Radiative decay of the ^{229m}Th nuclear clock isomer in different host materials

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A comparative vacuum ultraviolet spectroscopy study conducted at ISOLDE-CERN of the radiative decay of the 229m Th nuclear clock isomer embedded in different host materials is reported. The ratio of the number of radiative decay photons and the number of 229m Th embedded are determined for single crystalline CaF₂, MgF₂, LiSrAlF₆, AlN, and amorphous SiO₂. For the latter two materials, no radiative decay signal was observed and an upper limit of the ratio is reported. The radiative decay wavelength was determined in LiSrAlF₆ and CaF₂, reducing its uncertainty by a factor of 2.5 relative to our previous measurement. This value is in agreement with the recently reported improved values from laser excitation.

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I. INTRODUCTION

The ²²⁹Th nucleus contains a unique low-lying isomeric state which is accessible to laser spectroscopy in the vacuumultraviolet (VUV) regime [1–3]. Its existence allows for the development of a nuclear clock operated with VUV lasers which exist today, possibly providing an improved stability when compared to atomic clocks [4,5]. A nuclear clock also has the potential to widen the breadth of applications by touting ultralight dark matter detection and sensitivity to

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variations of fundamental constants [6], as well as improved geodesy [7,8].

After the detection of the internal electron conversion decay of the ²²⁹Th nuclear clock isomer was achieved [2] and following the approach described in Ref. [9], the ^{229m}Th radiative decay was observed in an experiment whereby the isomer was populated via the β decay of ²²⁹Ac produced from its shorter-lived precursors implanted in CaF_2 and MgF_2 wide band-gap crystals [3]. The implanted nuclei decayed to ²²⁹Ac which in turn β decayed to the ^{229m}Th isomeric state with a branching ratio in the range of 14 to 93% [9]. The photons from the decay of the isomer were observed in a VUV spectrometer and a wavelength value of 148.7 ± 0.4 nm was obtained, whose uncertainty expressed as a photon frequency is on the order of THz. This opens the route for the development of a solid-state based nuclear clock. Recently, based on Ref. [3] and the present work, laser excitation of ²²⁹Th embedded in a CaF₂ crystal [10] and a LiSrAlF₆ crystal [11]

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was achieved resulting in an improved wavelength value whose uncertainty is on the order of GHz [11,12]. Subsequently, narrow-band laser excitation with a VUV frequency comb of 229 Th in CaF₂ has determined the radiative decay transition frequency on the order of a few hundred kHz, allowing to resolve the quadrupole splitting of the nuclear resonance [13].

The ^{229m}Th nucleus has two primary decay modes, either decaying via an $M1(E2) \gamma$ transition and emitting a photon or via internal conversion and delivering its energy to an electron. For the purpose of this experiment, the radiative decay and the detection of the emitted photon are critical. In case of neutral ^{229m}Th the expected extremely large internal conversion coefficient, i.e., the ratio between the decay widths of IC and γ decay $\alpha_{\rm IC} = \Gamma_{\rm IC}/\Gamma_{\gamma} = 10^9$ results in a strong dominance of the IC decay branch once it is energetically allowed and makes the detection of the weak γ decay branch experimentally unfeasible [14,15]. While the conversion coefficient for doped Th is not known, it is generally accepted that decay of the isomer via electron conversion can be suppressed if the Th atoms are incorporated into a crystal with a band gap wider than the ^{229m}Th radiative decay energy in a way that ensures that the gap between the highest-energy filled electronic state and the lowest-energy empty state remains larger than the isomer energy [16-21]. Within the ²²⁹Th community, this is often referred to as preserving the band gap. If this condition is satisfied and electron conversion is suppressed, then the γ decay branch can be experimentally observed, i.e., VUV photons with the radiative decay wavelength are emitted. Alongside CaF₂, other large band-gap crystals, for example LiSrAlF₆, are being considered as hosts for ²²⁹Th [18].

With the ^{229m}Th laser excitation achieved, comparing different crystal materials represents an important step in the development of a (solid-state) nuclear clock. This paper reports the results from a measurement campaign using the same methodology reported in Ref. [3] to test different crystal materials and determine the radiative decay wavelength value.

II. EXPERIMENTAL SETUP

The experiment took place at the Isotope Separator On-Line DEvice (ISOLDE) facility [22] at CERN. A beam of 1.4 GeV protons at 2 μ A was impinged on a ThC_x target producing ^{229m}Th precursors which diffused to the surface by heating the target to 2000 °C. An ion beam of surface-ionized ²²⁹Ra⁺ and ²²⁹Fr⁺ was accelerated to 30 keV and separated according to its mass-to-charge ratio through the General Purpose mass Separator. The radioactive ion beam was subsequently transported to the VUV spectrometer (Resonance Ltd., VM180) [3,23,24].

A schematic diagram of the experimental setup can be found in Refs. [3,24]. The radioactive beam was implanted into crystals (see Table I) that were mounted on a rotatable wheel (see Refs. [23,24] for details). For the radiative decay fraction measurements the implantation times varied between 10 and 30 min, however, wavelength determination measurements had longer implantation times between 40 and 90 min. After implantation, the wheel was rotated by 180° to place the crystals in front of the adjustable entrance slit of the spectrometer. A stepper motor controlled the rotation

TABLE I. Specifications on each crystal used in the experiment. Amorphous SiO_2 is denoted as $a-SiO_2$ in this table. The Si(111) substrate was 0.75 mm thick, whereas the Si(100) substrate was 0.67 mm thick. The thickest crystals (5 mm thickness) are denoted "bulk."

Crystal	Dimensions $(l \times w \times t)$	Substrate	Manufacturer
CaF ₂ 350	$2 \text{ cm} \times 2 \text{ cm} \times 50 \text{ nm}$	Si(111)	Imec
CaF ₂ 850	$2 \text{ cm} \times 2 \text{ cm} \times 50 \text{ nm}$	Si(111)	Imec
AlN	$1 \text{ cm} \times 1 \text{ cm} \times 50 \text{ nm}$	Si(111)	Imec
a-SiO ₂	$2 \text{ cm} \times 2 \text{ cm} \times 300 \text{ nm}$	Si(100)	Imec
LiSrAlF ₆	$1 \text{ cm} \times 1 \text{ cm} \times 1 \text{ mm}$	_	AC Materials
MgF ₂ bulk	$\emptyset = 25.4 \text{ mm} \times 5 \text{ mm}$		Thorlabs, Inc.
CaF_2 bulk	$\varnothing = 25.4 \text{ mm} \times 5 \text{ mm}$	—	Thorlabs, Inc.

of the crystal holder to improve the reproducibility of crystal position compared to the manual rotation method used in the previous campaign reported in Ref. [3]. A deviation in the relative source position in front of the entrance slit based on the full step angle and the step angle accuracy of the motor driven wheel, given by the manufacturer, is negligible. VUV photons from the radiative decay entered the spectrometer, were then reflected to a diffraction grating in a Czerny-Turner configuration, and detected with a photomultiplier tube (PMT). A 250-µm slit size was used for wavelength determination measurements and a 2-mm slit size for radiative decay fraction and half-life measurements. In addition, a microchannel plate (MCP) detector with a phosphor screen and camera were installed at the radioactive beam position behind the wheel to perform beam diagnostics and identify the implantation location and size of the radioactive beam on the crystals.

For the wavelength measurements, the thin-film CaF₂ crystal (CaF₂ 350 in Table I) was used to reduce the Cherenkov background resulting from β decays of implanted isotopes in the sample [3]. Wavelength calibration measurements from a VUV light source consisting of a plasma discharge in air were taken before and after each series of wavelength measurements to account for any fluctuations in centroid position of the calibration lines.

In order to determine the number of implanted ²²⁹Fr and ²²⁹Ra isotopes, a high-purity germanium (HPGe) coaxial detector (Canberra, 75% efficiency) with an aluminum cap was placed 1 m away from the implantation point. Energy and absolute efficiency calibration of the HPGe detector were performed with activity calibrated γ -ray sources of ⁶⁰Co, ¹³⁷Cs, ¹⁵²Eu, and ²⁰⁷Bi.

A. Beam diagnostics

The radioactive ion beam was directed through an empty slot on the wheel crystal holder and impinged on the MCP detector that was equipped with a phosphorous screen anode. The screen was observed with a camera and images of the ion beam were collected. An example is shown in Fig. 1. The intensity of the image was projected onto the x and y axes and fitted with a Gaussian profile to determine the full width at half maximum of the beam spot for each axis. The axes were calibrated using an optically visible image of equally spaced grooves, leading to a conversion factor of 87 pixels/mm. The



FIG. 1. Image of the beam spot captured from the MCP+phosphor screen setup captured by a CCD camera. The dashed ellipse indicates the beam size at the full width at half maximum level. The dimensions of this ellipse are 1.5 mm \times 2.7 mm. The *x* and *y* axes correspond to the horizontal and vertical beam position, respectively. Axis tick labels are rounded to the nearest decimal in mm.

ion beam had a size of approximately $1.5 \text{ mm} \times 2.7 \text{ mm}$ at the full width at half-maximum.

B. Radioactive beam intensities and purity

To quantify radiative decay fractions on different samples, the implanted amount of ²²⁹Fr ($t_{1/2} = 50.2 \pm 2.0$ s), ²²⁹Ra ($t_{1/2} = 4.0 \pm 0.2$ min), and ²²⁹Ac ($t_{1/2} = 62.7 \pm 0.5$ min) isotopes were quantified. These amounts depend on the implantation time and the beam intensity of the specific isotopes. Using Bateman's equations [25] with the known half-lives and β -decay branching ratio range of ²²⁹Ac feeding ^{229m}Th, the amount of ²²⁹Th isomers can be determined as a function of time.

The beam intensities of ²²⁹Fr and ²²⁹Ra were determined using their characteristic γ -ray transitions measured with the HPGe detector during implantation. Based on the time behavior of the intensity of the characteristic γ transition from the ²²⁹Ac β decay, it was concluded that the beam intensity of 229 Ac $\mathcal{O}(10^6 \text{ pps})$ was negligible compared to 229 Ra. Information on the β -decay scheme of ²²⁹Ra is limited as no absolute γ -ray intensities are reported [26]. To improve this, the A = 229 beam was directed to the ISOLDE Decay Station (IDS) [27], and several intense γ lines could be attributed to the decay of ²²⁹Ra feeding levels in ²²⁹Ac. By comparing the observed decays from the newly identified γ transitions with the 569-keV γ line of ²²⁹Ac, for which the absolute intensity is reported [26], the absolute γ -ray intensities of the ²²⁹Ra lines were determined. The results of this decay study will be reported in a forthcoming publication [28]. The intensity of the characteristic γ rays of ²²⁹Fr, ²²⁹Ra, and ²²⁹Ac was measured as a function of time during implantation. The time evolution was fitted with Bateman's equations and after correction for γ -ray efficiency and absolute intensity, the beam intensity was determined.



FIG. 2. The α -decay spectrum of the CaF₂ 350 sample (see Table I for details of the crystal), the α lines from the A = 229 (square), A = 228 (triangle), and A = 227 (circle) decay chains are indicated.

To verify the procedure and to determine precisely the beam purity, α spectroscopy was performed on the implanted crystals about 10 months after the experiment. A 10 mm \times 10 mm Si PIN photodiode detector (Hamamatsu S3590-09) was used with a collimator which limited the detection area to $3.25 \text{ mm} \times 3.25 \text{ mm}$ to avoid edge effects from the surface of the detector. The α -decay setup was simulated to determine the detection efficiency. This was further verified with measurements taken at different detector-to-crystal distances using an intensity calibrated ²⁴¹Am source. To reduce the uncertainty on the α detection efficiency, the final measurements were performed with a detector-to-crystal distance of 6 cm. The crystals were all measured at this distance for several weeks to optimize the statistics. A typical α -decay energy spectrum is shown in Fig. 2. These spectra also allowed to determine the beam composition. For the A/Q = 229 radioactive ion beam setting of the mass separator this resulted in A =229 is 99.47 \pm 0.04%, A = 228 is 0.49 \pm 0.04%, and A =227 is $0.04 \pm 0.01\%$. Contaminants of neighboring masses are due to the finite-mass resolution and tailing from neighboring mass peaks. From the α lines from ²²⁹Th [29], it was possible to calculate the implanted activity and estimate an average implantation rate for each crystal. In addition to the α -decay setup the implanted crystals were measured with an intensity calibrated HPGe detector, and the γ lines from ²²⁹Th and their absolute γ -ray intensities [29] were used to estimate the implanted activity. This was found to be in good agreement with the value obtained from the α -decay measurements. However, the total implantation activity obtained from the off-line α and γ spectroscopy measurements did not agree with the values deduced from the on-line γ spectroscopy measurements suggesting that the literature value [30] of the absolute γ -ray intensity of the ²²⁹Ac decay line used to estimate the absolute intensities of the 229 Ra γ lines needs to be corrected. The implanted activity determined from the offline measurements was about a factor of 2 smaller than the one deduced from the online implantations using the observed γ -ray intensities. Therefore, a correction factor of 0.53 ± 0.03 to the rates obtained from the online ν decay measurements was implemented, and the final average values for the beam intensities were found to be $1.42 \pm 0.09 \times 10^6$ pps for 229 Fr TABLE II. Experimentally determined band gaps for each host material. A host material with a band gap larger than the radiative decay energy of 229 Th (8.4 eV [11,12]) is expected to be a necessary condition to suppress the internal conversion decay channel [3]. The band gap of amorphous SiO₂ (or a-SiO₂), which is less well defined than for the other materials in this list (crystalline), is discussed in the text.

Material	Band gap (eV)	Band gap Ref.	
MgF ₂	12.4	[34]	
CaF ₂	12.1	[35]	
LiSrAlF ₆	12.1	[36]	
a-SiO ₂	9.3–9.6	[37,38]	
AlN	6.2	[39]	

and $1.24 \pm 0.08 \times 10^8$ pps for ²²⁹Ra. These rates were used to estimate the radiative decay fraction.

C. Crystal specifications

A summary of the specifications of the different crystals used in this experiment is shown in Table I and the band gaps for each material are tabulated in Table II. The CaF₂ epitaxial thin films were grown using molecular beam epitaxy (MBE) at Imec (Leuven, Belgium), using the same growth parameters except for different growth temperatures, indicated by the number in degrees Celsius in the first column of Table I, which is expected to result in different lattice defect densities and stacking sequence due to distinct Si/CaF₂ interfaces [31]. MBE is a process used to grow thin layers of materials with precise interface, thickness, and uniformity under ultra-high vacuum conditions [32]. Before being placed in the MBE reactor, the substrates, 0.75-mm-thick wafers of Si(111), were cleaned with 2% NH₄F for 60 s followed by high thermal annealing up to 875°C in ultra-high vacuum to remove oxides and organic contaminants. Once inside the growth chamber the 50-nm thin films were grown epitaxially at temperatures of 350°C and 850°C, leading to A-type stacking (F-interface) and B-type stacking (CaF interface), respectively. More details on the growth procedure can be found in Ref. [3]. The AlN epitaxial thin film was grown at Imec using metalorganic chemical vapor deposition (MOCVD) [33]. The amorphous SiO_2 (a-SiO₂) thin film on Si was prepared at Imec and consists of a dry thermal oxide layer created by annealing a Si wafer in a controlled O₂ environment, as widely used in microelectronics.

The LiSrAlF₆ crystal was produced by AC Materials for University of California, Los Angeles (UCLA) using the Czochralski method [40]. The bulk crystals, CaF₂ (crystal identifier nr. WG51050) and MgF₂ (WG61050) broadband uncoated precision windows, were purchased from Thorlabs, Inc. All thin-film crystals, as well as the LiSrAlF₆, were mounted on near-IR absorptive neutral density filters (Thorlabs, Inc., $\emptyset = 25 \text{ mm} \times 2.8 \text{ mm}$, OD: 6.0).

III. RADIATIVE DECAY SPECTRA

The methodology used to fit the radiative decay spectra was adapted from Refs. [3,23]. Spectra dedicated to the de-



FIG. 3. Cherenkov spectra from A = 230 implantations for CaF₂ (circles), MgF₂ (triangles), LiSrAlF₆ (x's), AlN (squares), and SiO₂ (diamonds) normalized by the activity deduced from the γ -data recording during implantation. Broad radioluminescence peaks are present in CaF₂ bulk at approximately 142 and 177 nm. All spectra were taken with a measurement time of 10 s per data point and a step size of 100 motor positions between each point.

termination of radiative decay fraction were acquired when the maximum number of 229m Th were present based on results from the Bateman equations (see Sec. II B). Spectra obtained from A = 230 implantations are shown in Fig. 3 while sample spectra from A = 229 are shown in Figs. 4(a)-4(g).

The A = 229 spectra obtained with a 2-mm slit size were fitted using three components: a constant PMT dark count rate, the Cherenkov background and the isomeric VUV signal. These are shown separately in Fig. 4. The Cherenkov background was modeled by a second-degree polynomial where the coefficients were constrained by the Cherenkov radiation observed from an implantation of A = 230 into each respective crystal (Fig. 3). The VUV signal was described by a Gaussian function.

A modification to this fitting procedure was applied to data obtained with the 5-mm-thick CaF_2 bulk crystal, which showed a broad radioluminescence peak excited by the Cherenkov radiation and emitting at approximately 142 nm on the left-hand side of the ^{229m}Th peak (see Fig. 3). An asymmetric Gaussian profile was used in addition to the polynomial and its parameters were constrained to fit results obtained from Fig. 3.

For the wavelength determination measurements with a 250 μ m slit size spectra were obtained when the β decay of ²²⁹Ac and ^{229m}Th were in transient equilibrium. The fitting procedure uses the same approach including a decay correction detailed in Ref. [23] and a Lorentzian profile instead of a Gaussian, since the Lorentzian describes the peak better at the smaller slit size. A Lorentzian line profile of the instrument dominates when using smaller slit sizes at or below 250 μ m, while at larger slit sizes the distribution of the implanted source leads to a lineshape that can be described by a Gaussian. Spectra for both the CaF₂ 350 thin film and the LiSrAlF₆ are shown in Figs. 4(h) and 4(i).



FIG. 4. Typical spectra taken with a 2 mm [(a)-(g)] and 250 µm [(h)-(i)] entrance slit demonstrating the fitting method for the radiative decay of ^{229m}Th. Measurements [(a)-(g)] were taken with a measurement time of 10 s per point and a step size of 100 motor positions between each point. Measurements [(h) and (i)] were taken with a 10-s measurement time per point and a step size of 15 motor positions between each point. The dashed curve is a Gaussian peak in (a) to (e) and a Lorentzian peak in (h) and (i). The dot-dashed curve is a polynomial representing the Cherenkov background radiation and the dotted curve is the radioluminescence peak possibly due to a color center. The solid black line is the dark count rate from the PMT. The reduced Cherenkov background in case of spectra taken with the thin-film crystals [(a), (d), and (h)] did not allow to distinguish clearly between the Cherenkov background from the dark countrate. (a) CaF₂ 350 thin film, (b) MgF₂ bulk, (c) CaF₂ bulk, (d) CaF₂ 850, (e) LiSrAlF₆, (f) AlN, and (g) SiO₂, (h) CaF₂ 350, and (i) LiSrAlF₆.

IV. RADIATIVE DECAY FRACTION

The radiative decay fraction of a crystal is the ratio between the number of 229m Th decaying via radiative decay [Eq. (1) I] versus the number of 229m Th embedded in the crystal [Eq. (1) II] and can be defined as

radiative decay fraction =
$$\frac{H}{\underbrace{\Lambda \varepsilon_{I}}_{I}} \frac{1}{\underbrace{N_{229m}}_{II}}$$
, (1)

where *H* is the measured maximum of the radiative decay count rate of the 148-nm line, $\Lambda = \ln(2)/t_{1/2}$ is the decay constant with $t_{1/2}$ the half-life of the ^{229m}Th isomer, ε_I is the total detection efficiency of the instrument, and N_{229m} is the number of ^{229m}Th nuclei. To minimize the statistical uncertainty, we determine the radiative decay fraction when the VUV signal is at its maximum count rate.

The efficiency of the instrument is $\varepsilon_I = \varepsilon_P \varepsilon_G \varepsilon_C$, where $\varepsilon_P = 19\%$ is the quantum efficiency of the PMT detector and $\varepsilon_G = 40\%$ is the grating efficiency, both specified by the manufacturer. The ε_C is the collection efficiency of the VUV photons based on the solid angle of the entrance slit and the collimation mirror for the emitted radiation from the source [24]. The collection efficiency was simulated for each crystal according to their different thicknesses and consequently their distance relative to the entrance slit (see Table I). For the CaF₂ bulk crystal, this resulted a collection efficiency of 2.4\%.

The VUV transmission through the crystal is assumed to be 100% due to the small implantation depth (16–18 nm for

TABLE III. Relative radiative decay fractions for each crystal. The number of implantation/measurement cycles for each crystal is denoted with #.

Crystal	Relative radiative decay fraction (%)	#
CaF ₂ bulk	100	2
LiSrAlF ₆	62.7 ± 10.7	2
CaF ₂ 350	47.5 ± 8.0	2
MgF ₂ bulk	47.1 ± 6.9	4
CaF ₂ 850	15.0 ± 2.5	2
a-SiO ₂	<0.68	1
AlN	<0.63	1

CaF₂, MgF₂, LiSrAlF₆, AlN, and 24 nm for SiO₂, according to SRIM simulations [41]) and reflection at the crystal surfaces is assumed to be negligible. Also, the reflectivity from both the collimation mirror and the focusing mirror of the spectrometer are assumed to be 100% [3].

As the efficiency of the instrument and the VUV transmission through the crystal should be considered as upper limits, only a lower limit of the absolute radiative decay fraction can be reported. For CaF₂, which has the highest radiative decay fraction, a lower limit of the absolute radiative decay fraction of $\ge 0.9\%$ or $\ge 5.7\%$ was obtained assuming the 93% or 14% ²²⁹Ac β branching ratio to the ^{229m}Th, respectively.

For the other host materials, the relative radiative decay fraction with respect to CaF₂ bulk was determined and is reported in Table III and Fig. 5 which removes the uncertainty related to the instrument efficiency. A weighted average radiative decay fraction for each crystal was obtained [the result from Eq. (1)]. To cope with the varying half-life of the ^{229m}Th in different crystal materials, radiative decay fractions were calculated by varying the half-life between $t_{1/2} = 500$ and $t_{1/2} = 800$ s which should cover the range of half lives in the different crystals [3,28]. The differences in the radiative decay fraction results using these two extreme values were considered as a systematic uncertainty. Additionally, the relative difference between the maximum number of ^{229m}Th nuclei



FIG. 5. Radiative decay fractions for each crystal relative to CaF_2 bulk. An upper limit is reported for AlN and SiO₂ due to the absence of a signal, therefore a downward-pointing arrow is shown for both of these crystals.

according to Bateman's equation [25] and the number of 229m Th nuclei at the time of the radiative decay measurement is on the order of 1% and is also considered as a systematic uncertainty. The statistical and systematic uncertainties were added in quadrature and reported in Table III.

A. CaF₂, MgF₂, and LiSrAlF₆

Although the measured radiative decay fractions are likely affected by various material parameters and physical processes that are currently unknown, it is worthwhile discussing potential reasons for the differences observed among crystals.

The highest radiative decay fraction was observed for the CaF₂ single crystal, indicating that, despite the defects created during ion implantation (of the order of 600 atomic displacements per implanted ion based on SRIM [41] simulations), and as reported in Ref. [3], the crystal structure is preserved and a substantial fraction of the Th atoms take up configurations that suppress internal conversion, i.e., substitute for Ca, likely forming complexes with neighboring defects (e.g., with two F interstitials or with one Ca vacancy) yielding an effective 4+ charge state and a band gap larger than the isomer transition energy (preserving the band gap) [16]. In addition to the atomic displacements created during implantation, the β^{-} decay of the precursor isotopes ²²⁹Ac, ²²⁹Ra, and ²²⁹Fr may also potentially create defects, namely atomic displacements originating from the recoiling atom and created by the emitted β^{-} particles. Both effects are, however, negligible compared to the effect of the implantation of 229 Ra and 229 Fr. The highest recoil energies correspond to the decay of ²²⁹Fr, at a maximum of about 31 eV, which may be enough to eventually cause atomic displacements (considering the threshold displacement energies of 23 and 12 eV for Ca and F in CaF₂ [42]) but far less than on implantation at 30 keV. The β^- particles emitted by the three precursors ²²⁹Ac, ²²⁹Ra, and ²²⁹Fr have energies of up 3 MeV (with average energies of the order of a few hundred keV), which is enough to generate a few atomic displacements per decay but, again, orders of magnitude less than on implantation at 30 keV.

Interestingly, the CaF₂ thin films show significantly lower radiative decay fractions than the bulk crystal, and by different amounts, depending in this case on the film growth temperature. Compared to high-quality single crystals, the thin films are expected to have a higher density of defects, both point defects (because the MBE growth occurs far from thermodynamic equilibrium) and extended defects (e.g., grain boundaries, due to the lattice mismatch between the film and the substrate). Many of these defects may produce in-gap states (not preserving the band gap), so that increasing the concentration of those defects (e.g., by growing a film at different temperatures, as here) increases the probability of such electronic states interacting with ^{229m}Th nuclei and open electron conversion channels. Moreover, such defects may form complexes with the Th atoms, resulting in local Th configurations that themselves have in-gap states. The CaF₂ layer grown at 350°C with A-type stacking sequence is fully strained to the Si(111) substrate leading to a reduced defect density with respect to the CaF₂ layer gown at 850°C with B-type stacking sequence which is fully relaxed and therefore present a larger defectivity [31].

Comparing our results on CaF2, MgF2, and LiSrAlF6 crystals is even more challenging, because it involves not only different compounds but likely also significant variations in the types and concentrations of defects that may contribute to conversion channels. Nevertheless, simply looking at the available literature, one may argue that MgF₂ and LiSrAlF₆ would indeed be more prone to electron conversion channels, because in both cases the lowest-energy Th configurations fail to preserve the band gap [11,17]. In MgF₂, the lowestenergy configuration consists of a complex containing a Mg-substitutional Th and one Mg vacancy, which introduces in-gap states, resulting in a predicted band gap that is smaller than the isomer transition energy [17]. A configuration involving two F interstitials is predicted to preserve a band gap larger than the isomer energy, but is itself less energetically favorable (by about 0.8 eV). In LiSrAlF₆, the lowest-energy configuration consists of Th substituting for Sr with two neighboring F interstitials, while the next most favorable configurations (at a cost of about 0.6 eV) consists of Th in a Sr site next to one F interstitial and one Li vacancy; both configurations fail to preserve the band gap [11]. In the present work, the Th atoms are introduced by ion implantation, far from equilibrium, which appears to allow for the creation of Th configurations that preserve the band gap despite being energetically unfavorable (such as that involving the Mg vacancy in MgF_2), so that radiative decay is still observed. Nevertheless, it is plausible that in MgF2 and LiSrAlF6 larger fractions (compared to CaF2) of the Th atoms take up configurations (such as the predicted lowest-energy ones) that allow for electron conversion, contrary to CaF₂, which would then explain why the radiative decay fraction is lower than for the CaF₂ crystal. Interestingly, this hypothesis would additionally suggest that, for MgF_2 and LiSrAlF₆, introducing the Th atoms by ion implantation may yield higher radiative decay fractions than doing so during growth, closer to equilibrium.

B. AlN and SiO₂ crystals

Contrary to CaF₂, MgF₂ and LiSrAlF₆, no radiative decay signal was detected in either of the AlN or SiO₂ crystals [Figs. 4(f) and 4(g)]. The A = 229 implantation measurements were fitted with a polynomial constrained to the Cherenkov spectra obtained from the A = 230 implantation. If a signal were to be present, then it was defined as being greater than or equal to a 3σ deviation from the residuals obtained by the A = 229 fit leading to the upperbound on the relative radiative decay fraction reported in Table III.

In the case of AlN, its band gap is lower than the 229m Th radiative decay energy, meaning the internal conversion channel is energetically favorable and a strong isomer decay signal was not expected. In contrast to AlN, amorphous SiO₂ has a band gap (9.3–9.6 eV [37,38]) that is larger than the 229m Th transition energy. Although amorphous insulators have a nonzero electronic density of states (DOS) within the band gap, these states are typically more localized compared to valence or conduction band states. Such localized states can still, in principle, enable internal conversion channels. However, due to their localized nature, in order for such states to fully account for the complete suppression of the radiative decay fraction, they would have to be spatially correlated with the positions of the Th nuclei. For true band states (valence or conduction), such correlation is not required, because band states are fully delocalized across a crystal, but in SiO₂ the gap between valence and conduction bands is larger than the isomer transition energy, i.e., electron conversion via such a channel is not allowed. Photon absorption is another potential reason for the nonobservation of VUV emission from SiO₂. However, considering the absorption coefficient of dry amorphous SiO₂ (of the order of 1000 cm⁻¹ around 8.4 eV) [43], one expects a transmission above 99% through a 40 nm SiO₂ layer (which should contain more than 90% of the emitting 229m Th nuclei). Therefore, the fact that the 229m Th radiative decay signal was not observed for SiO₂ strongly suggests that the introduction of Th atoms in SiO₂ creates electronic states within the band gap. Detailed calculations on Th:SiO₂ addressing this question are expanded on in the following section (Sec. V).

V. CALCULATIONS OF THORIUM IN A SILICON DIOXIDE ENVIRONMENT

The electronic properties of thorium atoms in SiO_2 were modelled using density functional theory (DFT) calculations, using the supercell approach. The purpose of the calculations was to gain insight into in-gap electronic states potentially created by the Th atoms, in an attempt to understand why radiative decay was not observed for SiO_2 . The model structures used in our DFT calculations are based on crystalline SiO_2 while the experiments use amorphous SiO_2 . Nevertheless, the model still allows us to obtain relevant insight, since the main conclusions, as described below, are more related to local effects (localized Th states and the nature of Th-O bonds) rather than to the long-range order (that exists in our DFT model but not in the experiment).

Two structures were used to model Th:SiO₂, one where thorium replaces a silicon atom (structure 1) and one where thorium and two oxygen atoms are added to SiO₂ (structure 2). This is not an exhaustive exploration of all possible Th configurations in SiO₂, merely examples of likely configurations with a ThO₄ environment, which one expects to be more prone to a Th⁴⁺ charge state and thus to suppress electron conversion. Naturally, many other structures are possible, in particular considering that the Th atoms were incorporated by ion implantation, far from equilibrium; however, the purpose of these calculations is to assess whether, even under the most favorable conditions for radiative decay that one can conceive, there are still characteristics specific to α -SiO₂ that could create conversion channels. To generate these two structures, we started with the crystal structure of α -SiO₂ (space group 152) and made a $3 \times 3 \times 3$ supercell with side lengths of approximately 15 Å to minimize unphysical Th-Th interactions. In the first structure, one Si atom was replaced by Th (a substitutional defect), and in the second, a Th atom and two O atoms were added to voids in the SiO₂ lattice (an interstitial defect). Both structures were optimized. The resulting geometry for structure 1, shown in Fig. 6, has Th in a ThO₄ tetrahedron that is significantly larger than the SiO₄ tetrahedra in the bulk material (5.12 Å³ vs 2.21 Å³) due to the larger size of Th⁴⁺. In structure 2, Th is in a low-symmetry ThO₇ polyhedron. Formation energies for the defects were



FIG. 6. (a) DFT structure 1 for the Th defect in SiO₂. Th is shown in green, Si in blue, and O in red. (b) DFT structure 2 for the Th defect in SiO₂. (c) Thorium projected density of states (PDOS) in Th:SiO₂ defect structure 1. Energies are relative to the highest occupied band, and the black dashed line at 8.355 eV marks the ²²⁹Th isomer transition energy (note that since the nuclear excited state is not an electronic state, marking it relative to the Fermi energy is an arbitrary choice). (d) Thorium PDOS in structure 2.

computed by writing balanced reactions between Th:SiO₂, pure SiO₂, and SiO₂. The formation energies are +2.4 eV for structure 1 and +7.9 eV for structure 2. Our intuition is that structure 2, featuring a higher coordination number for Th, is a better reflection of Th in amorphous SiO_2 . The calculations were performed with Vienna ab initio Simulation Package [44], version 6.4.2, using the projector augmentedwave [45] method with a plane-wave cutoff of 500 eV and a spin-restricted formalism. The Perdew-Burke-Ernzerhof [46] functional was used for all structural optimizations, and the modified Becke-Johnson (MBJ) [47,48] functional was used for density of states calculations. The unit cell of α -SiO₂ was optimized with a 9-9-6 Gamma-centered k-point grid, and the thorium-doped $3 \times 3 \times 3$ supercell calculations were done with a 3-3-2 k-point grid (0.03 Å⁻¹ spacing in all cases). Polyhedral volumes were computed using visualization for electronic and structural analysis [49,50].

The Th orbital energies were determined through the projected density of states (PDOS) for each structure, shown in Fig. 6. These calculations used the MBJ functional, which has been previously used to study thorium defects in wide bandgap crystals [11]. In both structures, empty Th states emerge within the band gap, and the energy difference between them and the top of the valence band is smaller than the isomer transition energy, so that internal conversion may be possible via excitation of an electron from oxygen (which dominates the top of the valence band) to these thorium-related in-gap states. The lowest unoccupied states are principally composed of Th 5f, with small admixture of Th 6d and 7s, and O 2pfrom the atoms closest to thorium. Higher unoccupied states also contain significant 5f and 6d character. In structure 2 the unoccupied bands are lower energy than in structure 1 and have a broader energy dispersion, which suggests that there are more pathways for internal conversion.

The Th PDOS in SiO₂ can be compared to that in Th-doped $LiSrAlF_6$ [11] in an attempt to understand why radiative nuclear decay has been observed in Th:LiSrAlF₆ but not Th:SiO₂, while in both cases in-gap states appear at energies lower than that of the isomer transition. The PDOS plots for SiO₂ show Th contributions to the valence band, which is principally composed of O 2p. Internal conversion would require the electronic wavefunction to overlap with the Th nucleus; a larger Th component in the valence band implies more overlap and thus higher conversion rates. This contribution is in fact consistent with the chemical notion that Th-O bonds ought to be more covalent in nature than the very ionic Th-F bonds in Th:LiSrAlF₆ or Th:CaF₂ due to the energy and size of O²⁻ and F⁻ valence orbitals. Therefore, it points to a general and intuitive difference between fluoride versus oxide hosts, namely the degree of hybridization between Th valence orbitals and anion orbitals. An alternative electron conversion mechanism would be that radiation (in particular β^{-}), produced by the decaying nuclei in the sample, excites electrons from the valence band to the Th-related in-gap states, so that these electrons can then be excited to the conduction band on decay of the isomer. However such a mechanism would in principle also occur for LiSrAlF₆, where such Th-related in-gap states are also predicted to occur even for the lowestenergy Th configurations [11], and yet the radiative decay is clearly observed in LiSrAlF₆ in the present work.

VI. WAVELENGTH DETERMINATION

A. Calibration procedure

Calibration scans with a 250-µm slit size covering a wavelength range of 120–180 nm (see Ref. [24]) were taken throughout the experimental campaign.

Since the plasma source used for wavelength calibration is 36 cm from the entrance slit and the implanted CaF₂ 350 crystal is 5.5 mm from the slit, VUV photons from the plasma source and the radioactive source enter under different angles with respect to the optical axis. To eliminate a possible angular dependence of the wavelength calibration procedure, a MgF₂ diffuser crystal was mounted on the wheel to diffuse the light from the plasma source at the position of the implanted crystals. The three most prominent oxygen and nitrogen peaks were isolated and fitted separately to deduce their centroids in terms of motor position. While each peak appeared as a singlet at the resolution of the spectrometer in the first diffraction order, each peak was a multiplet containing two or more peaks which could be partially resolved in the second diffraction order. The fit procedure included each peak within the multiplet



FIG. 7. An example spectrum of the nitrogen line at 141 nm used for the offset determination. The solid line is the fit to the data.

using experimentally deduced constraints on the relative peak positions and their intensities.

The wavelengths of the single lines used in the calibration are 130.2168, 141.194, 149.4675, and 174.2729 nm, and a full list of spectral lines can be found in Ref. [24]. The linear fit from the wavelength calibration measurements performed at ISOLDE resulted in a slope of $b = 115.24 \pm 0.08$ motor positions per nanometer. This corresponds to $0.008678 \pm$ 0.000006 nm per motor position which is within 1σ of the value reported in Ref. [24].

The single 141-nm (141.194-nm) nitrogen line was measured before and after each group of isomer wavelength measurements and used as an offset. Only scanning the 141nm nitrogen line allowed more calibration measurements to be performed in a shorter time period, resulting in better control over fluctuations in centroid position and compensating for any drifts of the system. A Lorentzian profile with a linear background, shown in Fig. 7, was used to fit the calibration line due to the invading tails of the neighboring 131 and 149nm multiplets. In the final wavelength determination of the isomer, the offset parameter is represented by M_{141} in Eq. (2).

B. Uncertainty analysis

1. Offset determination

The nitrogen calibration line used as the offset consists of a triplet of three closely spaced transitions of neutral nitrogen [51–53]. The wavelength of this triplet from NIST is reported as 141.194 nm, where the uncertainty is implied by a factor of 25% on the least significant digit [53,54], which corresponds to 0.001 nm. However, Ref. [51] shows that each of the nitrogen lines, given in Table IV, were determined to a precision of 0.0001 nm and a range of $\Delta \lambda = 0.0018$ nm between the lowest and highest wavelengths of the triplet. The range of the triplet as well as the uncertainty of the individual calibration lines were added in quadrature to give a conservative uncertainty of 0.002 nm, which corresponds to 0.2 motor positions.

TABLE IV. Nitrogen	141	nm	calibration	line	(Multiplet	uv10)
from Refs. [51,52].						

Wavelength (nm)	Lower	Upper
141.19318 ± 0.00010	$2s^2 2p^3 {}^2P_{1/2}^{\circ}$	$2s^2 2p^2 3s {}^2 D_{3/2}$
141.19395 ± 0.00010 141.19494 ± 0.00010	$\frac{2s^2 2p^3}{2s^2 2p^3} \frac{^2P_{3/2}^{\circ}}{^2P_{3/2}^{\circ}}$	$\frac{2s^2 2p^2 3s}{2s^2 2p^2 3s} \frac{^2 D_{3/2}}{^2 D_{5/2}}$

2. Alignment with respect to the optical axis

The position of the radioactive source with respect to the optical axis influences the wavelength determination as VUV light can enter the spectrometer under an, on average, nonzero angle. To evaluate this effect, the position was estimated by comparing the experimental radiative decay fraction for the CaF₂ 350 crystal at a 250- μ m slit size relative to the one at 2 mm, revealing a value that varied between 4.5% and 8.1% in the course of the experiment. This points to a potential deviation of the center of the source with respect to the optical axis of 2.5 mm. The extent of this effect on the wavelength determination was simulated using raytracing. This allowed to estimate the effect of a noncentered radioactive source as well as an off-center alignment of the entrance slit of less than 0.5 mm, revealing a maximum shift in wavelength of 0.15 nm which dominates the total systematic uncertainty.

C. Wavelength determination

The isomer wavelength for each implantation was determined using Eq. (2), where λ_{141} is the nitrogen calibration line wavelength in nanometers, *b* is the slope determined from the calibration measurements, M_{141} is the 141-nm nitrogen calibration line offset motor position, and M_{229m} is the isomer motor position. The values used for wavelength determination are shown in Table V. A weighted average wavelength value of $148.491 \pm 0.019_{(stat.)} \pm 0.15_{(syst.)}$ nm for CaF₂ and $148.402 \pm 0.086_{(stat.)} \pm 0.15_{(syst.)}$ nm for LiSrAlF₆ are reported,

$$\lambda_{229m} = \lambda_{141} - b(M_{141} - M_{229m}). \tag{2}$$

VII. CONCLUSION

In testing several crystal materials the signal from the radiative decay of ^{229m}Th was observed in all but AlN and SiO₂. The AlN case follows the general understanding that a band gap smaller than the isomer transition energy facilitates the internal conversion process. However, such a mechanism does not necessarily apply to SiO₂. DFT calculations indicate that the absence of a radiative decay in SiO₂ may be due to internal conversion accelerated by the hybridization between Th valence orbitals and O²⁻. Production rates were determined for each implantation and verified in an offline α -decay analysis on the implanted crystals after the experiment, ensuring control over the amount of implanted isotopes and the purity of the beam. Relative radiative decay fractions were obtained and the CaF₂ bulk crystal was determined to have the highest radiative decay fraction.

The measured emission wavelength of the radiative decay of the 229m Th isomer was determined to be

in motor positions. The uncertainty is the standard deviation between the measurements and the value reported is the average.						
Nimp	$t_{\rm imp}$ (s)	Crystal	<i>M</i> ₁₄₁ (MP)	<i>M</i> _{229m} (MP)	λ_{229m} (nm)	
1	2233.50	CaF ₂ 350	-10834.6 ± 2.7	-9995.1 ± 2.6	148.479 ± 0.033	
2	2132.15	CaF ₂ 350	-10835.7 ± 2.0	-9993.4 ± 4.3	148.503 ± 0.041	
3	5486.23	CaF ₂ 350	-10831.7 ± 3.4	-9988.6 ± 2.5	148.510 ± 0.037	
4	3591.94	CaF ₂ 350	-10828.6 ± 2.7	-9989.4 ± 3.7	148.476 ± 0.040	
5	3669.53	LiSrAlF ₆	-10833.4 ± 1.9	-100002.7 ± 9.7	148.402 ± 0.086	

TABLE V. Isomer wavelength results for each series of wavelength determination measurements. N_{imp} is the implantation number for measurements taken at a 250-µm slit and t_{imp} is the time elapsed implanting onto the crystal. M_{141} is the centroid for the 141-nm calibration line in motor positions. The uncertainty is the standard deviation between the measurements and the value reported is the average.

 $\lambda_{229m} = 148.49 \pm 0.02_{(stat.)} \pm 0.15_{(syst.)}$ nm, improving a previous measurement using the same technique by a factor of 2.5 and in agreement with an independent recent determination [3,55]. Using the spectroscopic results from photon emission of the isomer's radiative decay, laser excitation of ^{229m}Th isomer became feasible and has meanwhile resulted in multiple observations [11, 12, 33]. This approach measures the wavelength of photon absorption when driving the ground-toisomeric nuclear transition. Laser excitation using broadband dye laser systems allowed to determine the absorption wavelength with a precision 0.0005 nm in CaF₂, 0.0003 nm in LiSrAlF₆ and frequency comb spectroscopy narrowed this value down to $\approx 10^{-10}$ nm in CaF₂. Within uncertainties, the results of emission spectroscopy presented in this work agree with the absorption wavelength obtained in laser excitation experiments.

The method of implanting an A = 229 radioactive beam of 229m Th β -decay precursors into different large-band-gap materials and observing the isomer's radiative decay using a VUV spectrometer constitutes an efficient method to test various different materials for their potential use in a future solid-state nuclear clock without the need to grow doped crystals.

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- [1] L. Kroger and C. Reich, Features of the low-energy level scheme of ²²⁹Th as observed in the α -decay of ²³³U, Nucl. Phys. A **259**, 29 (1976).
- [2] L. von der Wense, B. Seiferle, M. Laatiaoui, J. B. Neumayr, H.-J. Maier, H.-F. Wirth, C. Mokry, J. Runke, K. Eberhardt, C. E. Düllmann, N. G. Trautmann, and P. G. Thirolf, Direct detection of the ²²⁹Th nuclear clock transition, Nature (London) **533**, 47 (2016).
- [3] S. Kraemer, J. Moens, M. Athanasakis-Kaklamanakis, S. Bara, K. Beeks, P. Chhetri, K. Chrysalidis, A. Claessens, T. E. Cocolios, J. G. M. Correia, H. D. Witte, R. Ferrer, S. Geldhof, R. Heinke, N. Hosseini, M. Huyse, U. Köster, Y. Kudryavtsev, M. Laatiaoui, R. Lica *et al.*, Observation of the radiative decay of the ²²⁹Th nuclear clock isomer, Nature (London) **617**, 706 (2023).
- [4] E. Peik and C. Tamm, Nuclear laser spectroscopy of the 3.5 eV transition in Th – 229, Europhys. Lett. 61, 181 (2003).
- [5] C. J. Campbell, A. G. Radnaev, A. Kuzmich, V. A. Dzuba, V. V. Flambaum, and A. Derevianko, Single-ion nuclear clock for metrology at the 19th decimal place, Phys. Rev. Lett. **108**, 120802 (2012).

- [6] E. Peik, T. Schumm, M. S. Safronova, A. Pálffy, J. Weitenberg, and P. G. Thirolf, Nuclear clocks for testing fundamental physics, Quantum Sci. Technol. 6, 034002 (2021).
- [7] G. Blewitt, GPS and Space-Based Geodetic Methods, 2nd ed., (Elsevier, Oxford, 2015), Vol. 3.
- [8] P. G. Thirolf, B. Seiferle, and L. von der Wense, The 229thorium isomer: Doorway to the road from the atomic clock to the nuclear clock, J. Phys. B: At. Mol. Opt. Phys. 52, 203001 (2019).
- [9] M. Verlinde, S. Kraemer, J. Moens, K. Chrysalidis, J. G. Correia, S. Cottenier, H. De Witte, D. V. Fedorov, V. N. Fedosseev, R. Ferrer, L. M. Fraile, S. Geldhof, C. A. Granados, M. Laatiaoui, T. A. L. Lima, P.-C. Lin, V. Manea, B. A. Marsh, I. Moore, L. M. C. Pereira *et al.*, Alternative approach to populate and study the ²²⁹Th nuclear clock isomer, Phys. Rev. C 100, 024315 (2019).
- [10] K. Beeks, T. Sikorsky, V. Rosecker, M. Pressler, F. Schaden, D. Werban, N. Hosseini, L. Rudischer, F. Schneider, P. Berwian, J. Friedrich, D. Hainz, J. Welch, J. H. Sterba, G. Kazakov, and T. Schumm, Growth and characterization of thorium-doped calcium fluoride single crystals, Sci. Rep. 13, 3897 (2023).

- [11] R. Elwell, C. Schneider, J. Jeet, J. E. S. Terhune, H. W. T. Morgan, A. N. Alexandrova, H. B. Tran Tan, A. Derevianko, and E. R. Hudson, Laser excitation of the ²²⁹Th nuclear isomeric transition in a solid-state host, Phys. Rev. Lett. **133**, 013201 (2024).
- [12] J. Tiedau, M. V. Okhapkin, K. Zhang, J. Thielking, G. Zitzer, E. Peik, F. Schaden, T. Pronebner, I. Morawetz, L. T. De Col, F. Schneider, A. Leitner, M. Pressler, G. A. Kazakov, K. Beeks, T. Sikorsky, and T. Schumm, Laser excitation of the Th-229 nucleus, Phys. Rev. Lett. **132**, 182501 (2024).
- [13] C. Zhang, T. Ooi, J. S. Higgins, J. F. Doyle, L. von der Wense, K. Beeks, A. Leitner, G. A. Kazakov, P. Li, P. G. Thirolf, T. Schumm, and J. Ye, Frequency ratio of the ^{229m}Th nuclear isomeric transition and the ⁸⁷Sr atomic clock, Nature (London) 633, 63 (2024).
- [14] V. F. Strizhov and E. V. Tkalya, Decay channel of low-lying isomer state of the ²²⁹Th nucleus possibilities of experimental investigation, Zh. Eksp. Teor. Fiz. **99**, 697 (1991) [Sov. Phys. JETP **72**, 387 (1991)].
- [15] F. F. Karpeshin and M. B. Trzhaskovskaya, Impact of the electron environment on the lifetime of the ²²⁹Th^m low-lying isomer, Phys. Rev. C 76, 054313 (2007).
- [16] P. Dessovic, P. Mohn, R. A. Jackson, G. Winkler, M. Schreitl, G. Kazakov, and T. Schumm, ²²⁹thorium-doped calcium fluoride for nuclear laser spectroscopy, J. Phys.: Condens. Matter 26, 105402 (2014).
- [17] M. Pimon, J. Gugler, P. Mohn, G. A. Kazakov, N. Mauser, and T. Schumm, Dft calculation of ²²⁹thorium-doped magnesium fluoride for nuclear laser spectroscopy, J. Phys.: Condens. Matter **32**, 255503 (2020).
- [18] R. A. Jackson, J. B. Amaral, M. E. G. Valerio, D. P. DeMille, and E. R. Hudson, Computer modelling of thorium doping in LiCaAlF₆ and LiSrAlF₆: Application to the development of solid state optical frequency devices, J. Phys.: Condens. Matter 21, 325403 (2009).
- [19] E. V. Tkalya, A. N. Zherikhin, and V. I. Zhudov, Decay of the low-energy nuclear isomer 229m Th($3/2^+$, $3.5 \pm 1.0 \text{ eV}$) in solids (dielectrics and metals): A new scheme of experimental research, Phys. Rev. C **61**, 064308 (2000).
- [20] J. K. Ellis, X.-D. Wen, and R. L. Martin, Investigation of thorium salts as candidate materials for direct observation of the ^{229m}Th nuclear transition, Inorg. Chem. **53**, 6769 (2014).
- [21] W. G. Rellergert, D. DeMille, R. R. Greco, M. P. Hehlen, J. R. Torgerson, and E. R. Hudson, Constraining the evolution of the fundamental constants with a solid-state optical frequency reference based on the ²²⁹Th nucleus, Phys. Rev. Lett. **104**, 200802 (2010).
- [22] R. Catherall, W. Andreazza, M. Breitenfeldt, A. Dorsival, G. J. Focker, T. P. Gharsa, G. T. J, J.-L. Grenard, F. Locci, P. Martins, S. Marzari, J. Schipper, A. Shornikov, and T. Stora, The isolde facility, J. Phys. G: Nucl. Part. Phys. 44, 094002 (2017).
- [23] S. Kraemer, Vacuum-ultraviolet Spectroscopy of the Radiative Decay of the Low-energy Isomer in ²²⁹Th, Ph.D. thesis, KU Leuven 2022.
- [24] S. Kraemer, P. Chhetri, S. Bara, A. Claessens, H. De Witte, Y. Elskens, R. Ferrer, Y. Kudryavtsev, S. Sels, P. Van Den Bergh, and P. Van Duppen, A setup for vacuum-ultraviolet spectroscopy of the ²²⁹Th low-energy isomer, Nucl. Instrum. Methods B **542**, 1 (2023).

- [25] H. Bateman, Solution of a system of differential equations occurring in the theory of radio-active transformations, in *Proceedings of the Cambridge Philosophical Society, Mathematica and Physical Sciences* (Smithsonian Institution Libraries, Washington, DC, 1910), pp. 423–427.
- [26] E. Browne and J. K. Tuli, Nuclear data sheets for A = 229, Nucl. Data Sheets **109**, 2657 (2008).
- [27] ISOLDE Decay Station, https://isolde-ids.web.cern.ch/.
- [28] Y. Elskens et al. (unpublished).
- [29] A. K. Jain, R. Raut, and J. K. Tuli, Nuclear data sheets for 229 Th α decay, Nucl. Data Sheets **110**, 1409 (2009).
- [30] K. Gulda, W. Kurcewicz, A. Aas, M. Borge, D. Burke, B. Fogelberg, I. Grant, E. Hagebø, N. Kaffrell, J. Kvasil, G. Løvhøiden, H. Mach, A. Mackova, T. Martinez, G. Nyman, B. Rubio, J. Tain, O. Tengblad, and T. Thorsteinsen, The nuclear structure of ²²⁹Th, Nucl. Phys. A **703**, 45 (2002).
- [31] C. Wang, B. Müller, and K. Hofmann, Epitaxy of atomically flat caf2 films on si (1 1 1) substrates, Thin Solid Films **410**, 72 (2002).
- [32] S. Franchi, Molecular beam epitaxy: Fundamentals, historical background and future prospects, in *Molecular Beam Epitaxy*, edited by M. Henini (Elsevier, Oxford, 2013), pp. 1–46.
- [33] S. Chang, M. Zhao, V. Spampinato, A. Franquet, T.-H. Do, A. Uedono, T. T. Luong, T.-H. Wang, and L. Chang, The influence of aln nucleation layer on radio frequency transmission loss of aln-on-si heterostructure, Phys. Status Solidi (a) 217, 1900755 (2020).
- [34] J. Thomas, G. Stephan, J. C. Lemonnier, M. Nisar, and S. Robin, Optical anisotropy of MgF, in its UV absorption region, Phys. Status Solidi (b) 56, 163 (1973).
- [35] G. W. Rubloff, Far-ultraviolet reflectance spectra and the electronic structure of ionic crystals, Phys. Rev. B 5, 662 (1972).
- [36] N. Shiran, A. Gektin, S. Neicheva, M. Weber, S. Derenzo, M. Kirm, M. True, I. Shpinkov, D. Spassky, K. Shimamura, and N. Ichinose, Energy transfer in pure and Ce-doped LiCaAlF₆ and LiSrAlF₆ crystals, Nucl. Instrum. Methods A 537, 266 (2005).
- [37] Z. A. Weinberg, G. W. Rubloff, and E. Bassous, Transmission, photoconductivity, and the experimental band gap of thermally grown SiO₂ films, Phys. Rev. B 19, 3107 (1979).
- [38] N. M. Ravindra and J. Narayan, Optical properties of amorphous silicon and silicon dioxide, J. Appl. Phys. 60, 1139 (1986).
- [39] J. Edgar, Z. Yu, A. Ahmed, and A. Rys, Low temperature metalorganic chemical vapor deposition of aluminum nitride with nitrogen trifluoride as the nitrogen source, Thin Solid Films 189, L11 (1990).
- [40] D. Klimm, G. Lacayo, and P. Reiche, Growth of Cr : LiCaAlF₆ and Cr : LiSrAlF₆ by the czochralski method, J. Cryst. Growth 210, 683 (2000).
- [41] J. F. Ziegler, M. Ziegler, and J. Biersack, SRIM—The stopping and range of ions in matter (2010), Nucl. Instrum. Methods B 268, 1818 (2010).
- [42] J. Morris, B. J. Cowen, S. Teysseyre, and A. A. Hecht, Molecular dynamics investigation of threshold displacement energies in CaF₂, Comput. Mater. Sci. **172**, 109293 (2020).
- [43] E. Vella, R. Boscaino, and G. Navarra, Vacuum-ultraviolet absorption of amorphous SiO₂: Intrinsic contribution and role of silanol groups, Phys. Rev. B 77, 165203 (2008).

- [44] G. Kresse and J. Furthmuller, Efficient iterative schemes for *ab initio* total-energy calculations using a plane-wave basis set, Phys. Rev. B 54, 11169 (1996).
- [45] P. E. Blochl, Projector augmented wave method, Phys. Rev. B 50, 17953 (1994).
- [46] J. P. Perdew, K. Burke, and M. Ernzerhof, Generalized gradient approximation made simple, Phys. Rev. Lett. 77, 3865 (1996).
- [47] A. D. Becke and E. R. Johnson, A simple effective potential for exchange, J. Chem. Phys. 124, 221101 (2006).
- [48] F. Tran and P. Blaha, Accurate band gaps of semiconductors and insulators with a semilocal exchange-correlation potential, Phys. Rev. Lett. 102, 226401 (2009).
- [49] K. Momma and F. Izumi, VESTA: a three-dimensional visualization system for electronic and structural analysis, J. Appl. Crystallogr. 41, 653 (2008).

- [50] D. K. Swanson and R. C. Peterson, Polyhedral volume calculations, Can. Mineral. 18, 153 (1980).
- [51] V. Kaufman and J. F. Ward, Newly measured and calculated wavelengths in the vacuum ultraviolet spectrum of neutral nitrogen, Appl. Opt. 6, 43 (1967).
- [52] C. Goldbach and G. Nollez, Oscillator strength measurements in the vacuum-ultraviolet, Astron. Atrophys. **201**, 189 (1988).
- [53] C. Moore, Selected Tables of Atomic Spectra, Atomic Energy Levels and Multiplet Tables—NI, NII, NIII (National Bureau of Standards, US, 1975).
- [54] NIST, Nist atomic spectra database.
- [55] T. Hiraki, K. Okai, M. Bartokos, and K. Beeks, Controlling ²²⁹Th isomeric state population in a vuv transparent crystal, Nat. Commun. 15, 5536 (2024).