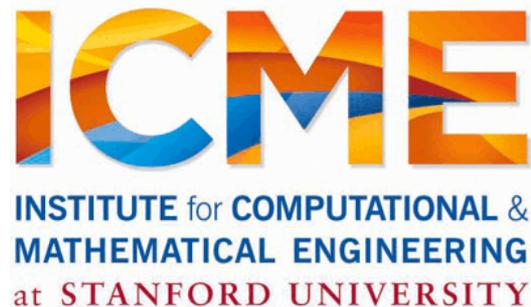


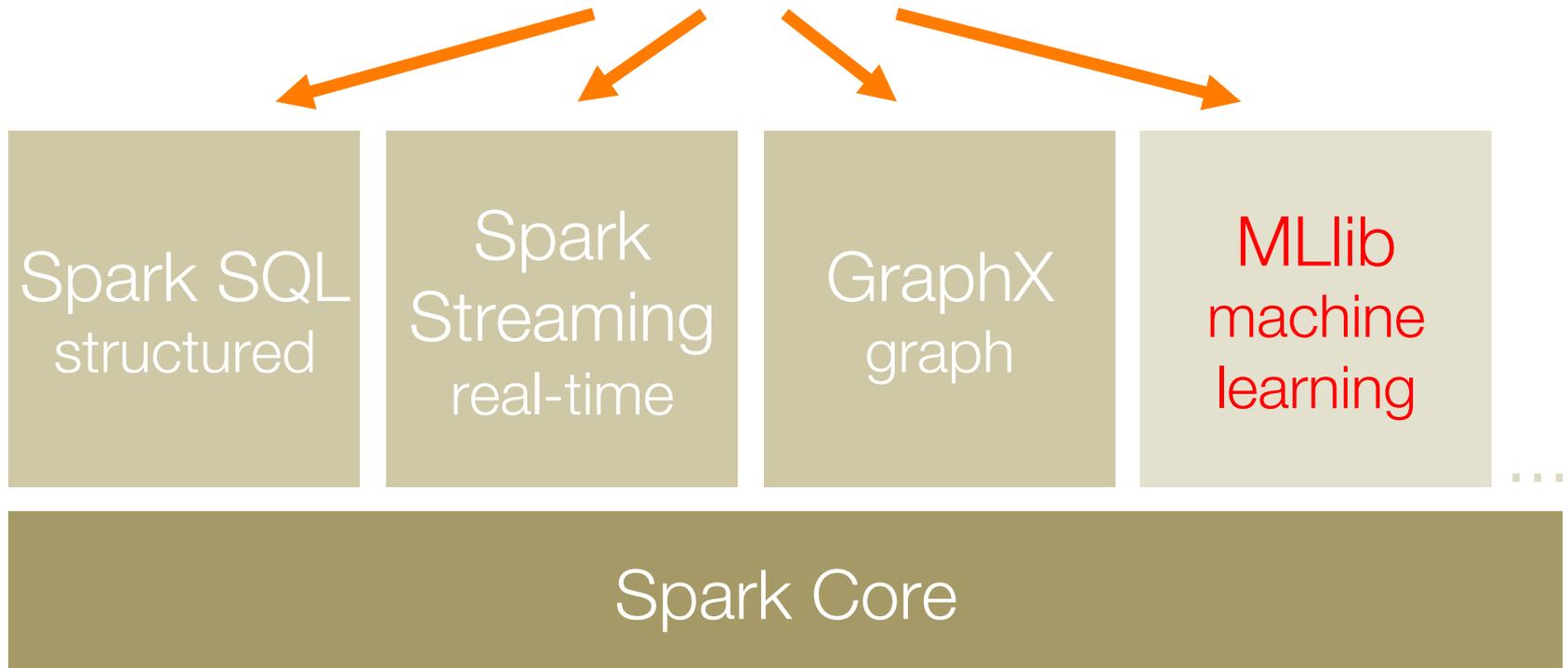
Distributing Matrix Computations with Spark MLlib

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A General Platform

Standard libraries included with Spark



Outline

Introduction to MLlib

Example Invocations

Benefits of Iterations: Optimization

Singular Value Decomposition

All-pairs Similarity Computation

MLlib + {Streaming, GraphX, SQL}

Introduction

MLlib History

MLlib is a Spark subproject providing machine learning primitives

Initial contribution from AMPLab, UC Berkeley

Shipped with Spark since Sept 2013

MLlib: Available algorithms

classification: logistic regression, linear SVM, naïve Bayes, least squares, classification tree

regression: generalized linear models (GLMs), regression tree

collaborative filtering: alternating least squares (ALS), non-negative matrix factorization (NMF)

clustering: k-means||

decomposition: SVD, PCA

optimization: stochastic gradient descent, L-BFGS

Example Invocations

Example: K-means

```
// Load and parse the data.
val data = sc.textFile("kmeans_data.txt")
val parsedData = data.map(_.split(' ').map(_.toDouble)).cache()

// Cluster the data into two classes using KMeans.
val clusters = KMeans.train(parsedData, 2, numIterations = 20)

// Compute the sum of squared errors.
val cost = clusters.computeCost(parsedData)
println("Sum of squared errors = " + cost)
```

Example: PCA

```
// compute principal components
val points: RDD[Vector] = ...
val mat = RowRDDMatrix(points)
val pc = mat.computePrincipalComponents(20)

// project points to a low-dimensional space
val projected = mat.multiply(pc).rows

// train a k-means model on the projected data
val model = KMeans.train(projected, 10)
```

Example: ALS

```
// Load and parse the data
val data = sc.textFile("mllib/data/als/test.data")
val ratings = data.map(_.split(',').match {
  case Array(user, item, rate) =>
    Rating(user.toInt, item.toInt, rate.toDouble)
})

// Build the recommendation model using ALS
val model = ALS.train(ratings, 1, 20, 0.01)

// Evaluate the model on rating data
val usersProducts = ratings.map { case Rating(user, product, rate) =>
  (user, product)
}
val predictions = model.predict(usersProducts)
```

Benefits of fast iterations

Optimization

At least two large classes of optimization problems humans can solve:

- Convex Programs
- Spectral Problems (SVD)

Optimization - LR

```
data = spark.textFile(...).map(readPoint).cache()

w = numpy.random.rand(D)

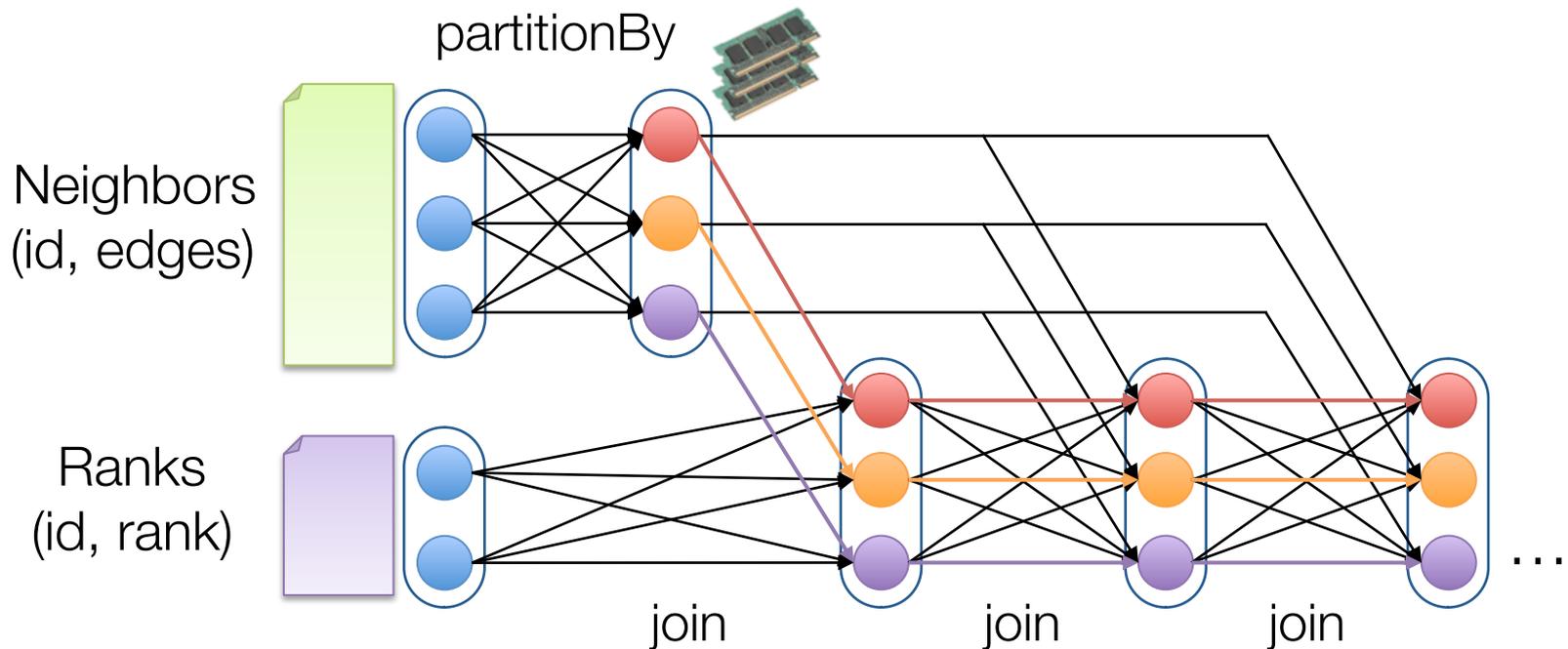
for i in range(iterations):
    gradient = data.map(lambda p:
        (1 / (1 + exp(-p.y * w.dot(p.x)))) * p.y * p.x
    ).reduce(lambda a, b: a + b)
    w -= gradient

print "Final w: %s" % w
```

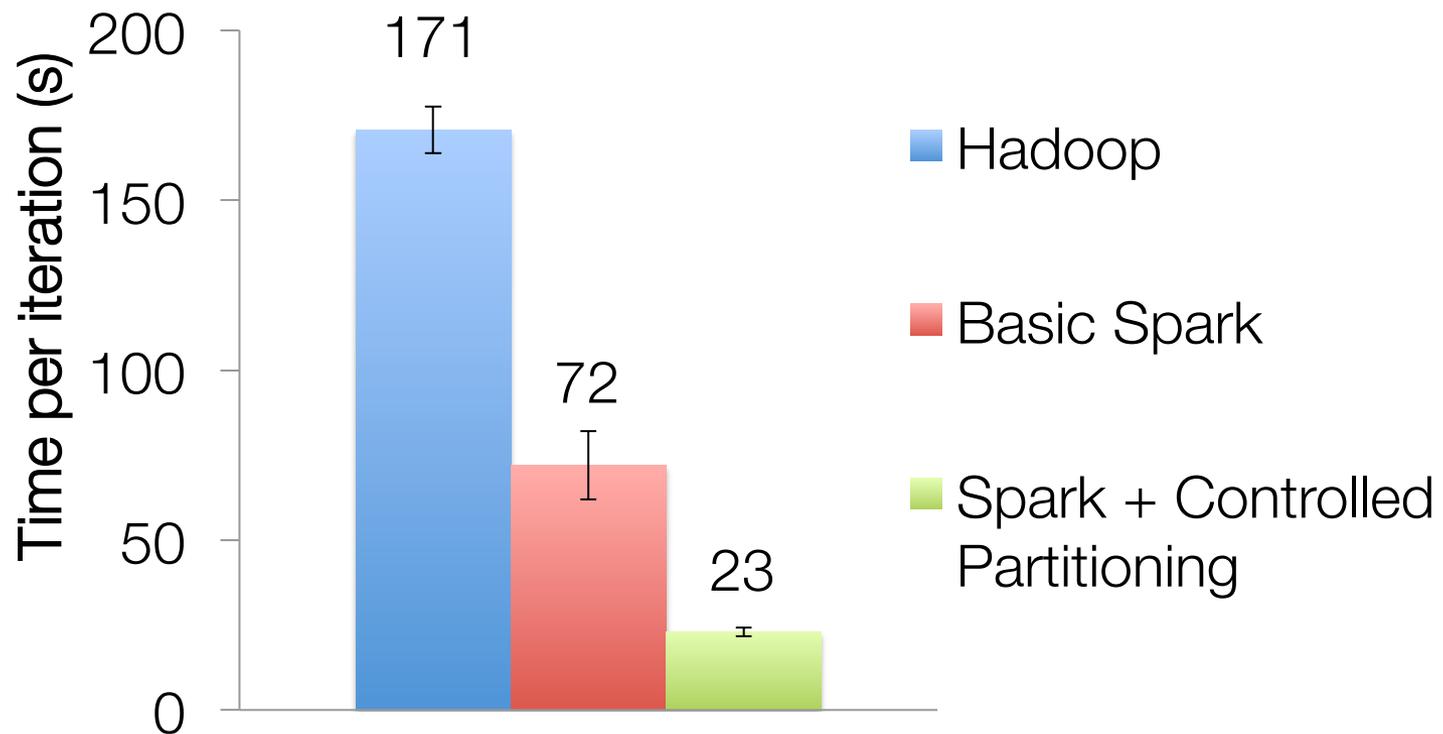
Spark PageRank

Using `cache()`, keep neighbor lists in RAM

Using partitioning, avoid repeated hashing



PageRank Results



Spark PageRank

Generalizes to Matrix Multiplication, opening many algorithms
from Numerical Linear Algebra

Deep Dive: Singular Value Decomposition

Singular Value Decomposition

Two cases: Tall and Skinny vs roughly Square

`computeSVD` function takes care of which one to call, so you don't have to.

SVD selection

```
if (n < 100 || k > n / 2) {  
    // If n is small or k is large compared with n, we better compute the Gramian matrix first  
    // and then compute its eigenvalues locally, instead of making multiple passes.  
    if (k < n / 3) {  
        SVDMode.LocalARPACK  
    } else {  
        SVDMode.LocalLAPACK  
    }  
} else {  
    // If k is small compared with n, we use ARPACK with distributed multiplication.  
    SVDMode.DistARPACK  
}
```

Tall and Skinny SVD

- Given $m \times n$ matrix A , with $m \gg n$.
- We compute $A^T A$.
- $A^T A$ is $n \times n$, considerably smaller than A .
- $A^T A$ is dense.
- Holds dot products between all pairs of columns of A .

$$A = U\Sigma V^T$$

$$A^T A = V\Sigma^2 V^T$$

Tall and Skinny SVD

$$A^T A = V \Sigma^2 V^T$$

Gets us V and the
singular values

$$A = U \Sigma V^T$$

Gets us U by one
matrix multiplication

Square SVD via ARPACK

Very mature Fortran77 package for
computing eigenvalue decompositions

JNI interface available via netlib-java

Distributed using Spark

Square SVD via ARPACK

Only needs to compute matrix vector multiplies to build Krylov subspaces

$$K_n = [b \quad Ab \quad A^2b \quad \dots \quad A^{n-1}b]$$

The result of matrix-vector multiply is small

The multiplication can be distributed

Deep Dive: All pairs Similarity

Deep Dive: All pairs Similarity

Compute via DIMSUM: “Dimension Independent Similarity Computation using MapReduce”

Will be in Spark 1.2 as a method in RowMatrix

All-pairs similarity computation

- Given $m \times n$ matrix A , with $m \gg n$.

$$A = \begin{pmatrix} a_{1,1} & a_{1,2} & \cdots & a_{1,n} \\ a_{2,1} & a_{2,2} & \cdots & a_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m,1} & a_{m,2} & \cdots & a_{m,n} \end{pmatrix}$$

- A is tall and skinny, example values $m = 10^{12}$, $n = 10^6$.
- A has sparse rows, each row has at most L nonzeros.
- A is stored across hundreds of machines and cannot be streamed through a single machine.

Naïve Approach

Algorithm 1 NaiveMapper(r_i)

for all pairs (a_{ij}, a_{ik}) in r_i **do**
 Emit $((j, k) \rightarrow a_{ij}a_{ik})$
end for

Algorithm 2 NaiveReducer($(i, j), \langle v_1, \dots, v_R \rangle$)

output $c_i^T c_j \rightarrow \sum_{i=1}^R v_i$

Naïve approach: analysis

- Very easy analysis
- 1) Shuffle size: $O(mL^2)$
- 2) Largest reduce-key: $O(m)$
- Both depend on m , the larger dimension, and are intractable for $m = 10^{12}, L = 100$.
- We'll bring both down via clever sampling
- Assuming column norms are known or estimates available

DIMSUM Sampling

Algorithm 3 DIMSUMv2Mapper(r_i)

for all a_{ij} in r_i **do**

With probability $\min\left(1, \frac{\sqrt{\gamma}}{\|c_j\|}\right)$

for all a_{ik} in r_i **do**

With probability $\min\left(1, \frac{\sqrt{\gamma}}{\|c_k\|}\right)$

emit $((j, k) \rightarrow \frac{a_{ij}a_{ik}}{\min(\sqrt{\gamma}, \|c_j\|) \min(\sqrt{\gamma}, \|c_k\|)})$

end for

end for

DIMSUM Analysis

The algorithm outputs b_{ij} , which is a matrix of cosine similarities, call it B .

Four things to prove:

- 1 Shuffle size: $O(nL\gamma)$
- 2 Largest reduce-key: $O(\gamma)$
- 3 The sampling scheme preserves similarities when $\gamma = \Omega(\log(n)/s)$
- 4 The sampling scheme preserves singular values when $\gamma = \Omega(n/\epsilon^2)$

Spark implementation

```
// Load and parse the data file.
```

```
val rows = sc.textFile(filename).map { line =>  
  val values = line.split(' ').map(_.toDouble)  
  Vectors.dense(values)  
}  
val mat = new RowMatrix(rows)
```

```
// Compute similar columns perfectly, with brute force.
```

```
val simsPerfect = mat.columnSimilarities()
```

```
// Compute similar columns with estimation using DIMSUM
```

```
val simsEstimate = mat.columnSimilarities(threshold)
```

Ongoing Work in MLlib

stats library (e.g. stratified sampling, ScaRSR)

ADMM

LDA

General Convex Optimization

MLlib + {Streaming, GraphX, SQL}

MLlib + Streaming

As of Spark 1.1, you can train linear models in a streaming fashion

Model weights are updated via SGD, thus amenable to streaming

More work needed for decision trees

MLlib + SQL

```
points = context.sql("select latitude, longitude from tweets")  
model = KMeans.train(points, 10)
```

MLlib + GraphX

```
// assemble link graph
val graph = Graph(pages, links)
val pageRank: RDD[(Long, Double)] = graph.staticPageRank(10).vertices

// load page labels (spam or not) and content features
val labelAndFeatures: RDD[(Long, (Double, Seq((Int, Double)))] = ...
val training: RDD[LabeledPoint] =
  labelAndFeatures.join(pageRank).map {
    case (id, ((label, features), pageRank)) =>
      LabeledPoint(label, Vectors.sparse(features ++ (1000, pageRank))
  }

// train a spam detector using logistic regression
val model = LogisticRegressionWithSGD.train(training)
```

Future of MLlib

General Linear Algebra

CoordinateMatrix

RowMatrix

BlockMatrix Goal: version 1.2

Local and distributed versions.

Operations in-between. Goal: version 1.3

Research Goal: General Convex Optimization

Distribute CVX by
backing CVXPY with
PySpark

Easy-to-express
distributable convex
programs

Need to know less
math to optimize
complicated
objectives

```
from cvxpy import *  
  
# Create two scalar optimization variables.  
x = Variable()  
y = Variable()  
  
# Create two constraints.  
constraints = [x + y == 1,  
              x - y >= 1]  
  
# Form objective.  
obj = Minimize(square(x - y))  
  
# Form and solve problem.  
prob = Problem(obj, constraints)  
prob.solve() # Returns the optimal value.  
print "status:", prob.status  
print "optimal value", prob.value  
print "optimal var", x.value, y.value
```

```
status: optimal  
optimal value 0.999999989323  
optimal var 0.999999998248 1.75244914951e-09
```

Spark and ML

Spark has all its roots in research, so we hope to keep incorporating new ideas!