Max-pooling layer
 - Fully-connected (Linear) layer
 - ReLU layer (or some other nonlinear activation function)
 - Softmax
- These can be arranged into arbitrarily deep topologies

Architecture #1: LeNet-5



Convolutional Layer

CNN key idea:

Treat convolution matrix as parameters and learn them!

Input Image

0	0	0	0	0	0	0
0	1	1	1	1	1	0
0	1	0	0	1	0	0
0	1	0	1	0	0	0
0	1	1	0	0	0	0
0	1	0	0	0	0	0
0	0	0	0	0	0	0



Learned Convolution

θ ₁₁	θ_{12}	θ_{13}
θ_{21}	θ_{22}	θ_{23}
θ_{31}	θ_{32}	θ_{33}

.4	•5	•5	•5	.4
.4	.2	.3	.6	.3
.5	•4	•4	.2	.1
•5	.6	.2	.1	0
.4	.3	.1	0	0

Downsampling by Averaging

- Downsampling by averaging used to be a common approach
- This is a special case of convolution where the weights are fixed to a uniform distribution
- The example below uses a stride of 2

Input Image

1	1	1	1	1	0
1	0	0	1	0	0
1	0	1	0	0	0
1	1	0	0	0	0
1	0	0	0	0	0
0	0	0	0	0	0

Convolution

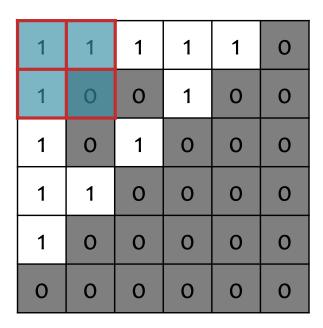
1/4	1/4
1/4	1/4

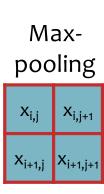
3/4	3/4	1/4
3/4	1/4	0
1/4	0	0

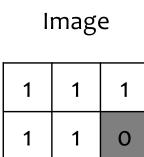
Max-Pooling

- Max-pooling is another (common) form of downsampling
- Instead of averaging, we take the max value within the same range as the equivalently-sized convolution
- The example below uses a stride of 2

Input Image







0

0

1

Max-Pooled

$$y_{ij} = \max(x_{ij}, x_{i,j+1}, x_{i+1,j}, x_{i+1,j+1})$$

TRAINING CNNS

A Recipe for Background Machine Learning

1. Given training data:

$$\{oldsymbol{x}_i, oldsymbol{y}_i\}_{i=1}^N$$

2. Choose each of these:

Decision function

$$\hat{\boldsymbol{y}} = f_{\boldsymbol{\theta}}(\boldsymbol{x}_i)$$

Loss function

$$\ell(\hat{m{y}},m{y}_i)\in\mathbb{R}$$

3. Define goal:

$$oldsymbol{ heta}^* = rg\min_{oldsymbol{ heta}} \sum_{i=1}^N \ell(f_{oldsymbol{ heta}}(oldsymbol{x}_i), oldsymbol{y}_i)$$

4. Train with SGD:

(take small steps opposite the gradient)

$$\boldsymbol{\theta}^{(t+1)} = \boldsymbol{\theta}^{(t)} - \eta_t \nabla \ell(f_{\boldsymbol{\theta}}(\boldsymbol{x}_i), \boldsymbol{y}_i)$$

A Recipe for Background Machine Learning

1. Given training data:

$$\{oldsymbol{x}_i, oldsymbol{y}_i\}_{i=1}^N$$

- 2. Choose each of the
 - Decision function

$$\hat{\boldsymbol{y}} = f_{\boldsymbol{\theta}}(\boldsymbol{x}_i)$$

Loss function

$$\ell(\hat{m{y}}, m{y}_i) \in \mathbb{R}$$

3. Define goal:

- $\{\boldsymbol{x}_i,\boldsymbol{y}_i\}_{i=1}^N$ Q: Now that we have the CNN as a decision function, how do we compute the gradient?
 - A: Backpropagation of course!

opposite the gradient)
$$oldsymbol{ heta}^{(t)} - \eta_t
abla \ell(f_{oldsymbol{ heta}}(oldsymbol{x}_i), oldsymbol{y}_i)$$

SGD for CNNs

[SGT] for CNN's]

Ex: Architecture: Given
$$\vec{x}$$
, \vec{y} *

$$J = l(y, y^{*})$$

$$y = \text{softmax}(z^{(5)}) \quad \text{Parameters } \vec{\Theta} = [\times , \beta, W]$$

$$z^{(5)} = l_{\text{new}}(z^{(4)}, W)$$

$$z^{(4)} = \text{rel}_{V}(z^{(3)}) \quad \text{SGD}:$$

$$z^{(3)} = (\text{conv}(z^{(2)}, \beta)) \quad \text{DIn't } \vec{\Theta}$$

$$z^{(2)} = (\text{conv}(z^{(2)}, \beta)) \quad \text{DIn't } \vec{\Theta}$$

$$z^{(2)} = \text{max-pool}(z^{(1)}) \quad \text{Supple } i \in \{1, ..., N\}$$

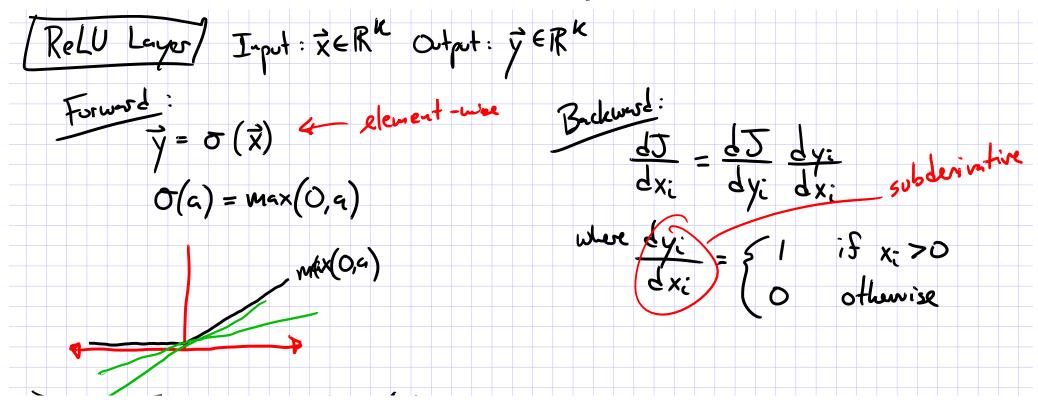
$$z^{(1)} = \text{conv}(\vec{x}, \infty) \quad \text{Torwad}: y = h_{\Theta}(\vec{x}^{(1)}), J_{I}(\Theta) = l(y, y^{*})$$

$$Backward: \vec{V}_{\Theta}J_{I}(\Theta) = ...$$

$$V_{Plake: \vec{\Theta}} = \vec{\Theta} - \vec{N}_{\Theta}J_{I}(\Theta)$$

LAYERS OF A CNN

ReLU Layer



Softmax Layer

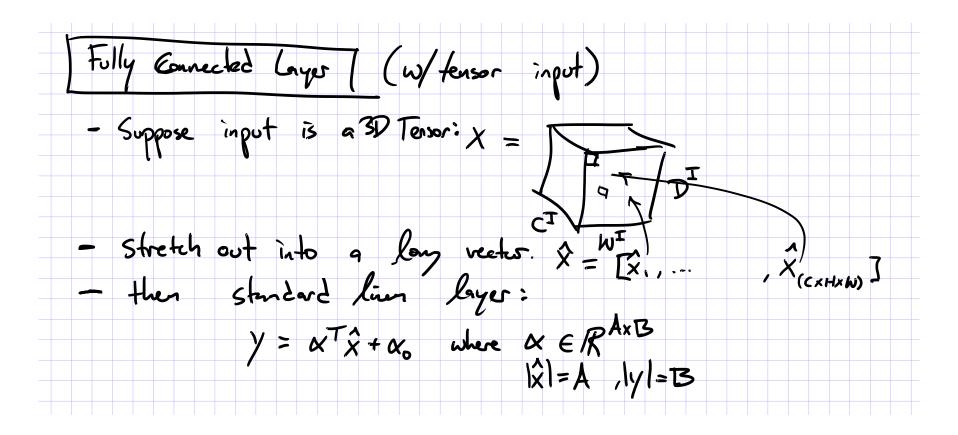
Softmax Layer

Input:
$$\vec{x} \in \mathbb{R}^{K}$$
 Output: $\vec{y} \in \mathbb{R}^{K}$

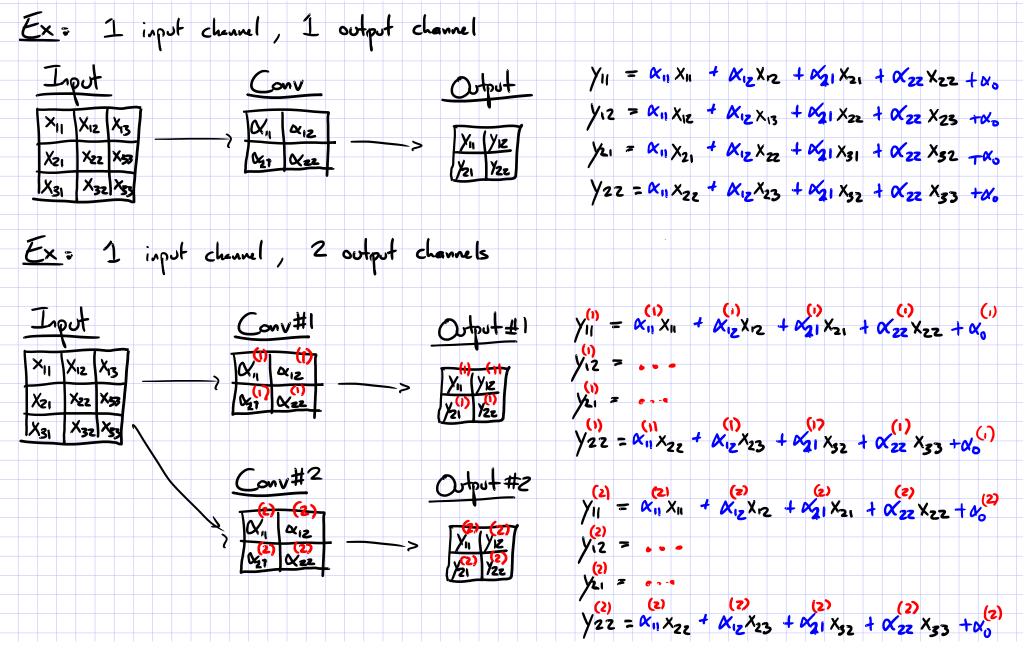
Forward:

 $y_i = \exp(x_i)$
 $X \in \mathbb{R}^{K}$
 $X \in \mathbb{R}^{K}$

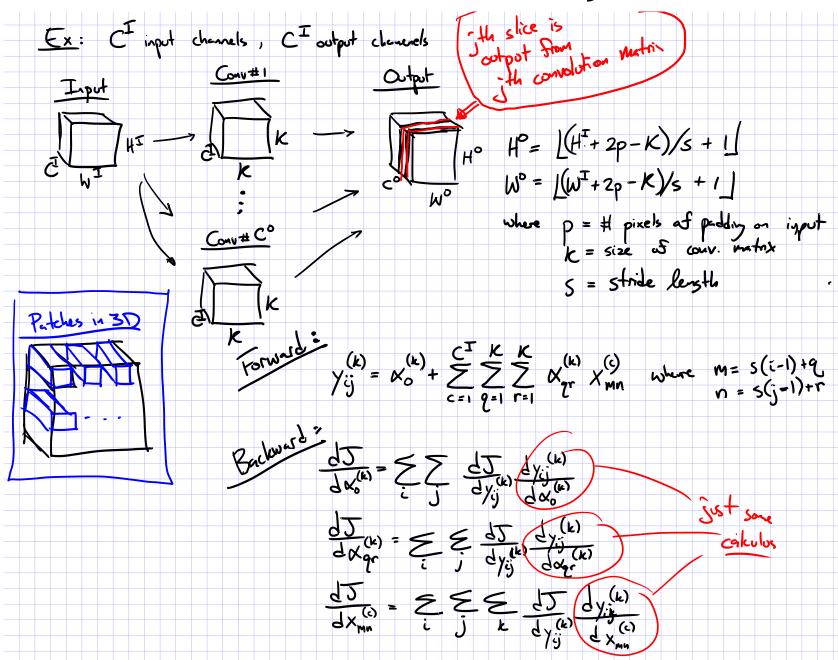
Fully-Connected Layer



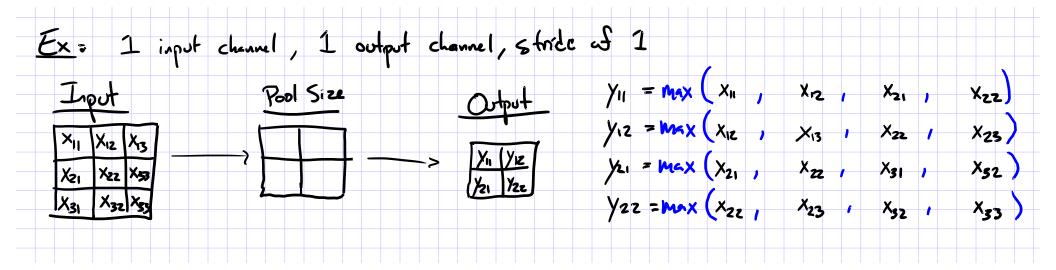
Convolutional Layer



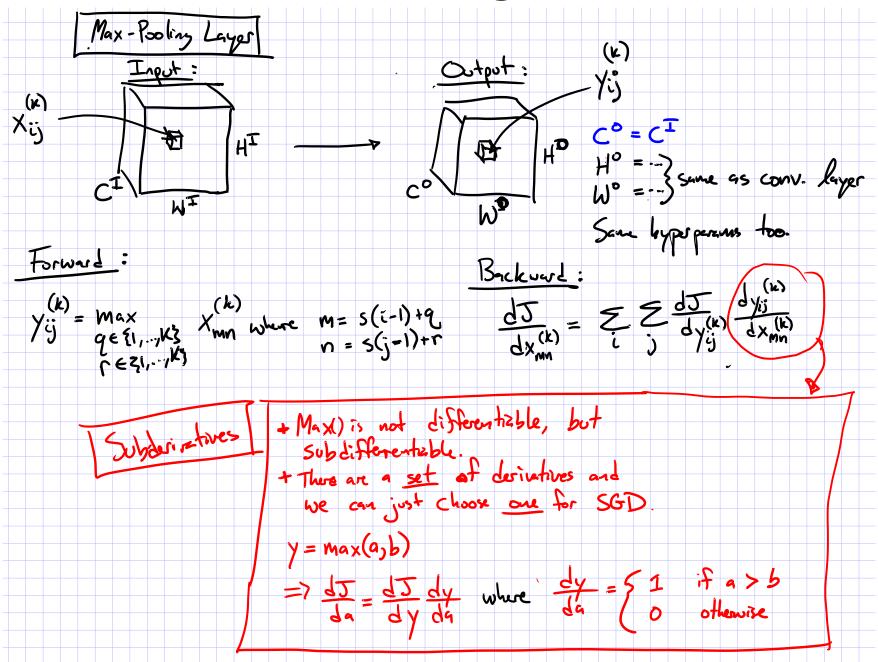
Convolutional Layer



Max-Pooling Layer



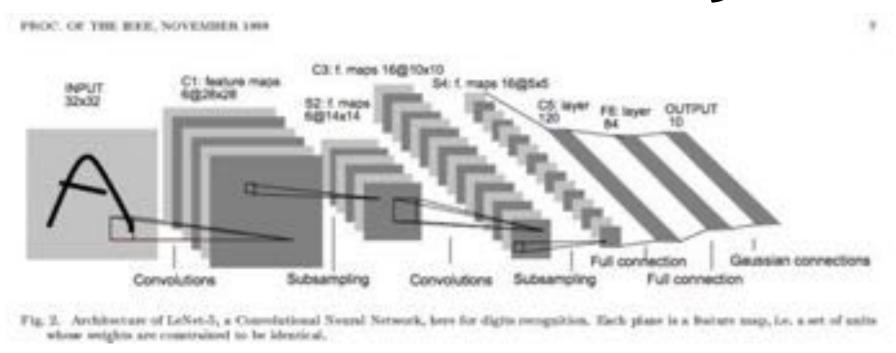
Max-Pooling Layer



Convolutional Neural Network (CNN)

- Typical layers include:
 - Convolutional layer
 - Max-pooling layer
 - Fully-connected (Linear) layer
 - ReLU layer (or some other nonlinear activation function)
 - Softmax
- These can be arranged into arbitrarily deep topologies

Architecture #1: LeNet-5



Architecture #2: AlexNet

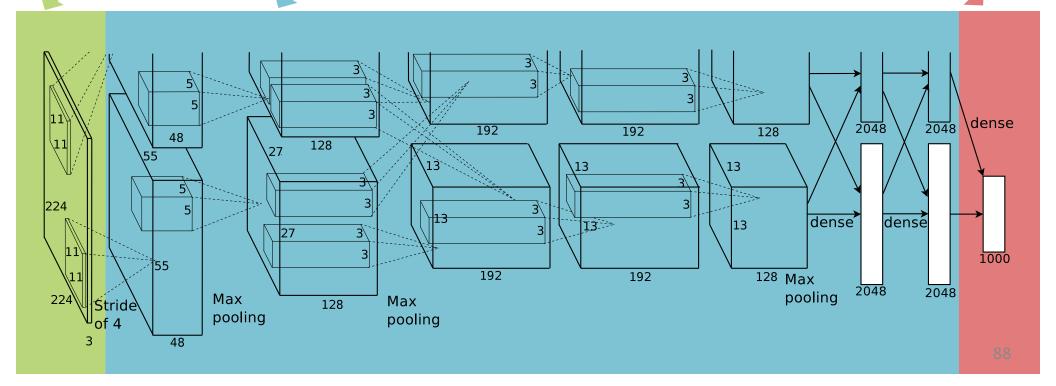
CNN for Image Classification

(Krizhevsky, Sutskever & Hinton, 2012) 15.3% error on ImageNet LSVRC-2012 contest

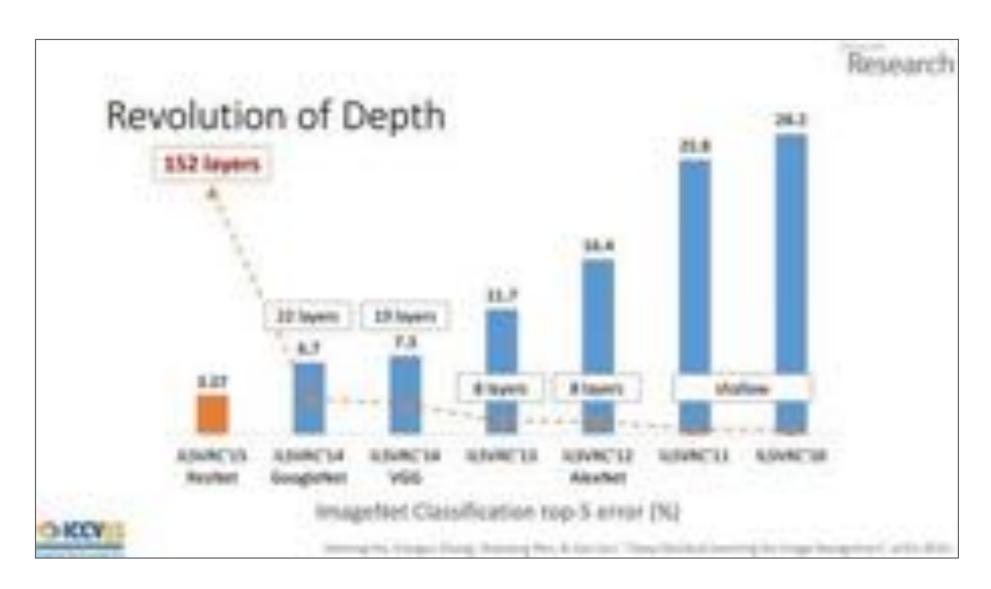
Input image (pixels)

- Five convolutional layers (w/max-pooling)
- Three fully connected layers

1000-way softmax



CNNs for Image Recognition



The key building block of ResNet

RESIDUAL CONNECTIONS

Slides in this section from...



Deep Residual Learning

MSRA @ ILSVRC & COCO 2015 competitions

Kaiming He

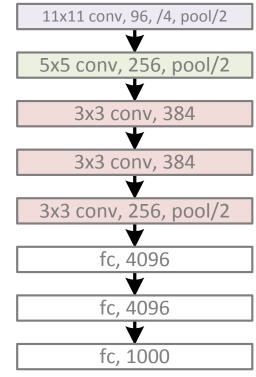
with Xiangyu Zhang, Shaoqing Ren, Jifeng Dai, & Jian Sun Microsoft Research Asia (MSRA)





Revolution of Depth

AlexNet, 8 layers (ILSVRC 2012)

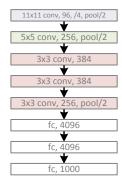




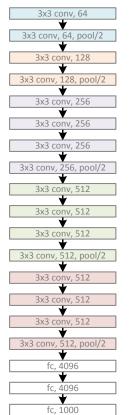


Revolution of Depth

AlexNet, 8 layers (ILSVRC 2012)



VGG, 19 layers (ILSVRC 2014)



GoogleNet, 22 layers (ILSVRC 2014)





Revolution of Depth

AlexNet, 8 layers (ILSVRC 2012)



VGG, 19 layers (ILSVRC 2014)



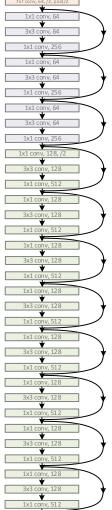
ResNet, 152 layers (ILSVRC 2015)





Revolution of Depth

ResNet, 152 layers



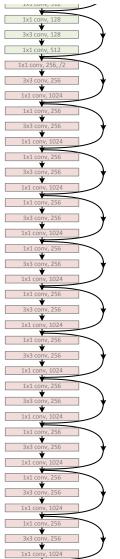
(there was an animation here)



Kaiming He, Xiangyu Zhang, Thang, Tha

Revolution of Depth

ResNet, 152 layers

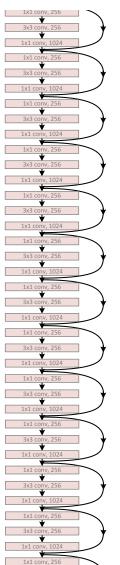


(there was an animation here)



Revolution of Depth

ResNet, 152 layers

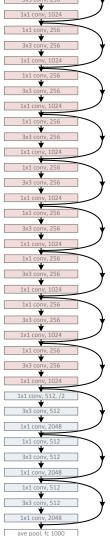


(there was an animation here)



Revolution of Depth

ResNet, 152 layers

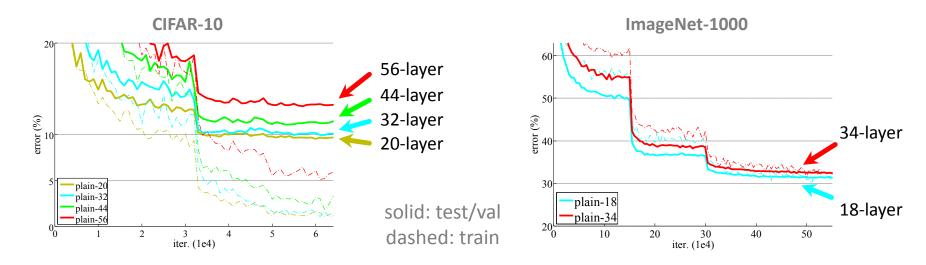


(there was an animation here)





Simply stacking layers?



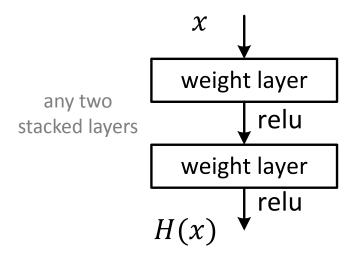
- "Overly deep" plain nets have higher training error
- A general phenomenon, observed in many datasets





Deep Residual Learning

• Plaint net



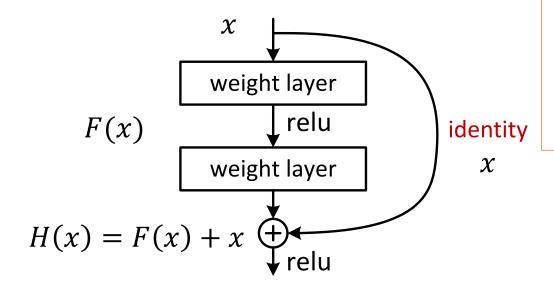
H(x) is any desired mapping, hope the 2 weight layers fit H(x)





Deep Residual Learning

Residual net



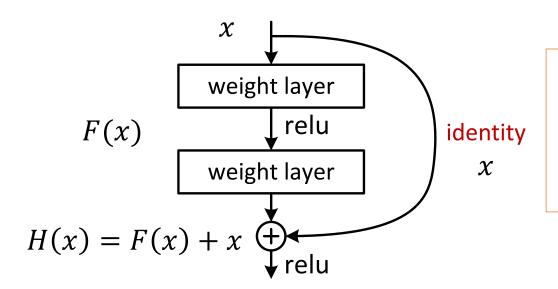
H(x) is any desired mapping, hope the 2 weight layers fit H(x)hope the 2 weight layers fit F(x)let H(x) = F(x) + x





Deep Residual Learning

• F(x) is a residual mapping w.r.t. identity



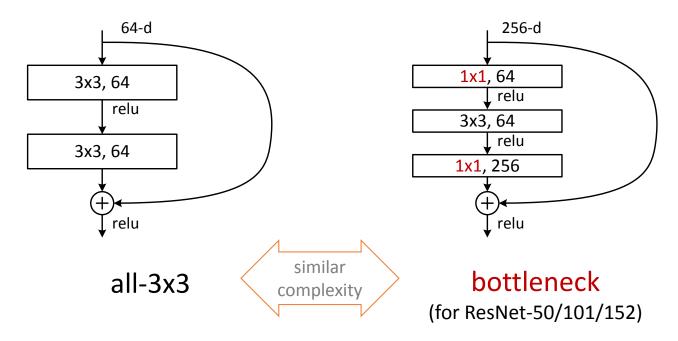
- If identity were optimal, easy to set weights as 0
- If optimal mapping is closer to identity, easier to find small fluctuations





ImageNet experiments

A practical design of going deeper





Network "Design"

- Keep it simple
- Our basic design (VGG-style)
 - all 3x3 conv (almost)
 - spatial size /2 => # filters x2
 - Simple design; just deep!
- Other remarks:
 - no max pooling (almost)
 - no hidden fc
 - no dropout

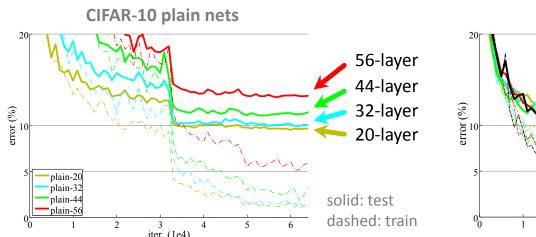


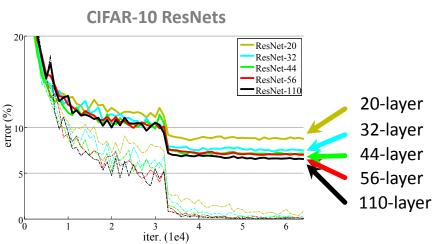
Microsoft 7x7 conv, 64, /2 Research 3x3 conv, 64 3x3 conv, 64 3x3 conv, 64 plain net ResNet 3x3 conv, 64 3x3 conv, 64 3x3 conv, 64 3x3 conv, 64 3x3 conv, 128 3x3 conv, 128 3x3 conv, 512, /2 3x3 conv, 512 3x3 conv, 512

avg pool



CIFAR-10 experiments

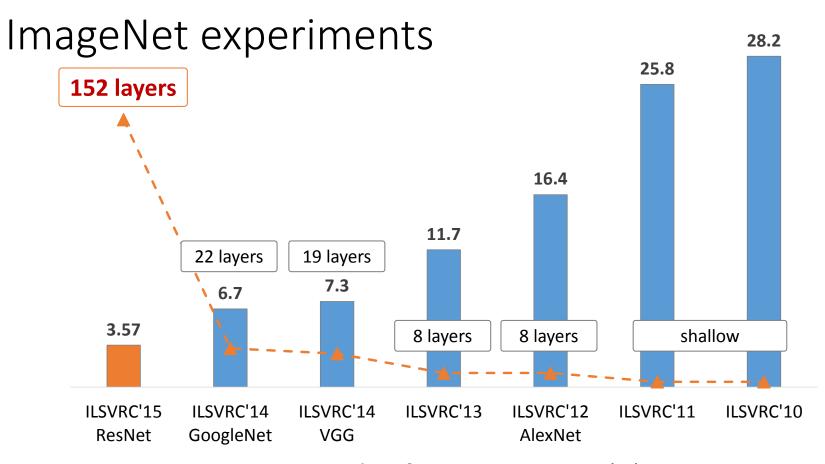


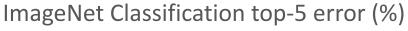


- Deep ResNets can be trained without difficulties
- Deeper ResNets have lower training error, and also lower test error











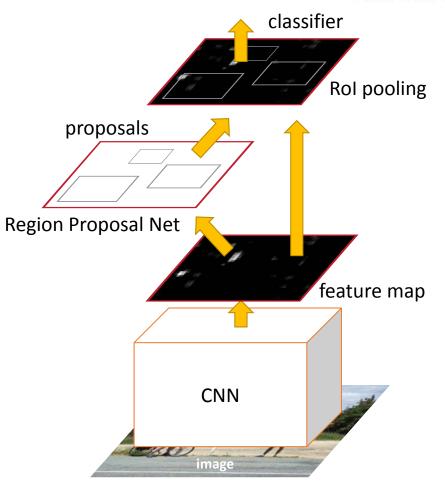
Object Detection (brief)

Simply "Faster R-CNN + ResNet"

Faster R-CNN baseline	mAP@.5	mAP@.5:.95
VGG-16	41.5	21.5
ResNet-101	48.4	27.2

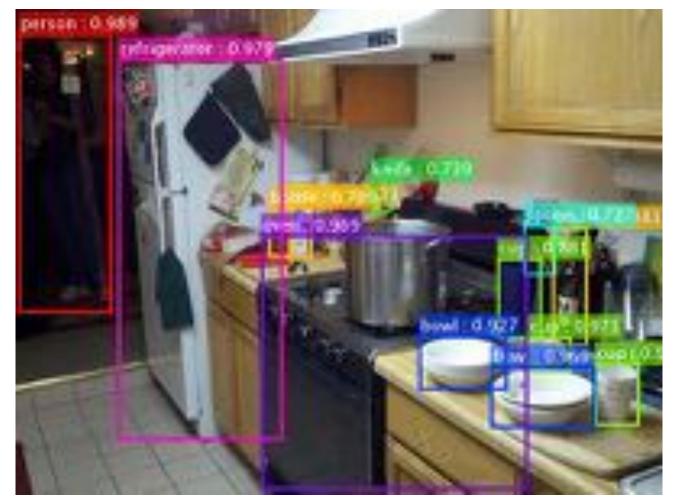
coco detection results

(ResNet has 28% relative gain)





Kaiming He, Xiangyu Zhang, Shaoqing Ren, & Jian Sun. "Deep Residual Learning for Image Recognition". arXiv 2015. Shaoqing Ren, Kaiming He, Ross Girshick, & Jian Sun. "Faster R-CNN: Towards Real-Time Object Detection with Region Proposal Networks". NIPS 2015.



*the original image is from the COCO dataset



Kaiming He, Xiangyu Zhang, Shaoqing Ren, & Jian Sun. "Deep Residual Learning for Image Recognition". arXiv 2015. Shaoqing Ren, Kaiming He, Ross Girshick, & Jian Sun. "Faster R-CNN: Towards Real-Time Object Detection with Region Proposal Networks". NIPS 2015.



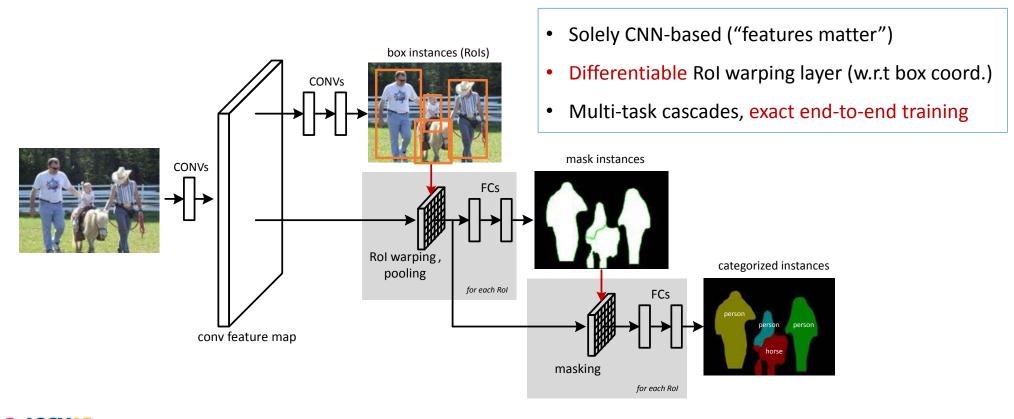
*the original image is from the COCO dataset



Kaiming He, Xiangyu Zhang, Shaoqing Ren, & Jian Sun. "Deep Residual Learning for Image Recognition". arXiv 2015. Shaoqing Ren, Kaiming He, Ross Girshick, & Jian Sun. "Faster R-CNN: Towards Real-Time Object Detection with Region Proposal Networks". NIPS 2015.

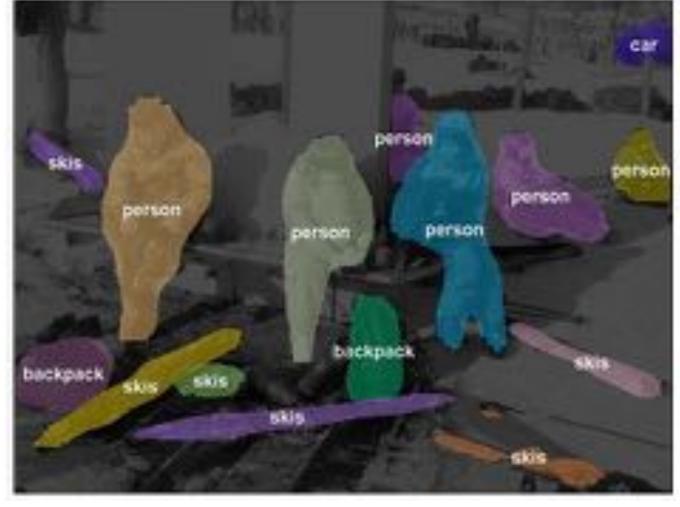


Instance Segmentation (brief)





Kaiming He, Xiangyu Zhang, Shaoqing Ren, & Jian Sun. "Deep Residual Learning for Image Recognition". arXiv 2015. Jifeng Dai, Kaiming He, & Jian Sun. "Instance-aware Semantic Segmentation via Multi-task Network Cascades". arXiv 2015.





input



*the original image is from the COCO dataset

Kaiming He, Xiangyu Zhang, Shaoqing Ren, & Jian Sun. "Deep Residual Learning for Image Recognition". arXiv 2015. Jifeng Dai, Kaiming He, & Jian Sun. "Instance-aware Semantic Segmentation via Multi-task Network Cascades". arXiv 2015.

CNN VISUALIZATIONS

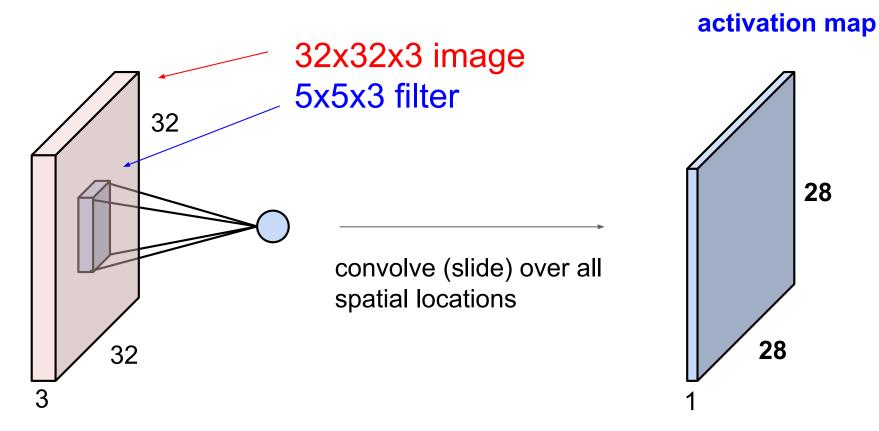
3D Visualization of CNN

http://scs.ryerson.ca/~aharley/vis/conv/



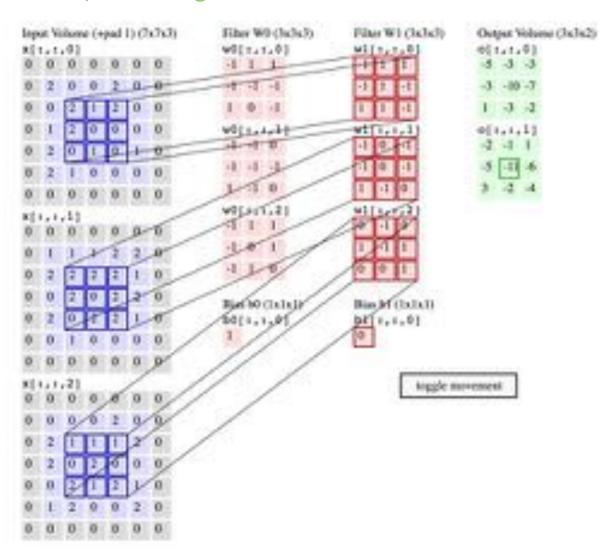
Convolution of a Color Image

- Color images consist of 3 floats per pixel for RGB (red, green blue) color values
- Convolution must also be 3-dimensional



Animation of 3D Convolution

http://cs231n.github.io/convolutional-networks/



MNIST Digit Recognition with CNNs (in your browser)

https://cs.stanford.edu/people/karpathy/convnetjs/demo/mnist.html



CNN Summary

CNNs

- Are used for all aspects of computer vision, and have won numerous pattern recognition competitions
- Able learn interpretable features at different levels of abstraction
- Typically, consist of convolution layers, pooling layers, nonlinearities, and fully connected layers