

# Gluon contributions to parity-violating asymmetries in polarized proton-proton scattering

---

John Ellis, Stefano Moretti and Douglas A. Ross\*

*Division Théorique, CERN*

*1211 Genève 23, Switzerland*

*E-mail: john.ellis@cern.ch, stefano.moretti@cern.ch,  
dar@phys.soton.ac.uk*

**ABSTRACT:** We report on a calculation of one-loop weak corrections to polarized quark-gluon scattering and the corresponding crossed channels. Such contributions are suppressed formally by one power of  $\alpha_s$  relative to  $W$ - or  $Z$ -mediated quark-quark scattering, but would enable the spin asymmetry of the gluon distribution to contribute to parity-violating asymmetries that will soon be investigated in polarized proton-proton scattering experiments at RHIC. In certain kinematic regions, gluon contributions to parity-violating asymmetries can be as large as 10% of the tree-level  $W$ - and  $Z$ -exchanges in quark-quark scattering, but usually only where the parity-violating asymmetries are already small.

**KEYWORDS:** NLO Computations, Spin and Polarization Effects.

---

\*On leave of absence from: Department of Physics and Astronomy, University of Southampton, Southampton SO17 1BJ, U.K.

---

## Contents

<b>1. Introduction</b>	<b>1</b>
<b>2. The one-loop weak corrections to gluon scattering matrix elements</b>	<b>2</b>
<b>3. Parton-level asymmetries</b>	<b>5</b>
<b>4. Asymmetries in polarized proton-proton scattering</b>	<b>6</b>
<b>5. Summary and conclusions</b>	<b>9</b>

---

## 1. Introduction

The forthcoming generation of hadron-hadron colliders — the Tevatron with Run 2, RHIC with polarized proton beams (RHIC-Spin) and the LHC — will produce unprecedented data on high- $p_T$  jets that merit the most accurate theoretical calculations. Next-to-leading order (NLO) jet calculations in QCD have been available for some time [1], whereas the major task of providing the complete NNLO QCD result is about to be completed [2, 3]. Formally, the latter introduce corrections relative to the leading-order predictions that are of order  $(\alpha_s/\pi)^2 = \mathcal{O}(10^{-3})$ , with the likelihood of parametric enhancements (or suppressions). When computing to this accuracy, one may then wonder whether NLO electroweak (EW) corrections could also be important. In fact, these are formally of order  $(\alpha_W/\pi) = \mathcal{O}(10^{-2})$ , again with the likelihood of parametric enhancement or suppression.

We report in this paper on a pilot one-loop calculation of purely weak corrections to high- $p_T$  jet production. We concentrate on quark-gluon scattering and processes related to this by crossing, namely  $\bar{q} + g \rightarrow \bar{q} + g$ ,  $q + \bar{q} \rightarrow g + g$  and  $g + g \rightarrow q + \bar{q}$ .<sup>1</sup> In order to focus on a possible distinctive experimental signal, we discuss parity-violating asymmetries in these processes that are in principle measurable at RHIC-Spin [4]. These weak corrections provide, in principle, sensitivity to the helicity-dependent component of the gluon distribution function inside a polarized proton,  $\Delta G$ , that is instead absent in pure QCD [5].

Contributions to such parity-violating asymmetries already arise at tree level from  $q + q \rightarrow q + q$  and  $q + \bar{q} \rightarrow q + \bar{q}$  scattering processes, due to purely weak

---

<sup>1</sup>Hereafter, the notation  $q$  is intended to represent any possible quark flavour.

amplitudes as well as to the interference of the latter with the QCD ones. These processes are sensitive to the helicity-dependent components of the quark distributions,  $\Delta Q_q$ , and their effects on parity-violating asymmetries are well known and rather small, at the level of few percent at best [6, 7]. As we show below, the new contributions that we calculate here are even smaller, as indeed expected on the ground of a naïve estimate based on counting powers of coupling constants, without any benefit from an enhancement due to the spin asymmetry of the gluon distribution function. For plausible values of the latter, there do exist regions of the high- $p_T$  jet phase space where the  $\Delta G$ -dependent contributions to the parity-violating asymmetries are non-negligible in comparison with the  $\Delta Q_q$ -dependent ones, but the experimental sensitivity seems unlikely to be able to disentangle the two, primarily because of the small absolute values of the observables.

Looking on the bright side, our results help stabilise the Standard Model (SM) predictions for parity-violating asymmetries at RHIC-Spin, thereby providing a solid baseline in the search for new physics. These parity-violating asymmetries have been proposed as signatures of new physics, such as a  $W'$ ,  $Z'$  or contact interactions that violate parity [7]. In other terms, the claimed RHIC-Spin sensitivities to these signatures are validated by our results.

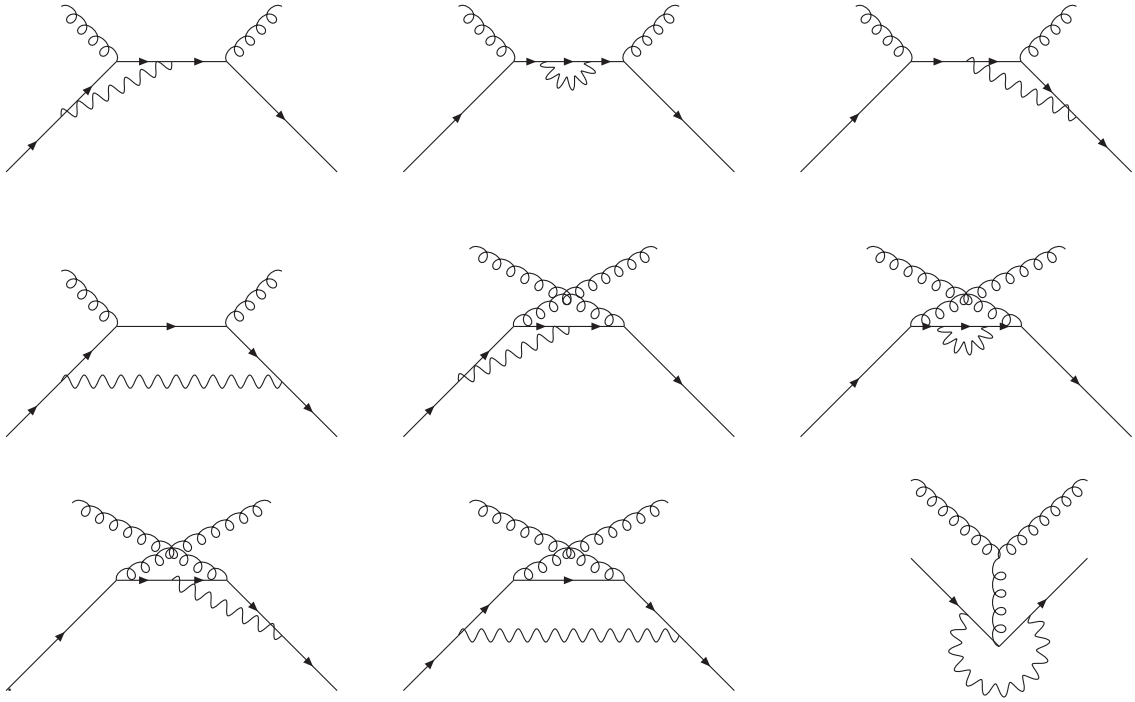
A caveat to our analysis is that we have not computed the one-loop weak corrections to  $q + \bar{q} \rightarrow q + \bar{q}$ . In fact, for the QCD-mediated scattering, they are formally of the same order as those for  $\bar{q} + g \rightarrow \bar{q} + g$ ,  $q + \bar{q} \rightarrow g + g$  and  $g + g \rightarrow q + \bar{q}$ . As is the case with unpolarized  $p-p$  scattering [1], these corrections may well be numerically significant. However, a full higher order QCD calculation of the processes considered in [6] would be a formidable task and is beyond the scope of the current paper. The calculation reported here has been carried out in order to investigate the possibility that the spin content of the gluons give a contribution to parity-violating asymmetries which are comparable in magnitude with those from quark-(anti)quark scattering at tree-level. The fact that we show that this is not the case boosts confidence in the usual perturbative expansion.

## 2. The one-loop weak corrections to gluon scattering matrix elements

One-loop graphs yielding weak corrections to the process

$$q + g \rightarrow q + g$$

are shown in figure 1. In addition to those shown, there is a correction due to the on-shell fermion wavefunction renormalization for each tree-level graph, which we have not shown. We have calculated the graphs in figure 1 with the help of FeynCalc [8] and FORM [9].



**Figure 1:** Diagrams contributing to the one-loop weak corrections to quark-gluon scattering. The helical lines represent gluons and the wiggly lines refer to either a  $W$ – or  $Z$ –boson.

The tree-level amplitudes  $\mathcal{A}_{\lambda\lambda',\sigma}$ , where  $\lambda$  and  $\lambda'$  are the helicities of the gluons and  $\sigma$  that of the (massless) quark line, can be written as

$$\mathcal{A}_{+,+,+} = -2g^2 \sqrt{\frac{-u}{s}} \left\{ \frac{s^2}{ut} \tau^a \tau^b + \frac{s}{t} \tau^b \tau^a \right\} \quad (2.1)$$

$$\mathcal{A}_{-,-,+} = 2g^2 \sqrt{\frac{-u}{s}} \left\{ \frac{s}{t} \tau^a \tau^b + \frac{u}{t} \tau^b \tau^a \right\}, \quad (2.2)$$

where the symbols  $\tau^a$  and  $\tau^b$  denote the colour matrices. By parity conservation, we have  $\mathcal{A}_{-,-,-} = \mathcal{A}_{+,+,+}$  and  $\mathcal{A}_{+,-,-} = \mathcal{A}_{-,-,+}$ .

At one-loop order, the exchanges of a vector boson of mass  $m$  and coupling  $g_+$  to right-handed quarks make corrections to these matrix elements that can be written in the forms:

$$\begin{aligned} \Delta\mathcal{A}_{+,+,+} = & \frac{g^2 g_+^2}{8\pi^2} \sqrt{\frac{-u}{s}} \left[ \left\{ 2 \left[ 1 - \frac{s}{t} - \frac{t}{s} \right] \left( 1 + \frac{m^2}{t} \right)^2 \left[ \frac{\pi^2}{6} - \text{Li}_2 \left( 1 + \frac{t}{m^2} \right) \right] - \right. \right. \\ & - 2 \frac{t^2}{us} \left( 1 + \frac{m^2}{t} \right)^2 \left[ \ln \left( 1 - \frac{u}{m^2} \right) \ln \left( \frac{-t}{m^2} \right) + \text{Li}_2 \left( \frac{u}{m^2} \right) \right] + \\ & \left. \left. + \left[ 4 \frac{s}{u} + 2 \left( 1 - \frac{m^2}{u} \right)^2 - \frac{s}{u} \left( 1 + \frac{m^2}{u} \right)^2 \right] \ln \left( 1 - \frac{u}{m^2} \right) + \right. \right. \end{aligned}$$

$$\begin{aligned}
& + \left[ \frac{s}{t} - 2 \left( 1 - \frac{s}{t} \right) \left( 1 + \frac{m^2}{t} \right) \right] \ln \left( \frac{-t}{m^2} \right) - \frac{7s}{2t} - \frac{5s}{2u} - \\
& - \frac{m^2 s}{t^2} \left( 1 + \frac{s^2}{u^2} \right) \} \tau^a \tau^b + \\
& + \left\{ -2 \frac{s^2}{ut} \left( 1 + \frac{m^2}{t} \right)^2 \left[ \frac{\pi^2}{6} - \text{Li}_2 \left( 1 + \frac{t}{m^2} \right) \right] - 2 \frac{s}{u} \times \right. \\
& \quad \times \left( 1 - \frac{m^2}{s} \right)^2 \left[ \ln \left( 1 - \frac{s}{m^2} \right) \ln \left( \frac{-t}{m^2} \right) + \text{Li}_2 \left( \frac{s}{m^2} \right) \right] + \\
& \quad + \left[ 2 \frac{m^2}{t} - 2 \frac{m^2 s}{t^2} - 3 \frac{s}{t} \right] \ln \left( \frac{-t}{m^2} \right) + \frac{7s}{2t} - \\
& \quad \left. - 2 \frac{m^2}{t} \left( 1 - \frac{s}{t} \right) \right\} \tau^b \tau^a, \tag{2.3}
\end{aligned}$$

$$\begin{aligned}
\Delta \mathcal{A}_{--, +} = & \frac{g_+^2 g_+^2}{8\pi^2} \sqrt{\frac{-u}{s}} \left[ \left\{ 2 \frac{u}{t} \left( 1 + \frac{m^2}{t} \right)^2 \left[ \frac{\pi^2}{6} - \text{Li}_2 \left( 1 + \frac{t}{m^2} \right) \right] + \right. \right. \\
& + 2 \left( 1 - \frac{m^2}{u} \right)^2 \left[ \ln \left( 1 - \frac{u}{m^2} \right) \ln \left( \frac{-t}{m^2} \right) + \text{Li}_2 \left( \frac{u}{m^2} \right) \right] + \\
& + \left[ 3 \frac{s}{t} + 2 \frac{m^2}{u} - 2 \frac{u m^2}{t^2} \right] \ln \left( \frac{-t}{m^2} \right) - \frac{7s}{2t} - \\
& \left. - 2 \frac{m^2}{u} \left( 1 - \frac{u^2}{t^2} \right) \right\} \tau^a \tau^b + \\
& + \left\{ -2 \left( \frac{u}{t} + \frac{t^2}{u^2} \right) \left( 1 + \frac{m^2}{t} \right)^2 \left[ \frac{\pi^2}{6} - \text{Li}_2 \left( 1 + \frac{t}{m^2} \right) \right] + \right. \\
& + 2 \left( \frac{(t+m^2)}{u} \right)^2 \left[ \ln \left( 1 - \frac{s}{m^2} \right) \ln \left( \frac{-t}{m^2} \right) + \text{Li}_2 \left( \frac{s}{m^2} \right) \right] - \\
& - \left[ 4 + 2 \frac{s}{u} \left( 1 - \frac{m^2}{s} \right)^2 - \left( 1 + \frac{m^2}{s} \right)^2 \right] \times \\
& \times \ln \left( 1 - \frac{s}{m^2} \right) + \left[ 2 \frac{s}{u} \left( 1 - \frac{m^2}{s} \right) - 3 \frac{s}{t} + 2 \frac{u m^2}{t^2} \right] \times \\
& \left. \times \ln \left( \frac{-t}{m^2} \right) + \frac{7s}{2t} + \frac{5}{2} + \frac{m^2}{s} \left( 1 - 2 \frac{us}{t^2} \right) \right\} \tau^b \tau^a \Big]. \tag{2.4}
\end{aligned}$$

We observe that  $\Delta \mathcal{A}_{--, -}$  can be obtained from  $\Delta \mathcal{A}_{++, +}$  and  $\Delta \mathcal{A}_{++, -}$  from  $\Delta \mathcal{A}_{--, +}$  by replacing  $g_+$  with the coupling of the gauge boson to left-handed quarks,  $g_-$ .

In the abelian limit,  $\tau^a \tau^b = \tau^b \tau^a$ , and after rearranging the couplings appropriately, we recover the results of [10] for the  $Z$ -boson corrections to polarized Compton scattering.

### 3. Parton-level asymmetries

In this section, we display the parity-violating asymmetries of the cross sections for the basic partonic subprocesses

$$q + q \rightarrow q + q, \tag{3.1}$$

$$q + \bar{q} \rightarrow q + \bar{q}, \tag{3.2}$$

$$q + g \rightarrow q + g, \tag{3.3}$$

$$q + \bar{q} \rightarrow g + g, \tag{3.4}$$

$$g + g \rightarrow q + \bar{q}. \tag{3.5}$$

For the sake of illustration, we choose  $q = d$ . The processes (3.1) and (3.2) can occur at tree level via  $W$ – or  $Z$ –boson exchange, and all their EW and QCD ingredients have been calculated in [6]. The processes (3.3)–(3.5) occur only at the one-loop level, and are computed numerically here using the amplitudes given in the previous section.

The parity-violating asymmetries of interest are [4]:

$$A_L d\sigma \equiv (d\sigma_- - d\sigma_+), \tag{3.6}$$

for the case where only one incident beam is polarized, and

$$A_{PV} d\sigma \equiv (d\sigma_{--} - d\sigma_{++}), \tag{3.7}$$

when both incident beams are polarized.<sup>2</sup> In eqs. (3.6) and (3.7), the quantity  $d\sigma$  refers to the sum of the differential cross-sections for all four polarizations, i.e.

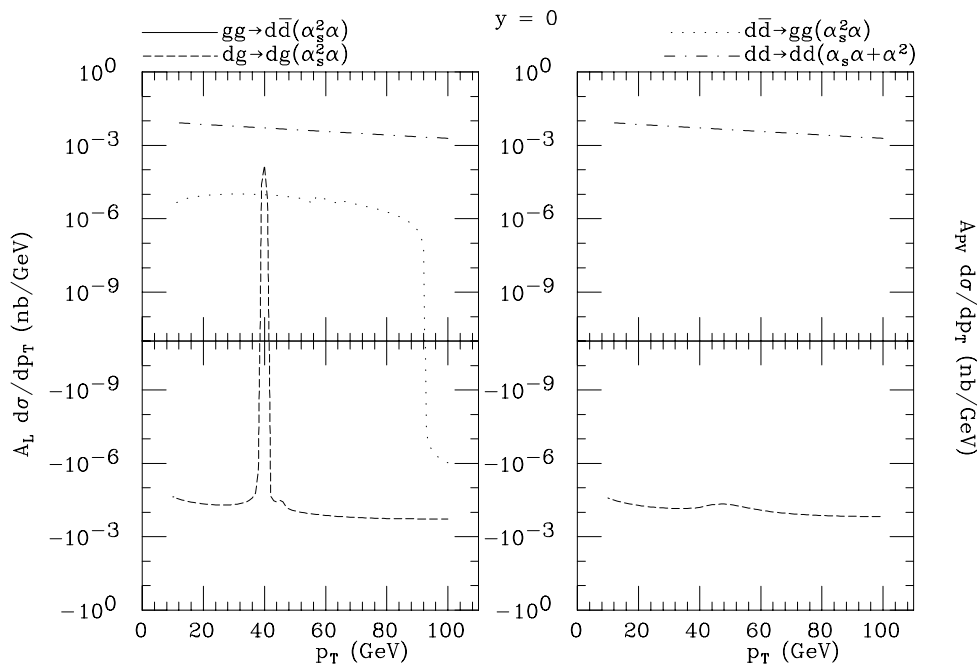
$$d\sigma = d\sigma_{++} + d\sigma_{+-} + d\sigma_{-+} + d\sigma_{--}.$$

In figure 2 we show these asymmetries in the central rapidity region. The dot-dashed line is the quark-quark scattering contribution calculated in [6], and the dashed line refers to quark-gluon scattering. We see that this asymmetry has the opposite sign from the quark-quark contribution, except for  $A_L$  in a small region near the weak threshold  $p_T \sim M_W/2$ . The magnitude of the effect increases with transverse momentum, reaching about 10% at the upper end of the spectrum. The dotted line refers to the crossed process of quark-antiquark annihilation into two gluons and we see that in this case the asymmetry is smaller by two orders of magnitude.

In figure 3 we show the same plots, but now at relatively large rapidity,  $y = 1$ . Here we see that the contributions from quark-gluon scattering to both asymmetries can have either sign, and at sufficiently large transverse momenta the contributions to both the asymmetries are comparable in magnitude, and opposite in sign, to that from tree-level quark-quark scattering. Also shown in figure 3 is the other

---

<sup>2</sup>In the case of quark-gluon scattering, the first index refers to the helicity of the quark.



**Figure 2:** Parton-level asymmetries at rapidity  $y = 0$ , as functions of the transverse momentum  $p_T$ .

crossed process, namely gluon-gluon annihilation into a quark-antiquark pair. This was suppressed in figure 2, because it is negligibly small for small rapidity. Once again, we see that the asymmetry is two orders of magnitude smaller than in the quark-gluon channel.

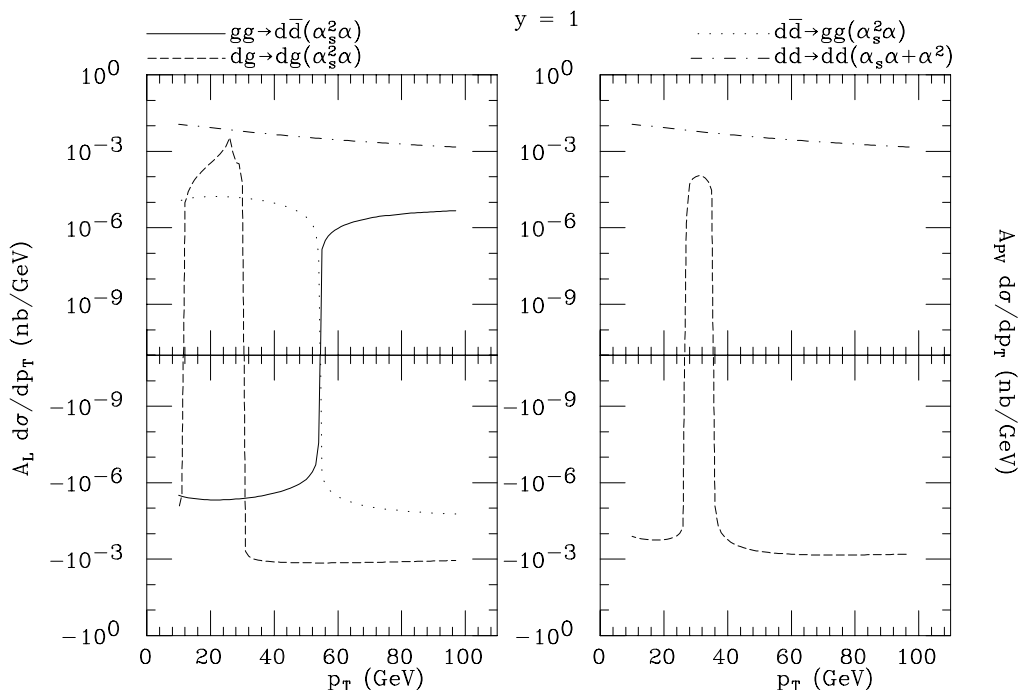
The very strong suppression of both crossed channels (3.4)–(3.5), compared to the subprocess (3.3), irrespective of the rapidity, was not intuitively obvious to us. It is in part responsible for the smallness of the overall corrections at the hadron level, discussed below. Finally, we note the overall normalization of all the curves, namely nanobarn/GeV, which takes into account the relative weights of the various subprocesses in the integrated quantities.

#### 4. Asymmetries in polarized proton-proton scattering

In this section we show the same asymmetries, but now in polarized proton-proton scattering, i.e., after folding the parton-level cross sections with polarized parton distribution functions. As examples, we take the latter from the LO set A of ref. [11] (GS) (see also [12])<sup>3</sup> at two collider energies,  $\sqrt{s} = 300$  and  $600$  GeV, representative of the RHIC-Spin programme. As already mentioned, one might *a priori* have

---

<sup>3</sup>The parton distribution functions are here evaluated at the scale  $Q = \sqrt{s}$ , i.e., the centre-of-mass (CM) energy at the parton level. The same choice is made for the argument of  $\alpha_s$ .



**Figure 3:** Parton-level asymmetries at rapidity  $y = 1$ , as functions of the transverse momentum  $p_T$ .

thought that the effect at the parton level discussed in the preceding section could be enhanced by a substantial contribution due to the asymmetry in the polarized gluon distribution function. In fact, we show that this is not the case. Qualitatively, one can understand this effect from the fact that the asymmetries at the parton level were only significant at large values of transverse momentum and/or rapidity. These kinematic regions probe the large  $x$  spectrum of the distributions, where the gluon content of the proton is no longer significant.

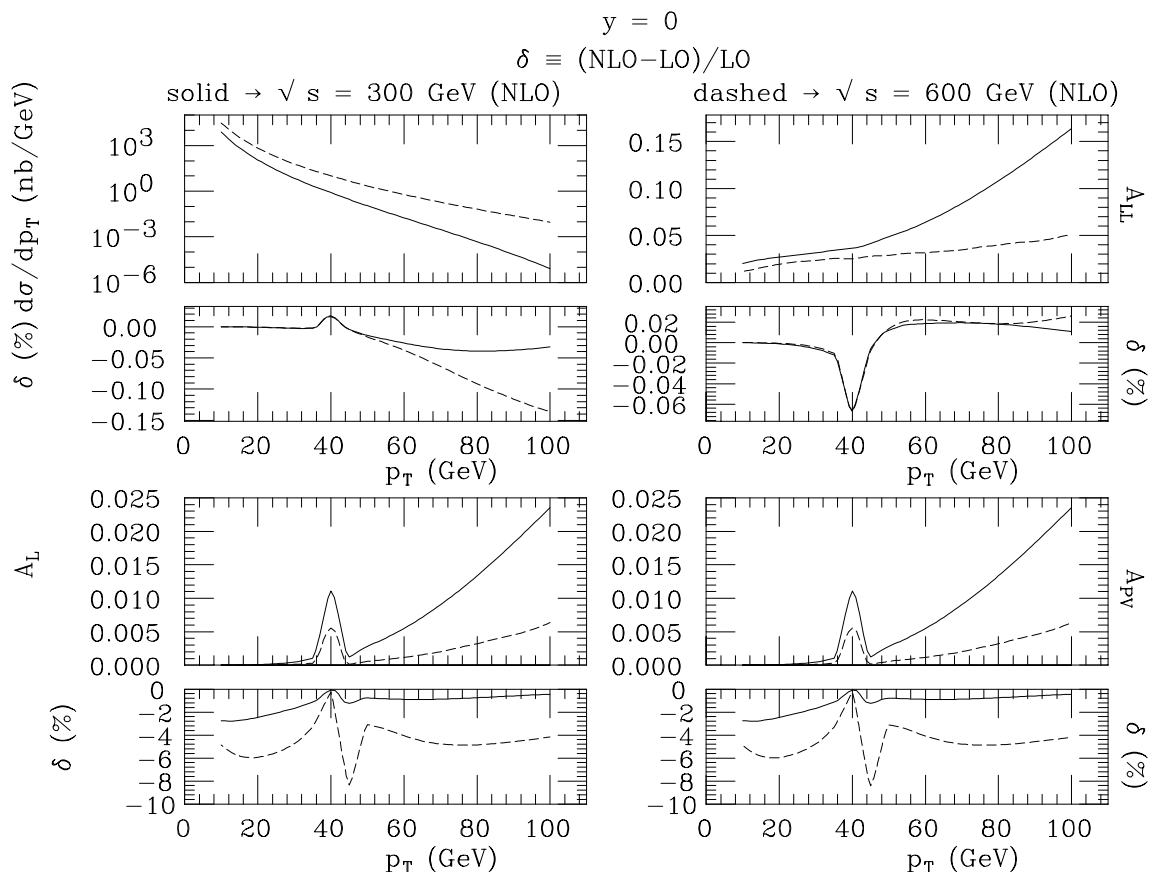
In figure 4 we present the differential cross sections and asymmetries for zero rapidity. Beneath each plot, we also show the percentage contribution due to the one-loop weak corrections, normalised to the LO rate. Each graph has two sets of curves, corresponding to the two mentioned CM energies, as indicated.

The top-left graph is the total differential cross-section, which is dominated by LO QCD. Here, as expected, the one-loop weak corrections are of the order of 0.1%. The top-right graph shows another asymmetry,  $A_{LL}$ , defined as

$$A_{LL} d\sigma \equiv d\sigma_{++} - d\sigma_{+-} + d\sigma_{--} - d\sigma_{-+}, \tag{4.1}$$

which is also present in QCD and depends entirely on the asymmetry of the parton distributions. Here we note that the contributions from the one-loop weak corrections are even smaller than for the differential cross-section itself, at both energies.



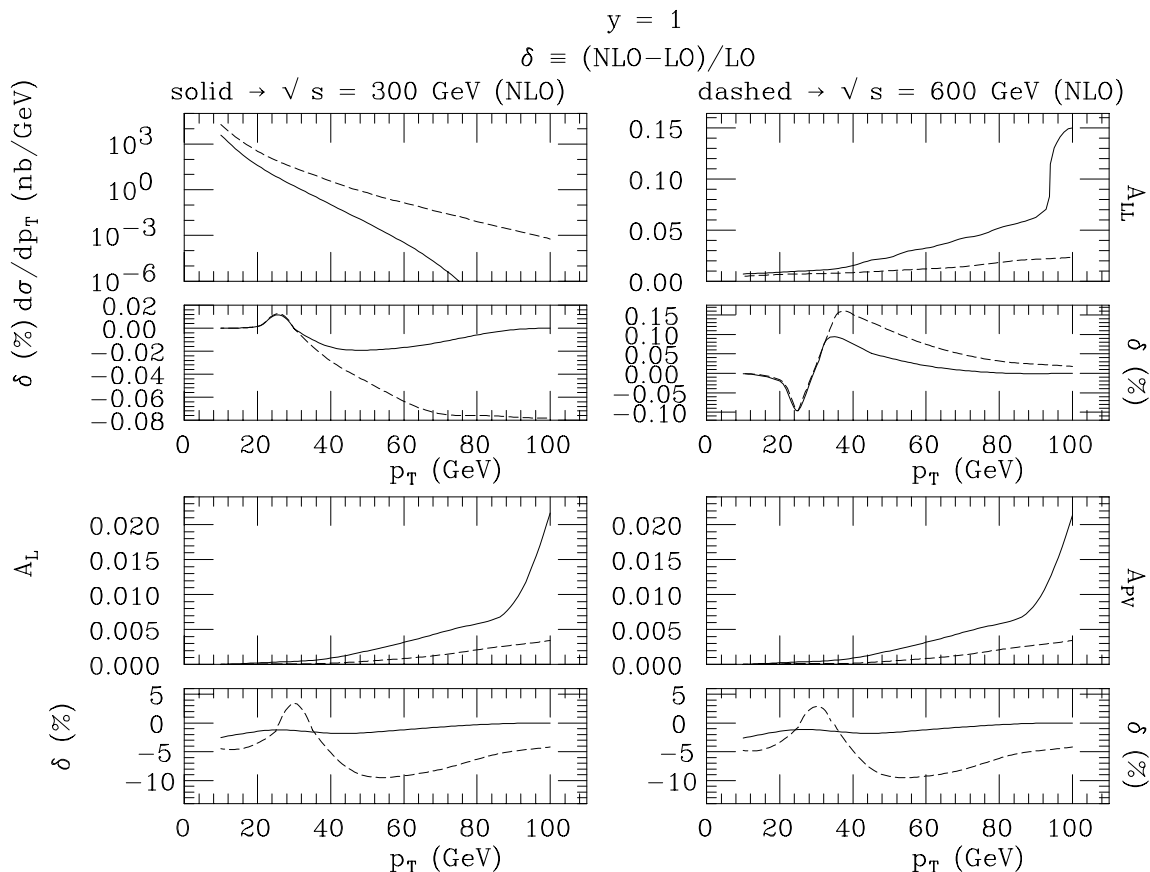


**Figure 4:** Differential cross sections and asymmetries in polarized proton-proton scattering at rapidity  $y = 0$ , as functions of the transverse momentum  $p_T$ .

The lower two graphs show the parity-violating asymmetries, normalized to the total cross section, so that the dimensionless quantities  $A_L$  and  $A_{PV}$  are shown. We have normalised  $A_{LL}$  in the same way. We see that the effect of the weak corrections to quark-gluon scattering is generally to reduce the two asymmetries by a few percent, i.e., of the same order as was found at the parton level.

Figure 5 plots the same quantities as in figure 4, but now at rapidity  $y = 1$ . Here is where one gets the largest effects at the one-loop level, as the weak corrections can reduce the parity-violating asymmetries by up to about 10–12%. The effects on the total rate and on  $A_{LL}$  are of the same order as at lower rapidity.

Finally, in figure 6, we display the usual selection of curves, but now integrated over rapidity, from  $y = 0$  to  $|y| = 1$ . The shapes modulate between the extreme trends seen in the two previous figures. The salient features already appreciated at fixed rapidities, that one-loop weak corrections are larger at higher energy and carry some visible structure induced by the  $W$ – or  $Z$ –mass threshold effects, remain clearly visible.

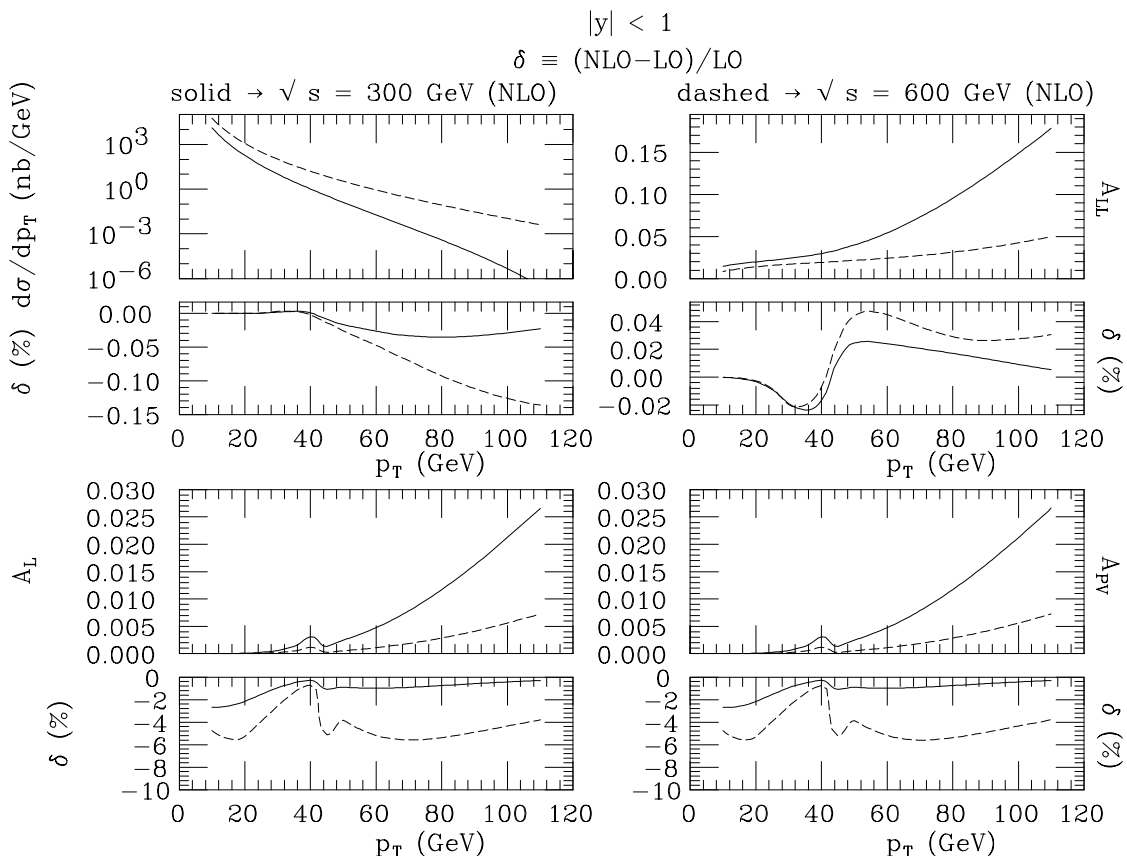


**Figure 5:** Differential cross sections and asymmetries in polarized proton-proton scattering at rapidity  $y = 1$ , as functions of the transverse momentum  $p_T$ .

## 5. Summary and conclusions

We have calculated the one-loop weak corrections to the quark-gluon scattering differential cross section, as a function of the transverse momentum and for selected values of rapidity, and crossed channels. We have evaluated the corresponding contributions to parity-violating asymmetries in polarized proton-proton scattering at energies relevant to RHIC-Spin. We have found that in certain kinematic regions these higher-order effects can be as large as 10% of the tree-level contributions to some parity-violating asymmetries. We recall that the study of these asymmetries has gathered particular attention lately [4], both because they are sensitive to the helicity-dependent components of the parton distribution functions, and because they can carry the distinctive hallmark of new physics.

It turns out that, the larger the rapidity and the collider energy, the bigger the effect of the one-loop weak corrections, with some resonant enhancement in the transverse momentum spectrum in the vicinity of the  $W$ - and  $Z$ -mass thresholds. These corrections are dominated by the contributions induced by quark-gluon scattering, as both quark-antiquark annihilation into two gluons and gluon-gluon scattering



**Figure 6:** Differential cross-sections and asymmetries in polarized proton-proton scattering integrated over the rapidity range  $|y| < 1$ , as functions of the transverse momentum  $p_T$ .

to a quark-antiquark pair are considerably suppressed in comparison. In fact, at the parton level, one-loop corrections via quark-gluon scattering can be comparable to the tree-level contribution due to electroweak processes involving four external (anti)quarks.

These parton-level effects are not enhanced when one folds the parton-level cross sections with polarized distribution functions. The main reason is that the effects on the parity-violating asymmetries are only large for large values of the Bjorken  $x$  variable, where the gluon distribution function is generally small.

In order to check whether our results depend on the particular polarized distribution functions we used, we have repeated our exercises using different sets [13], and find no significant variations. We find that the central qualitative result, namely that the contribution from quark-gluon scattering contributes around 10% to the parity-violating asymmetries  $A_L$  and  $A_{PV}$ , is unchanged. Nevertheless, we note that at the higher CM energy of 600 GeV, there is some sensitivity to the choice of polarized parton distributions. For the central rapidity case, the magnitude of the quark-gluon contribution is diminished by around 2% if one uses the polarized distribution functions of GRSV [13] or set C of GS [11]. For larger rapidity,  $y = 1$ , the GSRV

distributions and sets A,B of the GS distributions give very similar results, whereas set C of GS leads to substantial enhancements of the parity-violating asymmetries, namely up to  $-25\%$ , in the region of the mass threshold  $p_T \sim M_W$ . Set C of [11] differs qualitatively from the other sets in that the contribution to the proton spin from the gluons is *negative* over a substantial range of  $x$ .

Our calculations can readily be extended to evaluate similar corrections to direct photon production,  $\bar{q}^{(-)} + g \rightarrow \bar{q}^{(-)} + \gamma$  and  $\bar{q} + q \rightarrow g + \gamma$ . Besides these processes, which are of potential interest to RHIC-Spin, the generalization to the case of three-jet production in  $e^+e^-$  collisions, namely the one-loop weak corrections to  $\gamma^*/Z^* \rightarrow q + \bar{q} + g$ , is also relatively straightforward. This is especially worthy of attention, given that the NNLO QCD corrections to this process are also expected to become available soon, and in view of the copious three-jet data samples furnished by LEP. Presumably though, the one-loop weak corrections will be suppressed at the  $Z^0$  peak by a factor  $G_F Q^2$ , where  $Q$  is a typical virtuality scale of order  $M_{Z^0}$ . Hence, they would be relatively more important at LEP 2 or at a higher-energy  $e^+e^-$  linear collider.

## Acknowledgments

We are grateful to Dima Bardin, Stefano Catani, Stefan Dittmaier and Thomas Gehrmann for several fruitful discussions.

## References

- [1] R.K. Ellis and J.C. Sexton, *QCD radiative corrections to parton parton scattering*, *Nucl. Phys.* **B 269** (1986) 445;  
 S.D. Ellis, Z. Kunszt and D.E. Soper, *Jets at hadron colliders at order  $\alpha_s^3$ : a look inside*, *Phys. Rev. Lett.* **69** (1992) 3615 [[hep-ph/9208249](#)];  
 W.T. Giele, E.W. N. Glover and D.A. Kosower, *The inclusive two jet triply differential cross-section*, *Phys. Rev.* **D 52** (1995) 1486 [[hep-ph/9412338](#)].
- [2] J.F. Gunion and J. Kalinowski, *A direct calculation of the six gluon subprocess*, *Phys. Rev.* **D 34** (1986) 2119;  
 S.J. Parke and T.R. Taylor, *Gluonic two goes to four*, *Nucl. Phys.* **B 269** (1986) 410;  
 F.A. Berends and W. Giele, *The six gluon process as an example of Weyl-Van der Waerden spinor calculus*, *Nucl. Phys.* **B 294** (1987) 700;  
 M. Mangano, S. Parke and Z. Xu, *Duality and multi - gluon scattering*, *Nucl. Phys.* **B 298** (1988) 653;  
 Z. Kunszt, *Combined use of the CALKUL method and  $N = 1$  supersymmetry to calculate QCD six parton processes*, *Nucl. Phys.* **B 271** (1986) 333;  
 S.J. Parke and T.R. Taylor, *The cross-section for hard processes involving two quarks and four gluons*, *Phys. Rev.* **D 35** (1987) 313;

- J.F. Gunion and Z. Kunszt, *Four jet processes: gluon-gluon scattering to non-identical quark-anti-quark pairs*, *Phys. Lett.* **B 159** (1985) 167; *Six quark subprocesses in QCD*, *Phys. Lett.* **B 176** (1986) 163;
- Z. Bern, L. Dixon and D.A. Kosower, *One loop corrections to two-quark-three-gluon amplitudes*, *Nucl. Phys.* **B 437** (1995) 259 [[hep-ph/9409393](#)];
- Z. Kunszt, A. Signer and Z. Trocsanyi, *One loop radiative corrections to the helicity amplitudes of QCD processes involving four quarks and one gluon*, *Phys. Lett.* **B 336** (1994) 529 [[hep-ph/9405386](#)].
- [3] C. Anastasiou, E.W.N. Glover, C. Oleari and M.E. Tejeda-Yeomans, *Two-loop QCD corrections to massless quark-gluon scattering*, [hep-ph/0101304](#);  
E.W. N. Glover, C. Oleari and M.E. Tejeda-Yeomans, *Two-loop QCD corrections to gluon-gluon scattering*, [hep-ph/0102201](#).
- [4] G. Bunce, N. Saito, J. Soffer and W. Vogelsang, *Prospects for Spin Physics at RHIC*, *Ann. Rev. Nucl. Part. Sci.* **50** (2000) 525 [[hep-ph/0007218](#)].
- [5] J. Soffer and J.M. Virey, *Testing various polarized parton distributions at RHIC*, *Nucl. Phys.* **B 509** (1998) 297 [[hep-ph/9706229](#)].
- [6] C. Bourrely, J.P. Guillet and J. Soffer, *Spin effects with polarized protons at RHIC*, *Nucl. Phys.* **B 361** (1991) 72.
- [7] P. Taxil and J.M. Virey, *Sensitivity to a new right-handed charged current in polarized hadronic collisions at RHIC*, *Phys. Lett.* **B 404** (1997) 302 [[hep-ph/9704204](#)]; *Discovery limits for a new contact interaction at future hadronic colliders with polarized beams*, *Phys. Rev.* **D 55** (1997) 4480; *A light leptophobic  $Z'$  in polarized hadronic collisions*, *Phys. Lett.* **B 441** (1998) 376 [[hep-ph/9807487](#)]; *Spin asymmetries in one jet production at RHIC with polarized proton beams: the effects of a hadrophilic  $Z'$* , *Phys. Lett.* **B 383** (1996) 355 [[hep-ph/9604331](#)].
- [8] J. Küblbeck, M. Böhm and A. Denner, *FeynArts: computer algebraic generation of Feynman graphs and amplitudes*, *Comput. Phys. Commun.* **60** (1990) 165.
- [9] J.A. M. Vermaseren, *New features of FORM*, [math-ph/0010025](#).
- [10] A. Denner and S. Dittmaier, *Complete  $O(\alpha)$  QED corrections to polarized Compton scattering*, *Nucl. Phys.* **B 540** (1999) 58 [[hep-ph/9805443](#)].
- [11] T. Gehrmann and W.J. Stirling, *Polarized parton distributions in the nucleon*, *Phys. Rev.* **D 53** (1996) 6100 [[hep-ph/9512406](#)].
- [12] M. Gluck, E. Reya and A. Vogt, *Dynamical parton distributions of the proton and small  $x$  physics*, *Z. Physik* **C 67** (1995) 433.
- [13] M. Gluck, E. Reya, M. Stratmann and W. Vogelsang, *Next-to-leading order radiative parton model analysis of polarized deep inelastic lepton-nucleon scattering*, *Phys. Rev.* **D 53** (1996) 4775 [[hep-ph/9508347](#)].