

**A measurement of $D_s^\pm \rightarrow K^0 K^\pm$ branching ratio
and observation of the corresponding
semileptonic B_s decays**

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Abstract

The decay $D_s^\pm \rightarrow K^0 K^\pm$ has been searched for in a sample of 2770735 hadronic events recorded by ALEPH from 1990 to 1994. A signal of 418 events is seen. From this signal a value of $BR(D_s^\pm \rightarrow K^0 K^\pm) = 3.2 \pm 0.6 \pm 1.0\%$ has been determined.

In addition 34 D_s mesons correlated with a lepton are seen as a sign of the B_s meson. The product

$$BR(b \rightarrow B_s) \times BR(B_s \rightarrow D_s X l \nu) = 0.029 \pm 0.005_{\text{stat.}}^{+0.007} {}_{-0.009_{\text{syst.}}}$$

is deduce from this channel and from the $D_s^\pm \rightarrow K^{*\pm} K^0$ decay study.

1 D_s^\pm search

Measurements of the $D_s^\pm \rightarrow K^0 K^\pm$ branching ratio have already been published by 3 experiments [1, 2, 3] and studied in ALEPH on a fraction of the statistics [4]. Nevertheless these results are affected by rather large uncertainties and are determined with respect to the $\phi\pi$ channel. This study [5] uses the ALEPH statistics until 1994 and takes into account new intermediate values allowing a absolute measurement of the branching ratio.

To evaluate the efficiency 3000 events $c\bar{c}$ and 3000 $b\bar{b}$ Monte Carlo events containing at least two $D_s^\pm \rightarrow K^0 K^\pm$ per event have been generated. In addition 3000 events $c\bar{c}$ and 3000 $b\bar{b}$ Monte Carlo events containing at least two $D_s^\pm \rightarrow K^0 \pi^\pm$ per event have been generated for study of contamination.

The present analysis use the ALEPH TPC for K^\pm identification and the vertex detector.

Runs "PERF" and "MAYBE" from 1990 to 1994 have been selected, corresponding to 2770735 Z hadronic decays.

1.1 K_s^0 selection

The K^0 selection is similar to those done for the $K^* K^0$ analysis [6]:

- K_s^0 are selected amongst the V^0 rebuilt.
- The invariant mass $\pi^+\pi^-$ has to be equal to the K^0 mass $\pm 13 MeV$
- The distance of flight is greater than 1 cm
- K_s^0 momentum has to be greater than 2 GeV

1.2 K^\pm selection

Charged K are selected with the following criterias:

- Momentum of the charged track has to be greater than 2 GeV,
- dE/dx information muss exist and we required: $|\chi_K| < 2$, where:

$$\chi_K = \frac{I_{\text{mes}} - I_{\text{exp}}}{\sigma_I}$$

and I_{mes} is the measured ionisation in the TPC and σ_I is the measured resolution.

1.3 D_s^\pm selection

The $K^0 K$ invariant mass is calculated for Monte Carlo events (Fig.1) and data (Fig. 2), with Kaons satisfying the following cuts:

- The K_s^0 and K^\pm momentum have to be greater than 2 GeV ,
- D_s^\pm decay being in a small cone : $\cos(K^0, K) > 0.7$
- The $K^0 K$ combined momentum has to be greater than 10 GeV.

A gaussian fit and a second order polynomial for the background lead to a mass of 1961 ± 3 MeV, 7 MeV lower than the world value [7]. This effect can be explain by a D^\pm contamination.

1.4 Contamination study

The large number of D^\pm decaying into $K^0 \pi^\pm$ leads to a contamination of the $K^0 K^\pm$ channel when the π is misidentified like a K . We have compared the efficiencies for D^\pm and D_s events: $\epsilon_{D_s}^{c\bar{c}}$, $\epsilon_{D_s}^{b\bar{b}}$, $\epsilon_D^{c\bar{c}}$ and $\epsilon_D^{b\bar{b}}$, with different cuts. Efficiencies $\epsilon_D^{c\bar{c}}$ and $\epsilon_D^{b\bar{b}}$ are calculated by counting the number of true D^\pm with a $K^0 K$ invariant mass closer than 2σ from the D_s mass.

Different cuts have been tested. Best results are obtained with the cut:

$$-2 < \chi_K < 0$$

leading to the following efficiencies:

$$\begin{aligned} \epsilon_{D_s}^{c\bar{c}} &= 13.5 \pm 0.7\% & \epsilon_{D_s}^{b\bar{b}} &= 11.9 \pm 0.6\% \\ \epsilon_D^{c\bar{c}} &= 0.7 \pm 0.2\% & \epsilon_D^{b\bar{b}} &= 0.5 \pm 0.1\% \end{aligned}$$

With this last cut we obtain the $K^0 K^\pm$ invariant mass spectrum of the Figure 3.

A fit of the data with 2 gaussians and a second order polynomial for the background gives:

$$N_{D_s^\pm \rightarrow K^0 K^\pm} = 418.6 \pm 79.3 \text{ events,}$$

a mass of:

$$m = 1968.6 \pm 3.4 \text{ MeV,}$$

in agreement with the world value [7]

and a width of

$$\sigma = 13.2 \pm 3.5 \text{ MeV,}$$

The second gaussian corresponds to $D^\pm \rightarrow K^0 K^\pm$ events.

2 D_s^\pm branching ratio

As for the K^*K^0 channel [6], D_s^\pm branching ratio is usually determined with respect to the $\phi\pi$ channel, nevertheless, recent results from ALEPH [9, 10] allow a absolute determination using the following formula and table 1

$$\begin{aligned}
 N(D_s^\pm \rightarrow K^0 K^\pm) = 2 N_{q\bar{q}} & \times BR(D_s^\pm \rightarrow K^0 K^\pm) \times BR(K^0 \rightarrow K_s^0) \\
 & \times BR(K_s^0 \rightarrow \pi^+ \pi^-) \\
 & \times \left\{ \epsilon_{D_s}^{c\bar{c}} \times P(q \rightarrow c) \times f_s^c + \right. \\
 & \left. \epsilon_{D_s}^{b\bar{b}} \times P(q \rightarrow b) \times [f_s^b \times P_{B_s \rightarrow D_s} + P(b \rightarrow B) \times P_{B \rightarrow D_s}] \right\}
 \end{aligned} \tag{1}$$

where:

$N(D_s^\pm \rightarrow K^0 K^\pm)$ is the number of observed events,
 $N_{q\bar{q}}$ is the number of hadronic events analyzed,
 $BR(D_s^\pm \rightarrow K^0 K^\pm)$ is the branching ratio we are looking for,
 $P(q \rightarrow b) = \frac{\Gamma(Z^0 \rightarrow b\bar{b})}{\Gamma(Z^0 \rightarrow \text{hadrons})}$
 f_s^c is the probability for the primary quark $c(\bar{c})$ to hadronize with a quark $\bar{s}(s)$, creating a D_s : $BR(c \rightarrow D_s)$.
 f_s^b is the probability for the primary quark $b(\bar{b})$ to hadronize with a quark $\bar{s}(s)$, creating a B_s : $BR(b \rightarrow B_s)$.
Nevertheless the D^\pm contamination has to be considered. The number of D^\pm decaying into $K^0\pi^\pm$ is given by:

$$\begin{aligned}
 N(D^\pm \rightarrow K^0 \pi^\pm) = N_{q\bar{q}} & \times \mathcal{F} \times \mathcal{R}_{\text{PDG}} \times BR(K^0 \rightarrow K_s^0) \times BR(K_s^0 \rightarrow \pi^+ \pi^-) \\
 & \times \left[\epsilon_D^{c\bar{c}} \times P(q \rightarrow c) + \epsilon_D^{b\bar{b}} \times P(q \rightarrow b) \right]
 \end{aligned}$$

where:

$N(D^\pm \rightarrow K^0 \pi^\pm)$ is the number of D^\pm selected as D_s

the factor $\mathcal{F} = \frac{\Gamma(Z \rightarrow D^\pm X)}{\Gamma(Z \rightarrow \text{hadron s})} \times BR(D^\pm \rightarrow K^\mp \pi^\pm \pi^\pm)$ measured by ALEPH [11]

determine the production of D^\pm : $\mathcal{F} = 2.01 \pm 0.21\%$

$$\mathcal{R}_{\text{PDG}} = \frac{\Gamma(D^\pm \rightarrow K^0 \pi^\pm)}{\Gamma(D^\pm \rightarrow K^\mp \pi^\pm \pi^\pm)} = 0.302 \pm 0.031 \text{ [2, 7]}$$

Then we deduce the number of contaminating D :

$$N(D^\pm \rightarrow K^0 \pi^\pm) = 12.7 \pm 4.1$$

The corrected number of D_s is then :

$$N(D_s^\pm \rightarrow K^0 K^\pm) = 405.9 \pm 79.3$$

With the numerical values of the Table 1, we deduce the branching ratio :

$N_{q\bar{q}}$	2770735
$BR(K^0 \rightarrow K_s^0)$	0.5
$BR(K_s^0 \rightarrow \pi^+\pi^-)$	$68.61 \pm 0.21\%$
$P(q \rightarrow c)$	$15.83 \pm 0.98\%$
f_s^c	$12.7 \pm 2.5\%$
$P(q \rightarrow b)$	$22.02 \pm 0.20\%$
$f_s^b \times P_{B_s \rightarrow D_s}$	$8.6 \pm 3.1\%$
$P(b \rightarrow B)$	$77 \pm 5\%$
$P_{B \rightarrow D_s}$	$8.9 \pm 1.1\%$

Table 1: Values used for the $BR(D_s^\pm \rightarrow K^0 K^\pm)$ calculation

$$BR(D_s^\pm \rightarrow K^0 K^\pm) = 3.2 \pm 0.6 \pm 1.0\%$$

The systematic errors are due to the limited statistics of the Monte Carlo, the uncertainties on efficiencies, the uncertainties on the dE/dx cut for K^\pm selection and precision on the parameters of the Table 1.

Like for the $K^* K^0$ [6], this branching ratio can also be obtained via the relative width with respect to the $\phi\pi$ decay. We use an analysis done by ALEPH for this channel [12]. To limit the systematic errors we apply the same cuts on D_s than on the $\phi\pi$ channel:

$$X(D_s) > 0.4, \text{ where } X(D_s) = \frac{P(D_s)}{E_{\text{beam}}}.$$

It corresponds to an increase of the D_s momentum cut from 10 GeV to about 18 GeV, reducing strongly the statistics to $N_{D_s \rightarrow K^0 K} = 203 \pm 34$, and the selection efficiencies to:

$$\epsilon_{c\bar{c}}^{K^0 K} = 9.7 \pm 0.6\%, \quad \epsilon_{b\bar{b}}^{K^0 K} = 4.6 \pm 0.3\%$$

The corresponding values for the $D_s^\pm \rightarrow \phi\pi^\pm$ channel are : $N_{D_s \rightarrow \phi\pi} = 492 \pm 39$ and

$$\epsilon_{c\bar{c}}^{\phi\pi} = 15.0 \pm 0.5\%, \quad \epsilon_{b\bar{b}}^{\phi\pi} = 7.7 \pm 0.4\%$$

if we assume that:

$$\alpha_c = \frac{\epsilon_{c\bar{c}}^{K^0 K}}{\epsilon_{c\bar{c}}^{\phi\pi}} \approx \quad \alpha_b = \frac{\epsilon_{b\bar{b}}^{K^0 K}}{\epsilon_{b\bar{b}}^{\phi\pi}} \approx .62 \pm 0.07$$

we deduce:

$$\frac{\Gamma(D_s^\pm \rightarrow K^0 K^\pm)}{\Gamma(D_s^\pm \rightarrow \phi\pi^\pm)} = 0.97 \pm 0.16_{\text{stat.}} \pm 0.13_{\text{syst.}}$$

Systematic errors are coming from the Monte Carlo statistics, number of $D_s^\pm \rightarrow \phi\pi^\pm$, uncertainties on the dE/dx cut for K^\pm selection, and K_s^0 and ϕ branching ratios.

This value is in good agreement with the previous measurements:

$$\begin{array}{ll} 1.15 \pm 0.31_{\text{stat.}} \pm 0.19_{\text{syst.}} & \text{for E691} \\ 0.92 \pm 0.32_{\text{stat.}} \pm 0.20_{\text{syst.}} & \text{for MARK III} \\ 0.99 \pm 0.17_{\text{stat.}} \pm 0.10_{\text{syst.}} & \text{for CLEO} \end{array}$$

Using the world value for $BR(D_s^\pm \rightarrow \phi\pi^\pm) = 3.5 \pm 0.4\%$ [7], we obtain :

$$BR(D_s^\pm \rightarrow K^0 K^\pm) = 3.5 \pm 0.6 \pm 1.0\%$$

Statistics and systematic errors being added quadratically.

The values determined by these two ways agree with the other experiments:

	$BR(D_s^\pm \rightarrow K^0 K^\pm)$
This experiment, absolute measurement	$3.2 \pm 1.0\%$
This experiment, measurement / $\phi\pi^\pm$	$3.4 \pm 0.8\%$
World value [7] (E691, MARK III, CLEO)	$3.5 \pm 0.7\%$
Mean value with this experiment	$3.5 \pm 0.6\%$

Table 2: Comparison of the $BR(D_s^\pm \rightarrow K^0 K^\pm)$ experimental measurements

3 Comparison to theoretical predictions

There are essentially two theoretical models available: M.Bauer, B.Stech and M.Wirbel [13], using factorisation and B.Y.Blok and M.A.Shifman [14] based on sum rules. These models give, in particular, predictions for 4 of the D_s decays: $\phi\pi^\pm$, $K^0 K^\pm$, $K^{*\pm} K^0$, $K^\pm K^{*0}$. We can compare experimental results obtained by ALEPH on $K^0 K^\pm$, this analysis, and $K^{*\pm} K^0$, [5, 6], with the theoretical predictions, Table 3.

Values on $\phi\pi^\pm$ and $K^\pm K^{*0}$ are the world values [7].

We can see that, if predictions and results are compatible for $\phi\pi^\pm$, there is a rather large disagreement for other decays. In more the ratio $K^{*\pm} K^0 / K^\pm K^{*0}$ is reversed. These differences could be due to interactions in the final state, underestimated in the theoretical models.

	WBS	BS	Experiment
$BR(D_s^\pm \rightarrow \phi\pi^\pm)$	3.7%	2.0%	$3.5 \pm 0.4\%$
$BR(D_s^\pm \rightarrow K^0 K^\pm)$	1.8%	0.9%	$3.4 \pm 0.8\%$
$BR(D_s^\pm \rightarrow K^{*\pm} K^0)$	0.8%	0.2%	$4.6 \pm 1.1\%$
$BR(D_s^\pm \rightarrow K^\pm K^{*0})$	2.1%	1.5%	$3.3 \pm 0.5\%$

Table 3: Comparison of experimental D_s branching ratios measurements with theoretical predictions

4 D_s -lepton correlations

The significant number of D_s allows to try to correlate the D_s meson with a lepton in order to observe the presence of a B_s meson decaying in the semileptonic mode $B_s \rightarrow D_s l \nu$.

We require the same criterias than for the $K^{*\pm} K^0$ analysis [6]

- Electrons are identified by dE/dx , if available, and following cuts on estimators: $R2 > -1.6$, $-1.8 < R3 < 3$, $\chi_e > -2.5$
- Muons are identified by :
 - at least 40% of the expected and 5 amongst the last 10 HCAL plans fired,
 - at least 1 associated hit in muon chambers
- Lepton momentum has to be greater than 3 GeV
- D_s momentum has to be greater than 10 GeV
- D_s and lepton have to be in a cone: $\cos(D_s, \text{lepton}) > 0.7$
- Background being important at low mass and momentum, we required: $m(D_s^\pm, \text{lepton}) > 3 \text{ GeV}$, and $p(D_s^\pm - \text{lepton}) > 20 \text{ GeV}$

For background evaluation, combinations of D_s with a lepton of same sign are also selected.

For efficiency determination 6003 B_s decaying via $D_s \rightarrow K^0 K$ are generated by Monte Carlo.

With the previous cuts, the efficiency is:

$$\epsilon_{B_s}^{K^0 K} = 8.5 \pm 0.4\%$$

The $K^0 K$ invariant mass spectrum obtain with this criteria is shown Fig.4, indicating a signal of B_s but also a excess of events around 2100 MeV. This excess is due to the reflexion of a Λ_b baryon decaying into Λ_c -lepton, the Λ_c going into pK^0 where the

proton is misidentified like a K . A cut at $\pm 25 \text{ MeV}$ on the invariant mass calculated assuming a K^0 associated to a proton suppresses this reflexion. Final $K^0 K^\pm$ invariant mass spectrum is shown Fig.5, indicating a signal of

$$N_{B_s \rightarrow D_s \rightarrow K^0 K} = 34 \pm 7 \text{ events}$$

From this number and the following formula we can deduce the branching ratio produce:

$$N_{B_s \rightarrow D_s \rightarrow K^0 K} = 2 N_{q\bar{q}} \times BR(B_s \rightarrow D_s X l \nu) \times BR(D_s \rightarrow K^0 K) \\ \times BR(K^0 \rightarrow K_s^0) \times BR(K_s^0 \rightarrow \pi^+ \pi^-) \\ \times \epsilon_{B_s}^{K^0 K} \times P(q \rightarrow b) \times f_s^b$$

where:

$N_{B_s \rightarrow D_s \rightarrow K^0 K}$ is the number of observed events

$\epsilon_{B_s}^{K^0 K}$ is the efficiency.

We obtained:

$$f_s^b \times BR(B_s \rightarrow D_s X l \nu) \times BR(D_s \rightarrow K^0 K) = (9.55 \pm 1.97_{\text{stat.}}^{+0.46} {}_{-0.69}^{\text{syst.}}) \times 10^{-4}$$

Then using the branching ratio $BR(D_s \rightarrow K^0 K)$ determined above:

$$f_s^b \times BR(B_s \rightarrow D_s X l \nu) = 0.028 \pm 0.006_{\text{stat.}}^{+0.006} {}_{-0.007}^{\text{syst.}}$$

Systematic errors are due to uncertainties on $BR(K_s^0 \rightarrow \pi^+ \pi^-)$, $(P(q \rightarrow b))$, Monte Carlo statistics, evaluation of the $D^\pm \rightarrow K^0 \pi^\pm$ reflexion and non symmetric background coming from $B \rightarrow D_s "D" X$, $"D" \rightarrow X l \nu$ and $B \rightarrow D_s "K" W^*$, $W^* \rightarrow l \nu$

Results of this analysis and of the $D_s \rightarrow K^{*\pm} K^0$ [5, 6] can be added. Then we obtain the invariant mass spectrum of the Fig. 6, corresponding to 44 ± 8 events and to the product:

$$BR(b \rightarrow B_s) \times BR(B_s \rightarrow D_s X l \nu) = 0.029 \pm 0.005_{-0.009}^{+0.007}$$

Conclusion

A signal of 418 events $D_s^\pm \rightarrow K^0 K^\pm$ has been extracted from the 1990 to 1994 ALEPH data, allowing a determination of the branching ratio

$$BR(D_s^\pm \rightarrow K^0 K^\pm) = 3.2 \pm 0.6 \pm 1.0\%$$

A comparable value has been obtain by comparison to the $\phi\pi$ channel. Results are in good agreement with previous measurement but disagree strongly from the theoretical predictions.

Measurement of 34 D_s mesons correlated with a lepton is a sign of the B_s meson. The product

$$BR(b \rightarrow B_s) \times BR(B_s \rightarrow D_s X l \nu) = 0.029 \pm 0.005_{\text{stat.}}^{+0.007} {}_{-0.009_{\text{syst.}}}$$

is determined from this channel and from the $D_s^\pm \rightarrow K^{*\pm} K^0$ decay studies.

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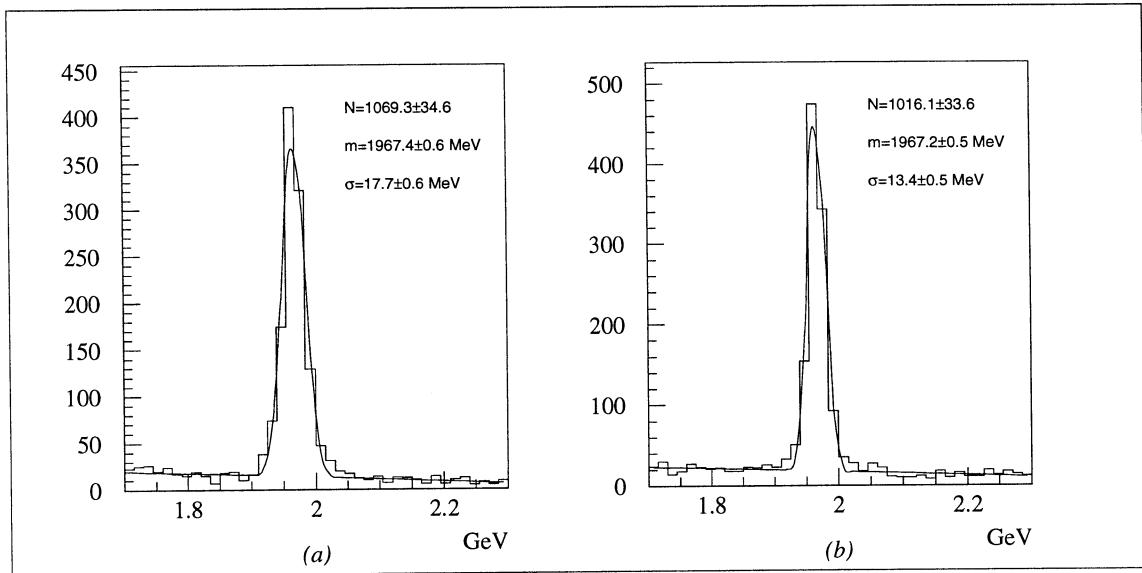


Figure 1: $K^0 K$ invariant mass spectrum for Monte Carlo $c\bar{c}$ (a) et $b\bar{b}$ (b) events. Background is fitted by a second order polynomial

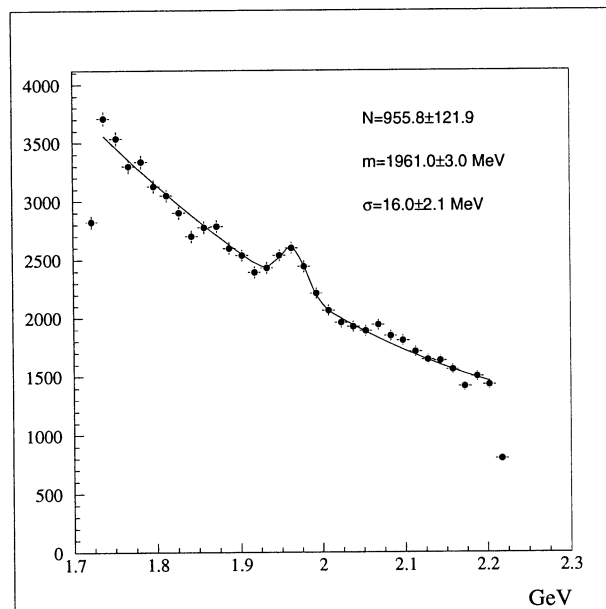


Figure 2: $K^0 K$ invariant mass spectrum for data. Background is fitted by a second order polynomial

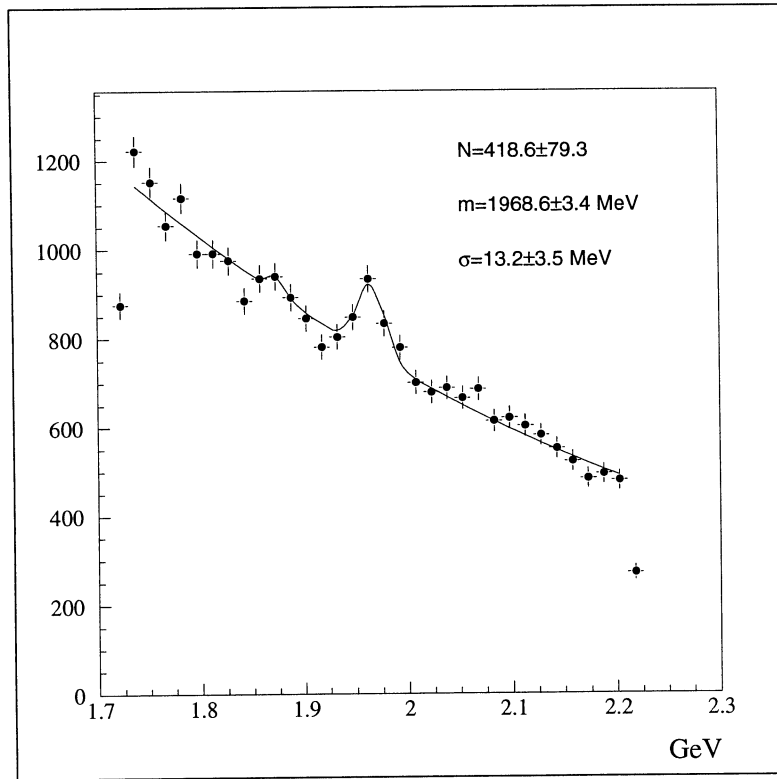


Figure 3: Final $K^0 K$ invariant mass spectrum for data

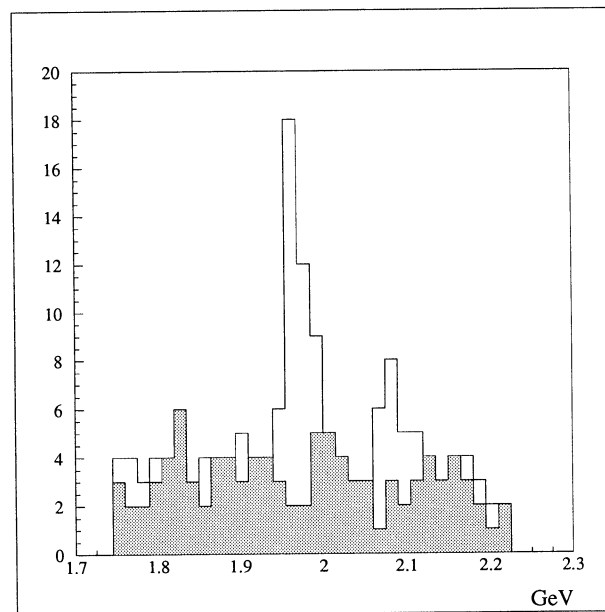


Figure 4: $K^\pm K^0$ invariant mass spectrum. Unshaded for opposite-sign $D_s - l$ pairs, hatched for same-sign $D_s - l$ pairs

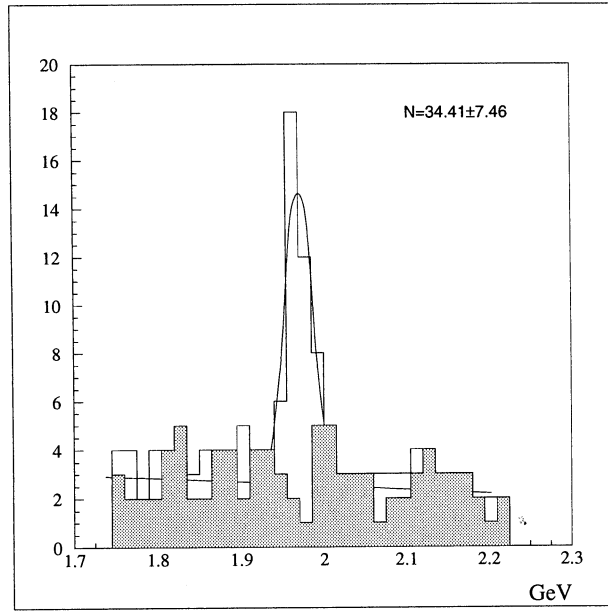


Figure 5: $K^\pm K^0$ invariant mass spectrum after the cut on Λ_c mass. Unshaded for opposite-sign, hatched for same-sign $D_s - l$ pairs

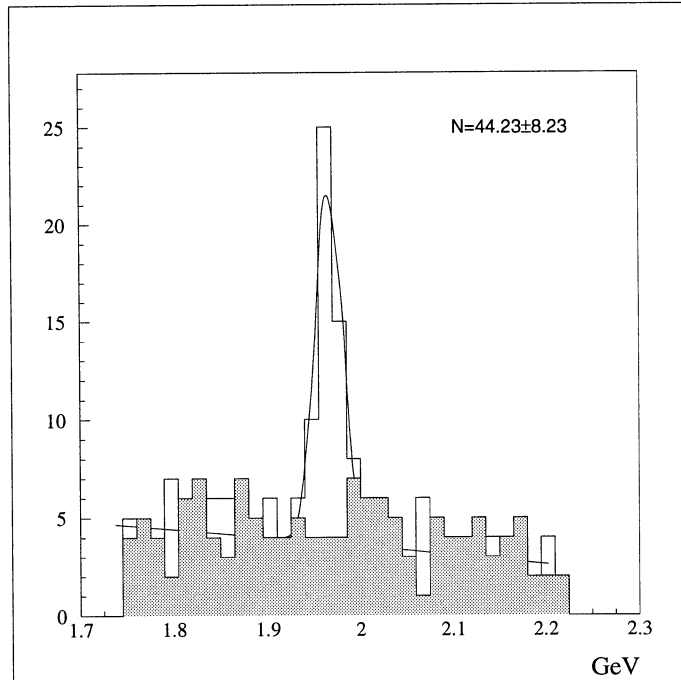


Figure 6: $K^\pm K^0$ invariant mass spectrum with $K^* K^0$ and $K^0 K$ channels. Unshaded for opposite-sign, hatched for same-sign $D_s - l$ pairs