Rectification and 3D Reconstruction of Curved Document Images

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Carnegie Mellon University Sponsors: NSF, ONR

Digitizing Documents Everywhere



Digitizing books



Foreign Language Translation



Rare manuscripts



Bills and Receipts

A distorted image from cell-phone camera



OCR Performance under distortion

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Imaging Documents using flat-bed scanner

remnant of a roll I had bought in a town we passed through at noon with a stray penny-my last coin. I saw ripe bilberries gleaming here and there, like jet beads in the heath: I gathered a handful and ate them with the bread. My hunger, sharp before, was, if not satisfied, appeased by this hermit's meal. I said my evening prayers at its conclusion, and then chose my couch.

Beside the crag the heath was very deep: when I lay down my feet were buried in it; rising high on each side, it left only a narrow space for the night-air to invade. I folded my shawl double, and spread it over me for a coverlet; a low, mossy swell was my pillow. Thus lodged, I was not, at least-at the commencement of the night, cold.

My rest might have been blissful enough, only a sad heart broke it. It plained of its gaping wounds, its inward bleeding, its riven chords. It trembled for Mr. Rochester and his doom; it bemoaned him with bitter pity; it demanded him with ceaseless longing; and, impotent as a bird with both wings broken, it still quivered its shattered pinions in vain attempts to seek him.

Worn out with this torture of thought, I rose to my knees. Night was come, and her planets were risen: a safe, still night: too serene for the companionship of fear. We know that God is everywhere; but certainly we feel His presence most when His works are on the grandest scale spread before us; and it is in the unclouded night-sky, where His worlds wheel their silent course, that we read clearest His infinitude, His omnipotence, His omnipresence. I had risen to my knees to pray for Mr. Rochester. Looking up, I, with tear-dimmed eyes, saw the mighty Milky-way. Remembering what it was-what countless systems there swept space like a soft trace of light–I felt the might and strength of God. Sure was I of His efficiency to save what He had made: convinced I grew that neither earth should perish, nor one of the souls it treasured. I turned my prayer to thanksgiving: the Source of Life was also the Saviour of spirits. Mr. Rochester was safe; he was God's, and by God would he be guarded. I again nestled to the breast of the hill; and ere long in sleep forgot sorrow.

OCR Performance on scanned image

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I wo of the most interesting development of the stelly been given almost identical development of the unfortunately been given almost identical taxes of P. E. O'Neil [Acta Inf 30 June 1997] The SB-tree of P. E. O'Neil [Acta Info 29 (1997)] The SD-tree of the line by allocating heady technologies in taining efficiency in applications where the taining to the second s maintaining efficiency in applications where man the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in th accessed at the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in the same time; in the same time; in this case "SB" is in the same time; in the sa "sequential." The SB-tree of P. Ferragina and R Grant and R (1006) 272-380 is an element 702; SODA 7 (1996), 373-382] is an elegant contraction of the trace with the Patricia trees that we will consider in Series 12 a fine w is in roman type and the S connotes "string." Street and and to large-scale text processing, and they provide a basis in diverse a variable-length strings on disk [see Arge, Ferragin Gran at the





Our contribution:

- Works for multiple languages, font types and sizes
- 2. No global constraints on the shape of text lines.



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- 1. Works on multiple languages, font types and sizes
- 2. No global constraints on the shape of text lines.

Previous works:

Connected Components/ Segmentation

[Zhang and Tan, ICDAR '05] [Koo and Cho, ECCV '10] [Zandifar, ICIAP '07] Image Binarization [Cao et al, ICDAR '03]

The SB-tree of P. E. O'Neil [Acta Inf. 29 (1992) and imize disk I/O time by allocating nearby records a maintaining efficiency in applications where many ccessed at the same time; in this case "SB" is interpretent sequential." The SB-tree of P. Ferragina and R Grad 102; SODA 7 (1996), 373–382] is an elegant order of with the Patricia trees that we will consider in Sector 1 is in roman type and the S connotes "string." SB-tree has been applied to large-scale text processing, and they provide a basis of the





Our contribution:

- 1. From a single image
- 2. No global shape model
- 3. Globally optimal solution



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Previous works:

Laser scanner, stereo [Brown and Seales, PAMI '04] [Based et al, HP White Paper '01] [Yamashita et al, ICPR '04]

Cylinder / Developable

[Cao et al, ICDAR '03] [Zhang et al, CVPR '04] [Liang et al, PAMI '07] Shape-from-texture [Forsyth, ICCV '01] [Witkin, Artificial Intelligence '81] [Malik and Rosenholtz, IJCV '97]

Final Rectification

Horizontal and Vertical Text Directions





Horizontal Direction --- Rescaling



Horizontal Direction --- Rescaling

















Mean Intensity Profile

Mean Intensity Profile

Horizontal Direction --- Line Refinement

Vertical Direction

b, d, l, k, f, B, E, F, L, D, M English

量子力学是描写微观物质的一个物理学理论,与相对论一起被认; 理学的两大基本支柱,许多物理学理论和科学如原子物理学、固体学、核物理学和粒子物理学以及其它相关的学科都是以量子力学; Chinese

> दिछी एक शहर है, लेकिन दिछी के दो केंद्र हैं। दिछी का एक केंद्र <mark>चाँदनी चौक</mark> है और दिछी का <u>दूसरा</u> केंद्र कनाट प्लेस है। लोग कहते <u>Hindi</u>

Vertical Direction

tunately been given almost ident The SB-tree of P. E. O'Neil Acta Inf. 29 (1992) 44 J mize disk I/O time by allocating nearby records to be naintaining efficiency in applications where many one ccessed at the same time; in this case "SB" is in the sequential." The SB-tree of P. Ferragina and R. Grad [02; SODA 7 (1996), 373-382] is an elegant contribution with the Patricia trees that we will consider in Series s in roman type and the S connotes "string." SB-tres lag to o large-scale text processing, and they provide

tunately been given almost identica The SB-tree of P. E. O'Neil Acta Inf. 29 (1992, 14-15) mize disk I/O time by allocating nearby records to the naintaining efficiency in applications where many ccessed at the same time; in this case 'B' equential." The SB-tree of P. Ferragine and R 2; SODA 7 (1996), 373–382] is an egant with the Patricia trees that we will consider in s in roman type and the S connotes "string." SB-tree lage b large-scale text processing, and they prov Close regions Faraway regions

tuna ely deen given almost identical The SB-tree of P. E. O'Neil Acta Inf. 19 (1992, 24-25) mize disk I/O time by allocating nearby records to the **naintaining** efficiency in applications where many or ccessed at the same time; in this case "SB" is in the same time; in the same time; in this case "SB" is in the same time; in this case "SB" is in the same time; in t sequential." The SB-tree of P. Ferragina and R. Grow D2; SODA 7 (1996), 373-382] is an elevant continue of with the Patricia trees that we will consider in Second and and s in roman type and the S connotes "string." SB-tres in and large-scale text processing, and they provide Darker regions **Brighter regions**

3D reconstruction

3D reconstruction --- Assumption II

Quadrilaterals versus Triangles

Our approach

Previous works [J. Taylor et al, CVPR '10]

Unknowns versus Constraints

mn < 3(m-1)(n-1)unknowns constraints

Formulation

Parameterization

$$P_i = (x_i Z_i, y_i Z_i, Z_i) \qquad \mathbf{Z} = [Z_1, Z_2, \dots, Z_n]$$

Deviation from Parallelogram $\Delta_{i} = P_{i1} - P_{i2} + P_{i3} - P_{i4}$

Minimization of sum of deviation: $f(\mathbf{Z}) = \sum_{j=1}^{M} \|\Delta_j\|^2 \qquad \text{s.t.} \quad \|\mathbf{Z}\|^2 = 1$

Homogenous Least Square \rightarrow SVD

3D-aided Rectification

out with this torture of thought, I rose to my knees. Night was come, and I n: a safe, still night: too serene for the companionship of fear. We know the re; but certainly we feel His presence most when His works are on the gran fore us; and it is in the unclouded night-sky, where His worlds wheel their sile ad clearest His infinitude, His omnipotence, His omnipresence. I had risen to r Mr. Rochester. Looking up, I, with tear-dimmed eyes, saw the mighty ing what it was-what countless systems there swept space like a soft trace ight and strength of God. Sure was I of His efficiency to save what He I grew that neither earth should perish, nor one of the souls it treasured. I thanksgiving: the Source of Life was also the Saviour of spirits. Mr. Roc is God's, and by God would he be guarded. I again nestled to the breast ig in sleep forgot sorrow.

at day, Want came to me pale and bare. Long after the little birds had left to bees had come in the sweet prime of day to gather the heath honey before the n the long morning shadows were curtailed, and the sun filled earth and sky d round me.

I still, hot, perfect day! What a golden desert this spreading moor! E I wished I could live in it and on it. I saw a lizard run over the crag; I g the sweet bilberries. I would fain at the moment have become bee or liza found fitting nutriment, permanent shelter here. But I was a human being, ng's wants: I must not linger where there was nothing to supply them. I ros be bed I had left. Hopeless of the future, I wished but this—that my Make ght good to require my soul of me while I slept; and that this weary frame om further conflict with fate, had now but to decay quietly, and mingle in p this wilderness. Life, however, was yet in my possession, with all its req and responsibilities. The burden must be carried: the want provided for: th his torture of the advance of the sweet prime of the torture of the sweet prime of the torture of the tort

this torture of thought, I rose to my knee still night: too serene for the companion stainly we feel His presence most when I d it is in the unclouded night-sky, where t His infinitude, His omnipotence, His om chester. Looking up, I, with tear-dimme it was-what countless systems there swe strength of God. Sure was I of His efficient t neither earth should perish, nor one of ng: the Source of Life was also the Sav and by God would he be guarded. I aga forgot sorrow.

nt came to me pale and bare. Long after

内厷观性质, 厷观性质由厷观量表征, 它们是可以直在 宏观观测来确定的物理量,包括热力学变量(如密度 力学函数(如内能、熵等),以及其他一些在传统热力等 的可观测量(如气体分子的速度分布,流体的密度剂 ,磁系统的自旋密度涨落关联函数等).为此,必须建立 观量之间的联系.统计物理学的基本观点是:宏观量 量的统计平均值,这可以从宏观观测的特点来说明,2 个基本特点:一是空间尺度上是宏观小(才有可能量 质的空间变化)、微观大(仍包含足够大量的粒子);二 上是宏观短(才有可能显示宏观性质随时间的变化)、 状态已经历足够多次变化).比如,以测量气体分子的 ,在0℃和1atm下,1cm³体积中包含气体分子数约 ¹⁹,如果选 10⁻⁶ cm³ 的体积来观测,宏观看它已 包含约2.7×10¹³个分子,因而微观看还是非常力 【样的宏观条件下,1cm³内气体分子在1秒内的 尚若洗 10-6秒 为观测时间, 宏观看已足够 cm³的宏观小体积,分子之间仍会有大约10 (碰撞发生,显然微观上已足够长. 由于宏观观测是宏观小、微观大,宏观短、微观

上是宏观短(才有可能显示宏观性质随时间 状态已经历足够多次变化).比如,以测量 ,在 0℃和 1 atm 下,1 cm³ 体积中包含气 ⁹,如果选 10⁻⁶ cm³ 的体积来观测,宏观看 包含约 2.7×10¹³个分子,因而微观看还是 的宏观条件下,1 cm³ 内气体分子在1利

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宏观量表征,它们是可以 ,包括热力学变量(如 以及其他一些在传统热的速度分布,流体的变 的速度分布,流体的变 并联函数等).为此,必 理学的基本观点是: 人宏观观测的特点来记 人宏观观测的特点来记

2. 《见星衣征,它们定可以上 1,包括热力学变量(如密 ,以及其他一些在传统热力 一的速度分布,流体的密度 关联函数等).为此,必须到 1理学的基本观点是:宏观 从宏观观测的特点来说明. 尺度上是宏观小(才有可能 (仍包含足够大量的粒子).

Did we achieve the goal?

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Did we achieve the goal?

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OCR Performance under distortion

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Conclusion

Two of the most interesting devices a second second

Rectification

The SB-tree of P. E. O'Neil [Acta Inf. 29 (1992) 24 mize disk I/O time by allocating nearby records to the naintaining efficiency in applications where many operations ccessed at the same time; in this case "SB" is in the sequential." The SB-tree of P. Ferragina and R. Green 102; SODA 7 (1996), 373–382] is an elegant continue with the Patricia trees that we will consider in Section is in roman type and the S connotes "string." SB-trees have the to large-scale text processing, and they provide a basis in effective

Globally optimal 3D reconstruction

Text analysis on gray-scale image

The Ultimate Goal

Thank you!

Contribution

• Language-independent text analysis on gray-scale and low-resolution images

• Previous works [CC, binarization]

• Reconstruction a broad range of 3D surface from a single image.

- Previous works [Parametric forms, developable surface]
- Previous works [Shape-from-X, complicated modeling, local solution.]
- Rectification of for-shortening and shading based on 3D surface.