# The Monte Carlo Event Generator YFSWW3 version 1.16 for W-Pair Production and Decay at LEP2/LC Energies†

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#### **Abstract**

We present the Monte Carlo event generator YFSWW3 version 1.16 for the process of W-pair production and decay in electron-positron collisions. It includes  $\mathcal{O}(\alpha)$  electroweak radiative corrections in the WW production stage together with the  $\mathcal{O}(\alpha^3)$  initial-state-radiation (ISR) corrections in the leading-logarithmic (LL) approximation, implemented within the Yennie-Frautschi-Suura (YFS) exclusive exponentiation framework. The photon radiation in the W decays is generated by the dedicated program PHOTOS up to  $\mathcal{O}(\alpha^2)$  LL, normalised to the W branching ratios. The program is interfaced with the  $\tau$  decay library TAUOLA and the quark fragmentation/hadronization package JETSET. The semi-analytical code KorWan for the calculations of the differential and total cross-sections at the Born level and in the ISR approximation is included.

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# **Contents**





### **PROGRAM SUMMARY**

*Title of the program:* YFSWW3, version 1.16 .

*Computer:* any with the FORTRAN 77 compiler and the UNIX/Linux operating system

*Operating system:* UNIX/Linux

*Programming language used:* FORTRAN 77

*High speed storage required:* < 10 MB

*Size of distributed program:* 3,237 kB

*Distribution format:* tar gzip file (size of 1,103 kB)

*No. of cards in combined program and test deck:* about 23,000 plus about 48,000 of auxiliary packages: KorWan, FF, JETSET, TAUOLA, PHOTOS.

#### *Keywords:*

Standard Model (SM), LEP2, linear colliders (LC), quantum electrodynamics (QED), quantum chromodynamics (QCD), boson  $W$ ,  $W$ -pair production,  $W$  decay,  $W$  branching ratio (BR), triple gauge boson couplings (TGC), quartic gauge boson couplings (QGC), four-fermion (4f) background, radiative corrections, Yennie-Frautschi-Suura (YFS) exponentiation, initial state radiation (ISR), leading-log (LL) approximation, Coulomb effect, final state radiation (FSR), electroweak (EW) corrections, leading-pole approximation (LPA), Monte Carlo (MC) simulation/generation.

#### *Nature of the physical problem:*

The process of the W-pair production is important for precise tests of the Standard Model as well as searches for "new physics" at LEP2 and future linear colliders. In order to match the experimental precision necessary for a successful physics programme, quantum effects (the so-called radiative corrections) have to be included into a theoretical description of this process. It turns out that not only the so-called universal corrections (initial state radiation, the Coulomb effect, "naive" QCD correction, etc.) are necessary, but also the  $\mathcal{O}(\alpha)$  electroweak corrections in the WW production are needed for the desired theoretical accuracy. All these effects should, preferably, be included in a Monte Carlo event generator in order to account for realistic experimental set-ups.

#### *Method of solution:*

The Monte Carlo event generator for the combined W-pair production and decay process including  $\mathcal{O}(\alpha^3)$  LL ISR effects, the Coulomb correction (usual or screened), the "naive" QCD effect, the  $\mathcal{O}(\alpha)$  EW corrections in the WW production stage, implemented within the YFS exclusive exponentiation framework is provided. Multi-photon radiation in the WW production is generated according to the YFS MC method. The photon radiation in the W decays, normalized to the W BR's, is generated by the LL-type MC program **PHOTOS** (up to two photons). The decays of  $\tau$ 's including radiative corrections are done by the dedicated package TAUOLA. The quark fragmentation/hadronization is performed with the help of the Lund program JETSET. The program can provide both weighted and unweighted (weight=1) events. Any experimental cut and apparatus efficiency may be introduced easily by rejecting some of the generated events.

### *Restrictions on the complexity of the problem:*

The leading pole approximation (LPA) is used (in two versions) to describe the signal  $WW$ production process. Multi-photon radiation according to the YFS exponentiation scheme is generated only for the WW production stage.  $\mathcal{O}(\alpha)$  EW corrections (in LPA) are included only in the WW production stage. The ISR effects beyond  $\mathcal{O}(\alpha)$  are included in the LL approximation. Non-factorizable corrections (interferences between the production and decay stages) are approximated by the so-called screened Coulomb ansatz. Spin correlations between the WW production and decays are fully included only at the Born and the ISR levels. Radiative corrections in the W decays are included into an overall normalisation through the W BR's, and the real photon radiation is generated in the LL approximation (up to two photons) by the program PHOTOS. Anomalous triple gauge boson couplings are included in the Born-like matrix element, i.e. with the universal SM corrections only. Quartic gauge boson couplings are implemented according to the Standard Model only (no anomalous couplings). The  $\tau$ -decays and quark hadronization are performed, respectively, with the help of the dedicated packages: TAUOLA and JETSET. No 4f background processes are included.

### *Typical running time:*

200 CPU seconds of a PC Intel Pentium III @ 550MHz per 1000 unweighted events, for the parameter settings as they are given in the demonstration program.

# **1 Introduction**

The process of W-pair production in electron–positron colliders is very important for testing the Standard Model (SM) and searching for signals of possible "new physics"; see e.g. Refs. [1, 2]. One of the main goals of investigating this process at present and future  $e^+e^-$  experiments is to measure precisely the basic properties of the W boson, such as its mass  $M_W$  and width  $\Gamma_W$ . This process also allows for a study of the triple and quartic gauge boson couplings at the tree level, where small deviations from the subtle SM gauge cancellations can lead to significant effects on physical observables – these can be signals of "new physics".

In this work we present the Monte Carlo (MC) event generator which simulates the production and decay of the W-pair at  $e^{\pm}$  colliders. The integrated cross sections and arbitrary differential distributions can be calculated from a series of the constant-weight fully inclusive MC events. The program embodies the Standard Model scattering matrix element with the  $\mathcal{O}(\alpha)$  radiative corrections for the double-resonant component of the scattering matrix element. The basics of the model used in the program and selected numerical results were already presented in the earlier publications [3–6]. The important components of the presented program/calculation are the complete  $\mathcal{O}(\alpha)$  radiative correction for on-shell W-pair production, which are implemented according to<sup>1</sup>, Refs. [7–9], see also Ref. [10].

Let us discuss briefly the basic physics properties of the W-pair production and decay process. Since the W's are unstable and short-lived particles, the W-pairs are not observed directly in the experiments but through their decay products: four-fermion  $(4f)$ final states (which may then also decay, radiate gluons/photons, hadronize, etc.). As high energy charged particles are involved in the process, one can also observe energetic radiative photons. So, at the parton level, one has to consider a general process:

$$
e^{+} + e^{-} \longrightarrow 4f + n\gamma, \ (n = 0, 1, 2, \dots), \tag{1}
$$

where also some background (non- $WW$ ) processes contribute. In a theoretical description of this process – according to quantum field theory – one also has to include virtual effects, the so-called loop corrections. This general process is very complicated since it involves  $\sim$  80 different channels (4f final states) with complex peaking behaviour in multi-particle phase space and a large number of Feynman diagrams. Even in the massless-fermion approximation the number of Feynman graphs grows up from 9–56 per channel at the Born level to an enormous 3579–15948 at the one-loop level [11]. The full one-loop calculations have not been finished yet, even for the simplest case (doubly plus singly W-resonant diagrams) [12]. But even if they existed one would be faced with problems in their numerical evaluations in practical applications, particularly within Monte Carlo event generators – they would be prohibitively huge and slow. These are the reasons why efficient approximations in the theoretical description of this process are necessary. These approximations should be such that on the one hand they would include all contributions/corrections that

<sup>&</sup>lt;sup>1</sup>We are grateful to the authors of these works for providing us the relevant parts of the computer code.

are necessary for the required theoretical accuracy (dependent on the experimental precision) and on the other hand they would be efficient enough for numerical computations. Given the complicated topologies of the  $(4f + n\gamma)$  final states, such calculations should be, preferably, given in terms of a Monte Carlo event generator that would allow one to simulate the process directly [13, 14].

Our solution to this consists of two complementary Monte Carlo event generators: YFSWW3 and KoralW. KoralW includes the full lowest-order  $e^+e^- \rightarrow 4f$  process but with simplified radiative corrections – the universal ones such as initial-state radiation (ISR), the Coulomb effect, etc. In YFSWW3, on the other hand, the lowest-order process is simplified – only the doubly W-resonant contributions are taken into account, but inclusion of the radiative corrections in this process goes beyond the universal ones. In the current version of YFSWW3 only those non-universal (non-leading) corrections are included that are necessary to achieve the theoretical precision for the total WW cross section of  $0.5\%$  required for LEP2<sup>2</sup>. In order to achieve a gauge-invariant description of the signal WW-process and employ the existing  $\mathcal{O}(\alpha)$  electroweak corrections for the on-shell Wpair production, we use the so-called leading-pole approximation (LPA) – see Refs. [6,15]. The important thing is that the two programs have a well established common part, which is the doubly W-resonant  $(WW)$  process with the same universal radiative corrections. This allows us to combine the results of the two programs to achieve the desired theoretical precision for WW observables. Detailed descriptions of KoralW were published in Refs. [16–19]. Here, we present a documentation of the program YFSWW3; physical aspects together with some numerical results are discussed in Refs. [3–6, 15]. Possible scenarios of combining the results of the two programs are presented in Refs.  $[6, 15, 20]$ .

The outline of the paper is as follows. In Section 2, we define our notation and describe the physics content of the program. In Section 3, we discuss the MC algorithm. In Section 4, we present the structure of the program, important routines, etc. Details about the practical use of the program are given in Section 5. Appendices contain useful technical information on the structure of the program, its input/output, etc.

<sup>2</sup>For the future linear colliders (LC) this may not be sufficient, so even some higher-order corrections would have to be added, which is possible within the framework of YFSWW3.

## **2 Physics Content of** YFSWW3

In this section we describe the physics content of YFSWW3, that is we define differential discributions used to calculate the cross section and generate events for the W-pair production and decay process. These distrubutions we define rather completely, because they were not defined in every detail in the past publications. On the other hand we shall skip the detailed discussion of the physics models which they represent. This will be done in a separate publication [21]. First, we discuss our notation. Then, we present the master formula and its ingredients. And finally, we give some details on the MC algorithms implemented in the program.

## **2.1 Notation**



Figure 1: Kinematics of the  $W$ -pair production and decay process with multiple photons in the production stage.

In YFSWW3 we adopt the notational convention similar to the one used in KoralW. The variables  $p_1, p_2$  are the incoming  $e^-, e^+$  four-momenta, respectively:

$$
p_1 = (E_e, 0, 0, p_e), \qquad p_2 = (E_e, 0, 0, -p_e), \qquad (2)
$$

where  $E_e$  is the beam energy and  $p_e = \sqrt{E_e^2 - m_e^2}$ , with  $m_e$  being the electron mass. The variables  $Q_1, Q_2$  are the four-momenta of the  $W^-$  and  $W^+$  bosons; their invariant masses are denoted by  $M_1$  and  $M_2$ , respectively.  $q_1, q_2$  and  $m_1, m_2$  are the four-momenta and masses of the  $W^-$  decay products;  $q_3, q_4$  and  $m_3, m_4$  are the analogous four-momenta and masses of the  $W^+$  decay products, with the first component of each pair corresponding to a fermion and the second to an anti-fermion. By  $k_i$  we denote the four-momenta of radiative photons. See also fig. 1 for a pictorial representation. The components of a four-vector are denoted by  $p = (p_0, p_x, p_y, p_z)$ , with the metric convention of  $\{1, -1, -1, -1\}$ . We also use the following Lorentz invariants:  $s = (p_1 + p_2)^2$ ,  $s_1 = Q_1^2 = M_1^2$  and  $s_2 = Q_2^2 = M_2^2$ .

### **2.2 Master Formula**

Here, we consider the process:

$$
e^- + e^+ \longrightarrow \{W^- \to f_1 + \bar{f}_2\} + \{W^+ \to f_3 + \bar{f}_4\} + n\gamma, \ (n = 0, 1, 2, \dots), \tag{3}
$$

where the radiative photons are emitted only at the  $WW$ -production stage. The photon radiation in W decays (FSR) in this version of YFSWW3 is done, in the  $\mathcal{O}(\alpha^2)$  leadinglogarithmic (LL) approximation, by the dedicated program PHOTOS  $[22]$  – in the same way as in KoralW. Since this is done externally on fully generated events (it does not change event weights), we do not include the FSR in our discussion of the master formula. It should be remembered that the use of PHOTOS in YFSWW3 is a temporary solution before the advent of the YFS-exponentiated MC for W decays.

As it was already mentioned in Introduction, we use the LPA to describe this process respecting the  $SU(2)_L \times U(1)$  gauge invariance. In YFSWW3, we implemented two options of the LPA, called LPA<sub>a</sub> and LPA<sub>b</sub>. The first one, which is the default (recommended) option, is based on the approach of R. Stuart [23], where only the Lorentz scalar functions in the S-matrix are expanded about poles corresponding to unstable  $W$ 's. In the lowest order, the  $LPA_a$  matrix element coincides with the so-called CC03 (see e.g. Ref. [11] for explanation of this notation) matrix element in the 't Hooft-Feynman gauge. In the following we shall use the notion "CC03" in that sense. The second option, intended for some dedicated tests, follows the method suggested in Ref. [11], where the whole S-matrix residuals are expanded about poles<sup>3</sup>; see Refs.  $[6, 15]$  for more details. In the following we shall describe explicitly the  $LPA_a$  scheme;  $LPA_b$  can be obtained from this by taking the W's on-shell (i.e.  $Q_1^2, Q_2^2 \to M_W^2$ ) everywhere, except for the Breit-Wigner denominators and the phase-space integration.

In the framework of the Yennie-Frautschi-Suura (YFS) exclusive exponentiation (EEX), the cross section for the process (3) can be written as

$$
\sigma_{\text{Best}} = \sum_{n=0}^{\infty} \frac{1}{n!} \int ds_1 ds_2 \frac{d^3 Q_1}{Q_1^0} \frac{d^3 Q_2}{Q_2^0} \prod_{l=1}^4 \frac{d^3 q_l}{q_l^0} \prod_{i=1}^n \frac{d^3 k_i}{k_i^0} \delta^{(4)} \left( p_1 + p_2 - Q_1 - Q_2 - \sum_{i=1}^n k_i \right)
$$
  

$$
\delta^{(4)} \left( Q_1 - q_1 - q_2 \right) \delta^{(4)} \left( Q_2 - q_3 - q_4 \right) \rho_n^{\text{Best}}(p_1, p_2; q_1, \dots, q_4, k_1, \dots, k_n),
$$
\n(4)

<sup>&</sup>lt;sup>3</sup>We do not apply, however, the pole approximation to the phase space as it was done in semi-analytical calculations of Ref. [24].

where  $\rho_n^{\text{Best}}$  is the following fully exclusive multi-photon differential distribution:

$$
\rho_n^{\text{Best}}(p_1, p_2; q_1, \dots, q_4, k_1, \dots, k_n) = \prod_{i=1}^n \tilde{S}(p_1, p_2, Q_1, Q_2, k_i) \ \theta(k_i^0 - k_\epsilon)
$$
\n
$$
\times e^{Y'(p_1, p_2, Q_1, Q_2; k_\epsilon)} \left[ 1 + \delta_C(Q_1, Q_2, M_W, \Gamma_W) \right] \sum_{\varphi \in \{I, W\}^n} p_\varphi \ \mathcal{B}\left(\{p, Q, q, k\}^{\mathcal{R}_\varphi}\right), \tag{5}
$$

with  $\beta$  being the contribution from the infrared-finite YFS residuals<sup>4</sup>:

$$
\mathcal{B}\left(\{p,Q,q,k\}^{\mathcal{R}_{\wp}}\right) = \left[1 + \delta_{An}^{\text{TGC}}\left(\{p,Q,q\}^{\mathcal{R}_{\wp}}\right)\right] \times \left\{\bar{\beta}_{0}^{(1)}\left(\{p,Q,q\}^{\mathcal{R}_{\wp}}\right) + \sum_{i=1}^{n} \frac{\bar{\beta}_{1}^{(1)}\left(\{p,Q,q,k_{i}\}^{\mathcal{R}_{\wp}}\right)}{\tilde{S}\left(\{p,Q,k_{i}\}^{\mathcal{R}_{\wp}}\right)} + \Delta\bar{\beta}_{0,ISR}^{(3)}(\{p,Q,q\}^{\mathcal{R}_{\wp}}) + \sum_{i=1}^{n} \frac{\Delta\bar{\beta}_{1,ISR}^{(3)}\left(\{p,Q,q\}^{\mathcal{R}_{\wp}},k_{i}\right)}{\tilde{S}_{I}(\{p\}^{\mathcal{R}_{\wp}},k_{i})} + \frac{1}{2!} \sum_{\varrho_{i,j}=I} \frac{\bar{\beta}_{2,ISR}^{(3)}\left(\{p,Q,q\}^{\mathcal{R}_{\wp}},k_{i},k_{j}\right)}{\tilde{S}_{I}(\{p\}^{\mathcal{R}_{\wp}},k_{i})\tilde{S}_{I}(\{p\}^{\mathcal{R}_{\wp}},k_{j})} \tag{6}
$$
\n
$$
+ \frac{1}{3!} \sum_{\varrho_{i,j,l}=I} \frac{\bar{\beta}_{3,ISR}^{(3)}\left(\{p,Q,q\}^{\mathcal{R}_{\wp}},k_{i},k_{j},k_{l}\right)}{\tilde{S}_{I}(\{p\}^{\mathcal{R}_{\wp}},k_{i})\tilde{S}_{I}(\{p\}^{\mathcal{R}_{\wp}},k_{j})\tilde{S}_{I}(\{p\}^{\mathcal{R}_{\wp}},k_{l})},\tag{6}
$$

where we use a short-hand notation of the type  $\{p, Q, q\} \equiv \{p_1, p_2, Q_1, Q_2, q_1, q_2, q_3, q_4\}.$ 

The sum  $\sum_{\varphi}$  in Eq. (5) runs over the photon partitions, i.e. all possible photon associations to the initial-state radiation (ISR) or the W-state radiation (WSR). For  $n$ photons we identify every of the  $2^n$  partitions  $\wp$  with a vector  $\wp \equiv (\wp_1, \ldots, \wp_n)$ , where  $\omega_i = I, W$ , and  $\overline{I}, \overline{W}$  denote the ISR or the WSR photons, respectively. The partition weight  $p_{\wp}$  is given by

$$
p_{\varphi} = \frac{\prod\limits_{\varphi_i=I} \tilde{S}_I(k_i) \prod\limits_{\varphi_j=W} \tilde{S}_W(k_j)}{\sum\limits_{\varphi} \prod\limits_{\varphi_i=I} \tilde{S}_I(k_i) \prod\limits_{\varphi_j=W} \tilde{S}_W(k_j)} = \frac{\prod\limits_{\varphi_i=I} \tilde{S}_I(k_i) \prod\limits_{\varphi_j=W} \tilde{S}_W(k_j)}{\prod\limits_{i=1}^n (\tilde{S}_I(k_i) + \tilde{S}_W(k_i))},
$$
(7)

where  $\tilde{S}_I(k)$  and  $\tilde{S}_W(k)$  are the real photon infrared (IR) factors for the ISR and the WSR, respectively:

$$
\tilde{S}_I(p_1, p_2, k) = -\frac{\alpha}{4\pi} \left( \frac{p_1}{kp_1} - \frac{p_2}{kp_2} \right)^2,
$$
\n
$$
\tilde{S}_W(Q_1, Q_2, k) = -\frac{\alpha}{4\pi} \left( \frac{Q_1}{kQ_1} - \frac{Q_2}{kQ_2} \right)^2.
$$
\n(8)

It is worth to stress that the partition dependence for the first two terms proportional to  $\bar{\beta}_0^{(1)}$  and  $\bar{\beta}_1^{(1)}$  cancels out, when truncated to  $\mathcal{O}(\alpha)$  (as it should), thanks to special

<sup>&</sup>lt;sup>4</sup>In the sums like  $\sum_{\varphi_{i,j}=I}$  we include all pairs of indices  $(i, j)$  such that  $i \neq j$ ,  $\varphi_i = I$  and  $\varphi_j = I$ .

normalisation choice for the partition weights:  $\sum$  $\wp \in \{I, W\}^n$  $p_{\wp} = 1$ . See also the definition

of  $\bar{\beta}_1^{(1)}$  and the discussion on the partition-dependend "reduction procedure"  $\mathcal{R}_{\varphi}$  in the following. The purpose of the sum over partitions is to helps the introduction of the LL corrections beyond the  $\mathcal{O}(\alpha)$ .

In Eq. (6) the two components proportional to  $\bar{\beta}_0^{(1)}$  and  $\bar{\beta}_1^{(1)}$  represent explicitly the complete  $\mathcal{O}(\alpha)$  contribution to the WW-production process while the remaining  $\bar{\beta}$ 's and  $\Delta\beta$ 's collect the second and third order ISR corrections in the LL approximation; see Section 2.2.4 for more details. The dependence of the  $\beta$ -functions on the photon partitions enters through the so-called reduction (extrapolation) procedures which take into account the CMS energy shift induced by the ISR; for more details see Subsection 2.2.4.

#### **2.2.1 YFS Infrared Factors**

The real photon IR factor

$$
\tilde{S}(p_1, p_2, Q_1, Q_2, k) = -\frac{\alpha}{4\pi^2} \left( \frac{p_1}{kp_1} - \frac{p_2}{kp_2} - \frac{Q_1}{kQ_1} + \frac{Q_2}{kQ_2} \right)^2
$$
\n(9)

includes the ISR, the WSR and the interferences between them.

The step function  $\theta(k^0 - k_\epsilon)$ , where  $k_\epsilon = \epsilon \sqrt{s}/2$ , cuts out the singular IR region, already included to all orders in the YFS form factor  $e^{Y'}$ , where

$$
Y'(p_1, p_2, Q_1, Q_2; k_{\epsilon}) = 2\alpha \Re B'(p_1, p_2, Q_1, Q_2) + 2\alpha \tilde{B}(p_1, p_2, Q_1, Q_2; k_{\epsilon}).
$$
 (10)

The IR functions  $\Re B'$  and  $\tilde{B}$ , correspond to virtual and real photons, respectively, and are defined explicitly in Ref. [3].

#### **2.2.2 Coulomb Correction**

The correction  $\delta_C$  is the Coulomb effect, included both (two options): in its standard form as given in Ref. [25] and in terms of the so-called screened Coulomb ansatz of Ref. [26], which is an efficient approximation of the non-factorizable corrections for singly-inclusive distributions [26]. It reads

$$
\delta_C^{\{\text{Std, Ser}\}}(Q_1, Q_2, M_W, \Gamma_W) = \frac{\alpha \pi}{2\beta} \left[ 1 - \left\{ 1, \left( 1 - \beta \right)^2 \right\} \frac{2}{\pi} \arctan\left( \frac{|\kappa|^2 - p^2}{2p \Re \kappa} \right) \right],\tag{11}
$$

with

$$
\beta = \sqrt{1 - 2(s_1 + s_2)/s_Q + [(s_1 - s_2)/s_Q]^2}, \quad p = \frac{1}{2}\beta\sqrt{s_Q}, \quad s_Q = (Q_1 + Q_2)^2,
$$

$$
\kappa = \sqrt{\frac{M_W}{2} \left(\sqrt{E^2 + \Gamma_W^2} - E\right)} - i\sqrt{\frac{M_W}{2} \left(\sqrt{E^2 + \Gamma_W^2} + E\right)}, \quad E = \frac{s_Q - 4M_W^2}{4M_W},
$$
(12)

where  $M_W$  and  $\Gamma_W$  are the on-shell W-mass and W-width, respectively. The first term in the curly brackets in Eq. (11) corresponds to the standard (Std) while the second one to the screeened (Scr) Coulomb correction. This correction is properly matched with the YFS form-factor, where the Coulomb-like singularity appears in the virtual IR function  $\Re B$ . After matching it with the full Coulomb correction  $\delta_C$ , the original YFS function  $\Re B$  is replaced by  $\Re B'$  as described in Ref. [3].  $M_W$  and  $\Gamma_W$  are the on-shell W-mass and W-width, respectively.

#### **2.2.3 Anomalous triple-gauge couplings**

The anomalous corrections to the triple-gauge couplings (TGC) WWV ( $V = Z, \gamma$ ) are included multiplicatively through

$$
1 + \delta_{An}^{\text{TGC}} = \frac{|\mathcal{M}_{\text{Born}}^{\text{AnTGC}}|^2}{|\mathcal{M}_{\text{Born}}^{\text{SM}}|^2},\tag{13}
$$

where  $\mathcal{M}_{\text{Born}}^{AnTGC}$  is the Born level matrix element with the anomalous TGC's, while  $\mathcal{M}_{\text{Born}}^{\text{SM}}$ is the corresponding SM matrix element. In YFSWW3 we use the same conventions (routines) for the TGC's as they are given in KoralW [18]. The anomalous couplings are included in the event generation only if an appropriate switch in the input parameters is on and the parameters corresponding to these couplings (in a given parametrisation) are set up to the non-SM values; see Appendix A for details.

## **2.2.4**  $\bar{\beta}$ 's for W-pair Production

In the IR-finite  $\bar{\beta}$ -functions of Eq. (5) we see the superscripts  $\mathcal{R}_{\varphi}$  in the four-momenta arguments like  $\{p, Q, q\}^{\mathcal{R}_{\wp}}$  or  $\{p, Q, q, k\}^{\mathcal{R}_{\wp}}$ . This means that these arguments are subject to the "reduction (extrapolation) procedures". These reductions procedures are partitiondependent – this is why they are denoted with the subscripts  $\wp$ . The partition-dependence enters through accounting for the ISR energy shift  $s \to s'$ , where  $s' = (p_1 + p_2 - \sum_{\varphi_i=I} k_i)^2$ in the evaluation of the  $\bar{\beta}$ -functions. For more discussion on the meaning of the reduction/extrapolation procedures see Subsection 2.3. In YFSWW3, we use the reduction procedures of the YFS2 and YFS3 programs of KORALZ [27–29], with some modifications: in constructing the reduced  $W$  four-momenta, we take into account that, in general,  $M_1 \neq M_2$ . We perform appropriate transformations of the  $W^{\pm}$  decay products, that is we boost them to  $W$ 's rest-frames before the reduction, and then, we make the inverse boost transformation to the reduced frame. In general, in these reduction procedures the effects of the CMS energy shift  $s \to s'$  (recoil) is taken due to the ISR photons only. This procedure is well justified for the ISR corrections beyond  $\mathcal{O}(\alpha)$  where we take  $\{p, Q, q\}^{\mathcal{R}_{\wp}}$ and for each photon we may say whether it belongs to the ISR or to the WSR. For the  $\mathcal{O}(\alpha)$ -specific corrections, in the corresponding  $\bar{\beta}$ 's we cannot make a distinction between the ISR and the WSR, and the  $\{p, Q, q, k_i\}^{\mathcal{R}_{\wp}}$  in their arguments means that, (i), the reduced  $\{p, Q, k_i\}^{\mathcal{R}_{\wp}}$  are within the 3-body phase space and, (ii), the photon  $k_i$  is excluded from the energy shift  $s \to s'$  calculation. For more discussion on this non-trivial point see Subsections 2.3 and 2.4.

Let us now describe in detail the  $\mathcal{O}(\alpha)$ -complete<sup>5</sup> functions  $\bar{\beta}_0^{(1)}$  and  $\bar{\beta}_1^{(1)}$ . The first one, which includes the  $\mathcal{O}(\alpha)$  electroweak (EW) virtual corrections, reads as follows:

$$
\bar{\beta}_0^{(1)}(\{p,Q\}) = \bar{\beta}_0^{(0)}(\{p,Q\}) \left[1 + \delta_{v+s}^{(1)}(\{p,Q\};k_{\epsilon}) - Y(\{p,Q\};k_{\epsilon})\right],\tag{14}
$$

where  $\bar{\beta}_0^{(0)}$  is the lowest order matrix element squared for the W-pair production and decay, and is identical to the corresponding  $\bar{\beta}_0^{(0)}$ -function in KoralW [16, 18]. In fact, the  $\bar{\beta}_0^{(1)}$ -function comes in two variants. The first one, referred to as the scheme (A) [6], reads as follows:

$$
\bar{\beta}_{0,A}^{(1)}(\{p,Q\}) = \bar{\beta}^{(0)}(\{p,Q\}) \left[1 + \delta_{ISR}^{(1)}(p_1, p_2)\right] \n+ \bar{\beta}^{(0)}(\{p,Q\}) \left[\delta_{v+s}^{(1)}(\{p,Q\};k_{\epsilon}) - Y(\{p,Q\};k_{\epsilon}) - \delta_{ISR}^{(1)}(p_1^{eff}, p_2^{eff})\right]_{G_{\mu}} \tag{15}
$$

where  $\delta_{ISR}^{(1)} = (\alpha/\pi)[\ln(s/m_e^2) - 1]$  is the LL pure QED  $\mathcal{O}(\alpha)$  ISR correction, and the subscript  $G_{\mu}$  means that the whole correction is calculated in the so-called  $G_{\mu}$ -scheme [7] as explained in Ref.  $[6]$ . Another option, referrred to as the scheme  $(B)$ , similar to the one used in the program RacoonWW [30], is defined as follows:

$$
\bar{\beta}_{0,B}^{(1)}(\{p,Q\}) = \bar{\beta}^{(0)}(\{p,Q\}) \left[1 + \delta_{ISR}^{(1)}(p_1, p_2)\right] \n+ \bar{\beta}^{(0)}(\{p,Q\}) \left[\delta_{v+s}^{(1)}(\{p,Q\};k_{\epsilon}) - Y(\{p,Q\};k_{\epsilon}) - \delta_{ISR}^{(1)}(p_1^{eff}, p_2^{eff})\right]_{G_{\mu}} \left(\frac{\alpha}{\alpha_{G_{\mu}}}\right),
$$
\n(16)

where  $\alpha$  is the fine structure constant and  $\alpha_{G_\mu} = (\sqrt{2}G_\mu M_W^2 \sin^2 \theta_W)/\pi$ . Here, although the  $\mathcal{O}(\alpha)$  corrections are calculated in the  $G_\mu$ -scheme, their relative coefficient is  $\alpha$  instead of  $\alpha_{G_\mu}$ . Our recommended option is the scheme (A) which is inspired by the renormalization group equations  $(RGE)$  [31, 6].

The  $\mathcal{O}(\alpha)$  virtual and soft photon corrections for the WW-production stage are included in  $\delta_{v+s}^{(1)}$ . In the current version of the program, we use the calculations of Ref. [7] for the on-shell  $WW$ -production. Since in our case the  $W$ 's are off-shell we have to perform some transformations/extrapolations (which can be viewed as an analytic continuation of the S-matrix) in order to employ these calculations. We do it in the following way. After performing the reduction procedure for the  $\beta_0$  function, as described above, we find  $\cos \theta_{eff}$  and the velocity  $\beta_{eff}$  of the W's in the reduced frame, where

$$
\beta_{eff} = \sqrt{1 - 2(s_1 + s_2)/s' + [(s_1 - s_2)/s']^2},
$$
  
\n
$$
\cos \theta_{eff} = (\vec{p}_1^{\mathcal{R}_\wp} \cdot \vec{Q}_1^{\mathcal{R}_\wp}) / (|\vec{p}_1^{\mathcal{R}_\wp}||\vec{Q}_1^{\mathcal{R}_\wp}|).
$$
\n(17)

Then, for this value of  $\beta_{eff}$  we calculate the effective CMS energy squared for on-shell  $W$ 's:

$$
s_{eff} = 4M_W^2/(1 - \beta_{eff}^2). \tag{18}
$$

<sup>&</sup>lt;sup>5</sup>In the early version of the present program called YFSWW2, corrections beyond the ISR were included only through the function  $Y'$  and S-factors [3].

Having  $(s_{eff}, \beta_{eff}, \cos \theta_{eff})$ , we construct the four-momenta  $(p_1^{eff}, p_2^{eff}, Q_1^{eff}, Q_2^{eff})$  for the on-shell process  $e^+e^- \to W^+W^-$  and use them to calculate the respective EW corrections. The same four-momenta are used to calculate the IR form factor  $Y$  according to Eq. (10), where now the Coulomb-like singularity in the virtual IR function  $\Re B$  is kept in order to cancel the corresponding singularity in  $\delta_{v+s}^{(1)}$ , and to calculate the  $\mathcal{O}(\alpha)$  ISR correction:

$$
\delta_{ISR}^{(1)}(p_1^{eff}, p_2^{eff}) = \frac{\alpha}{\pi} \left( \ln \frac{s_{eff}}{m_e^2} - 1 \right). \tag{19}
$$

Such a procedure allows us to use the EW corrections also in the WW-threshold region, however, in this region the LPA becomes less precise. Since no other calculation with the  $\mathcal{O}(\alpha)$  EW corrections for the W-pair production and decay process exits for the WWthreshold region, we estimate, for the moment, the precision of YFSWW3 in that region conservatively at 2%, just as for the ISR approximation. This can be improved in the future when more calculations/tests are done.

Two comments are in order about approximation used in evaluation of Eqs. (14-16):

- 1. In the  $LPA_{a,b}$ , the 1-loop corrections should be evaluated "on-pole", i.e. for the complex W mass:  $M^2 = M_W^2 - iM_W \Gamma_W$ . This would, however, require the analytic continuation of the on-shell 1-loop corrections to the second Riemann sheet. We avoid this by using in the LPA residuals the approximation  $M \simeq M_W$ . Since this is done for the  $\mathcal{O}(\alpha)$  corrections the error introduced by this approximation is of the order of  $(\alpha/\pi)(\Gamma_W/M_W) < 10^{-4}$ , which is negligible for our aimed precision.
- 2. A coherent sum over  $W$  spins between the production and decay stages is included in Eq. (14) in the  $\bar{\beta}_0^{(0)}$  function, but not in the non-leading (NL)  $\mathcal{O}(\alpha)$  EW correction. This should be sufficient for the LEP2 precision as the total EW correction in the LEP2 energy range is typically  $\sim 1-2\%$ . However, the W-spin effects can be included also in the NL  $\mathcal{O}(\alpha)$  EW correction, if necessary.

The  $\mathcal{O}(\alpha)$  real photon ISR and photon emission in the WW-production stage are included through the following IR-finite function:

$$
\bar{\beta}_{1}^{(1)}(\{p,Q,q,k\}^{\mathcal{R}_{\wp}}) = D_{\gamma}^{(1)}(\{p,Q,q,k\}^{\mathcal{R}_{\wp}}) - \tilde{S}(\{p,Q,q,k\}^{\mathcal{R}_{\wp}}) \bar{\beta}_{0}^{(0)}(\{p,Q,q\}^{\mathcal{R}_{\wp}})
$$
(20)

where  $D_{\gamma}^{(1)}$  is the differential cross section for the single hard photon radiation in the  $WW$ -production stage and the non-radiative  $W$ -decays. For this we use the calculations of Ref. [32], where the W's are taken on-shell. In order to accommodate them in our offshell process, we use general formulae for W-polarisation vectors in terms of their off-shell four-momenta [33] in the spin amplitude calculations, and perform a coherent summation over the W's polarisations of the production and decay amplitudes. In fact, the hardphoton amplitudes of Ref. [32] are given in the massless-fermion approximation, so they become inaccurate when a photon is emitted close to a fermion direction. To correct this, we supplement these amplitudes with the mass terms according to the CALKUL prescription of Ref. [34].

In Eqs. (4-5) we use the IR-finite  $\bar{\beta}$ -functions for the ISR  $\bar{\beta}_{0,ISR}^{(3)}$ ,  $\bar{\beta}_{1,ISR}^{(3)}$ ,  $\bar{\beta}_{2,ISR}^{(3)}$  and  $\bar{\beta}_{3,ISR}^{(3)}$ , calculated up to  $\mathcal{O}(\alpha^3)$  LL. They are exactly the same as in KoralW, see Ref. [18]. We define in addition:

$$
\Delta \bar{\beta}^{(3)}_{0,ISR} = \bar{\beta}^{(3)}_{0,ISR} - \bar{\beta}^{(1)}_{0,ISR}, \quad \Delta \bar{\beta}^{(3)}_{1,ISR} = \bar{\beta}^{(3)}_{1,ISR} - \bar{\beta}^{(1)}_{1,ISR}.
$$
 (21)

In Eqs. (4-5) they are evaluated only for the ISR photons. In principle, these ISR residuals could be calculated for all photons – it is still consistent with the LL ISR approximation.

#### **2.2.5 Pre-tabulated EW Corrections**

We have implemented also the pre-tabulated (or "fast") version of the EW corrections. In this mode, a pre-tabulation of the NL  $\mathcal{O}(\alpha)$  EW corrections

$$
\delta_{EW}^{NL}(\{p,Q\}) = \delta_{v+s}^{(1)}(\{p,Q\};k_{\epsilon}) - Y(\{p,Q\};k_{\epsilon}) - \delta_{ISR}^{(1)}(p_1,p_2) \tag{22}
$$

is done in the initialisation stage of the program. Then, during the event generation, a linear interpolation of the pre-tabulated values is performed for each event. The pretabulation is done as a function of  $\cos \theta$  of the W<sup>−</sup> for fixed values of the CMS energy  $\sqrt{s}$ (set-up to the nominal energy) and of the W invariant masses (set-up to  $M_W$ ). This means that in this approach the ISR energy shift  $s \to s'$  as well as off-shellnes of the W's are not taken into account (the latter prevents this method from being used below the WWthreshold). In that respect, the pre-tabulated version of the EW corrections should be regarded as some approximation of the YFSWW3 "best" prediction. The main advantage of this version is that it is much faster in computing time than the exact ("best") one, because here the time consuming EW library is invoked only at the beginning of the program run for some number of equally spaced points instead of calling it for each generated event. We have checked that at  $\sqrt{s} = 200$  GeV, the results for the total cross section and main distributions of the pre-tabulated version differ from the corresponding results of the "best" one by only 0.1%, which is well below the required theoretical precision for the LEP2 data analysis.

#### **2.2.6 Fixed-Order Calculation**

By truncating the master formula (4) at some power of the coupling constant  $\alpha$  one can obtain a fixed order calculation, e.g.  $\mathcal{O}(\alpha^0)$ ,  $\mathcal{O}(\alpha^1)$ .

At  $\mathcal{O}(\alpha^0)$  (the Born approximation), one gets the differential distribution

$$
\rho_0^{(0)}(\{p,Q,q\}) = \bar{\beta}_0^{(0)}(\{p,Q,q\}).\tag{23}
$$

At  $\mathcal{O}(\alpha^1)$ , there are two contributions: (1) from the one-loop virtual corrections and the real soft photon radiation

$$
\rho_0^{(1)}(\{p,Q,q\};k_\epsilon) = \bar{\beta}_0^{(0)}(\{p,Q,q\}) \left[1 + \delta_{v+s}^{(1)}(\{p,Q\};k_\epsilon)\right],\tag{24}
$$

and (2) from the real hard photon radiation

$$
\rho_1^{(1)}(\{p,Q,q\},k) = D_\gamma^{(1)}(\{p,Q,q\},k). \tag{25}
$$

We have implemented the above fixed order calculations in YFSWW3. They are available through the parallel weights as explained in Table 9 of Appendix A.

#### **2.2.7 Radiative Corrections for** W**-Decays**

Radiative corrections in W decays are not included in the above formulae explicitly. However, we include them in the overall normalisation of the cross section by normalising the W decay amplitudes to the W branching ratios  $(BR)$ , which can be provided through the input parameters of the program. This means that in the  $\beta$ -functions of Eq. (6) for the  $(i, j)$ -th  $W^-W^+$  decay channel, we use the normalisation constant

$$
\mathcal{N}_{ij} = \frac{B_i B_j}{B_{ref}^2},\tag{26}
$$

with

$$
B_{ref} = \frac{\alpha_W M_W}{12\Gamma_W \sin^2 \theta_W},\tag{27}
$$

where  $\theta_W$  is the weak mixing angle, and  $\alpha_W = \alpha_{G_\mu}$  in our recommended  $G_\mu$ -scheme while in the so-called  $\alpha$ -scheme we set  $\alpha_W = \alpha$ .  $B_i$  is the BR for the *i*-th *W*-decay channel, while  $B_{ref}$  is the reference BR used for the normalisation of the actual matrix element; see Ref. [16] for more details. For the fully inclusive process (all channels), the normalisation constant is

$$
\mathcal{N}_{all} = \frac{1}{B_{ref}^2}.\tag{28}
$$

It turns out that the BR's calculated at the Born level in the  $G_{\mu}$ -scheme – the socalled improved-Born approximation  $(IBA)$  – agree within 0.1% with the full one-loop results [11]. Such an IBA option is also included in the program – for this one needs only to supply (through the input parameters) the values of the CKM matrix elements. In that case

$$
B_i = \begin{cases} B_{ref} : & \text{for leptons,} \\ 3|V_i^{\text{CKM}}|^2 \left(1 + \frac{\alpha_s(M_W^2)}{\pi}\right) B_{ref} : & \text{for quarks,} \end{cases}
$$
(29)

where  $V_i^{\text{CKM}}$  is the CKM matrix element for the *i*-th *W*-decay channel, and  $\alpha_s(M_W^2)$  is the QCD coupling constant at the  $M_W$  scale.

The real photon radiation in  $W$  decays which is generated by **PHOTOS**, by construction does not affect the overall normalisation of the cross section – this is of course motivated by the KLN theorem [35, 36].

#### **2.2.8 ISR Reference Differential Distribution**

Eqs. (4-5) define the so-called "best" physics model of YFSWW3 and if the corresponding weight is used as a rejection weight in order to generate unweighted (constant-weight) events, then we say that YFSWW3 is run in the "best" mode. For the purpose of combining the fully exclusive (multi-photon) differential distributions from YFSWW3 and KoralW, such that the resulting distributions contain both the LPA  $\mathcal{O}(\alpha)$  EW corrections (missing in KoralW) and 4f-background diagram corrections (missing in YFSWW3), using eventper-event correction-weights, it is necessary to define a certain simplified auxiliary fully exclusive differential distribution  $d\sigma_R$ , which is *common to both programs*, and to implement the corresponding MC weight  $w_R$ . In YFSWW3 the weight  $w_R$  can be used also optionally as a main rejection weight – this is the so-called "ISR mode". Otherwise,  $w_R$ is one of many alternative weights calculated simultaneously with the "best mode" and is available to the user, and/or it is used to calculate the correction-weight which serves for the purpose of introducing the missing  $\mathcal{O}(\alpha)$  EW corrections in events generated by KoralW.

In the reference distribution  $d\sigma_R$  only the *numerically leading* corrections, that is the ISR, the Coulomb correction, etc. are taken into account. It includes the CC03 matrix element defined identically in YFSWW3 and KoralW. We say also sometimes that this is the distribution of the ISR-type model. The corresponding fully exclusive reference differential distribution, replacing  $\rho_n$  of Eq. (5), we define as follows:

$$
\rho_n^R(p_1, p_2; q_1, \dots, q_4, k_1, \dots, k_n) = \prod_{i=1}^n \tilde{S}_I(p_1, p_2, k_i) \theta(k_i^0 - k_\epsilon)
$$
  
\n
$$
\times e^{Y_I(p_1, p_2; \epsilon)} \left[ 1 + \delta_C(Q_1, Q_2, M_W, \Gamma_W) \right] \left[ 1 + \delta_{An}^{\text{TGC}} (\{p, Q, q\}^{\mathcal{R}}) \right]
$$
  
\n
$$
\left\{ \bar{\beta}_{0,ISR}^{(3)} (\{p, Q, q\}^{\mathcal{R}}) + \sum_{i=1}^n \frac{\bar{\beta}_{1,ISR}^{(3)} (\{p, Q, q\}^{\mathcal{R}}, k_i)}{\tilde{S}_I (\{p\}^{\mathcal{R}}, k_i)} + \sum_{i>j}^n \frac{\bar{\beta}_{2,ISR}^{(3)} (\{p, Q, q\}^{\mathcal{R}}, k_i, k_j)}{\tilde{S}_I (\{p\}^{\mathcal{R}}, k_i) \tilde{S}_I (\{p\}^{\mathcal{R}}, k_j)}
$$
  
\n
$$
+ \sum_{i>j>l}^n \frac{\bar{\beta}_{3,ISR}^{(3)} (\{p, Q, q\}^{\mathcal{R}}, k_i, k_j, k_l)}{\tilde{S}_I (\{p\}^{\mathcal{R}}, k_i) \tilde{S}_I (\{p\}^{\mathcal{R}}, k_i) \tilde{S}_I (\{p\}^{\mathcal{R}}, k_l)}
$$
 (30)

where with respect to Eq.  $(5)$  we have made the following replacements:

$$
Y' \longrightarrow Y_I(p_1, p_2; \epsilon) = 2 \frac{\alpha}{\pi} \left[ \left( \ln \frac{s}{m_e^2} - 1 \right) \ln \epsilon + \frac{1}{2} \ln \frac{s}{m_e^2} - 1 + \frac{\pi^2}{2} \right],
$$
\n
$$
\tilde{S} \longrightarrow \tilde{S}_I(p_1, p_2, k),
$$
\n(31)

and we include the pure ISR LL  $\bar{\beta}$ 's only. The WSR in the above distribution is just absent, which means that there is only one photon partition (where all photons are assoctiated to the ISR) with the weight  $p_{\varphi} = 1$ . In the actual MC program,  $\rho_n^R$  should be implemented with a MC weight in the operational mode when the WSR is switched of – through the parallel weights. Both these possibilities are included in YFSWW3. However, it can also be

also implemented as a MC weight when the WSR is switched on. In such a case the sums over  $\beta$ 's should extend to all photons.

The above ISR reference cross section is also used in this and other works to define the so-called non-leading (NL) corrections

$$
\sigma_{NL} \equiv \sigma - \sigma_R = \int \left( d\sigma - d\sigma_R \right). \tag{32}
$$

The subscript NL (non-leading) expresses the fact that these corrections are numerically smaller than the leading ISR corrections. It does not mean, however, that these corrections are free of logarithmic contributions, such as e.g.  $\ln(s/M_W^2)$ , but these logarithms are numerically much smaller than the ISR basic logarithm  $\ln(s/m_e^2)$ .

As already indicated, the same reference ISR differential distribution of Eq. (30) (for the same CC03 matrix element) is also implemented in KoralW, and it has been checked numerically to a very high accuracy [6, 20] that its KoralW implementation agrees with the one implemented in the present YFSWW3 program. Having done that, it is possible to combine the results of the KoralW and YFSWW3 programs by re-weighting the MC events, in order to include both the effects of the 4f-background and the LPA  $\mathcal{O}(\alpha)$  NL corrections in the MC predictions for the  $W$ -pair production and decay process. This is done in practice by re-weighting the MC events produced by KoralW with the correction-weight provided by YFSWW3. The correction  $\delta_{NL}^R$  to be used by KoralW is defined as follows

$$
1 + \delta_{NL}^{R} = \frac{\rho_n^{\text{Best}}(p_1, p_2; q_1, \dots, q_4, k_1, \dots, k_n)}{\rho_n^R(p_1, p_2; q_1, \dots, q_4, k_1, \dots, k_n)},
$$
\n(33)

where the numerator and denominators are defined in Eq.  $(5)$  and  $(30)$ . A few remarks are in due order. The above ratio is, in fact, calculated as a ratio of the corresponding MC weights. The YFSWW3 program has to be run in the mode with the WSR switched on, because  $\rho_n^{\text{Best}}$  includes the summation over the ISR–WSR photon partitions, see Eq. (5), through the multi-channel reduction procedure  $\mathcal{R}_{\varphi}$ . Under these conditions the above correction includes the complete  $\mathcal{O}(\alpha)$  correction, which can be used to correct the fully exclusive distributions generated by KoralW, on the event-per-event basis. As we shall see in Subsection 4.12, the YFSWW3 program provides at present only a numerically efficient approximation of the above  $\delta_{NL}^R$ .

## **2.3 YFS Reduction/Extrapolation Procedures**

It is characteristic and inherent feature of the YFS exponentiation that the IR-finite  $\beta_i$ distributions require extrapolation to a larger phase space with the additional "spectator" photons. For instance function  $\bar{\beta}_0$  is in our case originally defined at the  $(\{q_1, q_2, q_3, q_4\})$  $({q})$  point of the 4-particle phase space and it has to be also defined at every  $({q}, k_1, \ldots, k_n)$ point of the  $(4+n)$ -particle phase space. The procedure of extending the domain of the  $\bar{\beta}_0$ function  $\bar{\beta}_0(\lbrace q \rbrace) \rightarrow \bar{\beta}_0^E(\lbrace q \rbrace, k_1, \ldots, k_n)$  we call the "extrapolation procedure". The only true limitation in the choice of the extrapolation procedure is that  $\bar{\beta}_0^E(\{q\},0,\ldots,0)$  =

 $\bar{\beta}_0(\lbrace q \rbrace)$  must hold. Typically,  $\bar{\beta}_0(\lbrace q \rbrace)$  is defined in terms of dot-products of the fourmomenta  $p_i \cdot q_j$  (or inner spinor products). Extrapolation may be done in a natural way by using exactly the same algebraic expressions in the larger phase space that were originally obtained from the Feynman diagrams in the smaller phase space. In the smaller phase space the dot-products obey certain relations due to the four-momentum conservation, which in the presence of the additional photons do not hold any more – this is the main mechanism in the realization of such an extrapolation. Another useful method of implementing the extrapolation (especially in the case when  $\beta_0({q})$ ) is implemented in a form of a black-box procedure, which requires as the input the four-momenta in the 4-particle phase space) is to project the  $({q}, k_1, \ldots, k_n)$  point into the "reduced" point  ${q}R$  using some kinematical manipulations (boosts, rotations, re-scalings) on the fourmomenta, and subsequently plugging it into  $\bar{\beta}_0^E(\lbrace q \rbrace, k_1, \ldots, k_n) \equiv \bar{\beta}_0(\lbrace q \rbrace^{\mathcal{R}})$ . The above "reduction procedure" is, of course, less general than the extrapolation procedure. Last but not least, let us note that the extrapolation procedure  $({q}) \rightarrow ({q}, k_1, \ldots, k_n)$  is the reverse procedure to the procedure of defining the residua at the IR divergent points/poles  $({q}, k_1,..., k_n) \rightarrow ({q}) = ({q}, 0,..., 0)$  in the derivation of the resummation of the IR divergences to the infinite order (i.e. the derivation of the YFS exponentiation). The extrapolation procedure  $\bar{\beta}_1(\{q\}, k_j) \rightarrow \bar{\beta}_1^E(\{q\}, k_1, \ldots, k_j, \ldots, k_n)$  is quite analogous. It has to obey the relation  $\bar{\beta}_1(\{q\}, k_j) \to \bar{\beta}_1^E(\{q\}, 0, \ldots, 0, k_j, 0, \ldots, 0)$ . All photons except the j-th one are here the spectators.

## **2.4 Multichannel YFS Reduction/Extrapolation**

Sometimes it is useful to split the  $\beta$ 's into several components and introduce a different extrapolation/reduction procedure for each component. This is perfectly within the freedom which we have. For instance, in YFS3 in the centre-of-mass of the Z-boson neither the initial beams nor the final fermion pairs have the momenta back-to-back. There are four possible definitions of the scattering angles in this frame. One defines  $\bar{\beta}_0$  as a sum of four differential Born-level distributions, each for a different scattering angle. They might be summed up with the same weight  $1/4$ , but, in fact, also a more sophisticated mixture is implemented [37]. A similar multichannel extrapolation procedure is used in BHLUMI [38,39]. In the present work we employ another kind of the multichannel extrapolation, introduced for the first time in the unpublished program BHWIDE [40].

Let us elaborate on that method. Our exponentiation model is based on the real soft photon factor S and the corresponding virtual photon function  $\Re B$  to which photons emitted from the beams and from the  $W$ 's contribute coherently. One cannot, therefore, say whether a given photon is emitted from the initial state or from the  $W$ 's. One may, however, say something about that in a probabilistic way. If we split  $\tilde{S}$  as follows:

$$
\tilde{S}(k) = -\frac{\alpha}{4\pi^2} \left( \frac{p_1}{kp_1} - \frac{p_2}{kp_2} - \frac{Q_1}{kQ_1} + \frac{Q_2}{kQ_2} \right)^2 = \tilde{S}_I(k) + \tilde{S}_W(k) + \tilde{S}_{int}(k),
$$
\n
$$
\tilde{S}_I(k) = \left( \frac{p_1}{kp_1} - \frac{p_2}{kp_2} \right)^2, \quad \tilde{S}_W(k) = \left( \frac{Q_1}{kQ_1} - \frac{Q_2}{kQ_2} \right)^2,
$$
\n(34)

Then we may define for each photon a probability

$$
p_I(k) = \frac{\tilde{S}_I(k)}{\tilde{S}_I(k) + \tilde{S}_W(k)},
$$
\n(35)

that it was emitted from the beams, and the probability  $p_W (k) = 1 - p_I (k)$  that it was emitted from the  $W$ 's. The above probabilities are a kind of the LL concept which has to be used with care. It may help to sum up higher order QED corrections in the LL approximation. In particular, it may allow us to construct a multichannel type of the reduction/extrapolation in which we may say for the spectator photons whether they were emitted by the beams  $(ISR)$  or by the W bosons (WSR). This is done as follows. For each phase space point we split the differential distributions into  $2<sup>n</sup>$  components corresponding to  $2^n$  possible associations of n photons to the ISR or the WSR, with the weight being the product  $P(k)$  of the corresponding  $p_I(k_i)$  or  $p_W(k_i)$ . This product is exactly the partition weight  $p_{\varphi}$  in eqs. (4) and (7). For each component we may apply a separate reduction procedure which "knows" whether a given spectator photon belongs to the ISR or the WSR. The above procedure is, in practice, simpler than is said above, because in the MC realization we start from the YFS3 differential distribution in which  $S_{int}(k)$ is neglected, and the sum over the association of the photons to the ISR or the WSR is "randomised". In other words, we generate only one of the  $2<sup>n</sup>$  possible associations and therefore, for a given event, we work with only one component (association), for which we may immediately employ its "native" reduction procedure – that is we may use the information on the photon associations directly from the YFS3 MC generator, see also the following Section for additional discusion. Let us stress again that this solution should be used with great care, especially for the non-spectator photons.

# **3 Monte Carlo Algorithm**

In constructing the MC algorithm for the cross section calculation and the event generation, we start from the master formula of Eq. (4) and perform step-by-step simplifications in the differential distribution, compensating them with appropriate weights. We do this until we reach a differential distribution, which is simple enough to be generated by using the standard MC techniques. The MC algorithm of YFSWW3 for the Born-like WW production and decay is identical to the one used in KoralW for the so-called CC03 option [16], while the algorithm for the multi-photon radiation in the  $e^+e^- \rightarrow W^+W^-$  process is based on the one implemented in the program YFS3 of KORALZ [29] for the process  $e^+e^- \rightarrow f\bar{f}$ . Since  $W$ 's are much heavier than light fermions and, in general, have different invariant masses, we had to make a few modifications in the latter algorithm. The most important of them are:

• generalisation of the photon radiation formulae to allow for large and different masses of radiating particles<sup>6</sup>,

<sup>&</sup>lt;sup>6</sup>This extension is also included in the YFS3 of  $K\mathcal{K}$  MC program [37].

• inclusion of interferences between the radiation from the initial state and from the WW state, both in the YFS IR functions  $\tilde{S}$  and Y and in the IR finite residuals  $\bar{\beta}$ .

The algorithm of YFS3, although used for a decade as part of other programs, was not documented until recently. Its first full description can be found in two recent works [37,41]. We therefore do not describe it here in detail, but refer the interested reader to the above two papers. Below we explain only the main steps in the YFSWW3 algorithm that lead to the algorithms of YFS3 and KoralW, and then comment on the YFS reduction/extrapolation procedures.

## **3.1 Main Steps in Construction of the MC Weight**

The MC algorithm of YFSWW3 is based on the importance sampling method. In constructing it, we start from the master formula (4) and make a series of simplifications compensating them with appropriate weights until we reach a distribution that is simple enough to be generated using the basic MC methods (see e.g. Refs. [42, 43]), as we indicated above. Here, we describe only the main simplifications in Eq. (4) that lead to the formula which can be generated with the help of the MC algorithms used in the programs YFS3 and KoralW. They are:

## 1.  $\bar{\beta}$ -functions:

For the agregate of the  $\bar{\beta}$ -functions we do the following replacement:

$$
\mathcal{B}\left(\{p,Q,q,k\}^{\mathcal{R}_{\wp}}\right)\longrightarrow b_0\left(\{p,Q,q\}^{\mathcal{R}_{\wp}}\right),\tag{36}
$$

which is compensated with the "model" weight

$$
w_{\beta}^{\wp} = \frac{\mathcal{B}\left(\{p, Q, q, k\}^{\mathcal{R}_{\wp}}\right)}{b_0\left(\{p, Q, q\}^{\mathcal{R}_{\wp}}\right)},\tag{37}
$$

where  $b_0 = \bar{\beta}_0^{(0)}$  is the Born-level differential cross section for the W-pair production and decay process as given in Eq. (4) of Ref. [16]. To evaluate the model weight  $w_{\beta}^{\wp}$ , we use the partition-dependent reduction procedures described in Subsection 2.2.4.

#### 2. YFS form factor:

The YFS form-factor we simplify with the replacement:

$$
Y'(p_1, p_2, Q_1, Q_2; k_{\epsilon}) \longrightarrow Y_I(p_1, p_2; \epsilon) + Y_W(Q_1, Q_2; k_{\epsilon}), \tag{38}
$$

which is compensated with the weight

$$
w_Y = \exp[Y' - Y_I - Y_W],\tag{39}
$$

where  $Y_I$  is given in Eq. (31) and  $Y_W$  is the YFS IR function corresponding to the photon radiation from the  $W^-W^+$  electric dipole:

$$
Y_W(Q_1, Q_2; k_\epsilon) = 2\alpha \Re B(Q_1, Q_2) + 2\alpha \tilde{B}(Q_1, Q_2, k_\epsilon). \tag{40}
$$

The explicit formulae for the above  $\Re B$  and  $\tilde{B}$  are given in Ref. [3]; we do not repeat them here because they are rather lengthy. This simplification corresponds to neglecting the ISR-WSR interference terms in the YFS form factor.

3.  $S$ -factors:

In the  $\tilde{S}\text{-factors}$  we also neglect the ISR-WSR interferences:

$$
\tilde{S}(p_1, p_2, Q_1, Q_2, k) \longrightarrow \tilde{S}_I(p_1, p_2, k) + \tilde{S}_W(Q_1, Q_2, k), \tag{41}
$$

and compensate this with the weight

$$
w_{\tilde{S}} = \prod_{i=1}^{n} \frac{\tilde{S}(p_1, p_2, Q_1, Q_2, k)}{\tilde{S}_I(p_1, p_2, k) + \tilde{S}_W(Q_1, Q_2, k)},
$$
\n(42)

where  $\tilde{S}_I$  and  $\tilde{S}_W$  are given in Eq. (8).

After these simplifications, from Eq. (4) we obtain the formula for the first-level "crude" cross section:

$$
\sigma_{\text{Crude}} = \sum_{n=0}^{\infty} \frac{1}{n!} \int ds_1 ds_2 \frac{d^3 Q_1}{Q_1^0} \frac{d^3 Q_2}{Q_2^0} \prod_{l=1}^4 \frac{d^3 q_l}{q_l^0} \left[ \prod_{i=1}^n \frac{d^3 k_i}{k_i^0} \left\{ \tilde{S}_I(k_i) + \tilde{S}_W(k_i) \right\} \theta(k_i^0 - k_\epsilon) \right]
$$
  

$$
\delta^{(4)} \left( p_1 + p_2 - Q_1 - Q_2 - \sum_{i=1}^n k_i \right) \delta^{(4)} (Q_1 - q_1 - q_2) \delta^{(4)} (Q_2 - q_3 - q_4)
$$
  

$$
e^{Y_I + Y_W} \sum_{\varphi \in \{I, W\}^n} p_\varphi b_0 (\{p, Q, q\}^{\mathcal{R}_\varphi}).
$$
 (43)

The above distribution can be generated using the MC algorithms of YFS3 and KoralW. To make this more transparent, we shall write this formula in a slightly different but equivalent form.

The product of the  $\tilde{S}$ -factors in the square brackets in Eq. (43) together with the sum over the photon partition can be written as

$$
\prod_{i=1}^{n} \frac{d^{3}k_{i}}{k_{i}^{0}} \left\{ \tilde{S}_{I}(k_{i}) + \tilde{S}_{W}(k_{i}) \right\} \theta(k_{i}^{0} - k_{\epsilon}) \sum_{\varphi \in \{I, W\}^{n}} p_{\varphi} b_{0} \left( \{p, Q, q\}^{\mathcal{R}_{\varphi}} \right) =
$$
\n
$$
\sum_{\varphi \in \{I, W\}^{n}} \prod_{\varphi_{i} = I} \frac{d^{3}k_{i}}{k_{i}^{0}} \tilde{S}_{I}(k_{i}) \theta(k_{i}^{0} - k_{\epsilon}) \prod_{\varphi_{j} = W} \frac{d^{3}k_{j}}{k_{j}^{0}} \tilde{S}_{W}(k_{j}) \theta(k_{j}^{0} - k_{\epsilon}) b_{0} \left( \{p, Q, q\}^{\mathcal{R}_{\varphi}} \right)
$$
\n
$$
(44)
$$

where we have substituted Eq. (7) for the partition weight  $p_{\varphi}$ .

After some algebra, and exploiting the Bose-Einstein symmetry for photons, the formula of Eq. (43) can be written as

$$
\sigma_{\text{Crude}} = \sum_{n_I=0}^{\infty} \sum_{n_W=0}^{\infty} \int ds' \frac{d^3 P'}{P'^0} \delta^{(4)} \left( p_1 + p_2 - \sum_{i=1}^{n_I} k_i - P' \right) ds_1 ds_2 \frac{d^3 Q_1}{Q_1^0} \frac{d^3 Q_2}{Q_2^0} \n\left[ \frac{1}{n_I!} \prod_{i=1}^{n_I} \frac{d^3 k_i}{k_i^0} \tilde{S}_I(k_i) \theta(k_i^0 - k_\epsilon) \right] \left[ \frac{1}{n_W!} \prod_{j=1}^{n_W} \frac{d^3 k_j}{k_j^0} \tilde{S}_W(k_j) \theta(k_j^0 - k_\epsilon) \right] \n\delta^{(4)} \left( P' - Q_1 - Q_2 - \sum_{j=1}^{n_W} k_j \right) \prod_{l=1}^4 \frac{d^3 q_l}{q_l^0} \delta^{(4)} (Q_1 - q_1 - q_2) \delta^{(4)} (Q_2 - q_3 - q_4) \ne^{Y_I} e^{Y_W} b_0 (\{p, Q, q\}^{\mathcal{R}_{\varphi}}),
$$
\n(45)

where  $s' = P^2$  is the CMS energy squared in the ISR-reduced (effective) frame, and  $n_I$ and  $n_W$  are the multiplicities of the ISR and WSR photons, respectively.

To generate the ISR and WSR according to Eq. (45), we can use the MC algorithm of YFS3 (see Refs. [37,41]) for multi-photon radiation in the fermion-pair production, where the initial-final state interferences were neglected. The only modification we had to do in this algorithm was to extend it to the case of heavy particles of unequal masses (see Ref. [37]). Generating particular values of  $n<sub>I</sub>$  and  $n<sub>W</sub>$  corresponds to choosing a given photon partition for  $n = n_I + n_W$  in the sum of Eq. (44). This means that the sum over partitions is "randomised" in the program, i.e. not evaluated directly but generated using the MC methods. For the given-generated photon partition, we then calculate the weights  $w_{\beta}^{\wp}$ ,  $w_Y$  and  $w_{\tilde{S}}$ . Such a solution can be regarded as a multi-branch MC algorithm, see Ref. [43], where each branch corresponds to a particular photon partition.

## **3.2 MC Weights and Absolute Normalisation**

In the process of simplifying the fully differential distribution of Eq. (4)

$$
\sigma_{\text{Best}} = \sum_{n=0}^{\infty} \frac{1}{n!} \int d\text{Lips}_n(\{p; q\}, k_1, \dots, k_n) \rho_n^{\text{Best}}(\{p; q\}, k_1, \dots, k_n)
$$
(46)

described in the previous section we have finished with the "crude differential distribution"  $\rho^{\text{Crude}}$  inside the integral

$$
\sigma_{\text{Crude}} = \sum_{n_I=0}^{\infty} \sum_{n_W=0}^{\infty} \frac{1}{n_I!} \frac{1}{n_W!} \int d\text{Lips}_n(\{p; q\}, k_1, \dots, k_n) \; \rho_{n_I, n_F}^{\text{Crude}}(\{p; q\}, k_1, \dots, k_n), \quad (47)
$$

where  $n = n_I + n_F$ . Using the above notation, the total correcting weight is defined as follows:

$$
w^{(1)} = \frac{\rho_n^{\text{Best}}(\{p; q\}, k_1, \dots, k_n)}{\rho_{n_I, n_F}^{\text{Crude}}(\{p; q\}, k_1, \dots, k_n)} = w_\beta^\wp w_Y w_{\tilde{S}}.
$$
\n(48)

In the actual program it comes in several versions, because for the purpose of the technical tests, and for the discussion of the physical precision, we need to switch off/on certain contributions in the full distribution  $\rho_n^{\text{Best}}$ .

However, in the actual MC program we do not actualy generate the distribution  $\rho^{\text{Crude}}$ , but a certain more primitive "primary" distribution  $\rho^{\text{Prim}}$ . For its definition and full description, and the description how events are generated according to this distribution, starting from the uniform random numbers, we refer the reader to the most complete documentation of the YFS3 Monte Carlo algorithm in Ref. [37]; Refs. [16] and [27] can also be helpful. The weight correcting for the transition from the primary to crude distribution is given by

$$
w^{(2)} = \frac{\rho_{n_I, n_F}^{\text{Crude}}(\{p; q\}, k_1, \dots, k_n)}{\rho_{n_I, n_F}^{\text{Prim}}(\{p; q\}, k_1, \dots, k_n)}
$$
(49)

and is fully defined in Ref. [37]. The total MC weight is of course equal to the product

$$
w = w^{(1)} \ w^{(2)} \tag{50}
$$

or

$$
w = w^{\text{Model}} w^{\text{Crude}}, \tag{51}
$$

with

$$
w^{\text{Model}} = w^{\wp}_{\beta} b_0, \qquad w^{\text{Crude}} = w^{(2)} w_Y w_{\tilde{S}} b_0^{-1}, \qquad (52)
$$

where  $w^{\text{Model}}$  is called in the program the "model weight" (this weight and its many variants are provided in the WtSet array; see Section 5), and  $w^{Crude}$  is called the "crude weight" (in the program it is equal to the product  $WtCrud1*WtCrud2$ ; see Section 5).

The integrated cross section is given by the product of the average weight and the integrated primary cross section

$$
\sigma = \langle w \rangle \sigma^{\text{Prim}} = \langle w \rangle \int d\sigma^{\text{Prim}}.\tag{53}
$$

The integrated primary cross section we also call a "normalisation cross section", because it provides the absolute normalisation for the whole MC calculation.

# **4 Structure of the Program**

In this section we provide the reader with a brief guide of the YFSWW3 program. We shall describe its main routines, libraries and interfaces. We want to note here that the program, in the distribution version, is prepared for a UNIX/Linux-type operating system that supports directories and the make utility. The source code is distrubuted over a number of subdirectories, in order to make the structure of the program more transparent and

easier to handle. Also a system of the Makefile's is provided, for compilation, execution and other auxiliary functions (e.g. clean-up). (Of course, this organization, which is in fact rather simple, can be avoided and the whole source code can be put into a single FORTRAN file.) In the following we give a review of all YFSWW3 subdirectories. We start from the directories that are most interesting from the user's point of view and then go to the ones with more technical contents. In the distribution package, all these subdirectories are located in the main YFSWW3 directory: yfsww3-1.16-export. This directory also comprises two important files: README and RELEASE.NOTES, which we recommend the user to look trough before using the program. They contain some basic information about YFSWW3: how to compile/link and run the program, a brief documentation of the code, etc.

### **4.1** demo **– Demonstration Program**

The subdirectory demo contains a demonstration program in the file demo.f. Generally, the user is supposed to provide his/her own main program, nevertheless, the file quoted here provides a simple example of such a program. It has a double role: (1) as a useful template, and (2) as a first cross-check that the MC generator YFSWW3 runs correctly on a given installation. The essential part of this program is a loop in which a series of MC events is generated. It also reads the input from a disk file, but no histogramming is performed and most of the output comes from the generator itself. At the end of the program, a MC integrated cross section of YFSWW3 is compared with the Born-level and ISR results from the semi-analytical program KorWan. The program is compiled/linked and executed, with the help of the Makefile, for the input data set given in the files demo. input. The program also reads the default settings provided in the file data DEFAULTS located in the directory data files – some of these default settings are overridden by data from demo.input. The demonstration program is run for unweighted events with the external libraries PHOTOS, TAUOLA and JETSET switched on. The output, written into the disk file demo.output, can then be compared with the one provided in the file demo.output.linux. It was obtained on a PC Intel Pentium III under the Linux RedHat 6.1 operating system.

## **4.2** data files **– Default Input Data**

The subdirectory data files contains the input data file data DEFAULTS with the defaults settings for YFSWW3. It is identical with the one used in the program KoralW, so the two programs can be set-up from the same input data file! This facilitates considerably combining the results of both programs; see Ref. [20] for more details. Some entries in this data file are dummy for YFSWW3 and are kept only for compatibility with KoralW, while some of them are specific to YFSWW3 and are treated as dummy parameters in KoralW. They are denoted by appropriate comments. This file can also be used by the user as a template to create his/her own input data file, where only those entries that will have different settings than in the default data file may be included. The user input file should be read after reading the file data DEFAULTS, so that the user settings would override the default ones; see the example in the demo.f file described in the previous subsection. This directory comprises also some older data files kept for backward compatibility. Their names contain, after a dot, the two last digits of the year of their creation. The newest one is identical with the file data DEFAULTS.

## **4.3** yfsww **– Master Unit**

The subdirectory yfsww contains the actual Monte Carlo event generator. Subprograms used directly by the user are the following:

- YFSWW\_ReaDataX the subprogram used to read, from the disk file, the default input data of YFSWW3 and subsequently the data of the user into the array xpar at the very beginning of the use of YFSWW3.
- YFSWW Initialize the subprogram that does all initialisations of internal variables. First, it sets-up the main parameters of the program (through the routine filexp) according to the values in the input data files, then it calls several *initialis*ers of the main internal modules of the generator, such as  $KarLud(-1,...),$  and of external packages, such as TAUOLA, etc. It prints out directly or indirectly all the input parameters.
- YFSWW\_Make the most important subprogram of YFSWW3. It generates single MC events. Functionally, it is a high-level management subprogram in the event generation. It invokes (through the routine yfsww3) other routines that perform specific tasks, such as: generation of ISR photons (KarLud), generation of radiative photons from W's (KarFin), generation of the W's and final 4f four-momenta (WW Presam), evaluation of the Coulomb correction (WTCoul), calculation of the matrix element (Model), of the YFS form factor, of the interference corrections, etc. It builds up the total MC weight from the weights supplied by these routines. This weight is then returned, in the weighted-event mode, as the main event weight, or used in the rejection loop (in the routine yfsww3), in the unweighted-event mode, for constructing the weight=1 event. It also calls PHOTOS which generates photon radiation in the W decays, TAUOLA for decaying of the final state  $\tau$ 's (if they appear), and JETSET to perform fragmentation/hadronization of the final state quarks. It keeps track, through special monitoring routines, of all information necessary for the final results from the MC event generation.
- YFSWW Finalize does all final bookkeeping, including the calculation of the integrated (total) cross section. It prints a summary output on the whole sample of generated MC events.

The first subprogram is located in the file readata.f, while the following three are in the file yfsww3.f.

This directory contains also a collection of utility routines which can be used e.g. to access information on particle flavours and four-momenta, on event weights, etc. They are located in the file  $ww{\text -}get{\text -}f$  (see the comments in this file for more details).

## **4.4** model **– Matrix Elements**

The routines for the "model" weights calculations are located in the subdirectory model. The master routine here is the subroutine Model (in the file model of file which by calling some other routines, evaluates the "model" weights  $w^{\text{Model}}$  as defined in Eq. (52).

- 1. For **the Born-level matrix element** we use the same routines as in the program KoralW – they are collected in the file  $born.f.$  The same is for the ISR corrections, located in the file betas.f.
- 2. **The**  $\mathcal{O}(\alpha)$  **virtual and real soft photon corrections** are evaluated with the help of a special interface – the routine  $VirSof - in$  the file virsof.f. In the first call, this routine makes all the necessary initialisations, and then calculates the EW corrections by calling appropriate routines from the EW library for each generated event. The pre-tabulated (or "fast") version of the EW correction is invoked through the routine DnlFast (in the file dnlfast.f). This routine makes a pre-tabulation of the EW corrections in the initialisation stage of the program and then, during the event generation, it performs the linear interpolation of the pre-tabulated values to calculate the EW corrections for each event as described in Section 2.2.5.
- 3. **The**  $\mathcal{O}(\alpha)$  **hard photon matrix element** in the WW production, which contributes to the function  $\bar{\beta}_1$ , see Eq. (20), is calculated with the help of the routine eewwg, located in the file eewwg.f. This routines evaluates appropriate spin amplitudes for the process  $e^+e^- \to W^+W^-\gamma$  according to the formulas of Ref. [32], which are then combined coherently with the spin amplitudes for W decays.

In order to calculate all these contributions to the  $\bar{\beta}$ -functions, the subroutine Model calls the routines that perform appropriate "reduction" procedures as described in Section 2. Except for calculating the contributions to the YFS exponentiated cross section, this routine provides also the weights corresponding to the strict  $\mathcal{O}(\alpha^0)$  and  $\mathcal{O}(\alpha^1)$  calculations. In the end, the subroutine Model fills the array of weights with the weights corresponding to: (i) various variants of the SM models (for example different orders of QED ISR) (ii) and various components in the differential cross section for a give variant of the SM (for example contributions from various  $\bar{\beta}$ 's). The subroutine Model returns the best "model" weight.

The routine WTCoul – in the file coulco.  $f$  – for the Coulomb (both the "standard" and "screened") correction calculation is also located in this directory.

## **4.5** ewc **– Electroweak Library**

The subdirectory ewc contains the routines for the calculation of the electroweak (virtual plus soft photon) corrections in the on-shell WW production process according to Refs. [7, 10]. For the evaluation of one-loop integrals they use the package FF of Ref. [44], which is located in a separate directory (see below).

## **4.6** interfs **– Interfaces to External Libraries**

Interfaces to some external libraries are collected in the directory interfs. The most important routines are:

- inietc in the file tauola photos ini.f sets up some parameters of PHOTOS and TAUOLA.
- tohep in the file hepface.f fills in the  $/HEPEVT$  COMMON block, calls PHOTOS for photon radiation in W decays and TAUOLA for  $\tau$  decays.
- tohad in the file lundface.f calls JETSET for the quark fragmentation/hadronization.

Note that the COMMON block /HEPEVT/ is expected to contain single-precision (REAL\*4) variables.

## **4.7** wdeclib **– External Libraries for** W **Decay**

The subdirectory wdeclib provides the following programs:

- PHOTOS [22] for photon radiation in the W decays (up to two photons).
- TAUOLA [45] for  $\tau$  decays with radiative corrections.
- JETSET version 7.4 [46] for quark fragmentation/hadronization.

located in the files: photos.f, tauola.f and jetset74.f, respectively.

In YFSWW3 1.16 we use the recently modified PHOTOS, where also the photon radiation from quarks can be activated with the help of a special input parameter switch; see the tables with the input parameters in Appendix A. Note that in the distribution version of **TAUOLA** the parameters in the  $\tau$  decay modes are not adjusted to the recent experimental data. We recommend the user to replace this version of TAUOLA with the one accepted within his/her own collaboration. The technical update explained in Refs. [47, 48] will resolve this inconvenience in the future releases of the program.

## **4.8** glib **– Histogramming and Numerical Library**

A handy FORTRAN histogramming package, GlibK [49], is provided in the subdirectory glib (the file glibk.f). It is used by YFSWW3 both for hard-coded internal bookkeeping and for some optional "external" tests. The package is similar in its usage to the classic HBOOK of CERNLIB. This subdirectory also contains the useful numerical package yfslib.f with the routines for weight monitoring, random number generation, numerical integration, one and two-dimensional adaptive MC sampling, Lorentz transformations, etc.

## **4.9** semian **– Semi-analytical Program** KorWan

The subdirectory semian contains the package KorWan for the semi-analytical calculations of the cross section for the off-shell WW production and decay at the Born level and with the ISR corrections (using the structure function formalism). Also the Coulomb effect is included in KorWan in both versions: the "standard" and the "screened" ones. The package is described in detail in Refs. [16–18]. It can be used for a quick consistency check of the YFSWW3 results.

## **4.10** ff **–** FF **Package**

In the subdirectory ff is located the FF package [44] for the evaluation of one-loop integrals needed to calculate the  $\mathcal{O}(\alpha)$  EW virtual corrections.

## **4.11** dok **– Related Papers**

In the subdirectory dok, we include some of our papers related to YFSWW3. They are in the form of gzip'ed PostScript files.

## **4.12** rewt **– Re-weighting Tools**

The subdirectory rewt contains routines that are not needed for the standard MC event generation but for various event re-weighting purposes. We provide here the tools for two kinds of re-weighting: (1) the re-weighting of the KoralW generated events to correct for  $\mathcal{O}(\alpha)$  NL effects in WW production, and (2) the re-weighting of the YFSWW3 generated events to take into account effects due to some input parameters (typicaly W-mass) changes. All these tools are described in detail in the following, see also the file README provided in this subdirectory.

### **4.12.1 Re-weighting** KoralW **Events by** YFSWW3

The main tool for this kind of re-weighting is the function YFSWW\_WtNL located in the file rewt K.f. For the events, in terms of flavours and four-momenta of the final state fermions and the ISR photons, provided through its parameters, this function calculates and returns the corresponding correction weight from YFSWW3. This weight is a ratio of the fully differential distribution. In practice, we calculate the ratio of the MC weights corresponding to two distributions – this is more convenient. We can do it because the common crude distribution entering both weights cancels out. for a given number of real photons of Eq. (5), to the reference distribution in the "ISR approximation" defined in Eq. (30), which is the same as in KoralW in the CC03 mode (Eq. (4) of Ref. [18]). It is defined in Eq. (33). In the re-weighting mode of YFSWW3, we implement an approximate version of this weight:

$$
w_{NL}^{-} \equiv \frac{\rho_n^{\text{Best}-}(\{p, Q, q\}^{\mathcal{R}_I}, k_1, \dots, k_n)}{\rho_n^R(\{p, Q, q\}^{\mathcal{R}_I}, k_1, \dots, k_n)} = 1 + \delta_{NL-}^R,
$$
\n(54)

where  $\rho_n^{\text{Best}-}$  is a variant of  $\rho_n^{\text{Best}}$  in which the sum over the photon partitions is reduced to only one term in which all photons are associated to the ISR with the partition probability  $p_{\varphi} = 1$ , and  $\mathcal{R}_I$  means the respective reduction procedure. Unfortunately, we loose in this way a (small) part of the genuine  $\mathcal{O}(\alpha)$  corrections. The full  $\mathcal{O}(\alpha)$  correction can be included only if YFSWW3 is run in the event-generation mode, and the correction-weight for re-weighting (accounting for the  $4f$ -background) is supplied from KoralW. (This leads, however, to large MC weight fluctulations, see below.) We have checked, however, that at the LEP2 energy range the bias introduced by this approximation is within 0.1%, both for the total cross section and for distributions. This can be explained by the fact that the W's, as heavy and slowly moving particles, do not radiate much at these energies. Of course, the main weight of YFSWW3 based on  $\rho_n^{\text{Best}}$  does not have this bias. In this way, by assigning this correction-weight to the KoralW events, one can include, in a simple way, the  $\mathcal{O}(\alpha)$  NL correction  $\delta_{NL-}^R$  into the KoralW results. How to do it in practice, we explain in detail in Ref. [20].

#### **4.12.2 Re-weighting** YFSWW3 **Events by** YFSWW3

This kind of re-weighting can be useful in some data analyses, when e.g. one has a large sample of simulated events for a given input parameter set-up and one wants to asses the effects of changing some of the input parameters on the results, but without a necessity of repeating the full simulation with the new parameter set-ups. The tools for such a re-weighting are collected in the file rewt Y.f. We provide two methods: "exact" and "approximate". They differ in that, that in the exact method the partition vector for photons is stored along with their four-momenta, while in the approximate method the partition information is not recorded.

#### **(a) The exact method:**

The tool for the exact method is SUBROUTINE YFSWW\_WME(WtME), where WtME corresponds to the weight  $w^{\text{Model}}$  of Eq. (52). It requires storing on the disk/tape the entire content of four COMMON blocks: /MOMINI/, /MOMFIN/, /MOMDEC/ and /DeChan/ during the event generation run of YFSWW3. We assume that the appropriate tools for writing the above information on the disk/tape as well as for reading it in the re-weighting run of the program are provided by the user of the code (see the source code for more details).

### How to use it:

- 1. The primary run generating/storing events:
	- Run YFSWW3 and store on the disk/tape the whole content of the COMMON blocks: /MOMINI/, /MOMFIN/, /MOMDEC/, /DeChan/. This is done for some input parameters set-up (A).
- 2. The secondary run re-weighting events:
	- Initialise the program with the input parameters set-up (A) used for the event generation.
	- Instead of generating events, call YFSWW WME(WtME A) for all stored events and

save the computed matrix element weight WtME A (in some arbitrary units).

- Initialise the program with a different input parameters set-up (B).
- Calculate the weight WtME B and save as above.
- For each event calculate the ratio  $Wt = WtME_B/WtME_A$  and use it as the weight for re-weighting the original sample of events.
- This procedure can be repeated for any new input parameters set-up (B).

Example of running the program in the re-weighting mode:

```
CALL YFSWW ReaDataX('./data DEFAULTS',1,10000,xpar) ! reading general defaults
CALL YFSWW ReaDataX('./user.input' ,0,10000,xpar) ! reading user input
CALL YFSWW Initialize(xpar) ! initialize generator
NevTot = 1000 ! number of events to be re-weighted
DO Iev = 1, NevTot
  CALL YFSWW WME(WtME) ! calculate matrix element weight for stored events
ENDDO
```
For more information about running YFSWW3 see Section 5.

#### **(b) The approximate (simpler) version:**

In the case when one does not have all the information needed for the exact (recommended) method of re-weighting (because of the lack of disk/tape space or some other reasons), one can use

```
WtME = YFSWW_WME_Smpl(Iflav,pf1,pf2,pf3,pf4,Phot,Nphot)
```
instead of CALL YFSWW WME(WtME). In this case one needs to store for each event only the flavours and the four-momenta of the final state fermions and the number and the four-momenta of all photons. Important: They should come from YFSWW3 itself, not from PHOTOS after the FSR. These four-momenta and flavours are available from two COMMON blocks:

```
COMMON / DECAYS / Iflav(4),amdec(4)
COMMON / MOMDEC / pf1(4),pf2(4),pf3(4),pf4(4),Phot(100,4),Nphot
```
(the fermion mass array amdec(4) does not need to be stored). They can be alternatively accessed with the help of two getter-routines:

SUBROUTINE YFSWW\_Get4f(flav,p1,p2,p3,p4) SUBROUTINE YFSWW\_GetPhotAll(NphAll,PhoAll)

located in the file ww\_get.f in the subdirectory yfsww. The first one provides the flavours and the four-momenta of the final state 4-fermions, while the second one provides the number and the four-momenta of the radiative photons (excluding the ones from PHOTOS).

The FUNCTION YFSWW\_WME\_Smpl fills the appropriate COMMON blocks and calculates (returns) the matrix element weight (corresponding to WtME in the previous method). This method is approximate because it does not use the information on the photon partitions but assigns all the photons to the ISR in performing the partition-dependent reduction procedure (described in Section 2.2). Our tests show, however, that the differences between this and the exact method are numerically negligible, e.g. < 0.01% for the total cross section at  $\sqrt{s} = 200 \text{ GeV}.$ 

### **4.12.3 Re-weighting** YFSWW3 **Events by** KoralW

Similar re-weighting tools are provided in the new version of KoralW [20]. They can be used for re-weighting events generated by YFSWW3 with the weight provided by the KoralW in order to correct for the missing  $4f$  background contribution to the the signal  $WW$ process. The relevant re-weighting routines in KoralW require as an input the events from YFSWW3, which are generated according to the ISR-type reference differential distribution. Such events are provided by YFSWW3 in the standard generation mode with the help of the getter-routine YFSWW GetEvtISR, located in the file ww get.f of the directory yfsww. The correction-weight provided by KoralW can be used to re-weight the constant-weight (unweighted) events from YFSWW3 or to correct the YFSWW3 weights in the variable-weight (weighted-event) mode; see Ref. [20] for more details.

# **5 How to use the Program**

In this section we provide a short guide on how to use the current version of YFSWW3, and we describe the input parameters of the program and its output.

## **5.1 Principal Entries of** YFSWW3

The principal entries of the YFSWW3 package, which the user has to call in his/her application in order to generate a series of the MC events, were already listed and described briefly in Subsection 4.3. Here we shall add more information on their functionality. The calling sequence constituting a typical Monte Carlo run will look as follows:



In the first call of YFSWW\_ReaDataX, default data are read into the REAL\*8 array xpar(10000). The YFSWW3 has almost no data hidden in the source code (this is not true for TAUOLA and JETSET). The file data DEFAULTS, which is read first, is placed in the distribution subdirectory data files. This file provides necessary initial default values of all input parameters. The user should never modify it. It can be copied to a local directory or,

better, a symbolic link should be created to the original data files/data DEFAULTS. This file is quite sizable and the user is usually interested only in changing some subset of these data. In the second call of YFSWW ReaDataX, the user can overwrite the default data with his/her own smaller set of input data which are placed in the user.input file. For example, the simplest input data which defines only the CMS energy would look like this:

BeginX \*<ia><----data-----><-------------------comments-------------> 1 190d0 CMSEne =CMS total energy [GeV] EndX

As we see, data cards begin with the keyword BeginX and end with the keyword EndX. The comment lines are allowed – they begin with  $*$  in the first column. The data themselves are in a fixed format, with the index  $\mathbf i$  of the array  $\text{span}(\mathbf i)$  followed by the data value and a trailing comment. The example of the input data set for the demonstration program demo.f in the subdirectory demo provides a useful template for a typical user's data. The complete set of the data in data DEFAULTS is described in detail in Tables 1–5. Obviously, the user is interested in manipulating only some of them and will retain the default values in most of the cases.

The YFSWW Initialize is invoked to initialise the generator. It reads the input data from the array xpar, prints them out and sends them down to the various modules and auxiliary libraries. The programs have to be called in strictly the same order as in the above example. At this point one is ready to generate the series of the MC events. The generation of a single event is done with the help of YFSWW Make. After the generation loop is completed, we may invoke YFSWW Finalize, which does the final book-keeping, prints out various pieces of information on the MC run, and calculates the total MC integrated cross section (in pb). In order to obtain this cross section the user may call the routine YFSWW GetXSecMC(XSecMC,XErrMC).

## **5.2 Input/Output Parameters**

As we have already explained in the previous section, the input parameters enter through the xpar array, being a parameter of the routine YFSWW Initialize. The meaning of all of them is explained in Tables 1–5.

The principal output of YFSWW3 is the Monte Carlo event, which is just a list of final-state four-momenta (in GeV) and flavours, encoded in the standard /HEPEVT/ event record. At the present version we still provide the REAL\*4 version of /HEPEVT/ of the dimension of 2000. If the user is interested in the parton momenta before hadronization, then, in addition to /HEPEVT/, they are available (see also Table 8) through



Alternatively, all the four-momenta are available from the internal COMMON blocks /MOMWWP/ and /MOMDEC/, see Tables 6 and 7 for details.

In the case of a MC run with weighted events, the user is provided with the main weight (see also Table 10) through

#### CALL YFSWWW GetWtMain(WtMain) ! get main Monte Carlo weight

Of course, for unweighted event generation runs WtMain=1. For special purposes the user may also be interested in auxiliary weights, which are provided (see also Table 10) with the help of

CALL YFSWW GetWtAll(WtMain,WtCrud,WtSetAll) ! get all Monte Carlo weights

where REAL\*8 WtSetALL(100) is an array of the weights described in Table 9. The definition of the main weight WtMain depends on the input switches KeyCor and KeyLPA, see Table. 9, for instance, the best model for  $KeyCor = 5$  and  $KeyLPA = 0$  corresponding to Eq. (4) is defined as follows:

 $WtMod = Wtcru1*Wtcru2*(WtSet(41)-WtSet(2)+WtSet(4)).$ 

Alternatively, the auxiliary weights WtSet defined in Eq. (48) are available from the COMMON /WGTALL/, see Table 9. The total auxiliary weight should be defined as:

```
WtAuxEWC(i) = WtCru1*WtCru2*WtSetAll(i)
```
for  $\mathcal{O}(\alpha)$  EW corrections, and

```
WtAuxISR(i) = WtCru1*WtCru2*WtSetAll(i)
```
for the ISR corrections. The corresponding integrated cross section is simply obtained by multiplying the average of the total weight by the *normalisation* cross section of Eq. (53) (or the "primary cross section" in the terminology of Ref. [37]), which is provided through

CALL YFSWW GetXSecNR(XSecNR,XErrNR) ! get normalization x-section

Note that we expect from the user to use the auxiliary weights in the variable-weight mode only. It is, however, not impossible to use them also for the constant-weight events. In such a case we recommend the user to contact the authors for more instructions on how to do it correctly.

The complete description of the post-generation output parameters from YFSWW Finalize is collected in Table 11.

## **5.3 Printouts of the Program**

In this section we describe a printout of the demonstration program demo in the "best" mode, shown in Appendix B. The printout starts with the detailed specification of the actually used input parameters. Also, logos of some of the activated subprograms (KarLud, KarFin) and libraries (PHOTOS, TAUOLA, JETSET) are printed here. Next, the printout of one full event (in the standard PDG convention) is shown (in the actual demo.output file,

five events can be seen). Then, the printouts from the post-generation mode, i.e. CALL YFSWW Finalize, appear. First, one can see summary reports from the subprograms KarLud and KarFin. Their meaning is rather technical, so the average user of YFSWW3 does not have to worry about them (unless something unusual appears there). One thing that the user may check from time to time there is the entry B5 in the KarFin window B: the average value of the WCTRL weight should be equal to 1 within the statistical error (if it is not, notify the authors!). After these technical printouts from the YFSWW3 subprograms, there are several summary reports from TAUOLA on the  $\tau$  decays. The final reports of the main YFSWW3 MC generator are collected in three windows: A, B and C.

The window A contains the most important information from from the user's point of view. It provides the values of:

- A0 : the CMS energy in GeV;
- A1 : the best-order total cross section with its absolute statistical error for the generated statistics sample (in pb) ;
- A2 : the relative error of the above cross section;
- A3 : the total number of generated events;
- A4 : the number of accepted events;
- A5 : the number of the events with negative weights;
- A6 : the relative contribution to the total cross section from the events with the negative weights;
- A7 : the number of over-weighted events;
- A8 : the relative contribution to the total cross section from the over-weighted events;
- A9 : the value of the maximum weight for the event rejection;
- A10 : the average weight.

The numbers in the entries A5,A6,A7,A8 should be as small as possible. In particular, the relative contributions to the cross section from the negative weights and the over-weights should be much smaller than the expected accuracy of the MC calculations. If there is a large contribution from the over-weighted events, one should try to increase the value of the maximum weight WtMax, see Table 1. In the case of the large negative weight contribution, one should contact the authors. The ratio of the average weight (entry A10) to the maximum weight (entry A9) shows the efficiency of the MC algorithm in the unweighed events generation, i.e. the event acceptance rate. In the example given in the demo program it is  $\sim 20\%$ .

The window B is devoted to the technical information on the ISR corrections in different orders in  $\alpha$  within the YFS framework. This information is quite important, because it shows how big the contributions of subsequent orders of the perturbative series are, and thus allows us to estimate the missing higher-order effects. The entries B1–B4 provide the values of the total cross section (in pb) in the orders  $\mathcal{O}(\alpha^0)_{exp}-\mathcal{O}(\alpha^3)_{exp}$  of the ISR, while the entries B15–B17 give the differences of these values in subsequent orders. The entries B5–B14 contain the information on the contributions from the individual YFS ISR residuals  $\bar{\beta}_{i,ISR}$ , also in different orders in  $\alpha$ . The differences between various residuals and various orders for a given residual are provided in the entries B18–B26.

The window C contains the information on the exact  $\mathcal{O}(\alpha^1)_{exp}$  corrections to the WW production stage. The first entry (C1) shows the total  $\mathcal{O}(\alpha^1)_{exp}$  cross section for the exact EW corrections calculation, the second one (C2) shows the same for the approximate ("fast") EW corrections, and the third one (C3) contains the  $\mathcal{O}(\alpha^1)_{\text{exp}}$  LL cross section. The second part of this window shows the differences between the exact and approximate EW corrections (C4), and between the exact and the LL results (C5). The final part (entries C6–C8), contains the differences of various  $\bar{\beta}_i$  contributions. All these values are given in pb.

This completes the description of the output of YFSWW3. The remaining entries shown in the demo.output file (e.g. histograms) are produced by the demo main program.

## **6 Summary**

We presented Monte Carlo event generator YFSWW3 version 1.16 for the combined W-pair production and decay process. It includes the complete  $\mathcal{O}(\alpha)$  EW corrections in the WW production process in the leading pole approximation, in addition to other numericaly sizeable but physicaly less interesting effects like for instace up to  $\mathcal{O}(\alpha^3)$  QED ISR effects in the LL approximation. The program is precise enough for obtaining Standard Model prediction for the total cross section and any distribution at LEP2, understanding that contribution from the backgroud diagrams are included in the calculation with help of KoralW (or removed from the data). YFSWW3 includes programming tools for communicating with KoralW in the process of generating single MC event. The program was also tested and is applicable for the Linear Collider energy range. The next possible improvement in the program is the introduction of the YFS exponention in the MC simulation of the W decays.

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# **A Program Parameters and Their Settings**



Table 1: The list of input parameters of the YFSWW3 generator in the xpar vector. The default values are in brackets.



Table 2: The list of input parameters in the xpar vector specific to the YFSWW3 generator (not used in KoralW). The default values are in brackets.



Table 3: The list of input parameters of the YFSWW3 generator in the xpar vector (cont.). The default values are in brackets.



Table 4: The list of input parameters of the YFSWW3 generator in the xpar vector (cont.). The default values are in brackets.



Table 5: The list of input parameters of the YFSWW3 generator in the xpar vector (cont.). The default values are in brackets.



Table 6: The list of four-momenta in the COMMON /MOMWWP/ of the YFSWW3 generator. They are given in GeV in the CMS of the incoming beams.



Table 7: The list of four-momenta in the COMMON /MOMDEC/ of the YFSWW3 generator. They are given in GeV in the CMS of the incoming beams.



Table 8: The list of output parameters of the YFSWW3 generator transferred through parameters of the getter-routines: YFSWW GetBeams(q1,q2), YFSWW Get4f(flav,p1,p2,p3,p4) and YFSWW GetPhotAll(NphAll,PhoAll).

Parameter	Meaning
WtCru1	Crude weight for ISR,
WtCru2	Crude weight for the rest.
	They are necessary to build the total weight out of WtSet
WtMod	The "best" weight corresponding to eq. $(4)$ , e.g. for KeyCor=5:
	$WtMod = Wtcru1*Wtcru2*(WtSet(41)-WtSet(2)+WtSet(4))$
$WtSet(1-19)$	Various ISR-type contributions to the matrix element $(\bar{\beta}$
	functions) – to get the total weight they must be multiplied by
	WtCru1
WtSet(1)	Zero-order $(\beta_0)$
WtSet(2)	First-order ISR $(\bar{\beta}_0 + \bar{\beta}_1)$
WtSet(3)	Second-order ISR $(\bar{\beta}_0 + \bar{\beta}_1 + \bar{\beta}_2)$
WtSet(4)	Third-order ISR $(\bar{\beta}_0 + \bar{\beta}_1 + \beta_2 + \beta_3)$
WtSet(10)	$\mathcal{O}(\alpha^0)$ contribution from $\beta_0$
WtSet(11)	$\mathcal{O}(\alpha^1)$ ISR contribution from $\beta_0$
WtSet(12)	$\mathcal{O}(\alpha^1)$ ISR contribution from $\beta_1$
WtSet(13)	$\mathcal{O}(\alpha^2)$ ISR contribution from $\bar{\beta}_0$
WtSet(14)	$\mathcal{O}(\alpha^2)$ ISR contribution from $\bar{\beta}_1$
WtSet(15)	$\mathcal{O}(\alpha^2)$ ISR contribution from $\bar{\beta}_2$
WtSet(16)	$\mathcal{O}(\alpha^3)$ ISR contribution from $\bar{\beta}_0$
WtSet(17)	$\mathcal{O}(\alpha^3)$ ISR contribution from $\bar{\beta}_1$
WtSet(18)	$\mathcal{O}(\alpha^3)$ ISR contribution from $\beta_2$
WtSet(19)	$\mathcal{O}(\alpha^3)$ ISR contribution from $\bar{\beta}_3$
WtSet (41-52)	Contributions to the matrix element from $\mathcal{O}(\alpha)$ EW corrections
	in the $WW$ production stage – to get the total weight they must
	be multiplied by WtCru1*WtCru2
WtSet(41)	$\mathcal{O}(\alpha^1)$ EW corrections $(\beta_0 + \beta_1)$
WtSet(51)	Pretabulated ("fast") $\mathcal{O}(\alpha^1)$ EW corrections $(\bar{\beta}_0 + \bar{\beta}_1)$
WtSet(42)	$\mathcal{O}(\alpha^1)$ contribution from $\beta_0$
WtSet(43)	$\mathcal{O}(\alpha^1)$ contribution from $\beta_1$
WtSet(52)	Pretabulated $\mathcal{O}(\alpha^1)$ contribution from $\beta_0$
WtSet (65-68)	Fixed order (no exponentiation) contributions (for tests)
WtSet(65)	$\mathcal{O}(\alpha^0)$ , no exponentiation
WtSet(66)	$\mathcal{O}(\alpha^1)$ , no exponentiation
WtSet(67)	$\mathcal{O}(\alpha^1)$ virtual + soft real photon only, no exponentiation
WtSet(68)	$\mathcal{O}(\alpha^1)$ real hard photon only, no exponentiation

Table 9: The list of output weights in the COMMON /WGTALL/ of the YFSWW3 generator.



Table 10: The list of output parameters of the YFSWW3 generator transferred through parameters of the getter-routines: YFSWW GetWtMain(WtMain), YFSWW GetWtISR(WtISR) and YFSWW GetWtAll(WtMain,WtCrud,WtSetAll).



Table 11: The list of output parameters of the YFSWW3 generator transferred through parameters of the getter-routines: YFSWW GetXSecMC(XSecMC,XErrMC), YFSWW\_GetXSecNR(XSecNR,XErrNR) and YFSWW\_GetNevMC(NevMC).

# **B Output of the Demo Program**







# --------------- YFSWW demo ------------------- NevTot = 1000 events to be generated ...

..... skipped ....

Event listing (standard)













..... skipped ....



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