

A one-time single-bit fault  
leaks all previous  
NTRU-HRSS session keys  
to a chosen-ciphertext attack

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[cr.yp.to/papers.html#ntrw](http://cr.yp.to/papers.html#ntrw)

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Thanks to Lange for pointing  
out plaintext confirmation as a  
countermeasure to fault attacks.

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“Kyber has high performance . . . but still lacks some clarification from NIST about its Intellectual Property status”, i.e., patents.

2010–2017 patents listed in  
[NTRU Prime FAQ](#): US9094189,  
US9246675, CN107566121,  
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For deploying software to protect  
users *now*, NTRU-HRSS is  
attractive: small, fast, unpatented.



## Is NTRU-HRSS secure?

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HRSS uses Fujisaki–Okamoto (FO) transform, specifically one of the variants from [2002 Dent](#).

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If encryption is randomized, first derandomize it: obtain random bits as  $H(m)$ . Make sure  $m$  has high entropy! See recent [collapse](#) of “[FrodoKEM parameter sets comfortably match their target security levels with a large margin](#)”.



Defense 3 (in the numbering from ntrw's survey of attacks and defenses): plaintext confirmation.

Instead of ciphertext  $E(m)$ ,  
send ciphertext  $(E(m), H'(m))$   
where  $H'$  is a hash function.

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This stops chosen-ciphertext attacks that exploit structure of the public-key encryption function  $E$  to convert  $E(m)$  for secret  $m$  into, e.g.,  $E(m + 1)$ . Attacker has no way to convert  $H'(m)$  into  $H'(m + 1)$  for “unstructured”  $H'$ .

Current NTRU-HRSS is different

2019 NTRU-HRSS proposal  
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2017 Saito–Xagawa–Yamakawa.

Modified proposal **removes  
plaintext confirmation** and  
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Defense 4, implicit rejection (from  
2017 Hofheinz–Hövelmanns–Kiltz,  
generalizing 2012 Persichetti):  
instead of having a KEM reject  
an invalid ciphertext  $C$ , have  
it output  $H''(r, C)$  where  $r$  is a  
random string stored in secret key.

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Issue 1: Proof is only in QRROM; are there non-QRROM attacks?

Issue 2: Proof is tight only in ROM; can this be exploited?

Issue 3, my focus today: Are there chosen-ciphertext attacks beyond the IND-CCA2 model?

2007 [Koblitz](#), regarding HMQV:

“Anyone working in cryptography should think very carefully before dropping a validation step that had been put in to prevent security problems. Certainly someone with Krawczyk’s experience and expertise would never have made such a blunder if he hadn’t been over-confident because of his ‘proof’ of security.”

See also 2019 [survey of failures](#).

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## 2018 Bernstein–Persichetti:

implicit rejection “produces random-looking session keys” for invalid ciphertexts, “so it hides the pattern of valid ciphertexts”; plaintext confirmation “stops an earlier stage of the attack”; current proofs do not “show any advantages for the dual-defense construction” **but** it “seems difficult to justify a recommendation against the dual-defense construction” given that the defenses “target different aspects of attacks”.

## An attack against NTRU-HRSS

DRAM hardware is unreliable.  
Often stored bits are corrupted.  
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Main point of the `ntrw` paper:  
implicit rejection doesn't do its job  
if  $r$  is corrupted. Attacker detects  
invalid ciphertexts: changing  $r$   
changes decryption output. See  
paper for application to NTRU-  
HRSS and full attack software.

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Use ECC in crypto libraries?

Use ECC in applications?

Programming language? OS?

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Point fingers and do nothing?

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Describes ECC as a defense.

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2022.10: Classic McEliece **recommends** dropping plaintext confirmation “to proactively eliminate any concerns regarding U.S. patent 9912479” .

Warns that this allows the  $ntrw$  attack whenever  $r$  is corrupted.  
Describes ECC as a defense.

Introduces principle of factoring “any generic transformation aiming at a goal beyond IND-CCA2” out of KEM specifications, to simplify design and review.