## Probing CP-violating Higgs contributions in $\gamma\gamma \to f\bar{f}$ through fermion polarization

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We discuss the use of fermion polarization for studying neutral Higgs bosons at a photon collider. To this aim we construct polarization asymmetries which can isolate the contribution of a Higgs boson  $\phi$  in  $\gamma\gamma\to f\bar f$ ,  $f=\tau/t$ , from that of the QED continuum. This can help in getting information on the  $\gamma\gamma\phi$  coupling in case  $\phi$  is a CP eigenstate. We also construct CP-violating asymmetries which can probe CP mixing in case  $\phi$  has indeterminate CP. Furthermore, we take the MSSM with CP violation as an example to demonstrate the potential of these asymmetries in a numerical analysis. We find that these asymmetries are sensitive to the presence of a Higgs boson as well as its CP properties over a wide range of MSSM parameters. In particular, the method suggested can cover the region where a light Higgs boson may have been missed by LEP due to CP violation in the Higgs sector, and may be missed as well at the LHC.

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#### I. INTRODUCTION

The Higgs boson is the only particle of the Standard Model (SM) to have eluded experimental discovery so far. The discovery of the Higgs boson and the subsequent study of electroweak symmetry breaking is one of the prime aims of all the current and next generation colliders [1]. Electroweak precision measurements indicate, in the SM, the existence of a Higgs boson lighter than 204 GeV at 95% C.L. [2]. A Higgs boson with SM couplings lighter than 114.4 GeV is ruled out by direct searches at LEP [3]. Thus one expects to find the SM Higgs boson with a mass in this range. In models with an extended (and possibly CP-violating) Higgs sector, the couplings of electroweak vector bosons to the lightest Higgs can be suppressed [4]. In such a case direct searches allow the existence of a Higgs boson much lighter than 114.4 GeV [5].

The Large Hadron Collider (LHC), scheduled to go in operation in 2007, is expected [6] to be capable of searching for the SM Higgs boson in the entire mass range expected theoretically and still allowed experimentally. The International Linear Collider (ILC) [7], currently in planning, is expected to be capable of profiling the Higgs boson very accurately, again for the entire mass range mentioned above. Determination of the CP properties of the spin-0 particle, which we hope will be discovered and studied at the LHC and the ILC, is an important part of this project of profiling the Higgs boson, see e.g. [8]. The

Higgs couplings with a pair of electroweak gauge bosons (V=W/Z) and those with a pair of heavy fermions  $(f=t/\tau)$  are the ones that prove the most useful in this context. These couplings, for a neutral Higgs boson  $\phi$ , which may or may not be a CP eigenstate, can be written as

$$\phi f \bar{f} : \frac{-ig \, m_f}{2 \, M_W} \left( v_f + i a_f \, \gamma_5 \right) \tag{1}$$

$$\phi VV : \frac{ig \ M_V^2}{M_W} \left( A_V g_{\mu\nu} + B_V \frac{p_{\mu} p_{\nu}}{M_Z^2} + i \ C_V \epsilon_{\mu\nu\rho\sigma} \frac{p^{\rho} q^{\sigma}}{M_Z^2} \right)$$
(2)

where  $p = P_{V_1} + P_{V_2}$ ,  $q = P_{V_1} - P_{V_2}$  and  $P_{V_1}$ ,  $P_{V_2}$  are the four momenta of the two massive vector bosons. In the SM,  $v_f = A_V = 1$  and  $a_f = B_V = C_V = 0$ . At the LHC, the  $t\bar{t}$  final state produced in the decay of an inclusively produced Higgs can provide knowledge of the CP nature of the  $t\bar{t}\phi$  coupling through spin-spin correlations [9] whereas  $t\bar{t}\phi$  production can allow a determination of  $v_f$ and  $a_f$  [10]. It should also be possible to exploit the  $\phi ZZ$ coupling via  $\phi \to ZZ \to l^+l^-l'^+l'^-$  [11], and the vector boson fusion mode [12]. At the ILC [7], a rather clean determination of the CP of the Higgs boson should be possible using the Higgsstrahlung process [13]. Angular correlations of the decay products of the  $\phi$ , in particular  $\phi \to f\bar{f}$ , may be used effectively at an  $e^+e^-$  collider to distinguish between  $v_f = 1$ ,  $a_f = 0$  and  $v_f = 0$ ,  $a_f = 1$  as well as to get information on CP mixing [14]. A remark is in order here. The different methods which exploit the  $VV\phi$  coupling test the terms with tensor structure  $g_{\mu\nu}$ and  $\epsilon_{\mu\nu\rho\sigma}$  in Eq. (2); actually in most cases the CP-even part  $\propto g_{\mu\nu}$  is projected out since in most CP violating (CPV) extensions of the SM one has  $A_V \gg B_V$ ,  $C_V$ . The  $f\bar{f}\phi$  coupling, on the other hand, allows equal sensitivity

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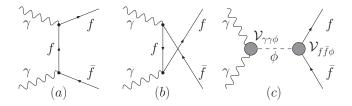


FIG. 1: Feynman diagrams contributing to  $\gamma\gamma \to f\bar{f}$  production.

to the CP-even and CP-odd parts. At both colliders, the LHC and the ILC, the determination of the CP quantum number of the Higgs boson seems feasible, while determination of CP mixing seems difficult; the best chance for the latter being offered by the exploitation of the  $f\bar{f}\phi$  coupling [15].

A more sensitive laboratory for studying the CP properties of a neutral Higgs boson is the photon collider option [16] of the ILC. At a photon collider, the Higgs boson is produced resonantly in the s-channel and thus one will be able to produce it copiously even if the  $\gamma\gamma\phi$  coupling is small. In presence of CP violation (CPV), the CP-even and CP-odd components of the Higgs couple to photons with comparable strength. A study of the production rates with linearly- and circularly-polarized photons can help determine the CP quantum numbers if conserved, as well as the CP mixing phases in the case of CP violation. Angular distributions of decay products (VV, bb) of the produced  $\phi$  along with measurements of  $\Gamma(\phi \to b\bar{b}), \ \Gamma(\phi \to \gamma\gamma)$  may also allow the determination of a CP-mixing phase [17]; the  $\phi \to t\bar{t}$  decay can also be used [18, 19] if it is kinematically allowed. While a complete reconstruction of couplings would require both circularly and linearly polarized photons [18], substantial information can already be obtained using circularly polarized photons alone [19]. Polarization of the final state fermions, which are pair produced, can be a probe of CP violation in the production process [18, 19, 20]. Among SM fermions, the polarization can be measured only for t-quarks and tau-leptons. The t-quark decays before it hadronizes and hence the polarization information gets reflected in the angular distributions of decay products, whereas for the  $\tau$  lepton one can extract polarization information by looking at the energy distribution of pions [21, 22]. For a Higgs mass larger than  $2m_t$ , top polarization is the best probe of the Higgs interaction. However, for a CP-violating light Higgs boson, which could have escaped detection at LEP, the decay into  $t\bar{t}$  is not possible. In this case the  $\tau^+\tau^-$  final state might provide a useful probe. We therefore study the contribution of a light Higgs boson to  $\tau$  production via  $\gamma\gamma \to \phi \to \tau^+\tau^-$  and that of heavier Higgs bosons to t production via  $\gamma\gamma \to \phi \to t\bar{t}$ . Higgs contribution to  $\tau$ polarization has also been studied recently for the LHC [23], for a photon collider [24] and for an  $e^+e^-$  linear collider [25] in the context of resonant CP violation in the MSSM. The effect of neutral Higgs boson exchange in  $\gamma\gamma \to t\bar{t}$  has been addressed in Ref. [18, 19, 26], in

terms of various correlations and asymmetries for a photon collider.

In this paper, we investigate the possibility of using tau/top polarization to get information on the  $\phi f \bar{f}$  and  $\phi\gamma\gamma$  couplings, as well as to probe possible CP violation in them in a generic scenario. First, we formulate the method in a model-independent way. We then apply it in a numerical analysis to the minimal supersymmetric standard model with CP violation (CPV-MSSM). The neutral Higgs sector of the CPV-MSSM has been studied in detail theoretically [27], and constraints from LEP are available [5]. In this work, we study  $\tau/t$  polarization in the CPX scenario [28] over regions of the CPV-MSSM parameter space that are allowed by the current data, and assess the feasibility of using it to probe the Higgs contribution to  $f\bar{f}$  production. In the numerical analysis, we use CPsuperH [29] and FeynHiggs 2.1 [30] for calculating the masses, the decay widths and the relevant couplings of the Higgs bosons.

The rest of the paper is organized as follows. In section II, we describe fermion pair production at a  $\gamma\gamma$  collider in a model-independent way. Section III deals with polarization observables as potential probes of the Higgs contribution and its CP structure. Numerical results within the CPV-MSSM are presented in section IV, and in section V we present our conclusions.

# II. FERMION PAIR PRODUCTION IN $\gamma\gamma$ COLLISION

At a photon collider, the production of a fermion pair involves the  $\gamma f \bar{f}$ ,  $\gamma \gamma \phi$  and  $\phi f \bar{f}$  vertices as shown in Fig. 1. We take the  $\gamma f \bar{f}$  vertex to be the standard QED one, while the vertices involving Higgs bosons are taken to be the most general allowed. The model independent vertex for Higgs interactions with fermions is given in Eq. (1) and with a pair of photons, allowing for CP violation, can be written as :

$$\mathcal{V}^{\mu\nu}_{\gamma\gamma\phi} = \frac{-i\sqrt{s}\alpha}{4\pi} \left[ A_{\gamma}(s) \left( g^{\mu\nu} - \frac{2}{s} k_1^{\nu} k_2^{\mu} \right) - B_{\gamma}(s) \frac{2}{s} \epsilon^{\mu\nu\alpha\beta} k_{1\alpha} k_{2\beta} \right]. \tag{3}$$

Here  $k_1$  and  $k_2$  are the four-momenta of the colliding photons. The helicity amplitudes for fermion pair production in the s- and the t/u-channels can be obtained from those given in [18, 19]:

those given in [16, 15].  

$$M_{\phi}(\lambda_{1}, \lambda_{2}; \lambda_{f}, \lambda_{\bar{f}}) = \frac{-ig\alpha m_{f}}{8\pi M_{W}} \frac{s}{s - m_{\phi}^{2} + im_{\phi}\Gamma_{\phi}}$$

$$[A_{\gamma}(s) + i\lambda_{1}B_{\gamma}(s)] [\lambda_{f}\beta v_{f} - ia_{f}] \delta_{\lambda_{1},\lambda_{2}}\delta_{\lambda_{f},\lambda_{\bar{f}}}, (4)$$

$$M_{QED}(\lambda_{1}, \lambda_{2}; \lambda_{f}, \lambda_{\bar{f}}) = \frac{-i4\pi\alpha Q^{2}}{1 - \beta^{2}\cos^{2}\theta_{f}}$$

$$\left[\frac{4m_{f}}{\sqrt{s}} (\lambda_{1} + \lambda_{f}\beta) \delta_{\lambda_{1},\lambda_{2}}\delta_{\lambda_{f},\lambda_{\bar{f}}} - \frac{4m_{f}}{\sqrt{s}} \lambda_{f}\beta\sin^{2}\theta_{f} \delta_{\lambda_{1},-\lambda_{2}}\delta_{\lambda_{f},\lambda_{\bar{f}}} - 2\beta (\cos\theta_{f} + \lambda_{1}\lambda_{f})\sin\theta_{f} \delta_{\lambda_{1},-\lambda_{2}}\delta_{\lambda_{f},-\lambda_{\bar{f}}}\right]. (5)$$

TABLE I: Combinations of form factors  $v_f$ ,  $a_f$ ,  $A_{\gamma}$  and  $B_{\gamma}$  that occur in the helicity amplitudes of Eqs. (4) and (5).

| Combination        | Alias | CP   | Combination        | Alias | CP   |
|--------------------|-------|------|--------------------|-------|------|
| $v_f\Re(A_\gamma)$ | $x_1$ | even | $v_f\Im(A_\gamma)$ | $x_2$ | even |
| $v_f\Re(B_\gamma)$ | $y_1$ | odd  | $v_f\Im(B_\gamma)$ | $y_2$ | odd  |
| $a_f\Re(A_\gamma)$ | $y_3$ | odd  | $a_f\Im(A_\gamma)$ | $y_4$ | odd  |
| $a_f\Re(B_\gamma)$ | $x_3$ | even | $a_f\Im(B_\gamma)$ | $x_4$ | even |

The form factors  $A_{\gamma}$  and  $B_{\gamma}$  are complex whereas  $v_f, a_f$  can be taken to be real without loss of generality. The non-standard vertices given by Eqs. (1) and (3) involve four independent form factors:  $v_f, a_f, A_{\gamma}, B_{\gamma}$ . In the MSSM with CPV, these form factors are functions of various model parameters:  $\tan \beta; m_{H^+}; (|\mu|, \Phi_{\mu}); (|A_{\bar{f}}|, \Phi_{\bar{f}}); (|M_i|, \Phi_i), i = 1, 2, 3; m_{\tilde{q}, \tilde{l}};$  etc., where  $(|x|, \Phi_x)$  denotes  $x = |x|e^{i\Phi_x}$ .

The helicity amplitudes of Eqs. (4) and (5) involve only certain combinations of the form factors which are listed in Table I. Only five of these eight combinations are independent, the other three can be obtained by interrelations such as  $x_1x_3 = y_1y_3$ , etc. In all the extensions of the SM,  $A_{\gamma}$  and  $B_{\gamma}$  are generated at the one-loop level. Simultaneous existence of  $v_f$  and  $a_f$ , or  $A_{\gamma}$  and  $B_{\gamma}$  violates CP, i.e. non-vanishing values of  $y_i$ , (i=1,...,4) imply CP violation. Even in case of CP invariance, where only the  $x_i$ 's are non-zero, the Higgs contribution can alter the polarization of the fermions f from that predicted by pure QED. CP violation, giving rise to non-zero  $y_i$ 's, gives an additional contribution to the fermion polarization.

It should be noted that the Higgs-mediated diagram contributes only when the helicities of the colliding photons are equal. The helicities of f and  $\bar{f}$  are also equal in this case. The QED contribution for this helicity combination is proportional to the fermion mass. Both these facts indicate that one should choose equal photon helicities to enhance the effect of the Higgs mediated diagram. The contribution with opposite helicities of photons comes from QED diagrams alone and it is large as compared to that of equal photon helicities for  $\sqrt{s} \gg 4m_f$ . Thus with unpolarized photons the net contribution from Higgs exchange will be relatively small. Hence one expects poor sensitivity to the Higgs contribution with unpolarized initial state photons.

Among the vertices contributing to fermion-pair production, the standard  $\gamma f \bar{f}$  vertex conserves chirality, while the  $\phi f \bar{f}$  vertex mixes different chiralities. Owing to the finite mass  $m_f$  of the fermion, there is a chirality-mixing contribution even for the pure QED diagrams (Figs. 1a,b). The presence of the Higgs boson exchange, Fig. 1c, provides an additional, polarization dependent, spatially isotropic, chirality-mixing contribution. The property of spatial isotropy is unique to Higgs exchange contribution, in contrast to other means of chirality mixing, such as the finite mass effect. With unpolarized initial-state photons, the QED as well as a CP-conserving Higgs contribution lead to unpolarized fermions in the final state; CP violation in the Higgs sector leads to a net, though very small, fermion polarization. With

polarized initial-state photons, already pure QED leads to a finite polarization. The additional chirality mixing from the Higgs exchange causes a change in this polarization in both the CP-conserving and the CP-violating case. It is thus possible to construct observables relating initial-state photon and final-state  $\tau/t$  polarizations which probe the Higgs couplings as well as possible CP violation in the Higgs sector.

## III. FERMION POLARIZATION IN $\gamma\gamma$ COLLISION

At a  $\gamma\gamma$  collider, Compton back-scattering of a laser from  $e^-/e^+$  is used to produce high-energy photons[31]. The energy spectrum of the back-scattered photons depends upon the polarizations of the  $e^-/e^+$  beams and the laser as shown in Fig. 2. This figure shows the distribution of the reduced invariant mass of the  $\gamma\gamma$  system  $z = \sqrt{\omega_1\omega_2}/E_b$ , where  $\omega_{1,2}$  are the energies of the two colliding photons in the lab frame, for a laser energy  $\omega_0$  corresponding to

$$x_c = \frac{4E_b\omega_0}{m_c^2} = 4.8. (6)$$

The spectrum is peaked in the high energy region for opposite polarizations of the electron and laser beams. Further, most of these high-energy photons have a large degree of polarization. By choosing appropriate polarizations for the  $e^-/e^+$  and laser beams, one can thus obtain a peaked and highly polarized spectrum for the colliding photons. We shall use this fact when constructing various observables with  $\tau$  polarization.

The polarization of fermions is defined as the fractional surplus of positive helicity fermions over negative helicity ones, i.e.

$$P_f^{ij} = \frac{N_+^{ij} - N_-^{ij}}{N_+^{ij} + N_-^{ij}} \,, \tag{7}$$

where the superscript ij stands for the polarizations of the parent  $e^-$ ,  $e^+$  beams of the ILC (with  $P_f^{++}$  meaning 100% right polarized electrons and 100% right polarized positrons);  $N_+$  and  $N_-$  stands for the number of fermions with positive and negative helicities, respectively. Analogously,  $\bar{P}_f^{ij}$  is the polarization of the anti-fermion. Due to the left-chiral nature of the W-boson interaction, the positively and negatively polarized f's lead to different distributions of the decay products. For  $\tau$ 's, by looking at the net energy distribution of decay  $\pi$  one can get information on its polarization [21]. On the other hand, for t-quarks, it is the energy distribution of b-quarks or the angular distribution of decay leptons.

the angular distribution of decay leptons. The various  $N_{\pm}^{ij}$ , and hence  $P_f^{ij}$ , with different polarizations of initial-state photons are related to each other via discrete symmetry transformations, such as C, P and CP, if these symmetries are respected by the underlying dynamics. Thus any deviation from these relations can be a probe of the violation of the corresponding discrete symmetry.

For unpolarized initial-state photons the polarization,  $P_f^U$ , is zero for the QED diagrams (Figs. 1a,b). Even in

TABLE II: Polarization observables and interactions and combinations that they can probe.

| Observables                                  | Interactions                      | Combinations       |  |
|--|-----------------------------------|--------------------|--|
|  | probed                            | probed             |  |
| $P_f^U$                                      | P/CP violating                    | $y_i$ 's           |  |
| $\delta P_f^+ = P_f^{++} - (P_f^{++})^{QED}$ | Chirality-mixing                  | $x_i$ 's, $y_i$ 's |  |
| $\delta P_f^- = P_f^{} - (P_f^{})^{QED}$     | Chirality-mixing $P/CP$ violating | $x_i$ 's, $y_i$ 's |  |
| $\delta P_f^{\text{CP}} = P_f^{++} + P_f^{}$ | P/CP violating                    | $y_i$ 's           |  |

the presence of a CP-conserving Higgs  $P_f^U$  is zero. This is because the left chiral and the right chiral components of fermions couple to the Higgs boson with equal strength. Thus the net polarization of the fermions, if any, will signal CP violation in the Higgs sector. In general it is a signal of P violation, but in the process under consideration f couples only to self-conjugate neutral particles,  $\gamma$  and  $\phi$ . Hence  $P_f^U \neq 0$  is also a signal of CP violation. We note that  $P_f^U$  is a pure but a poor probe of CPV. For polarized initial state photons, QED predicts a

For polarized initial state photons, QED predicts a non-zero value of  $P_f$  and this prediction is modified by the presence of the Higgs exchange diagram. The deviation from the QED prediction is a probe of the Higgs contribution and hence its couplings. We define

$$\delta P_f^+ = P_f^{++} - (P_f^{++})^{QED},$$
 (8)

$$\delta P_f^- = P_f^{--} - (P_f^{--})^{QED}. \tag{9}$$

Such a deviation does not have any definite P or CP property, thus it can be non-zero even when the Higgs boson is a CP eigenstate. This allows us to detect the presence of a Higgs over a large range of  $x_i$ 's and  $y_i$ 's (and hence a large range of model parameters, as we will see later) by measuring the fermion  $(t/\tau)$  polarization. We choose equal polarization of  $e^+$  and  $e^-$  beams so as to have equal helicities for the colliding photons; this enhances the chirality-mixing Higgs contribution as discussed in the previous section, c.f. Eqs. (4) and (5).

In QED, the polarization of f flips its sign if we change the signs of the polarizations of the initial state photons (actually those of the electron and positron of the parent collider), i.e.  $P_f^{++} = -P_f^{--}$ . This is due to P invariance of QED. Also, due to the self-conjugate nature of the neutral particles involved, we have  $P_f^{ii} = \bar{P}_f^{ii}$ . In CP-violating models, however, we expect  $P_f^{++} + P_f^{--} \neq 0$ . Although it is a probe of P violation in general, it will be a probe of CP violation in our process. In Table II we list all the observables and their potentials. The definitions in Eqs. (8) and (9), along with the fact that  $(P_f^{++})^{QED} = -(P_f^{--})^{QED}$ , implies

$$\delta P_f^{\rm CP} = \delta P_f^+ + \delta P_f^-. \tag{10}$$

For polarized photons we therefore have two independent observables,  $\delta P_f^-$  and  $\delta P_f^{\rm CP}$ . These can be sizable over a large range of, for instance, MSSM parameters and hence can be used to probe the Higgs interactions. As we have already mentioned, the expected polarization  $P_f^U$  for unpolarized photons is very small. In Fig. 3 we show, as an example, expected values of  $\delta P_\tau^\pm$  and  $\delta P_\tau^{\rm CP}$  as functions of  $E_b$  for a Higgs mass of 54 GeV and  $v_\tau=2.0$ ,

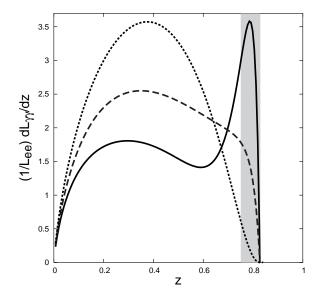


FIG. 2: Luminosity distribution plotted against z (which is related to the  $\gamma\gamma$  invariant mass  $W=2\sqrt{\omega_1\omega_2}$  via  $z=W/(2E_b)$ ) for  $x_c=4.8$ . The solid line corresponds to  $\lambda_e\lambda_l=-1$ , the short-dashed line is for  $\lambda_e\lambda_l=1$ , and the long-dashed one for  $\lambda_e\lambda_l=0$ . The conversion distance is taken to be zero. The grey patch highlights the region 0.75 < z < 0.83.

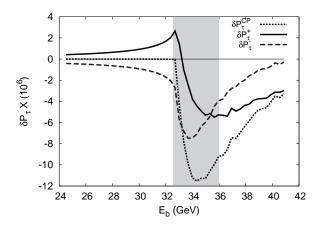


FIG. 3: Variation of  $\delta P^+$ ,  $\delta P^-$  and  $\delta P^{\rm CP}$  as a function of  $E_b$  for a Higgs boson of mass 54 GeV. For a value of  $E_b$  in the grey patch, the mass of the Higgs boson matches with the  $\gamma\gamma$  invariant mass in the grey band shown in Fig. 2.

 $a_{\tau} = -2.3$ ,  $A_{\gamma} = -0.76 + 0.032i$ ,  $B_{\gamma} = -0.13 + 0.039i$ . The peak in  $\delta P$  occurs when the Higgs mass matches with the  $\gamma \gamma$  invariant mass corresponding to the peak of photon spectrum in Fig. 2. By adjusting the beam energy  $E_b$ , we can thus maximize the sensitivity of the polarization observables defined above. Details of the selection criteria for  $E_b$  for a scan over the parameters of a model are discussed in Section V.

### IV. THE CPV-MSSM HIGGS SECTOR

We choose the MSSM as an example for demonstrating the potential of the observables constructed in the previous section to isolate the Higgs boson contribution

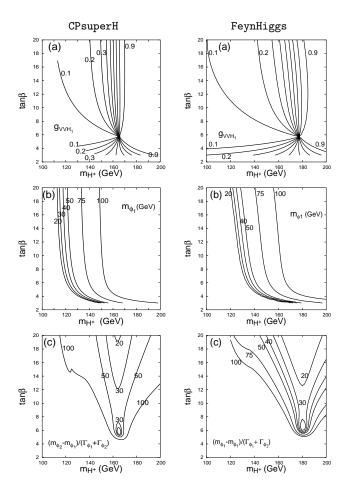


FIG. 4: CPX scenario: contours of (a)  $A_V$  (see Eq.(2)) for V=W,Z, (b)  $m_{\phi_1}$  and (c)  $(m_{\phi_2}-m_{\phi_1})/(\Gamma_{\phi_1}+\Gamma_{\phi_2})$  computed with CPsuperH as well as FeynHiggs.

TABLE III: List of MSSM parameters for the CPX scenario used as input for the programs CPsuperH and FeynHiggs.

| MSSM         | Value  | MSSM                        | Value  |
|--------------|--|-----------------------------|--|
| param.       |  | param.                      |  |
| $\tan \beta$ | 3-40 (for scan)<br>2 TeV, $\Phi_{\mu} = 0$<br>1 TeV, $\Phi_{3} = 90^{\circ}$ | $m_{H^+}$                   | 150-500  GeV (for scan)                      |
| $\mu$        | $2 \text{ TeV}, \Phi_{\mu} = 0$  | $M_1, M_2$                  | 200 GeV, $\Phi_{1,2} = 0$                    |
| $M_3$        | 1 TeV, $\Phi_3 = 90^{\circ}$   | $m_{\tilde{a}}$ $\tilde{i}$ | $500 \; \mathrm{GeV}$                        |
| $A_{t,b}$    | 1 TeV, $\Phi_{t,b} = 90^{\circ}$   | $A_{	au}^{\eta, i}$         | $500 \text{ GeV},  \Phi_{\tau} = 90^{\circ}$ |

and to probe the CP properties of its couplings. In the CP-conserving MSSM, there exist three neutral Higgs bosons: the CP-even h, H and the CP-odd A. CPviolating phases of the MSSM parameters such as the higgsino mass parameter  $\mu$ , gaugino masses  $M_i$  (i = 1, 2, 3) and trilinear couplings  $A_f$   $(f = t, b, \tau)$ , can induce CP violation in the Higgs sector via loops. This allows Higgs states with different CP to mix; the three mass eigenstates hence do not have definite CP. These states are denoted by  $\phi_1$ ,  $\phi_2$  and  $\phi_3$  with their masses in increasing order. For the numerical analysis, we choose the so-called CPX [28] scenario with parameters as listed in Table III. In this scenario, one can have large CP-violating effects in the Higgs sector depending upon the size of the phases of the trilinear couplings  $A_{t,b,\tau}$ . Due to this large CP violation, the coupling of the lightest state  $\phi_1$  to vector

bosons can go down drastically for some values of  $m_{H^+}$ and  $\tan \beta$ , see Fig. 4(a). This results in highly suppressed production rates for the lightest Higgs boson; the lower bound on the mass of such a Higgs boson from direct searches at LEP can be as low as 10–50 GeV [5]. We take into account all three neutral Higgs bosons in the calculation of the fermion polarization by adding their s-channel diagrams. This may, however, not be valid in some regions of the CPV-MSSM parameter space where the Higgs masses become nearly degenerate, i.e. the mass difference of two Higgs bosons is smaller than sum of their widths and hence mixing between these states is resonantly enhanced. In this case one should do a coupled channel analyze [26, 32] of the degenerate states. Fortunately, in the region of parameter space we consider, the mass differences are always much larger than the sum of the decay widths, see Fig. 4(c). Thus our analysis is complementary to that of Refs. [26, 32].

#### V. NUMERICAL RESULTS

At a photon collider, the center of mass energy of the colliding photons is not fixed but has a wide spectrum. The shape of this spectrum depends upon the polarizations of the laser and the  $e^+/e^-$  beams of the parent collider. For the numerical calculation of cross sections, we use the ideal Compton back-scattered spectrum [31] with polarizations of the electron beam and the laser chosen such that one obtains the hard spectrum in Fig 2. The parent electron beam energy,  $E_b$ , can be chosen to maximize the deviation from the QED prediction, cf. Fig. 3. Our observables are maximized when the Higgs mass matches the value of the  $\gamma\gamma$  invariant mass at the peak of the polarized photon spectrum. This happens for  $E_b = (m_{\phi_i}/2)/z$ , where z (the scaled  $\gamma \gamma$  invariant mass,  $z = \sqrt{\omega_1 \omega_2}/E_b$ ) takes a value between 0.75 to 0.83 for  $x_c = 4.8$ . This corresponds to the case where the scaled Higgs mass,  $m_{\phi_i}/2E_b$ , lies in the grey band of Fig. 2.

We can therefore pursue two different strategies for choosing  $E_b$ :

- 1. Parameterizing the relationship between  $m_{\phi_i}$  and  $E_b$  in terms of  $z_0$  as  $E_b = (m_{\phi_i}/2)/z_0$ , we choose an optimal value of  $z_0$ , say  $z_0 = 0.80$ , for each point in the scan such that  $\delta P$  is maximized. This gives a very good estimate of the ultimate potential of the particular observable used in adaptation. We call this the "peak  $E_b$ " choice.
- 2. Fixing  $E_b$  such that the relevant Higgs mass  $(m_{\phi_1}$  for  $\tau^+\tau^-$  and  $m_{\phi_2,\phi_3}$  for  $t\bar{t}$  production) matches approximately with the  $\gamma\gamma$  invariant mass corresponding to z values within the peak of the photon spectrum (the grey band in Fig. 2). Though this choice does not exploit the observable optimally, it is closer to what will be done in a realistic experiment. We call this the "fixed  $E_b$ " choice.

In the case of  $\tau$  polarization, due to the small values of  $m_{\tau}$  and  $\Gamma_{\phi_1}$ , the absolute values of the polarization observables are  $\lesssim 10^{-5}$ . These can be enhanced by

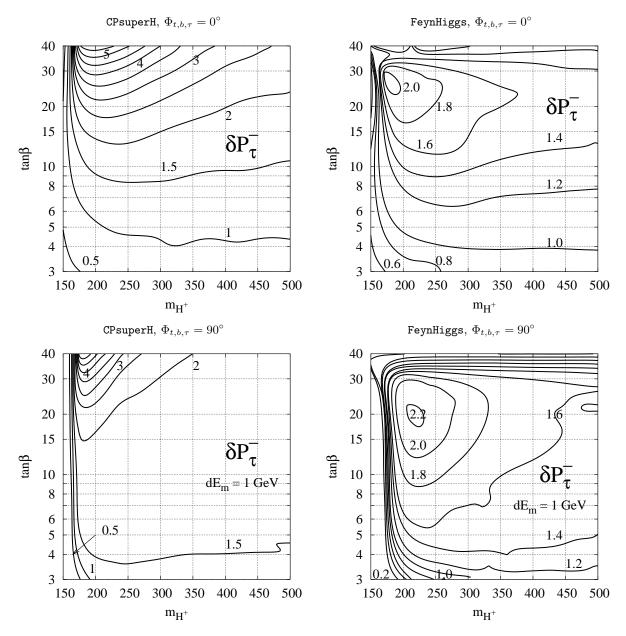


FIG. 5: Contours of constant  $\delta P_{\tau}^-$  in units of  $10^{-2}$  in the  $(\tan \beta - m_{H^+})$  plane for the CPX scenario with  $\Phi_{t,b,\tau} = 0^{\circ}$  (top panels) and  $\Phi_{t,b,\tau} = 90^{\circ}$  (bottom panels) for the "peak  $E_b$ " choice with  $dE_m = 1$  GeV. The left panels show the results obtained with CPsuperH, the rights panels those obtained with FeynHiggs.

putting a cut on the invariant mass of the  $\tau^+\tau^-$  pair to select the ones coming from  $\phi_1$  decay [33]:

$$|m_{\tau\tau} - m_{\phi_1}| \le \max(dE_m, 5 \Gamma_{\phi_1}),$$
 (11)

where  $dE_m$  is the minimum resolution of  $m_{\tau\tau}$  reconstruction. We use  $dE_m=1$  GeV for purposes of illustration in this paper. For the case of top production such a cut is not necessary.

In the following, we perform a scan over the MSSM parameters as given in Table III and calculate the  $\tau$  and t polarization observables for both the peak and the fixed  $E_b$  choices using both CPsuperH and FeynHiggs for calculating the Higgs masses, couplings, and widths. The statistical fluctuation in the value of the fermion polar-

ization is given by

$$\Delta P_f = \frac{\sqrt{1 - P_f^2}}{\sqrt{N_+ + N_-}} \,. \tag{12}$$

The typical value of  $\Delta P_f$  for an integrated luminosity of 100 fb<sup>-1</sup> is about 0.003 for a total rate of 1 pb. The typical  $\tau$ -pair production rate with the above cut is about 1–10 pb over the  $(\tan \beta - m_{H^+})$  plane.  $\tau$  decays into hadronic channels reduce the useful cross section and hence cause this error to increase. As a conservative measure we take  $\delta P_{\tau} \geq 0.01$  in order to be measurable. The  $t\bar{t}$  production rate, on the other hand, is less than 1 pb for the energies considered, and it can be as low as 8 fb with the "peak  $E_b$ " choice in some regions of the  $(\tan \beta - m_{H^+})$  plane. Thus the statistical error in the polarization measurements.

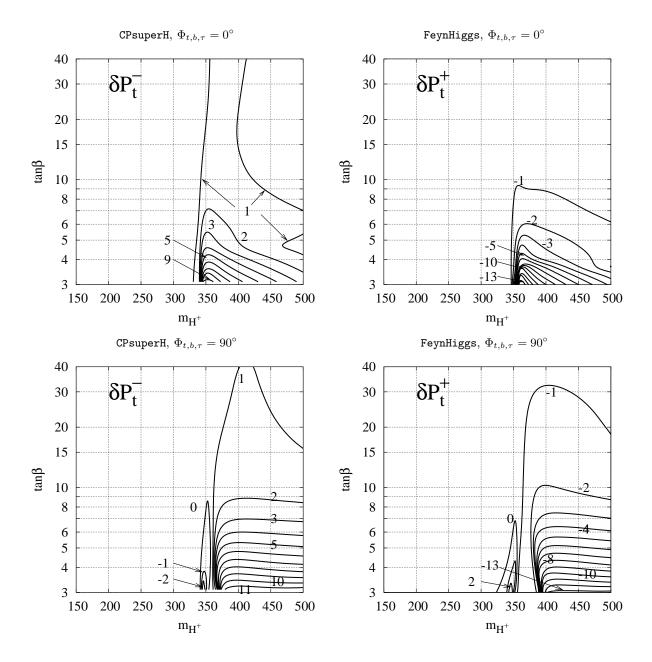


FIG. 6: Contours of constant  $\delta P_t^{\pm}$  in units of  $10^{-2}$  in the  $(\tan \beta - m_{H^+})$  plane for the CPX scenario with  $\Phi_{t,b,\tau} = 0^{\circ}$  (top panels) and  $\Phi_{t,b,\tau} = 90^{\circ}$  (bottom panels) for the "peak  $E_b$ " choice. The left panels show the results for  $\delta P_t^-$  obtained with CPsuperH and the rights panels those for  $\delta P_t^+$  obtained with FeynHiggs, see text.

surement goes up and the sensitivity goes down in this case, even if the polarization asymmetry is large.

## A. Peak $E_b$ scan

We first discuss the case of  $\tau$ -pair production through  $\phi_1$  exchange for the "peak  $E_b$ " choice. Figure 5 shows contours of constant  $\delta P_{\tau}^-$  as obtained with CPsuperH and FeynHiggs in the  $(\tan \beta - m_{H^+})$  plane for  $\Phi_{t,b,\tau} = 0^\circ$  and  $\Phi_{t,b,\tau} = 90^\circ$ . For each point in the scan, the beam energy is set to  $E_b = m_{\phi_1}/(2z_0)$  to maximize  $\delta P_{\tau}^{\pm}$ . In the CP-conserving case,  $\Phi_{t,b,\tau} = 0^\circ$ ,  $\delta P_{\tau}^-$  should be measurable for  $\tan \beta \geq 4$  and  $m_{H^+} \geq 200$  GeV; smaller values of  $m_{H^+}$  require somewhat higher  $\tan \beta$  to achieve

 $\delta P_{\tau}^- \geq 0.01.$  In the case of maximal CPV phases,  $\Phi_{t,b,\tau} = 90^{\circ}, \delta P_{\tau}^- > 0.01$  holds over practically the entire parameter range, including the region where a very light Higgs boson may have been missed at LEP2 [5]. Such a light CPV Higgs boson will also be difficult to discover at the LHC [34]. The process  $\gamma\gamma \to \tau^+\tau^-$  may hence offer a unique possibility for this case. While  $\delta P_{\tau}^-$  covers a large part of the parameter space, the CP-odd observable  $\delta P_{\tau}^{\rm CP}$  is very small,  $\delta P_{\tau}^{\rm CP} \sim 10^{-5},$  and hence below the limit of measurability even if the CPV phases are maximal. This means in turn that  $\delta P_{\tau}^+ \approx -\delta P_{\tau}^-$ . It is also worth noting that the size of the observable is rather sensitive to the value of  $dE_m$ : increasing for instance  $dE_m$  from 1 GeV to 2 GeV,  $\delta P_{\tau}^-$  goes down by about a factor of 2 over most of the parameter space in Fig. 5.

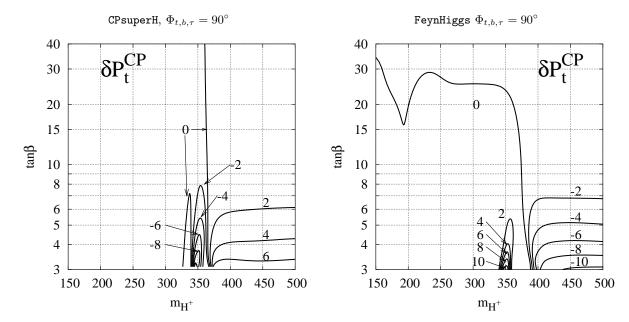


FIG. 7: Contours of constant  $\delta P_t^{\rm CP}$  in units of  $10^{-2}$  in the  $(\tan \beta - m_{H^+})$  plane for the CPX scenario with  $\Phi_{t,b,\tau} = 90^{\circ}$  and "peak  $E_b$ " choice. The left panel shows the results obtained with CPsuperH, the right panel those obtained with FeynHiggs.

Let us now turn to the top polarization in  $\gamma\gamma \to t\bar{t}$ . Due to the large top quark mass, here only the heavier Higgs bosons  $\phi_{2,3}$  contribute. For the comparatively large  $m_{H^+}$  values needed to obtain  $m_{\phi_{2,3}} \geq 2m_t$ , the mass difference between  $\phi_2$  and  $\phi_3$  is usually so small that both their scaled masses can be within the peak of the hard photon spectrum of Fig. 2, although  $m_{\phi_3} - m_{\phi_2} \gg \Gamma_{2,3}$  is still maintained. We therefore choose

$$E_b^{peak} = \max \left[ E_b^0, (m_{\phi_2} + m_{\phi_3})/(4z_0) \right],$$
 (13)

where  $E_b^0=220~{\rm GeV}$  and  $z_0=0.8$ . Figure 6 shows contours of constant  $\delta P_t^\pm$  in the  $(\tan\beta-m_{H^+})$  plane analogous to Fig. 5. Owing to different sign conventions the two programs,  $\delta P_t^\pm$  of CPsuperH corresponds to  $-\delta P_t^\mp$  in FeynHiggs. In Fig. 6 we therefore plot  $\delta P_t^-$  for CPsuperH and  $\delta P_t^+$  for FeynHiggs. The deviation from the pure QED prediction (i.e. the Higgs contribution) is sizable for  $\tan\beta\lesssim 10$ . Note that the CP-even polarization observables for  $t\bar{t}$  can reach much larger values than those for  $\tau^+\tau^-$ . Moreover, in the case of  $\gamma\gamma\to t\bar{t}$  also the CP-odd observable,  $\delta P_t^{\rm CP}$ , may be large enough to be measurable. This is shown in Fig. 7 for  $\Phi_{t,b,\tau}=90^\circ$ . Because of the low cross sections, ranging from 8 fb to 150 fb in Fig. 7, as compared to 1–10 pb for the  $\tau$  case, the statistical fluctuations are large, about  $\Delta P_t \sim 0.10-0.03$ . Therefore the region of sensitivity to the Higgs-boson contributions is restricted to low  $\tan\beta$  values.

### B. Fixed $E_b$ scan

The "peak  $E_b$ " choice discussed above gives an estimate of the ultimate potential of our polarization observables. In reality, however, one will have a collider running at some fixed beam energy. Obviously it will be of advantage to set  $E_b$  such that one is sensitive to the

Higgs contributions over a large part of the parameter space.

In the CPX scenario, CPsuperH predicts  $m_{\phi_1} \lesssim 123$ GeV. Thus  $E_b = 77$  GeV leads to a good sensitivity over most of the parameter space. With FeynHiggs, however, the maximum value of  $m_{\phi_1}$  considerably changes with  $\Phi_{t,b,\tau}$  in the scan; we obtain maximum values of  $m_{\phi_1} = 123 \text{ GeV for } \Phi_{t,b,\tau} = 0^{\circ} \text{ and } m_{\phi_1} = 131 \text{ GeV for }$  $\Phi_{t,b,\tau} = 90^{\circ}$ , respectively. Hence we choose  $E_b = 77 \text{ GeV}$ for  $\Phi_{t,b,\tau} = 0^{\circ}$  and  $E_b = 82 \text{ GeV}$  for  $\Phi_{t,b,\tau} = 90^{\circ}$  in the computation with FeynHiggs. The polarization observable  $\delta P_{\tau}^{-}$  for this fixed  $E_{b}$  choice is shown in the  $(\tan \beta - m_{H^+})$  plane in Fig. 8. We observe that for  $\Phi_{t,b,\tau} = 90^{\circ}, \, \delta P_{\tau}^{-} \geq 0.01 \text{ unless } \tan \beta \text{ is very small. For}$  $\Phi_{t,b,\tau} = 0^{\circ}$ , on the other hand, observability of  $\delta P_{\tau}^{-}$  is limited to  $\tan \beta \gtrsim 8-10$ . It is apparent that  $\delta P_{\tau}$  will be mainly useful if  $\tan \beta$  is large. To explicitly see the phase dependence we show in Fig. 9 contours of constant  $\delta P_{\tau}^{-}$  in the  $(m_{H^{+}} - \Phi)$  plane for  $E_{b} = 77$  GeV. There is a rather large difference in the results of the two codes, which is also apparent in the other figures, due to differences in the implementation of radiative corrections in the two programs [35]. It is clear that for analyses as suggested in this paper, more precise computations will be necessary.

We next turn to  $t\bar{t}$  production with fixed  $E_b$ . In this case, as for the peak  $E_b$  choice, it is the mean mass of  $\phi_2$  and  $\phi_3$  that should be within the peak of the photon spectrum. However, since  $m_{\phi_{2,3}}$  change linearly with  $m_{H^+}$ , one cannot have optimal sensitivity over the whole parameter space with fixed  $E_b$ . We hence take  $E_b=300$  GeV as a good compromise. For this choice one has comparatively large rates while the scaled masses of  $\phi_{2,3}$  still lie within the peak of the photon spectrum for a sizable portion of the  $(\tan\beta-m_{H^+})$  plane. The results for  $\delta P_t^\pm$  obtained with CPsuperH and FeynHiggs for  $\Phi_{t,b,\tau}=0^\circ$  and  $\Phi_{t,b,\tau}=90^\circ$  are shown in Fig. 10.

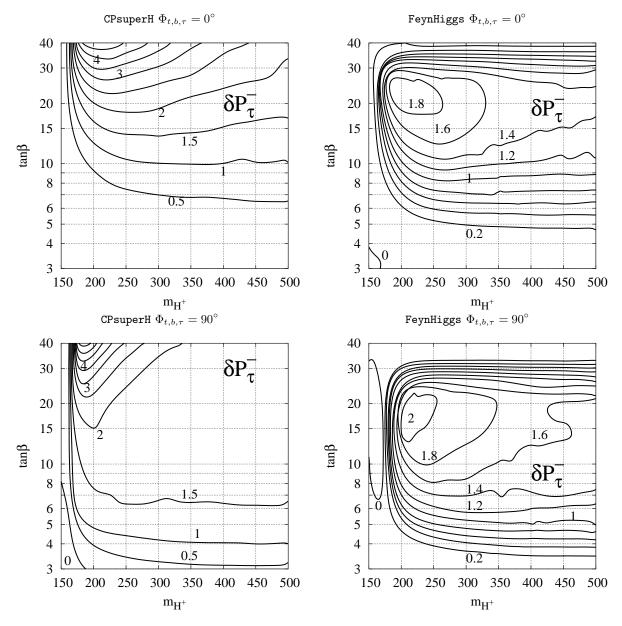


FIG. 8: Contours of constant  $\delta P_{\tau}^-$  in units of  $10^{-2}$  for fixed  $E_b$  and  $\Phi_{t,b,\tau}=0^{\circ}$  and  $90^{\circ}$  using CPsuperH (left panels) and FeynHiggs (right panels) to compute the Higgs masses, couplings and widths.  $E_b=77$  GeV, except for the lower-right plot where  $E_b=82$  GeV, see text.

Again the role of  $\delta P_t^+$  and  $\delta P_t^-$  is interchanged in the two codes. In Fig. 11, we show contours of constant  $\delta P_t^{\rm CP}$  in the  $(\Phi-m_{H^+})$  plane for  $\tan\beta=4$  and in Fig. 12 in the  $(\Phi-\tan\beta)$  plane for  $m_{H^+}=475$  GeV. As one can see, there is sensitivity to CP violation if  $\tan\beta$  is small. Moreover, there is rather good agreement between CPsuperH and FeynHiggs in  $\delta P_t^{\rm CP}$  (up to a sign). Note also that the signal can be enhanced by tuning  $E_b$ .

Comparing these results with the "peak  $E_b$ " choice, we see that for  $\gamma\gamma \to \tau\tau$  one can be sensitive to as large a region of the parameter space if  $E_b$  is chosen carefully. For  $\gamma\gamma \to t\bar{t}$ , on the other hand, we loose sensitivity to part of the parameters space with fixed  $E_b$ .

#### C. Lepton asymmetries

The polarization of  $\tau$  leptons can be measured using the energy distribution of the decay pions [22, 36, 37, 38, 39, 40]. The polarization of top quarks can be measured using energy distribution of b quarks [41] or the angular distribution of decay leptons [42, 43, 44, 45]. This kind of analysis requires the full reconstruction of the top momentum. Such a reconstruction may not always be possible for the semi-leptonic decay of the t (or  $\bar{t}$ ) quark. On the other hand, it is possible to construct simple asymmetries involving the polarization of the initial-state  $e^{\pm}$  (and hence of the photons) and the charge of the final-state lepton, which are sensitive to CP violation. We denote the integrated cross section for the process  $\gamma\gamma \to t\bar{t} \to l^+\nu b\bar{t}$  ( $tl^-\bar{\nu}b$ ) by  $\sigma(\lambda_{e^-},Q_l)$ , where  $\lambda_{e^-}$ 

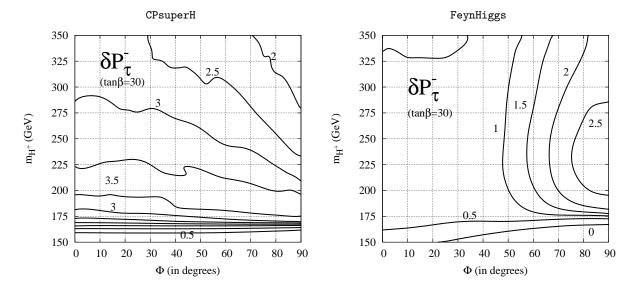


FIG. 9: Contours of constant  $\delta P_{\tau}^-$  in units of  $10^{-2}$  in the  $(\Phi_{t,b,\tau} - m_{H^+})$  plane for  $\tan \beta = 30$  and  $E_b = 77$  GeV with CPsuperH (left panel) and FeynHiggs (right panel).

is the polarization of the electron beam in the parent collider and  $Q_l$  the charge of the secondary lepton coming from the  $t/(\bar{t})$  decay. The polarizations of all the other beams are adjusted to get a peaked spectrum and equal helicities for the incident photons. With this setup, we can define the following asymmetries [19]:

$$\mathcal{A}_{1} = \frac{\sigma(+,+) - \sigma(-,-)}{\sigma(+,+) + \sigma(-,-)}, 
\mathcal{A}_{2} = \frac{\sigma(+,-) - \sigma(-,+)}{\sigma(+,-) + \sigma(-,+)}, 
\mathcal{A}_{3} = \frac{\sigma(+,+) - \sigma(-,+)}{\sigma(+,+) + \sigma(-,+)}, 
\mathcal{A}_{4} = \frac{\sigma(+,-) - \sigma(-,-)}{\sigma(+,-) + \sigma(-,-)},$$
(14)

Only one of the above asymmetries is independent [19] if no cut is put on the lepton's polar angle in the laboratory frame. Even with a finite cut on the polar angle, the  $A_{1...4}$  have almost identical sensitivities to the Higgs couplings. We use a  $20^{\circ}$  beam-pipe cut on the lepton. The contours of constant  $A_3$  for  $\Phi_{t,b,\tau} = 30^{\circ}$  and  $90^{\circ}$ , using CPsuperH, are shown in Fig. 13 for the "peak  $E_b$ " choice. Analogously, Fig. 14 shows  $A_3$  for fixed  $E_b = 300 \text{ GeV}$ and  $\Phi_{t,b,\tau} = 30^{\circ}$  and  $90^{\circ}$ . The asymmetries are sizable for  $\Phi_{t,b,\tau} = 90^{\circ}$  and decrease rapidly as  $\Phi_{t,b,\tau}$  decreases. For  $\Phi_{t,b,\tau} = 0^{\circ}$  the only source of CPV is the phase of  $M_3$ ,  $\Phi_3 = 90^{\circ}$ , in our scenario. All the  $y_i$ 's are then negligibly small as compared to the  $x_i$ 's, leading to very small values of the  $A_i$ . Here note that, as shown in Ref. [19], the lepton asymmetries of Eq. (14) are sensitive only to CP-odd combinations of the form factors, i.e. the  $y_i$ 's. This should be contrasted with the polarization observables, which are sensitive to both the CP-odd and CPeven combinations.

#### VI. CONCLUSIONS

We have investigated the use of fermion polarization in the process  $\gamma\gamma\to f\bar f$  (with f=t or  $\tau$ ) for studying neutral Higgs bosons at a photon collider. To this aim we have constructed polarization asymmetries  $\delta P_f^\pm$ , which are sensitive to the Higgs exchange contributions. We have also constructed a CP-odd asymmetry  $\delta P_f^{\rm CP}$  which is sensitive to CP violation in the Higgs sector. All these asymmetries are constructed in a model-independent way and can be used to study Higgs bosons in various models beyond the SM.

We have applied this in a numerical analysis to the case of the MSSM with explicit CP violation. In particular we have evaluated our asymmetries for the CPX scenario, using the two public codes CPsuperH and FeynHiggs to calculate the Higgs masses, couplings and widths.

Scanning the  $(\tan \beta - m_{H^+})$  plane for various phases  $\Phi_{t,b,\tau}$ , we found that  $\delta P_{\tau}^{\pm}$  is sensitive to a light Higgs, especially if  $\tan \beta$  is large. Assuming a measurement accuracy of  $10^{-2}$  for  $\tau$  polarization,  $\delta P_{\tau}^{\pm}$  can in fact probe a large part of the CPV-MSSM parameter space. A cut on the  $\tau\tau$  invariant mass is, however, necessary to enhance the signal. The CP-odd asymmetry  $\delta P_{\tau}^{\rm CP}$ , on the other hand, is always very small, well below measurability. While  $\delta P_{\tau}^{\pm}$  can be enhanced by the cut mentioned above, this does not work for  $\delta P_{\tau}^{\rm CP}$ .

This is complemented by the top polarization in  $t\bar{t}$  production, which is sensitive to the heavier neutral Higgs bosons  $\phi_{2,3}$ , and also to CP mixing between them, for  $m_{\phi_{2,3}} \geq 2m_t$  and small  $\tan \beta$ . A similar region is covered by the lepton asymmetries constructed from top decays, which are a pure measure of CP violation. These lepton asymmetries are large for large  $\Phi_{t,b,\tau}$  but quickly decrease as this phase decreases.

To conclude, the top and tau polarization asymmetries presented in this paper may prove useful to study the effects of a CP-violating Higgs sector at a photon collider. They may in particular cover the parameter region

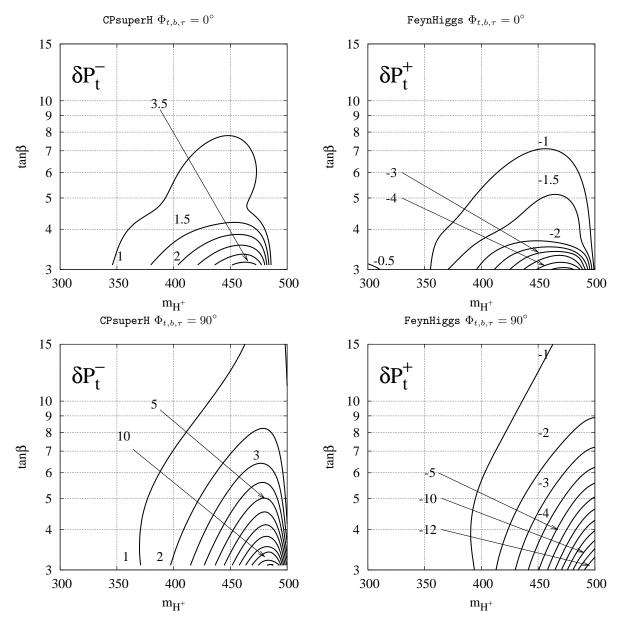


FIG. 10: Contours of constant  $\delta P_t^{\pm}$  in units of  $10^{-2}$  for fixed  $E_b = 300$  GeV and  $\Phi_{t,b,\tau} = 0^{\circ}$  (top) and  $90^{\circ}$  (bottom) using CPsuperH (left) and FeynHiggs (right) to compute the Higgs masses, couplings and widths.

where a light CP-violating Higgs may have been missed at LEP, and may be missed as well at LHC. We found, however, large quantitative differences between the results obtained with CPsuperH and FeynHiggs. In this regard we emphasize the need for a standardization of these tools.

#### Note added

While this paper was in preparation, at a point where the numerical analysis was already finished, a new version of FeynHiggs was released, see http://www.feynhiggs.de and the contribution on FeynHiggs in [8]. This version contains new radiative corrections also for the CP-violating case. It will be inter-

esting to see their effect on the polarization observables discussed in this paper.

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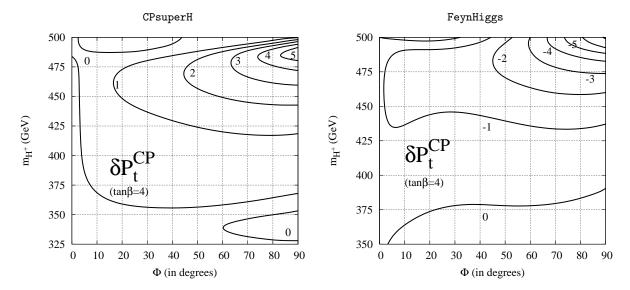


FIG. 11: Contours of constant  $\delta P_t^{\rm CP}$  in units of  $10^{-2}$  in the  $(\Phi_{t,b\tau} - m_{H^+})$  plane for  $\tan \beta = 4$  and  $E_b = 300$  GeV with CPsuperH (left panel) and FeynHiggs (right panel).

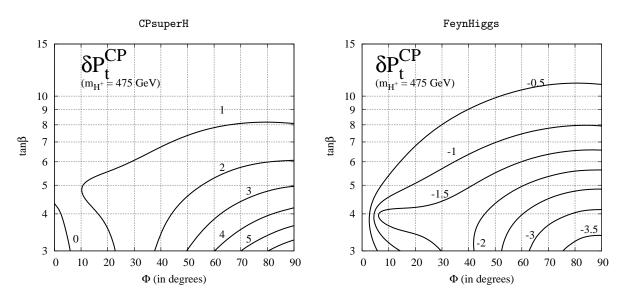


FIG. 12: Contours of constant  $\delta P_t^{\rm CP}$  in units of  $10^{-2}$  in the  $(\Phi_{t,b\tau} - \tan \beta)$  plane for  $m_{H^+} = 475$  GeV and  $E_b = 300$  GeV with CPsuperH (left panel) and FeynHiggs (right panel).

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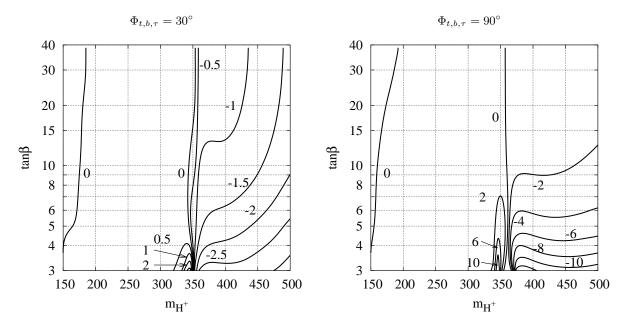


FIG. 13: Contours of constant  $A_3$  in units of  $10^{-2}$  for "peak  $E_b$ " and  $\Phi_{t,b,\tau}=30^\circ$  and  $90^\circ$ ; Higgs masses, couplings and widths computed with CPsuperH.

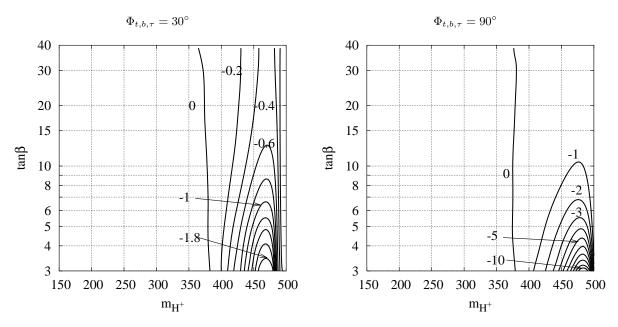


FIG. 14: Contours of constant  $A_3$  in units of  $10^{-2}$  for fixed  $E_b = 300$  GeV and  $\Phi_{t,b,\tau} = 30^{\circ}$  and  $90^{\circ}$ ; Higgs masses, couplings and widths computed with CPsuperH.

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