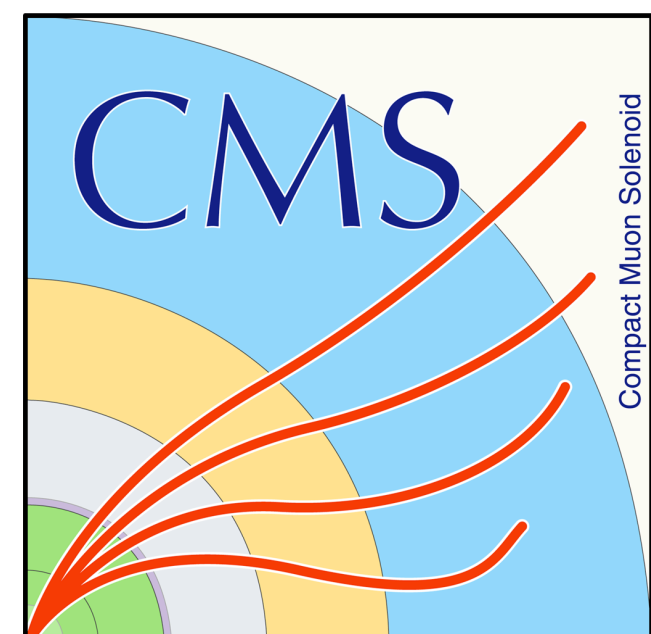


# QCD at High Energies

ICFA2023, Hamburg, 28. 11. 2023

Oldrich Kepka  
Institute of Physics, Prague

On behalf of ATLAS and CMS Collaborations

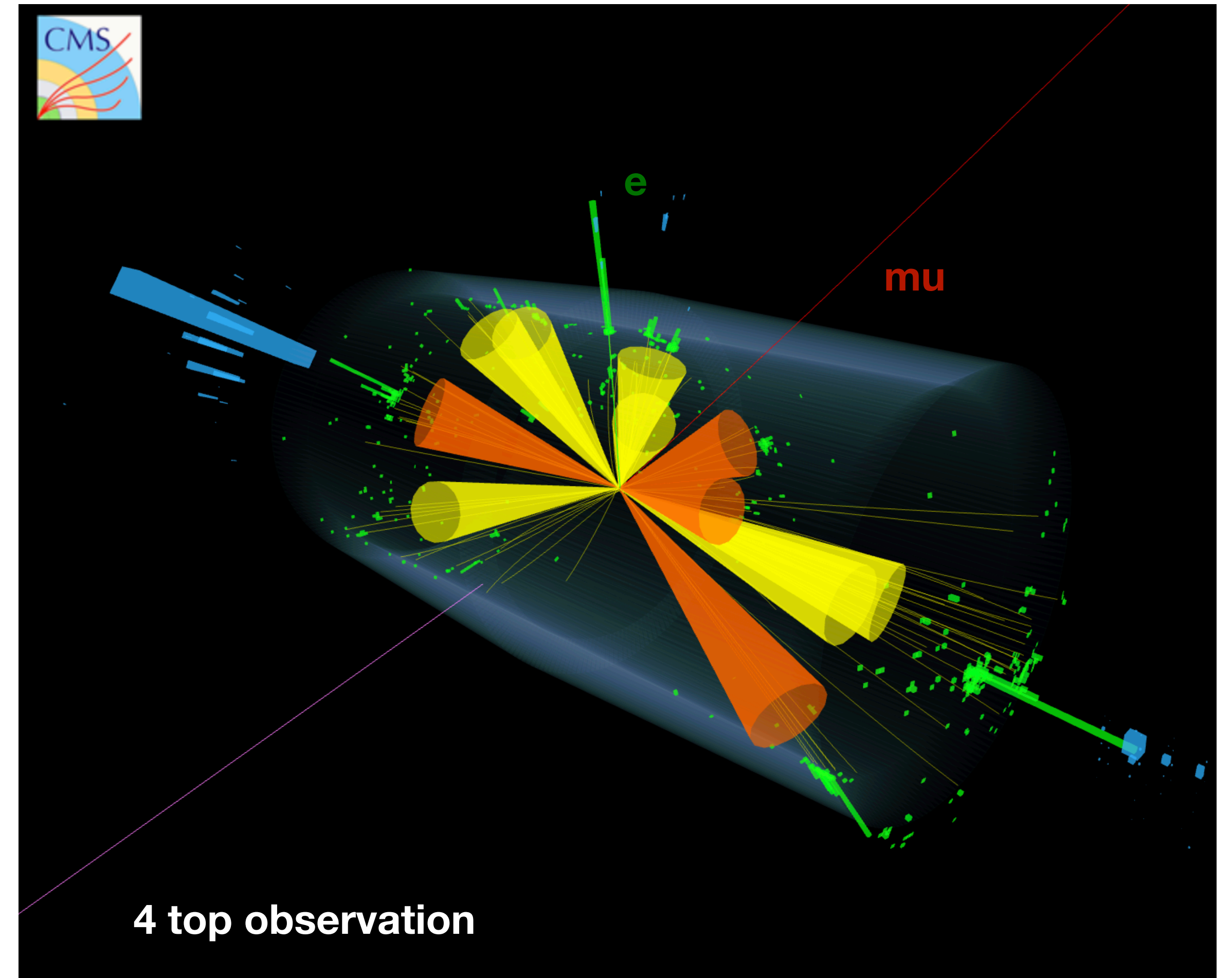


# Quantum Chromodynamics at LHC

- All LHC observations rely on the modeling of QCD production, jets are ubiquitous at LHC

## Objectives of QCD exploration

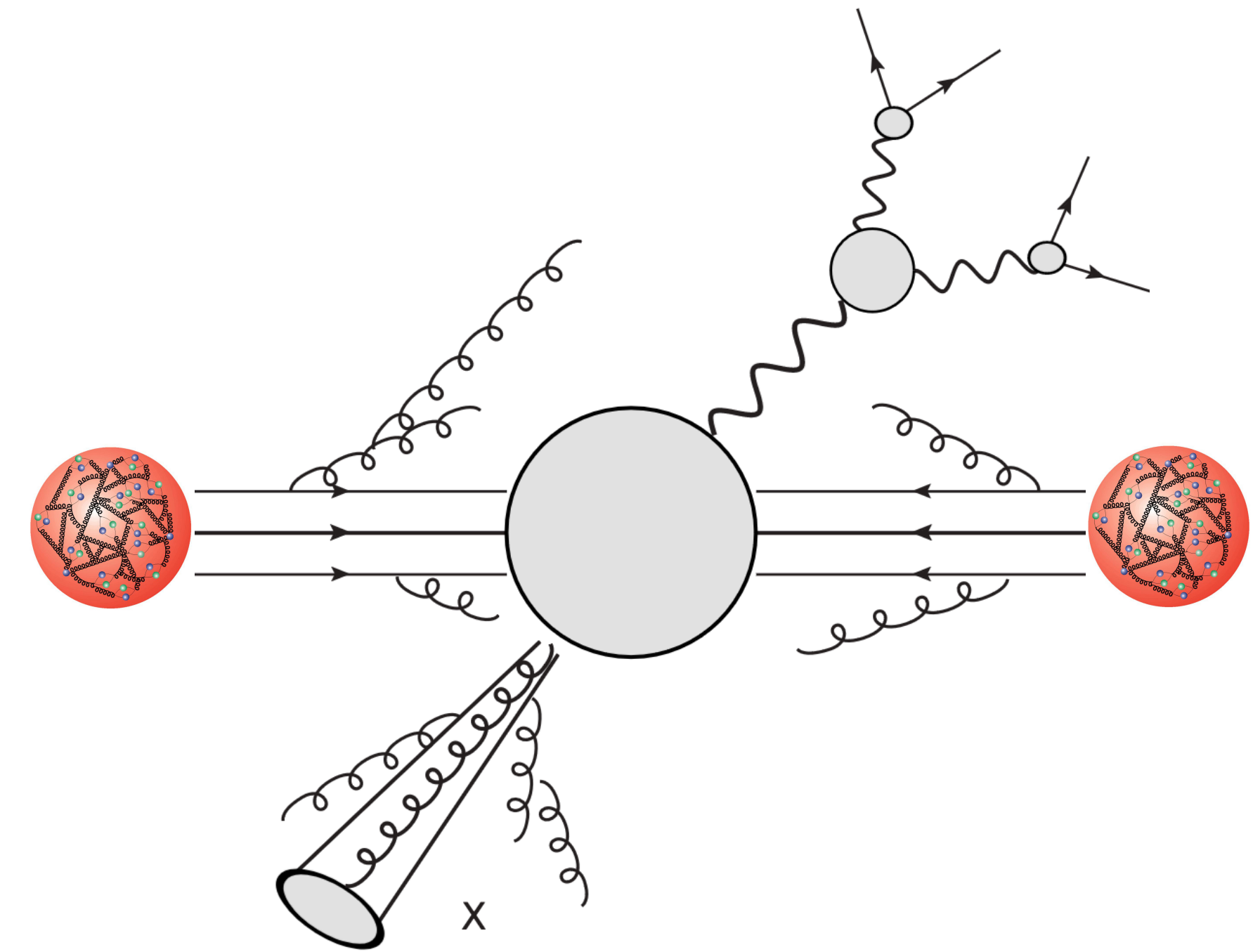
- More precise understanding of fundamental parameters of QCD
- Valuable inputs for theory development to describe the complexity of hadronic final state
- Improve future physics searches - isolate and measure SM processes which are backgrounds



ATLAS and CMS briefings

# QCD in proton-proton collision

- **At short distances:** QCD is a theory of free partons scattering off each other
  - High-order perturbative calculation in  $\alpha_s$
  - Parton showers
  - Resummation of logarithmic corrections due to soft/collinear emissions
  - QCD dynamics of heavy quarks
- **At large distances:** strongly bound hadronic resonances, QCD confinement
  - PDF, Fragmentation functions (evolution still perturbative)
  - non-perturbative effects (color-reconnection, underlying event, multiparton interactions)



Collider experiments continue to produce extraordinary results with innovative techniques

**Interpretations of LHC data need precise theory with higher-order QCD and EW calculations**



# Outline

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- **At short distances:** QCD is a theory of free partons scattering off each other

## High-order pQCD

- High-order perturbative calculations
- Parton showers
- Resummation of logarithmic corrections due to soft/collinear emissions
- QCD dynamics of heavy quarks

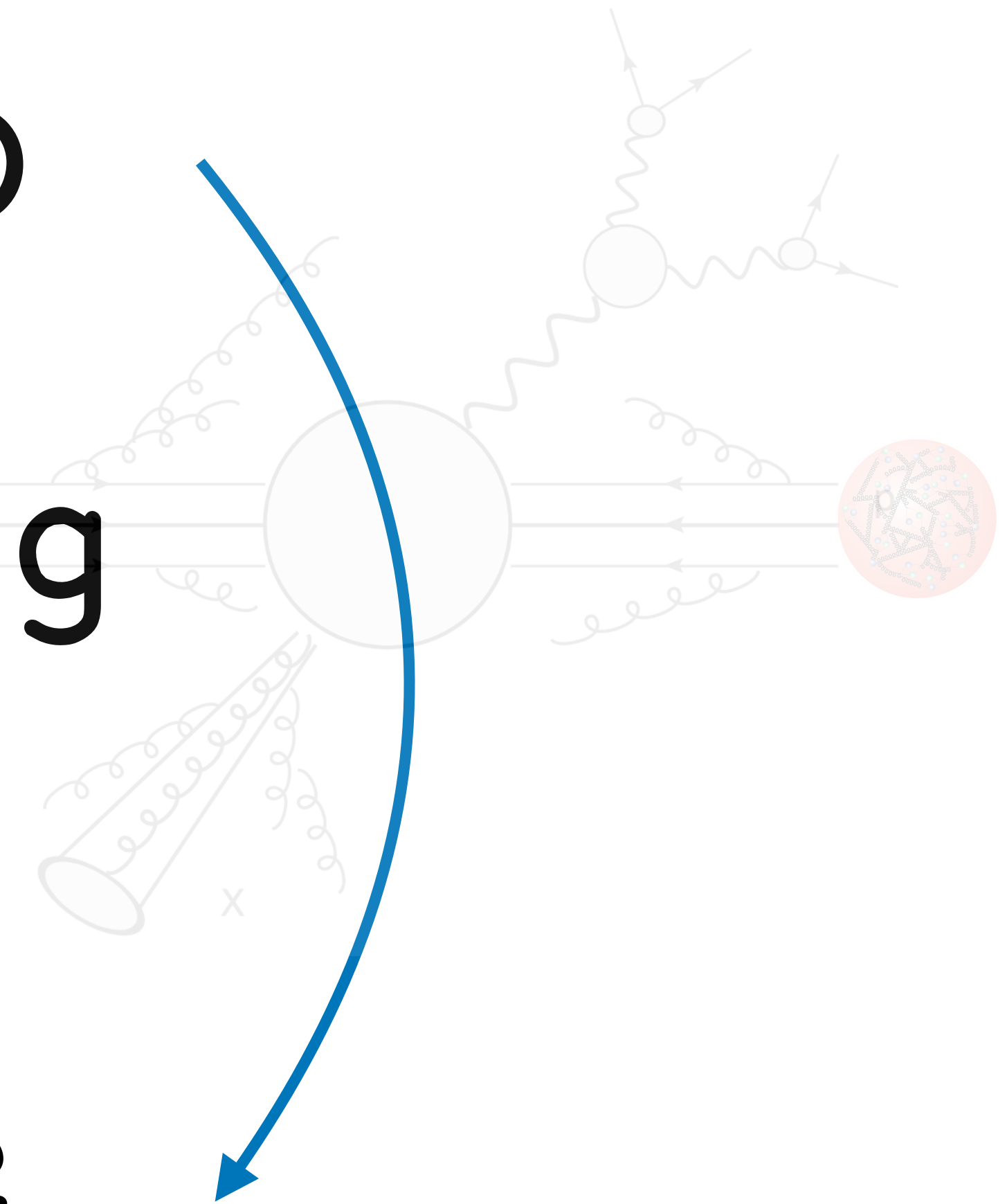
## $\alpha_s$ strong coupling

- **At large distances:** strongly bound hadronic resonances, QCD confinement

## PDF

- PDF, Fragmentation functions (evolution still perturbative)
- non-perturbative effects (color-reconnection, underlying event, multiparton interactions)

## Jet substructure



Collider experiments continue to produce extraordinary results with innovative techniques  
Interpretations of LHC data need precise theory with higher-order QCD and EW calculations



# High-order pQCD

# Accuracy of QCD calculations

- **Fixed order calculations**

- NNLO has become standard
- Reduction of scale uncertainties from 10-20% (NLO) to  $O(\%)$  at NNLO
- Computational costs often limiting factor

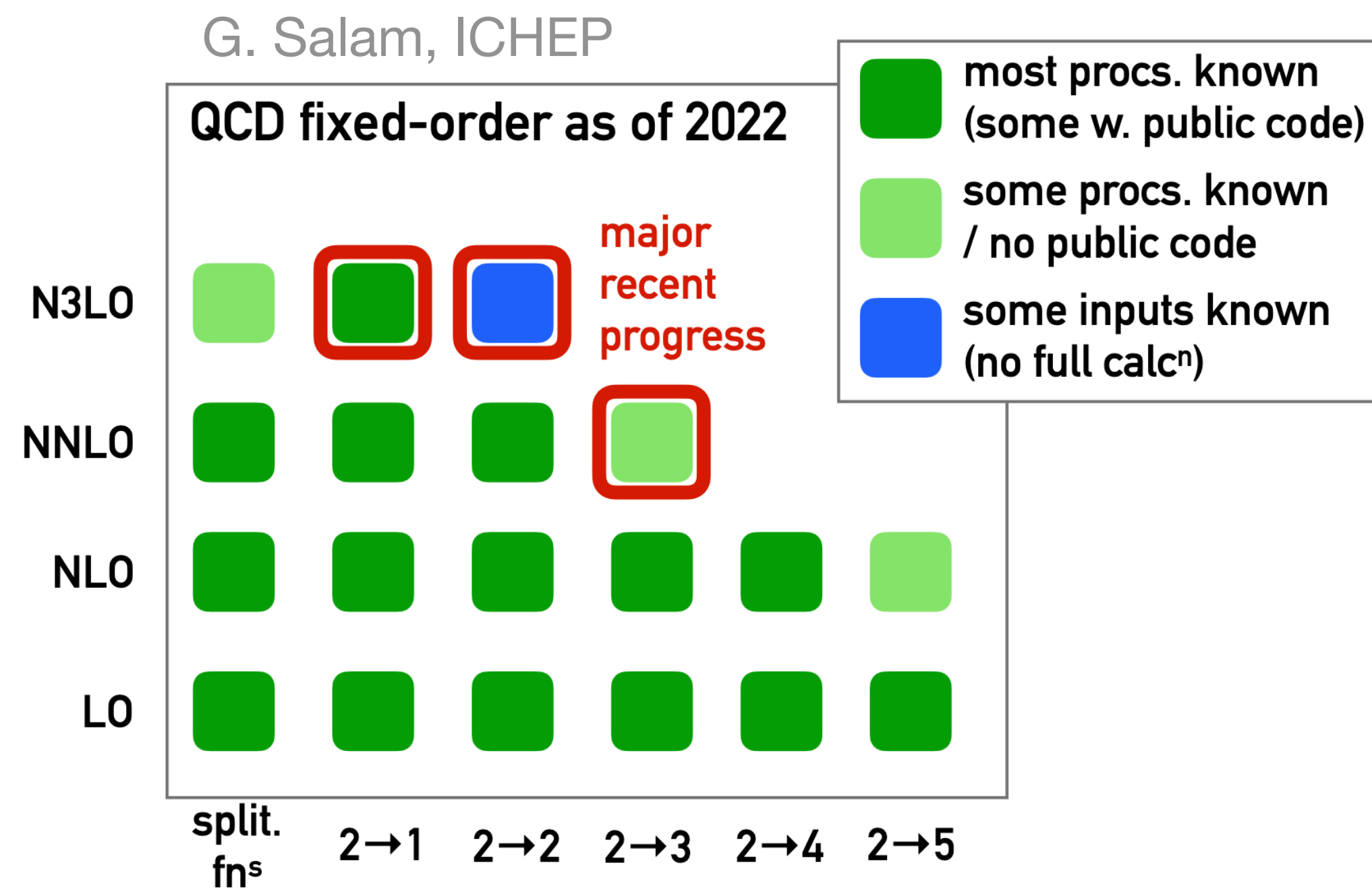
- **MC with Parton Shower Simulations** (Pythia, Herwig, Sherpa)

- **Matching** NLO ME to PS automated, matching to NNLO to PS is state-of-the art
- **Merging** of exclusive 2  $\rightarrow$  n-jet productions at NLO or LO improves modeling of events with large number of jets

- Active development of **more accurate parton showers** (NLL)

- The first shower algorithm introduced in  $\sim$ 1980
- At the threshold of major breakthrough

- **Parton shower uncertainties are dominant in many LHC measurements involving jets, in particular with the top**

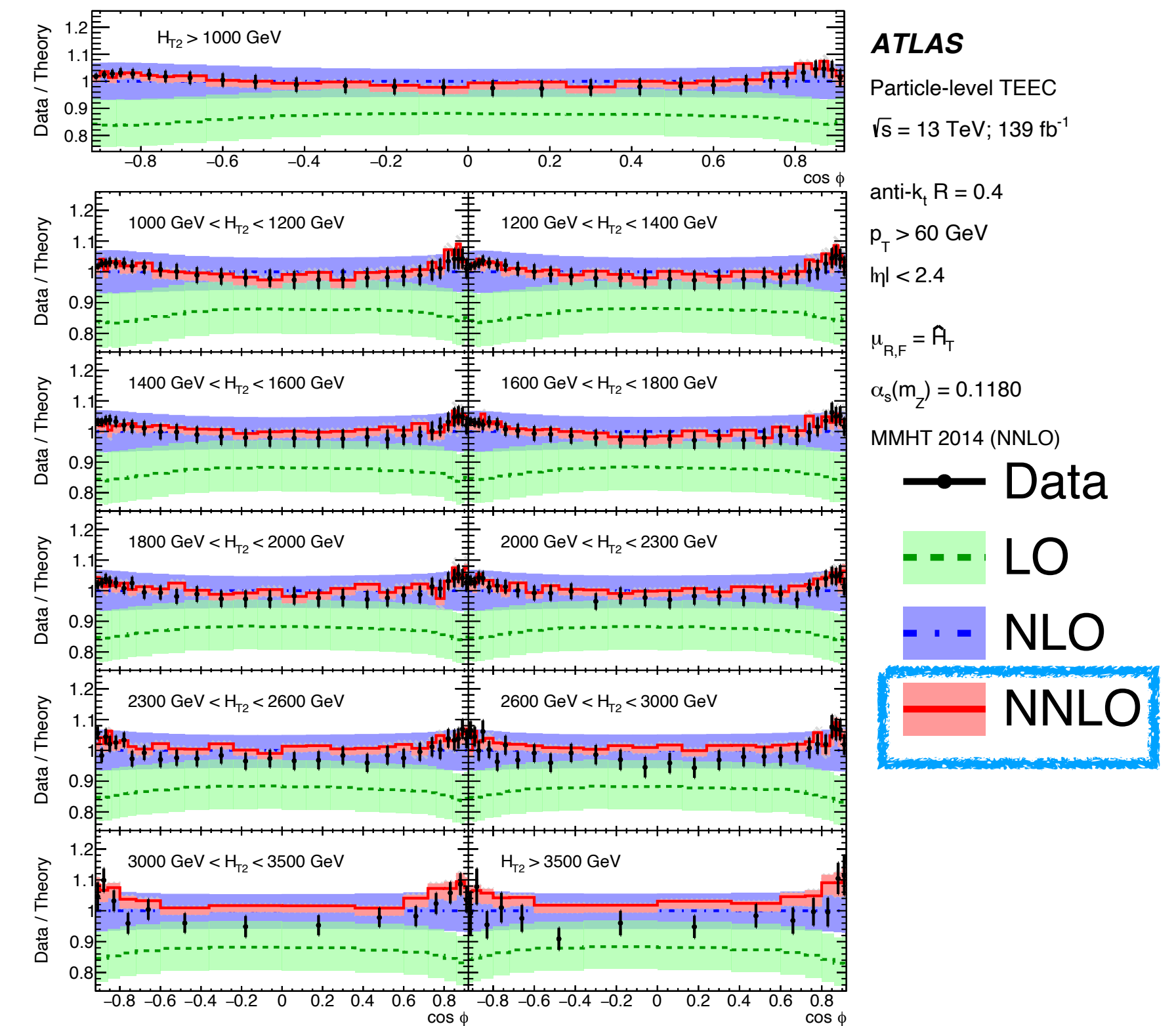
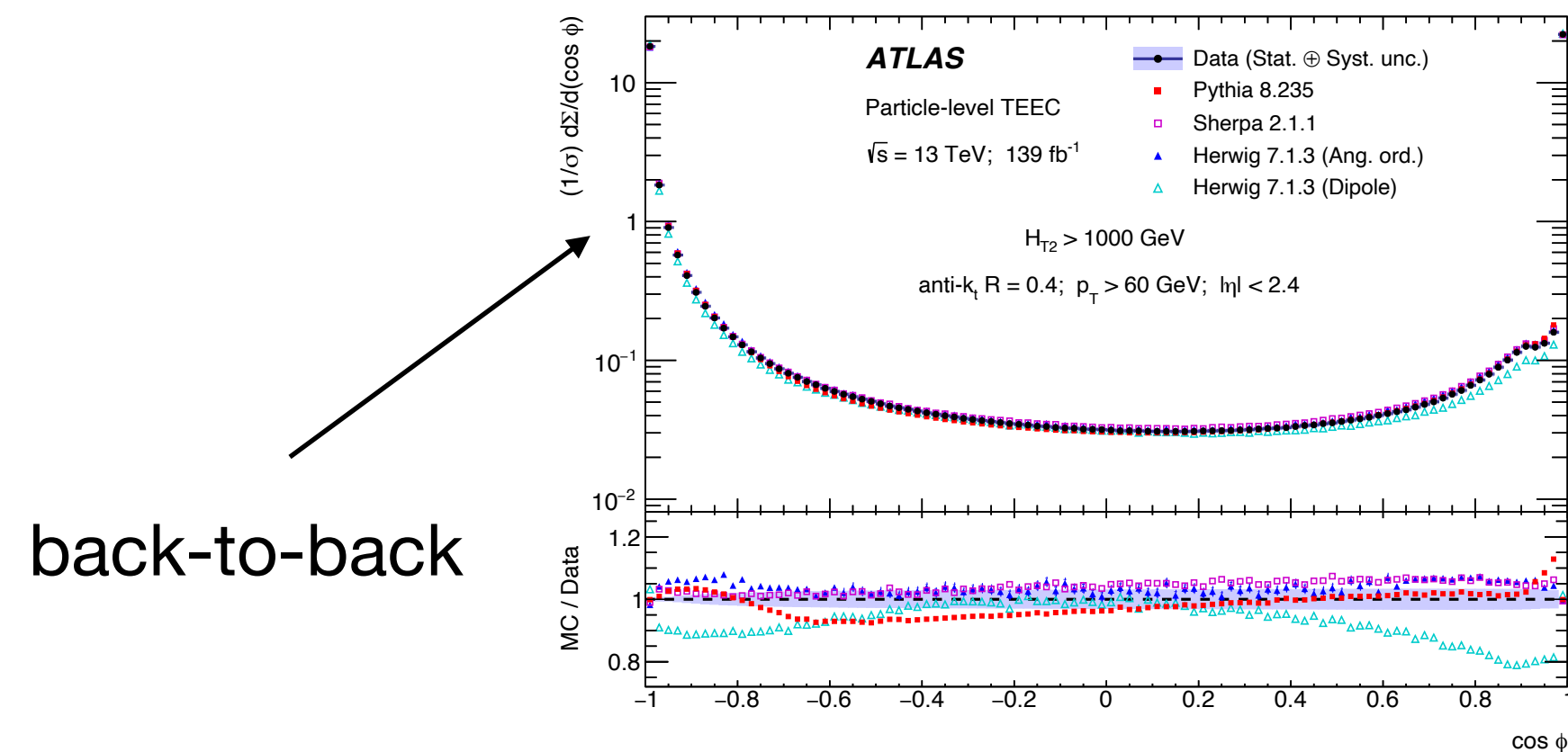
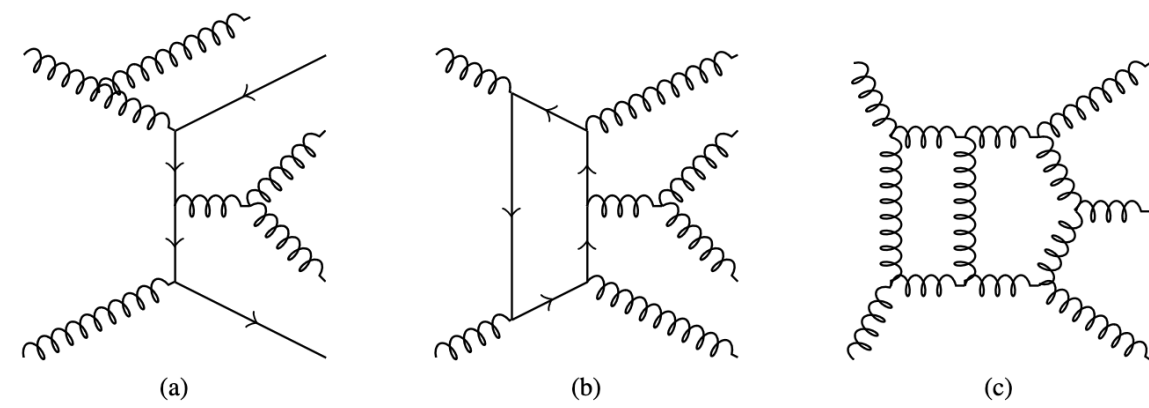


# Correlation in multijet events

- Multi-jet event shape observables, large sensitivity to QCD radiation and  $\alpha_s$  (see later)
- **TEEC** - energy-weighted distribution of azimuthal difference between jet pairs

$$\frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} \equiv \frac{1}{\sigma} \sum_{ij} \int \frac{d\sigma}{dx_{Ti} dx_{Tj} d \cos \phi} x_{Ti} x_{Tj} dx_{Ti} dx_{Tj} = \frac{1}{N} \sum_{A=1}^N \sum_{ij} \frac{E_{Ti}^A E_{Tj}^A}{\left(\sum_k E_{Tk}^A\right)^2} \delta(\cos \phi - \cos \varphi_{ij})$$

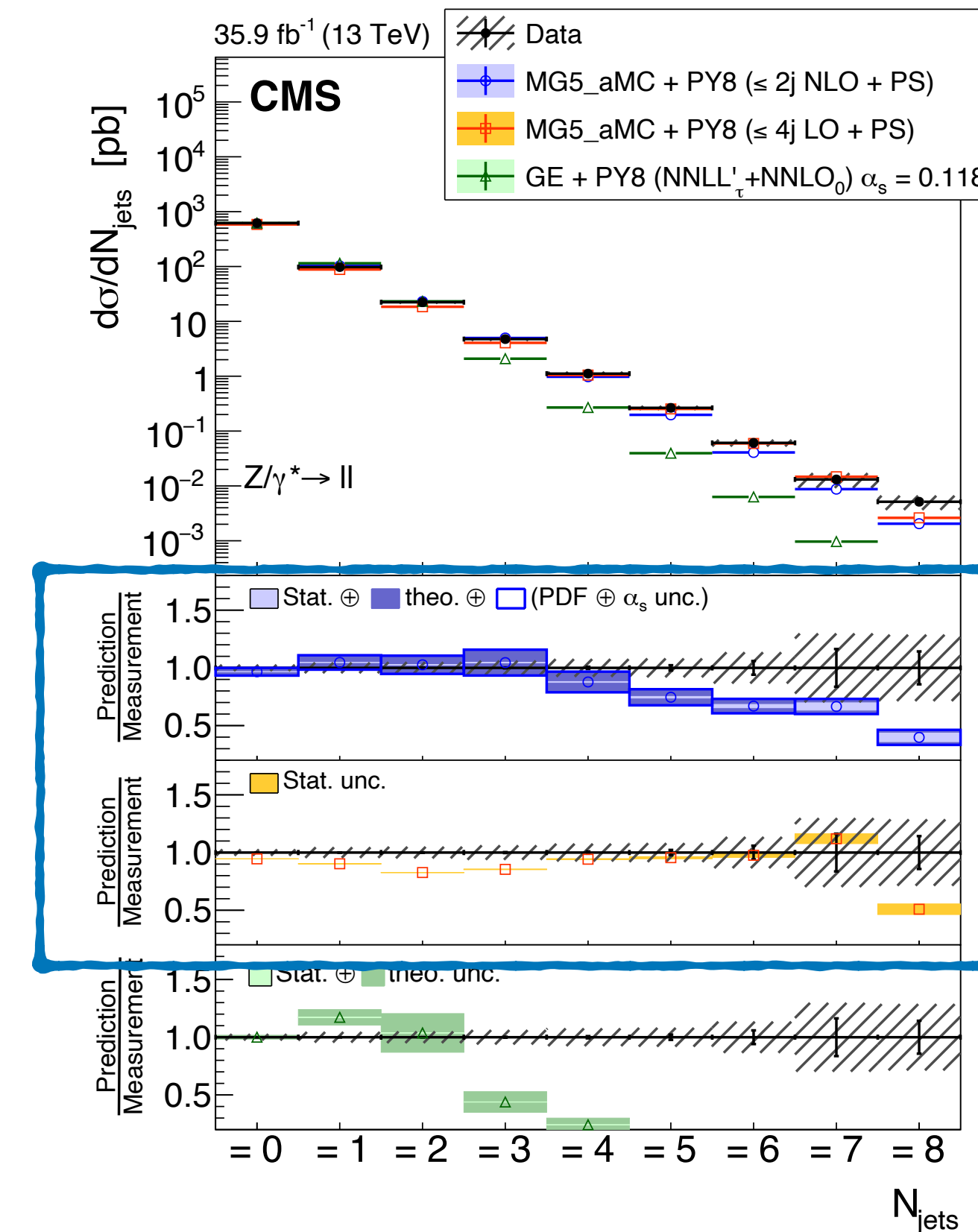
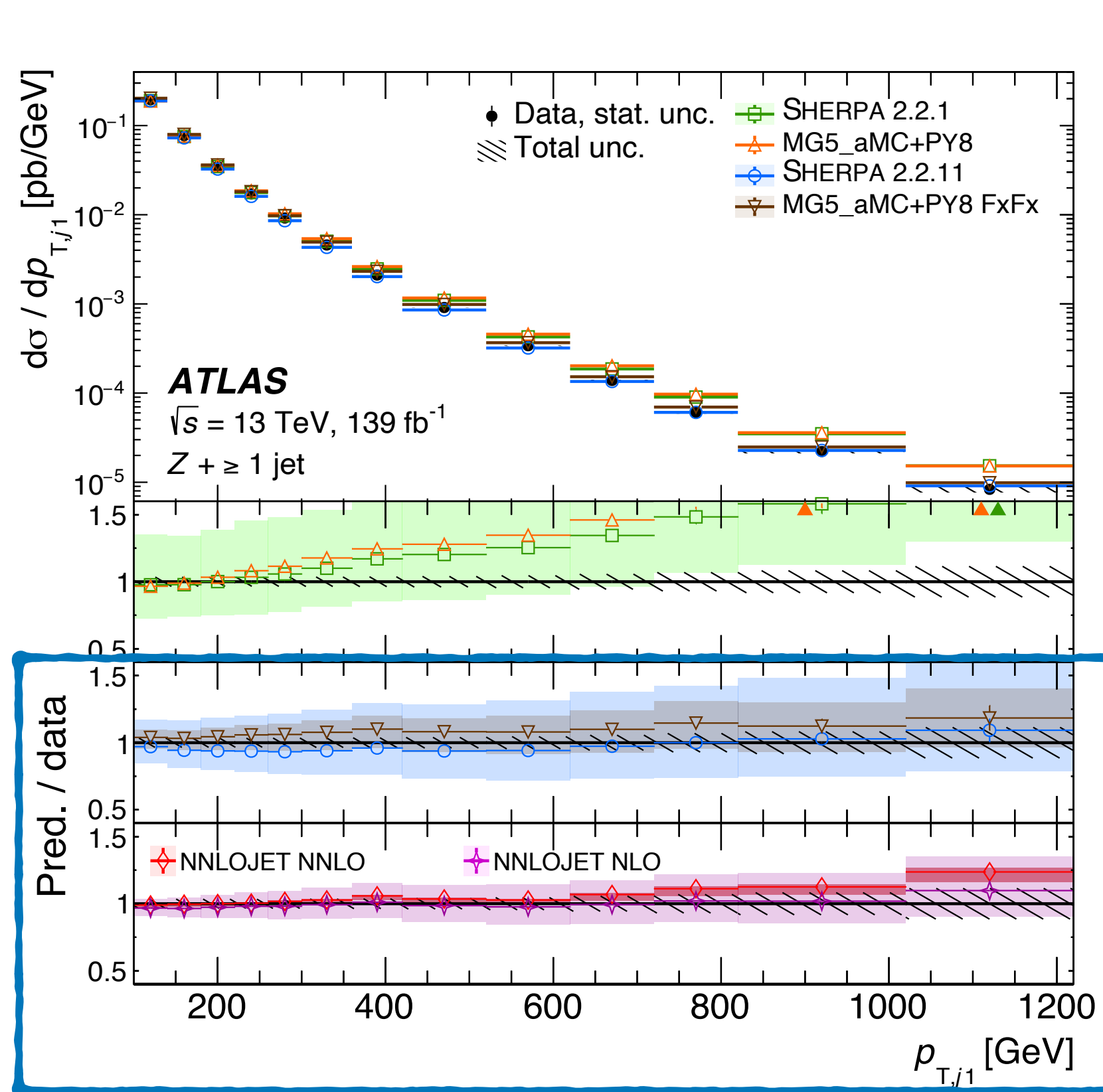
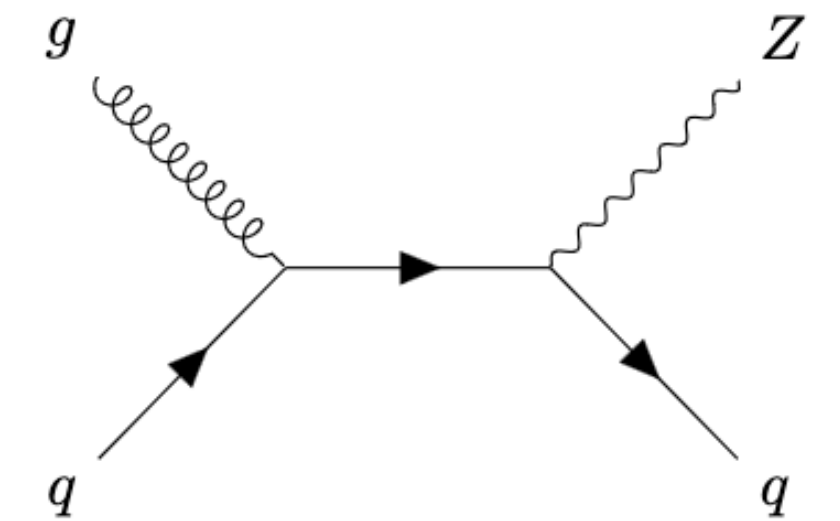
- Definition reduces exp. and theo. uncertainties
- **Requires 2 → 3 jet at NNLO** state-of-the-art calculation



Excellent description with higher order QCD, substantial reduction of scale theory uncertainties with NNLO

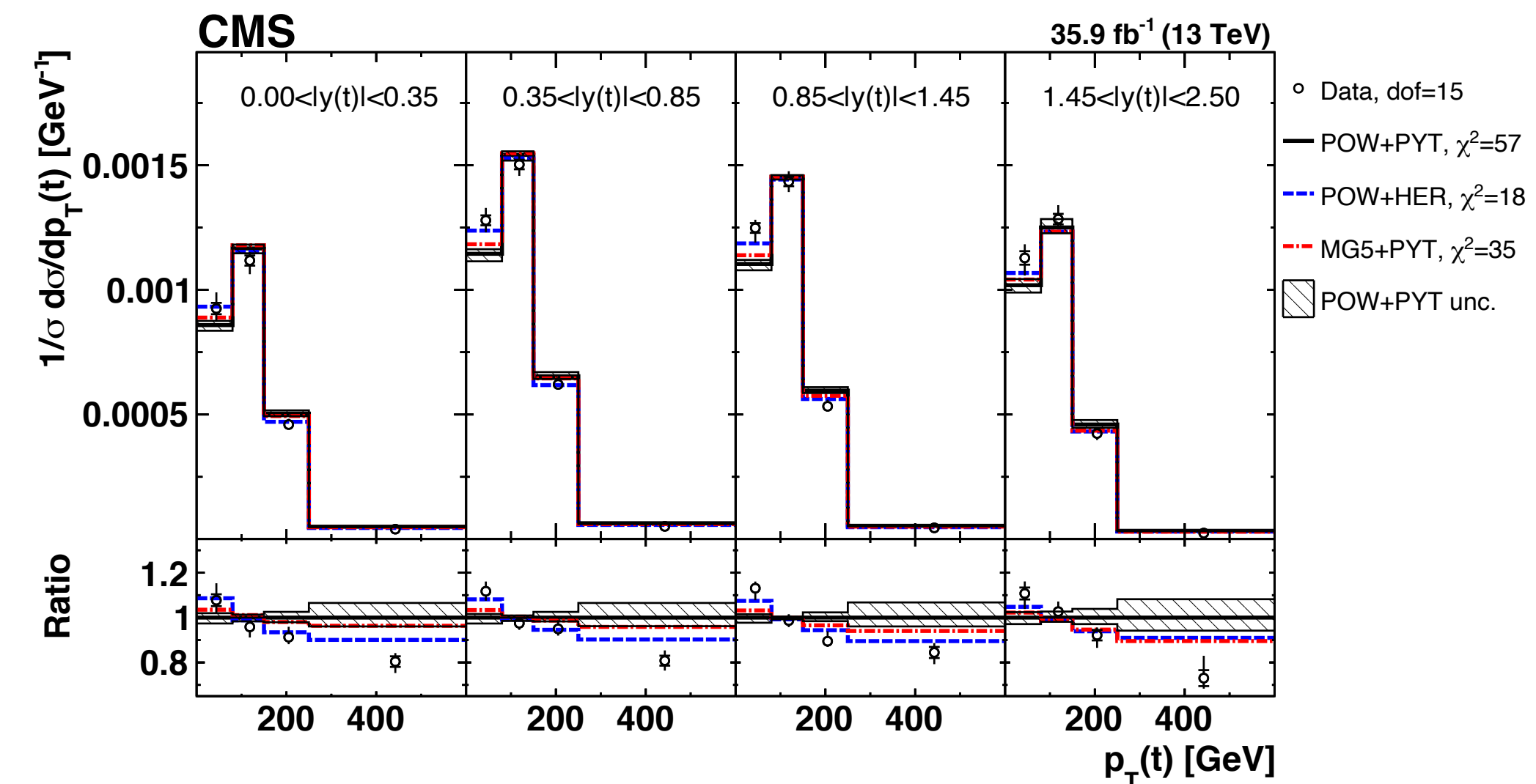
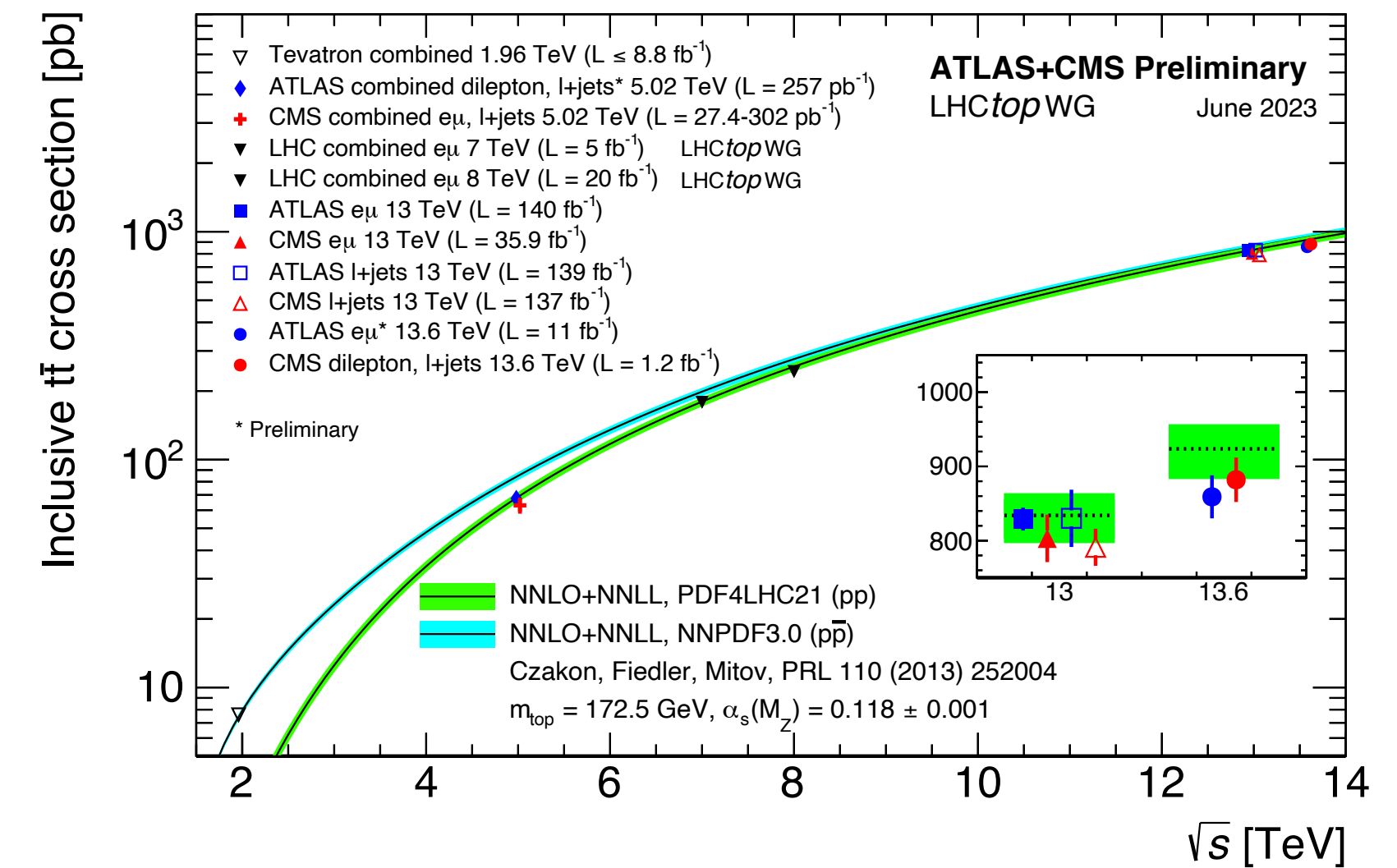


- High-precision measurements over wide range: up to 8 jets and jets beyond 1 TeV
- Testing ground for higher-order QCD predictions
  - Advanced multi-jet merged calculations (Madgraph FxFx and Sherpa) describe data well
  - Best description by fixed order NNLO calculations



- Inclusive top-pair production
  - Impressive agreement over 2 orders of magnitude
  - At 13 TeV, exp. unc. of 1.8% (ATLAS  $e\mu$ +b-jets), compare with ~4% with PDF4LHC21
- Differential measurements
  - Issues with modelling of  $t$  and  $t\bar{t}$   $p_T$  distributions
  - Ad-hoc 2-point systematic comparisons
- **Full exploitation of present and future top samples needs improved MC**
  - Yields (ll, l+jet):  $O(10M)$  in Run2  $\rightarrow O(100M)$  at HL-LHC

Future: move to NNLO+PS simulation and improve shower uncertainty prescriptions



$\alpha_s$  strong coupling

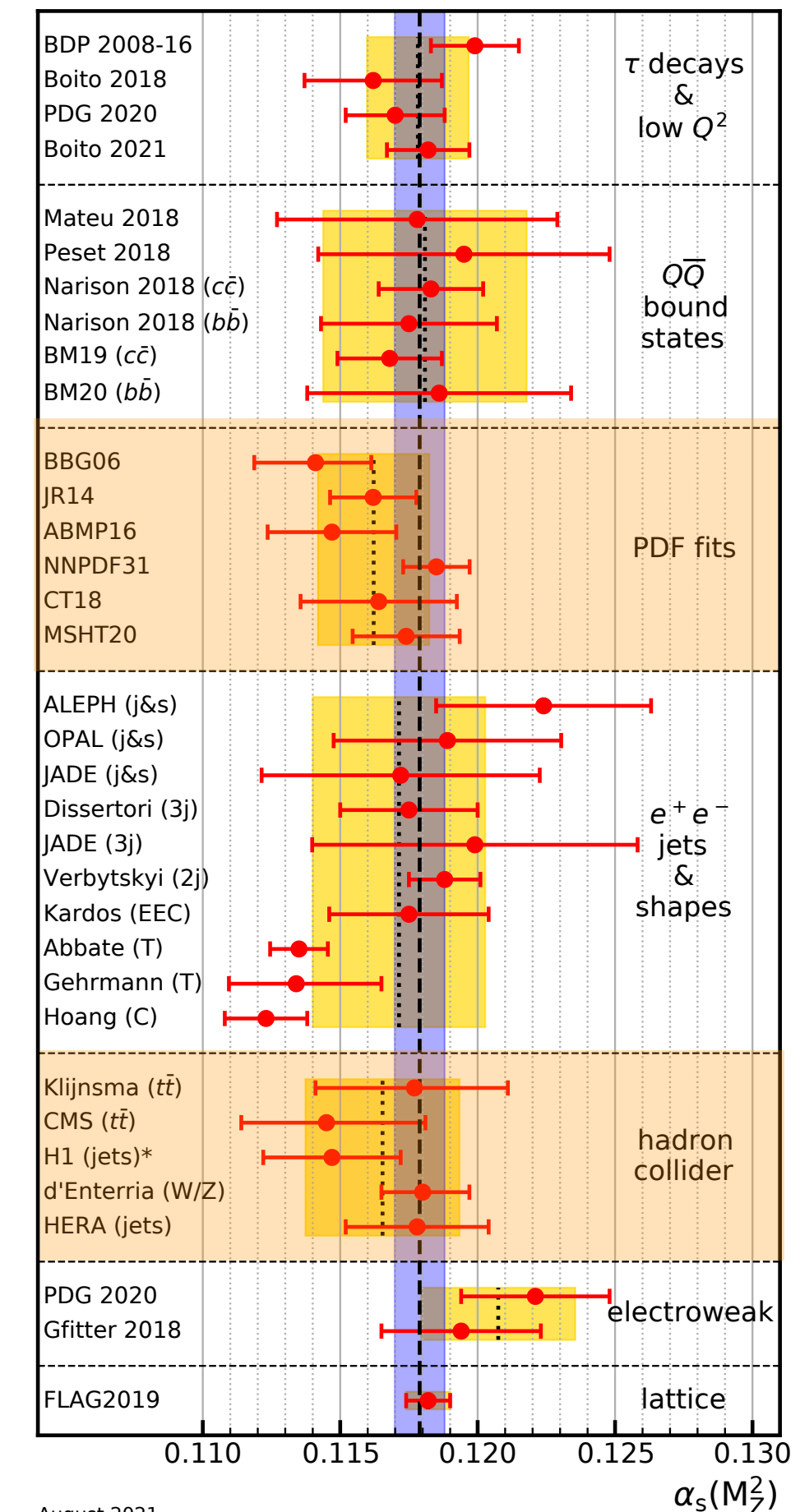
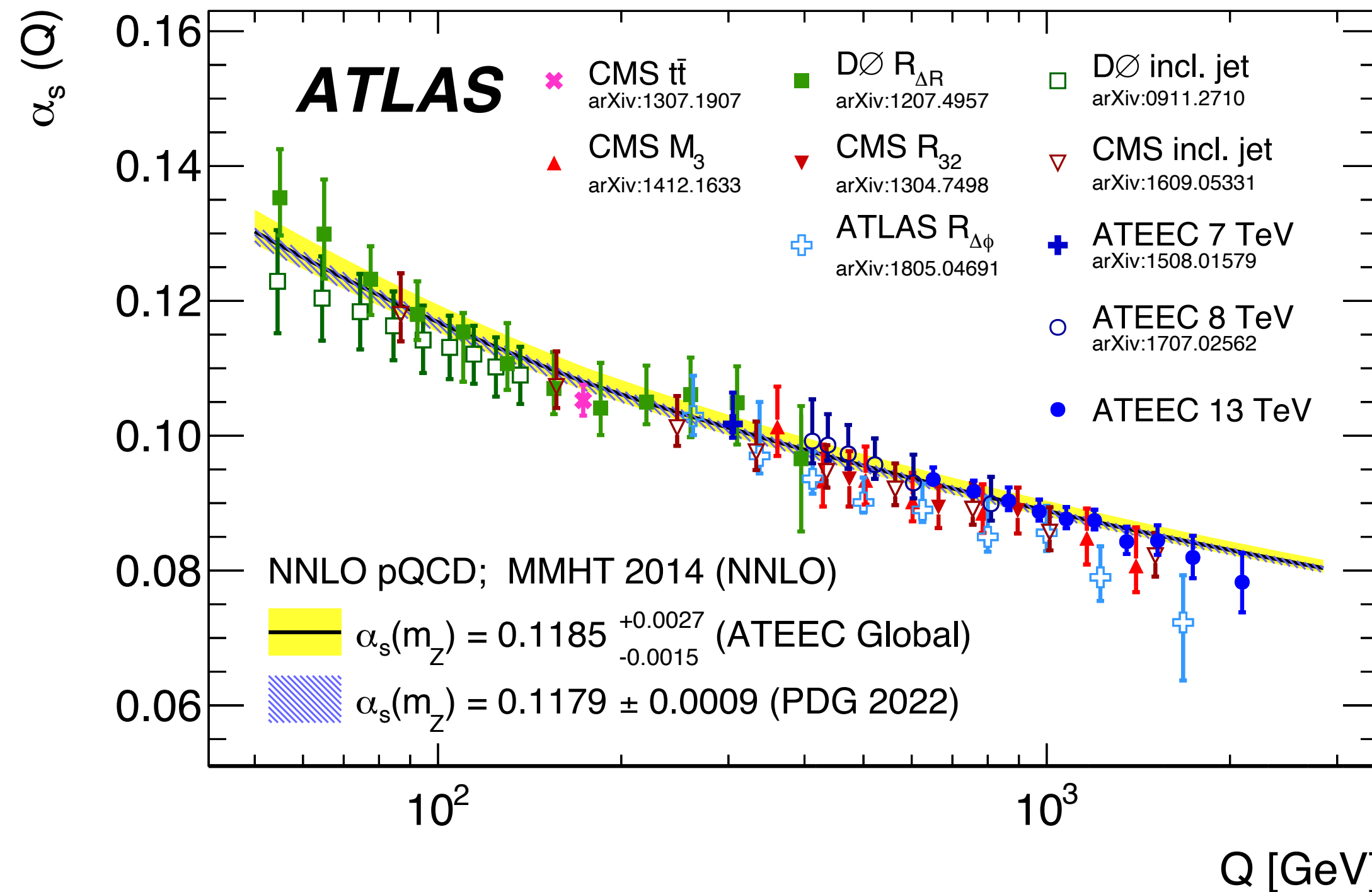


# The strong-coupling strength

- **Least known** fundamental forces of nature
  - Large uncertainty in many LHC measurements, e.g. Higgs couplings
- Single free parameter in massless QCD limit
- **Asymptotic freedom** - decreasing with scale of the process  $\sim \ln Q^2/\Lambda^2$ , tested up to multi-TeV scale

$$\delta\alpha \sim 10^{-10} \ll \delta G_F \ll 10^{-7} \ll \delta G \sim 10^{-5} \ll \delta\alpha_s \sim 10^{-2}$$

World PDG average over 7 categories  
 $\alpha_s(Q^2 = m_Z^2) = 0.1179 \pm 0.0009$



# State-of-the-art for the strong coupling

CMS-PAS-SMP-21-008  
JHEP 12 (2022) 035 (CMS)

- Most precise results from tau decays and Lattice

S. Camarda, QCD@LHC23

Category	$\alpha_s(m_Z)$	$\delta\alpha_s(m_Z)$	Rel. Unc.	Results
Tau decays and low $Q^2$	0.1178	0.0019	1.6%	4
$Q\bar{Q}$ bound states	0.1181	0.0037	3.1%	4
DIS and PDF fits	0.1162	0.0020	1.7%	6
e+e- jets and shapes	0.1171	0.0031	2.6%	10
Hadron colliders	0.1165	0.0028	2.4%	5
Electroweak boson decays	0.1208	0.0028	2.4%	2
Lattice QCD (FLAG 21)	0.1184	0.0008	0.7%	11
PDG 22 World Average	0.1179	0.0009	0.8%	39

	$\alpha_s(m_Z)$	$\delta\alpha_s(m_Z)$	Rel. Unc.
ATLAS ATEEC	0.1185	0.0021	1.7%
CMS inclusive jets	0.1166	0.0016	1.4%
CMS dijets	0.1201	0.0020	1.7%
ATLAS Z pT	0.1183	0.0009	0.7%

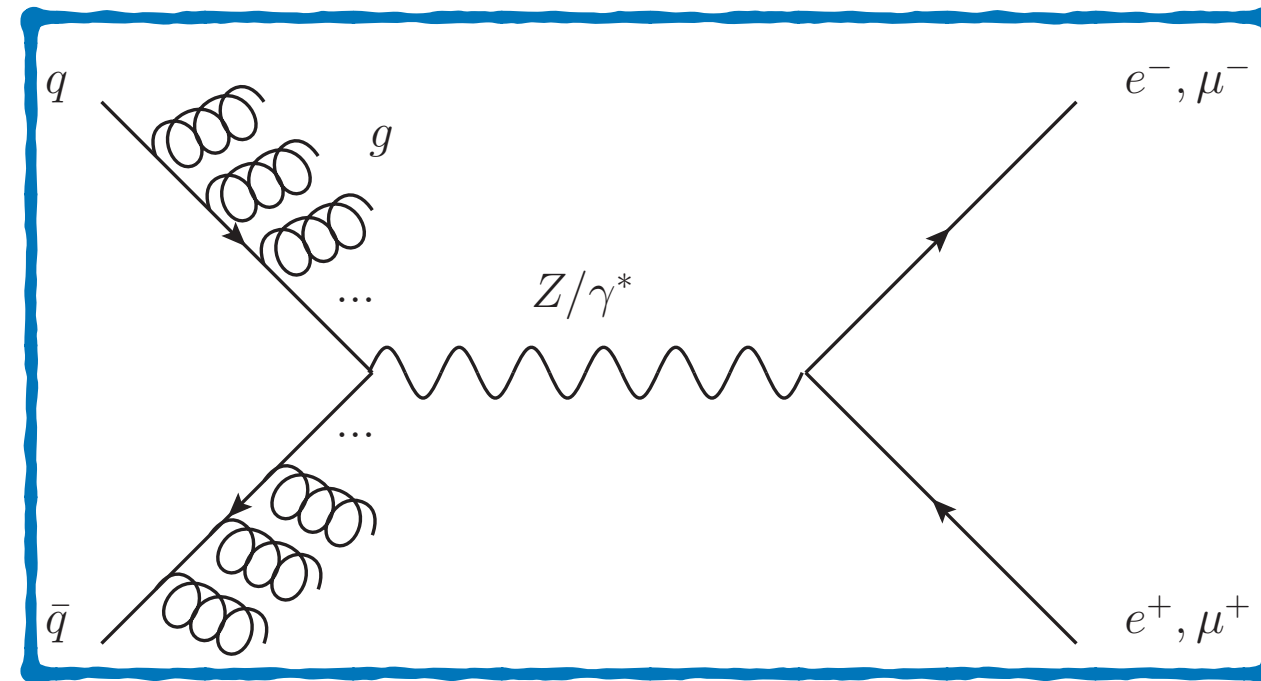


- Several recent determinations from LHC at 13 and 8 TeV using NNLO reached percent level accuracy and **will have impact on the PDG world average**
- NNLO Theory scale uncertainty is the dominant source for jet based measurements, N<sup>3</sup>LO for jets not within reach

# Strong coupling from Z p<sub>T</sub> distribution

2309.12986 (ATLAS)

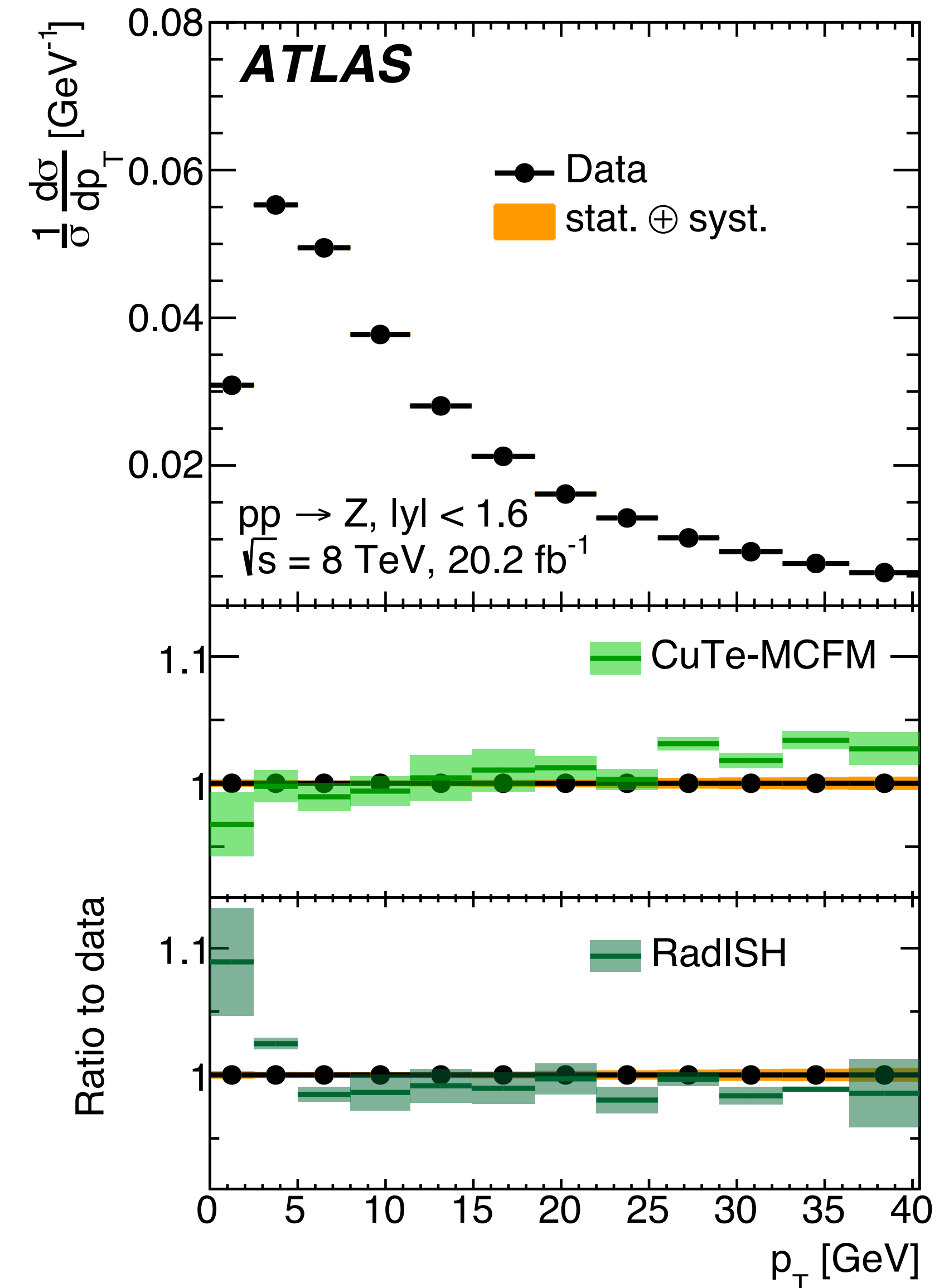
- A novel approach - extraction using low transverse momentum of Z, Z boson recoiling against QCD initial-state radiation



- Radiation inhibited observable requires resummation
  - Excellent agreement between data and predictions
  - Impressive progress in understanding of boson p<sub>T</sub> modelling from theory and experiment => **also impact on m<sub>w</sub> determination**
- Coupling extracted using state-of-the-art theory  
(aN<sup>4</sup>LL resummation matched to N<sup>3</sup>LO fixed order calculation, approximate N<sup>3</sup>LO MSHT20 PDF)

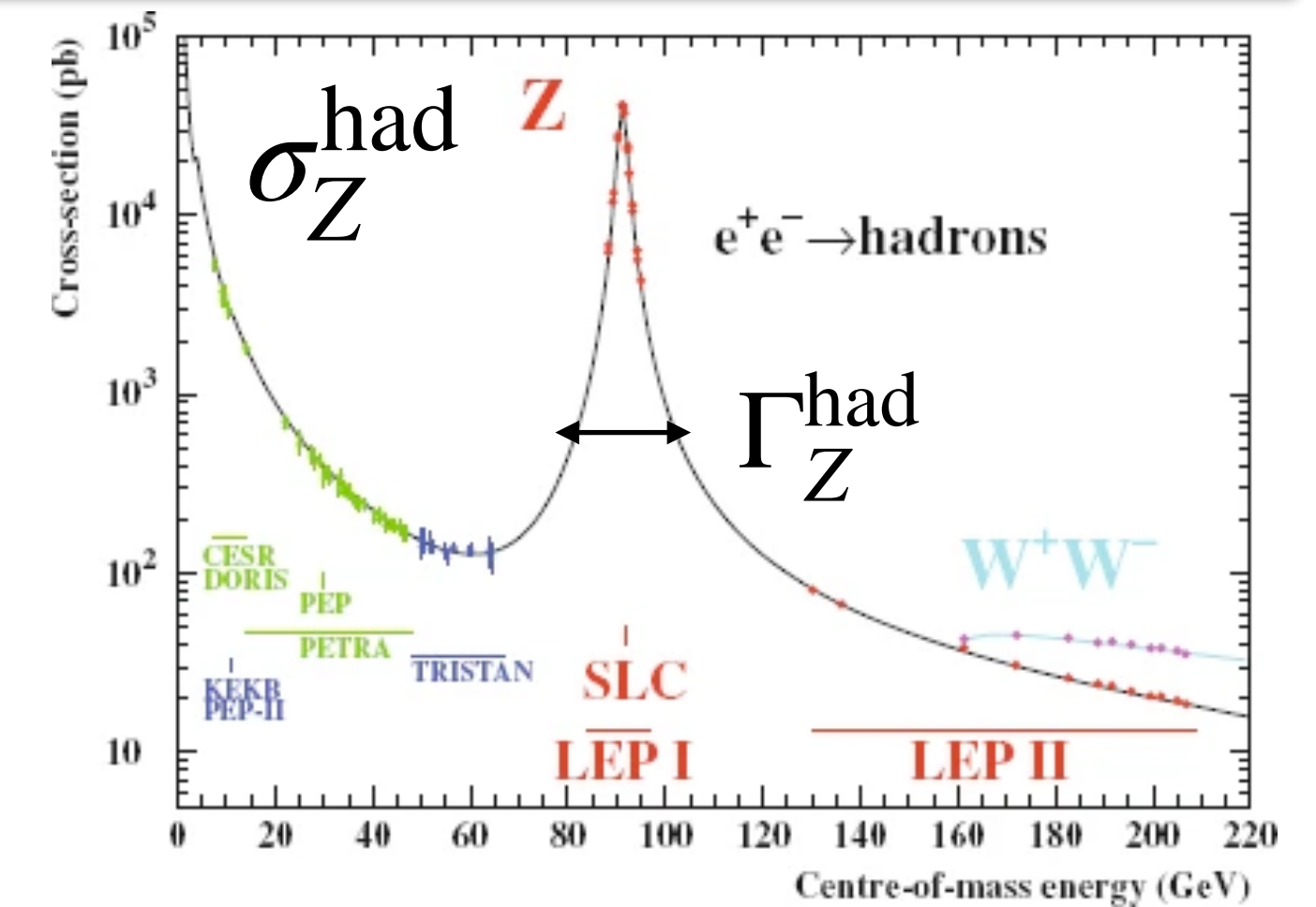
$$\alpha_s(m_Z) = 0.1183 \pm 0.0009 \text{ (0.74\%)}$$

**Most precise experimental measurement of the strong coupling**





- **Hadronic W and Z decays**  $\Delta\alpha_s/\alpha_s = 0.1 - 0.2\%$ 
  - Combined fit of Z pseudo observables ( $R_Z = \Gamma_Z^{\text{had}}/\Gamma_Z^{\text{lep}}$ ,  $\Gamma_Z^{\text{tot}}$ ,  $\sigma_Z^{\text{had}}$ ) precisely measured using energy scan, Tera-Z FCC-ee(90)
  - Similar for WW, increase over LEP ( $10^4 \rightarrow 10^8$ ), can be competitive (Improved  $\alpha_{\text{QED}}(m_Z)$ ,  $|V_{cs}|$ ,  $|V_{cd}|$ ,  $m_W$ , assume N<sup>4</sup>LO QCD)

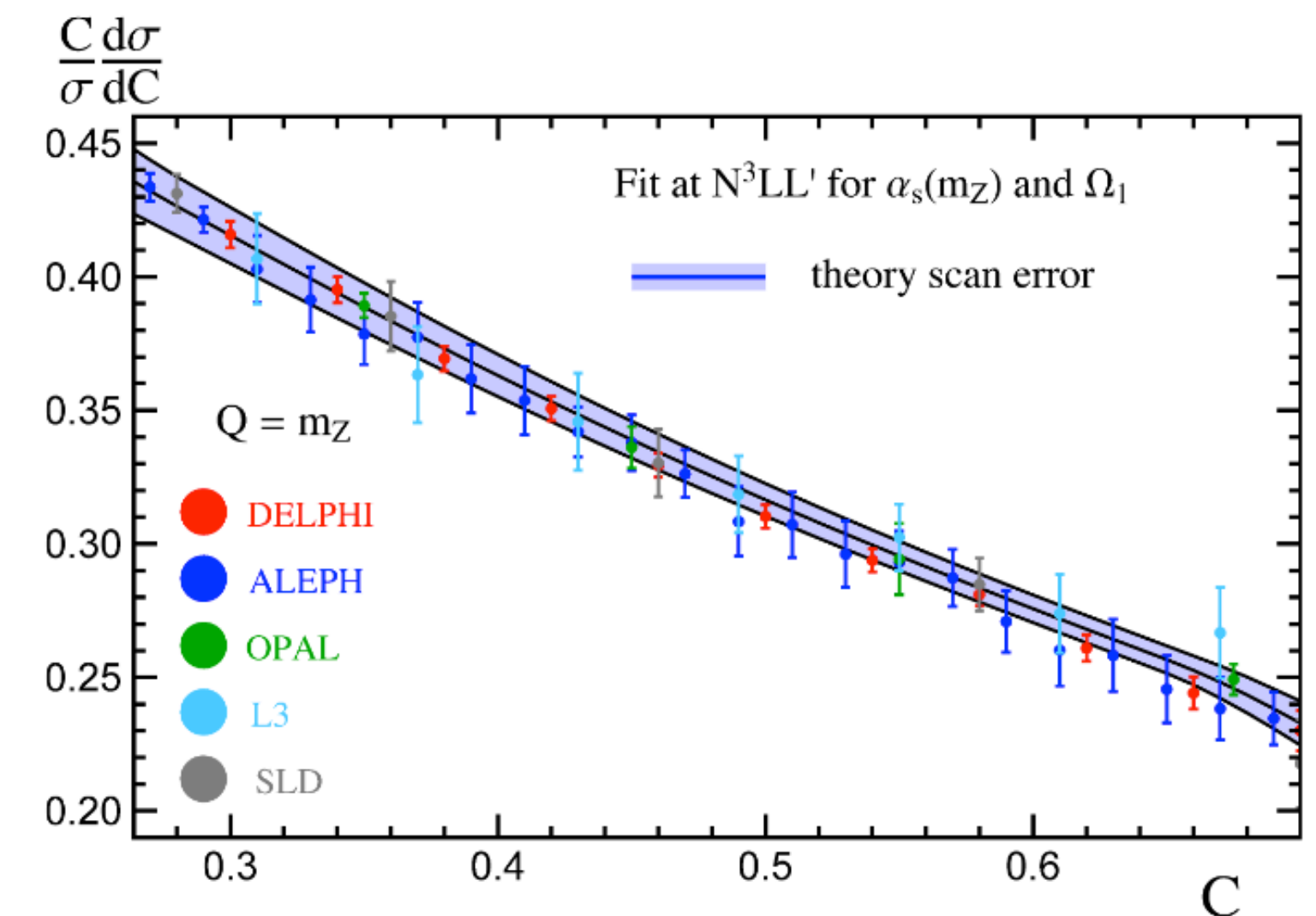


- **$\tau$ -leptonic decays**  $\rightarrow \Delta\alpha_s/\alpha_s \ll 1\%$ 
  - O(10<sup>11</sup>) from  $Z \rightarrow \tau\tau$  at FCC-ee (90 GeV)

$$R_\tau \equiv \frac{\Gamma(\tau^- \rightarrow \nu_\tau + \text{hadrons})}{\Gamma(\tau^- \rightarrow \nu_\tau e^- \bar{\nu}_e)} = S_{\text{EW}} N_C \left( 1 + \sum_{n=1}^4 c_n \left( \frac{\alpha_s}{\pi} \right)^n + \mathcal{O}(\alpha_s^5) \right) + \delta_{\text{np}}$$

(With expected improvements: N<sup>4</sup>LO, improved  $\tau$  spectral functions, estimate of higher pQCD (FOPT vs CIPT))

- **Thrust, C-parameter, event shapes 3-jet cross sections**
  - Recent progress in understanding non-perturbative effects in C-parameter measured at LEP resolved tensions with the world average  $\alpha_s$ , grooming techniques to suppress non-pert.



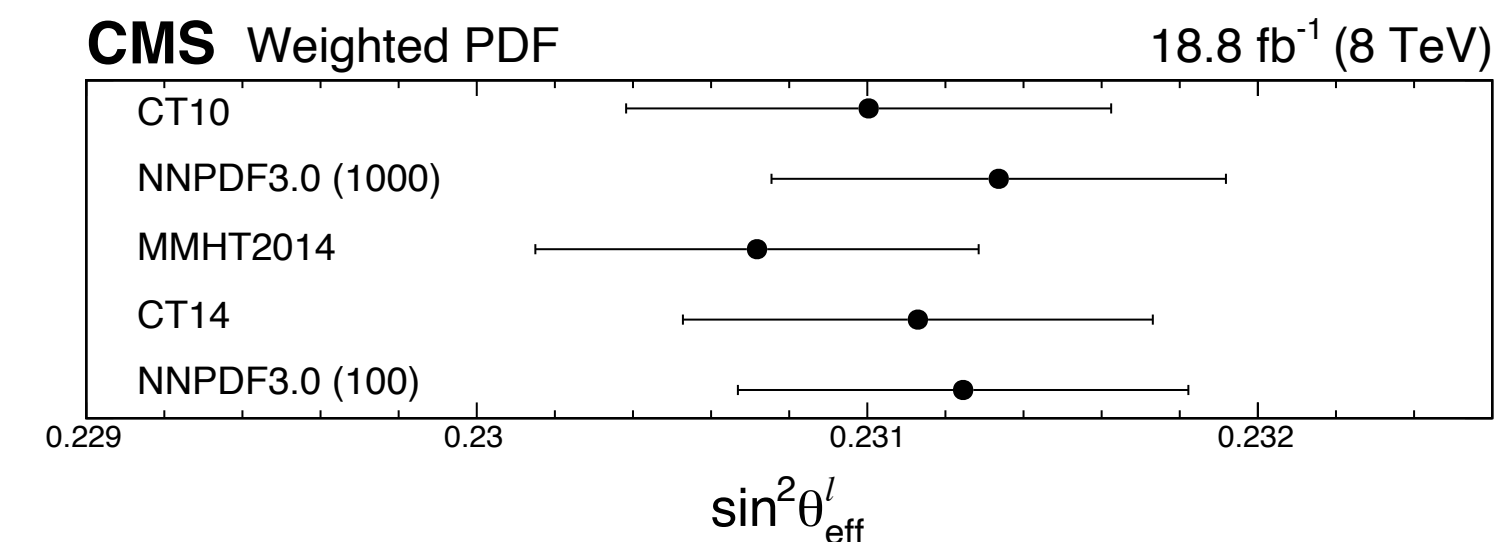
PDF

- PDF uncertainties are a limiting factor in precision measurements at LHC
- **Uncertainty variations within 1 PDF set not covering difference with other PDF**
  - ATLAS  $m_W$  mass
  - ATLAS and CMS  $\sin^2 \theta_W$
  - CMS  $\alpha_s$  extraction from  $t\bar{t}$  production
  - ...

*Do we understand our PDF and uncertainties sufficiently well?*

PDF-Set	$p_T^\ell$ [MeV]	$m_T$ [MeV]	combined [MeV]
CT10	$80355.6^{+15.8}_{-15.7}$	$80378.1^{+24.4}_{-24.8}$	$80355.8^{+15.7}_{-15.7}$
CT14	$80358.0^{+16.3}_{-16.3}$	$80388.8^{+25.2}_{-25.5}$	$80358.4^{+16.3}_{-16.3}$
CT18	$80360.1^{+16.3}_{-16.3}$	$80382.2^{+25.3}_{-25.3}$	$80360.4^{+16.3}_{-16.3}$
MMHT2014	$80360.3^{+15.9}_{-15.9}$	$80386.2^{+23.9}_{-24.4}$	$80361.0^{+15.9}_{-15.9}$
MSHT20	$80358.9^{+13.0}_{-16.3}$	$80379.4^{+24.6}_{-25.1}$	$80356.3^{+14.6}_{-14.6}$
NNPDF3.1	$80344.7^{+15.6}_{-15.5}$	$80354.3^{+23.6}_{-23.7}$	$80345.0^{+15.5}_{-15.5}$
NNPDF4.0	$80342.2^{+15.3}_{-15.3}$	$80354.3^{+22.3}_{-22.4}$	$80342.9^{+15.3}_{-15.3}$

NNPDF4.0 and CT10 differ by 18 MeV  
Estimated PDF uncertainties 3 → 9 MeV



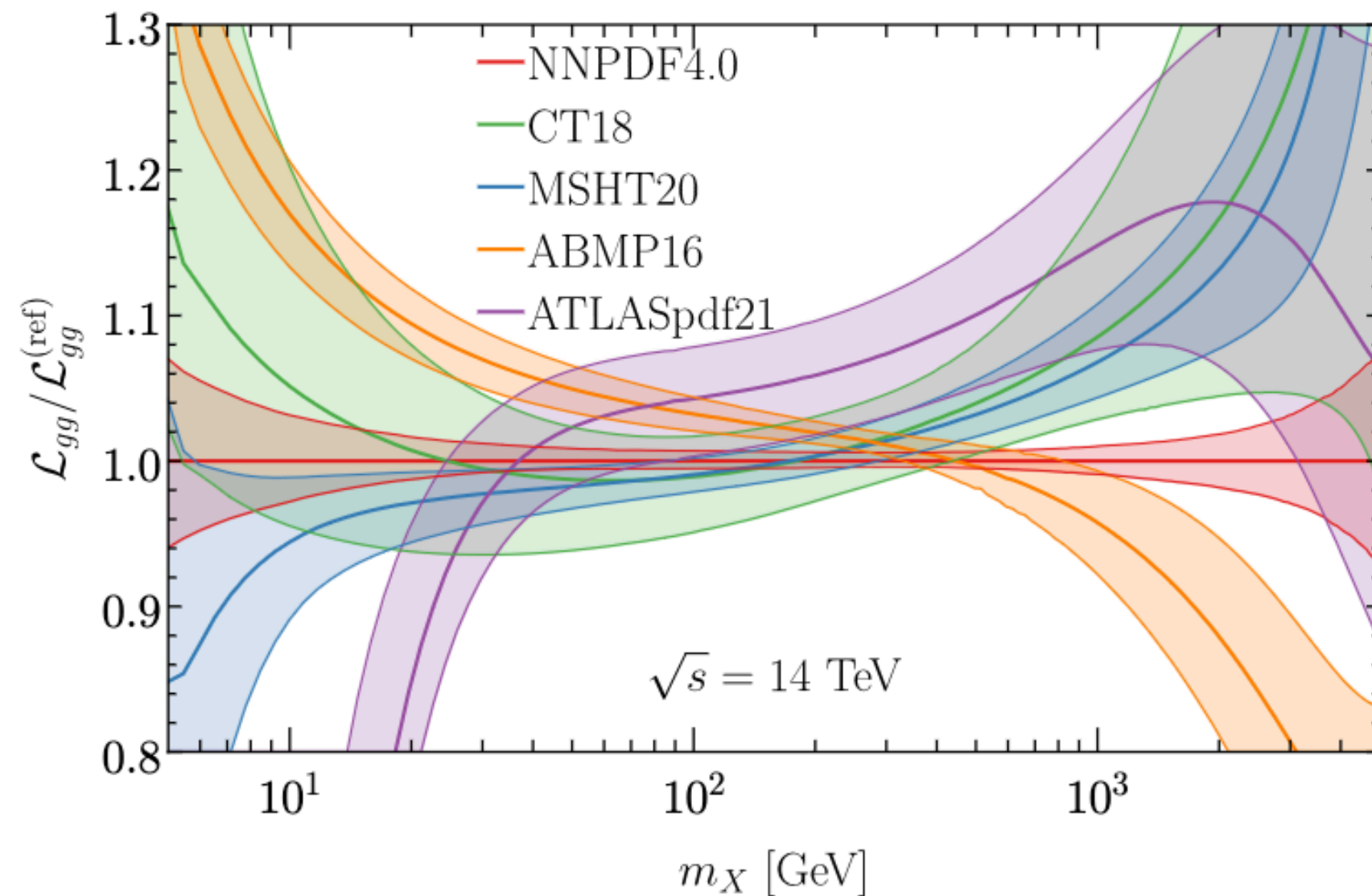
$$\sin^2 \theta_{\text{eff}}^\ell = 0.23101 \pm 0.00036 \text{ (stat)} \pm 0.00018 \text{ (syst)} \\ \pm 0.00016 \text{ (theo)} \pm 0.00031 \text{ (PDF)},$$

PDF envelope 0.0006 (MMHT2014 - NNPDF3.0)

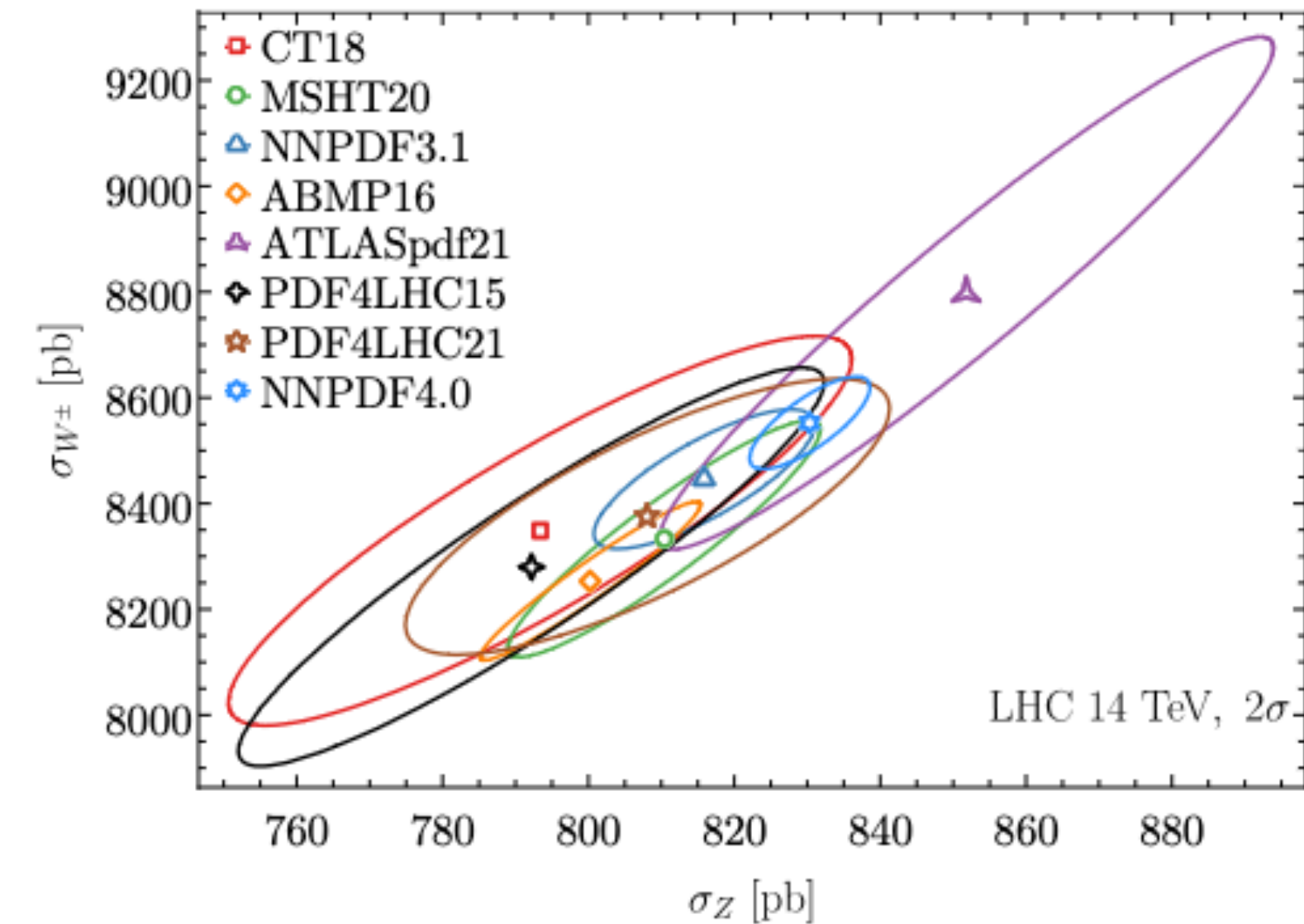


- PDF determined in global fits to fixed target, DIS and collider data
- More data are included as NNLO predictions become available, towards N<sup>3</sup>LO PDFs is in progress
- Precisions of 1% is being achieved for medium Bjorken- $x$
- **PDF Benchmarking**
  - Important effort to understand correlations between PDF set
  - $gg$  luminosity shows spread of more than 20% in the multi-TeV region,  $q\bar{q}$  agrees better, except around 300 GeV

## Impact on searches



## Impact on precision measurements



# PDF constraining measurements

- **High-x gluon**

- Jet and multijet production (multi-differential), precise jet energy scale at the level of 1-2%
- Inclusive  $\gamma$
- $t\bar{t}$  and  $t\bar{t}+j$

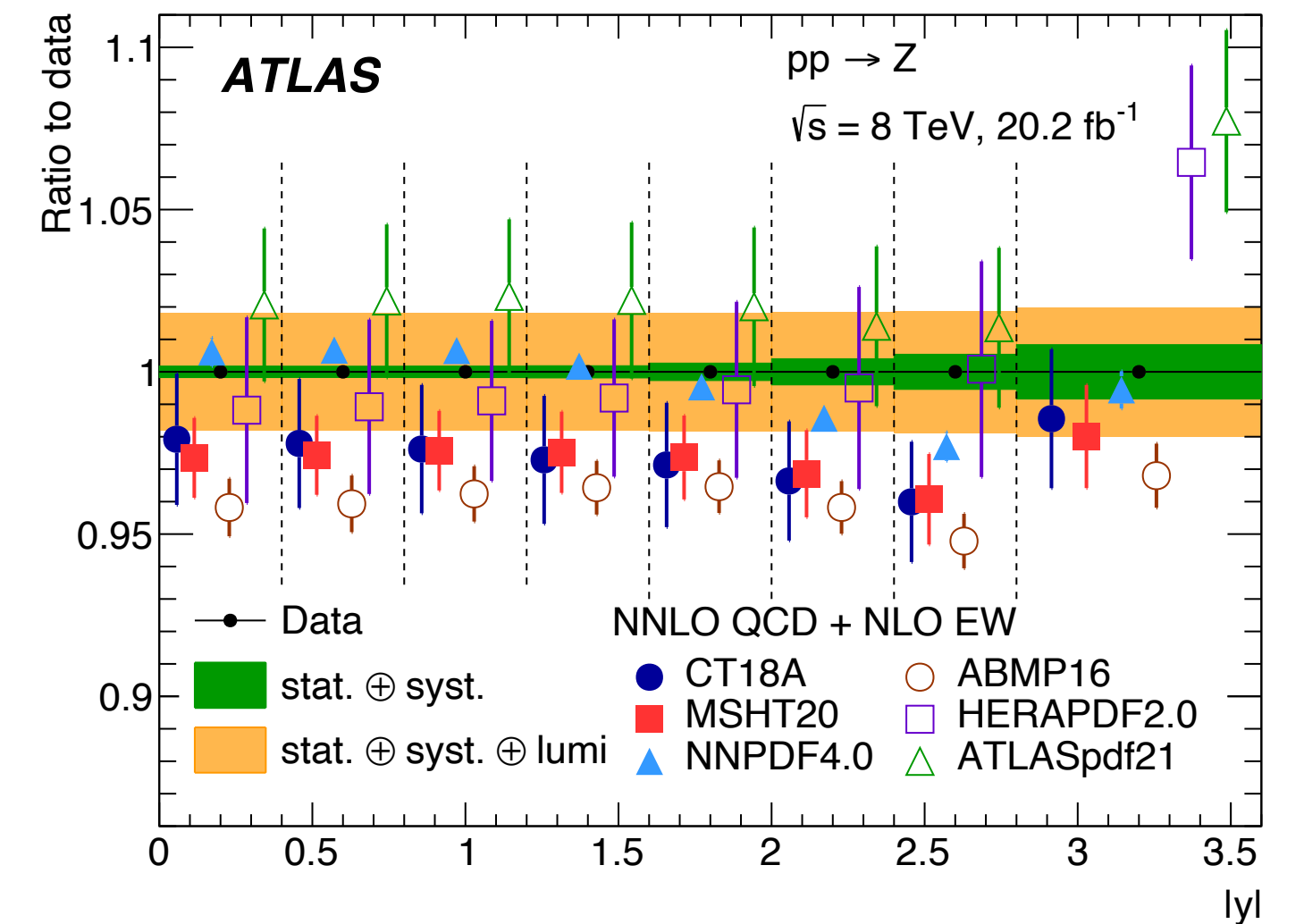
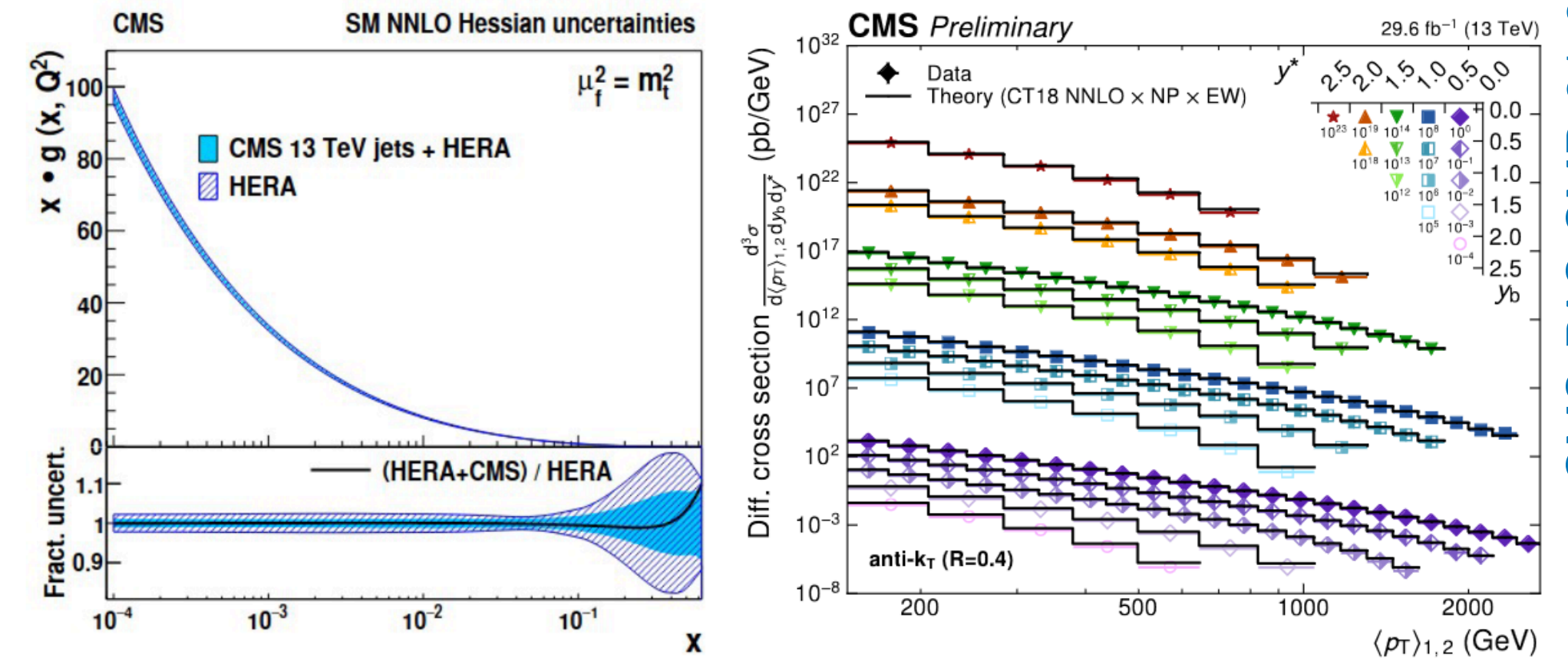
- **Medium-x parton densities**

- Most precise measurement of Z boson - new methodology
- Per-mile uncertainty in the central and less than % in the forward regions
- Full-lepton phase-space offers **unambiguous interpretation of PDFs**

- **Strange and charm parton densities**

- Probed with  $W+D$ ,  $W+b$  jet measurements

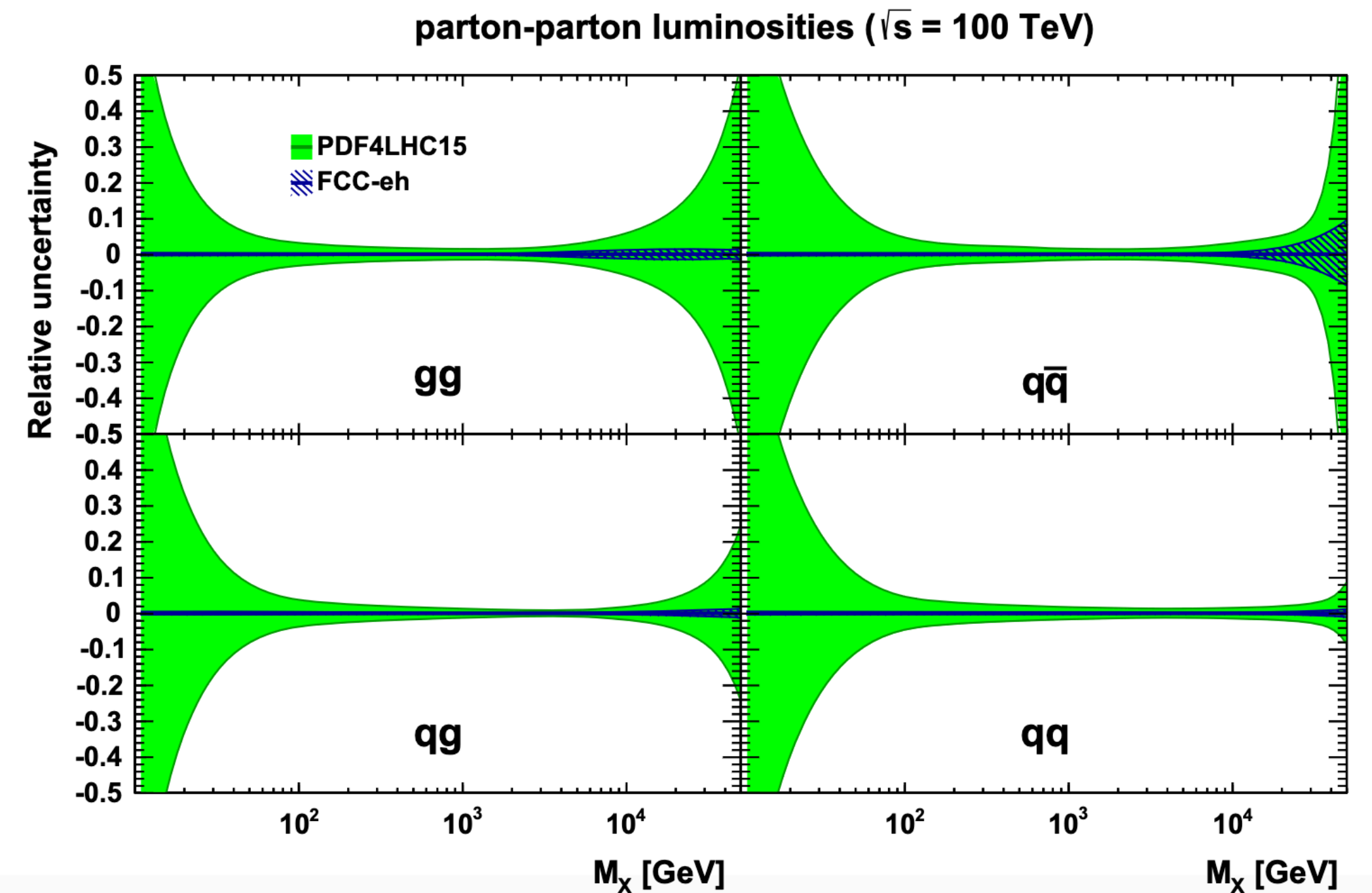
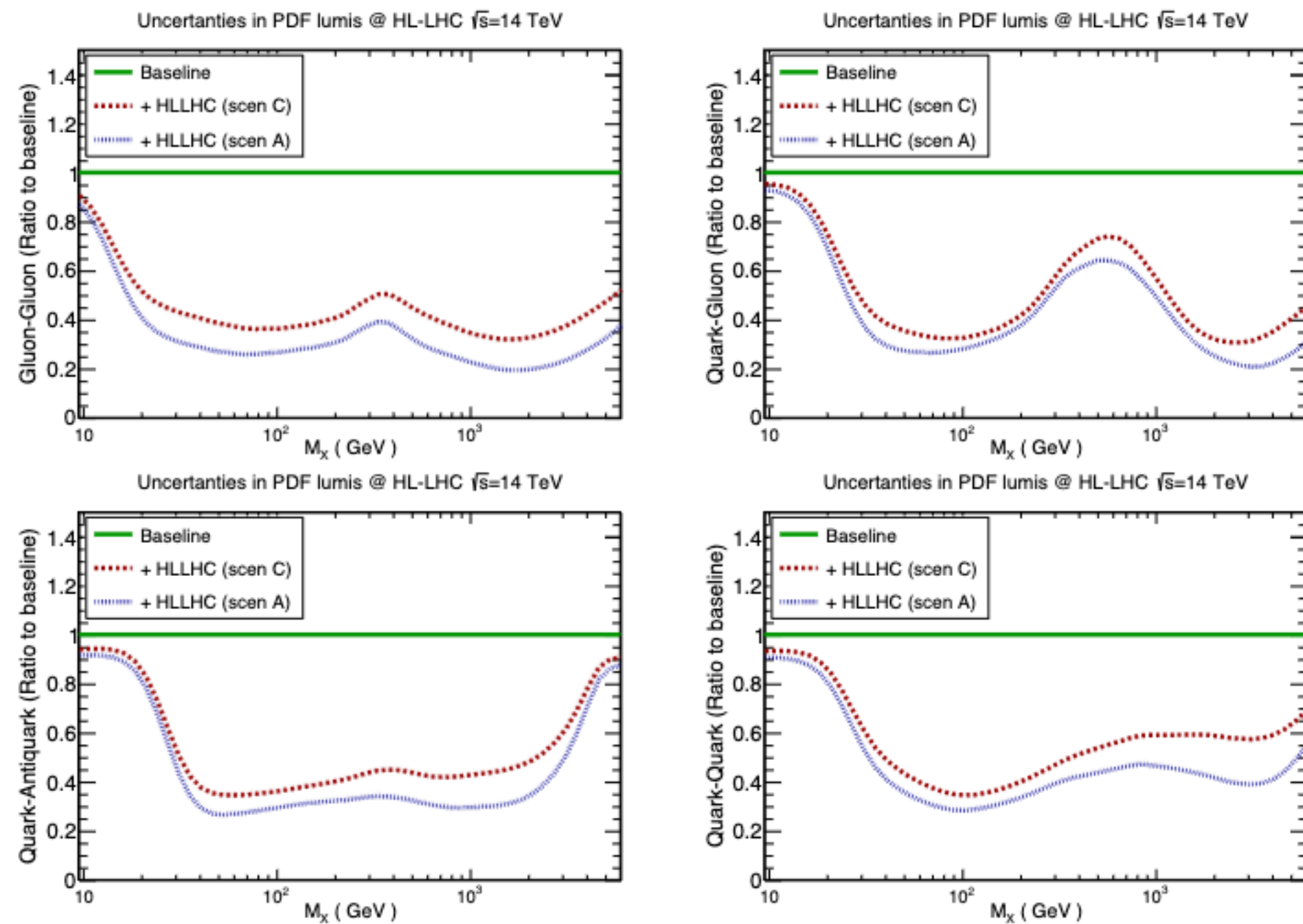
... also, LHCb brings in valuable coverage of forward region



Achievable precision depends on syst. uncertainties of the data - correlations insufficiently known  $\rightarrow$  results in tensions between dataset



- Factor 2 reduction of PDF uncertainties at the end of HL-LHC
- At FCC-eh - PDF uncertainties are strongly reduced, EIC in the next talk
- Precise PDF determination demanded by the precision physics program at hadron-hadron FCC-hh machine



# Jet substructure

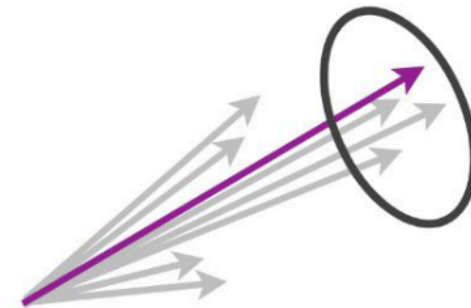


# Jet substructure

- Jet constituents four-momenta are mapped onto physically meaningful observable: (m<sub>J</sub>, LJP, generalised angularities - LHA, width, thrust, multiplicity, ...)

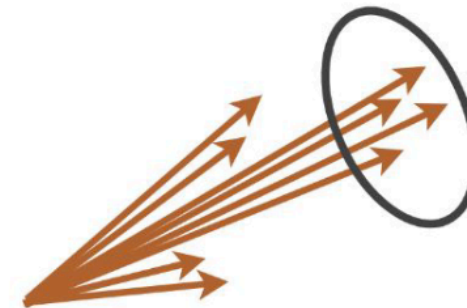
$$\{p_i\} \rightarrow \lambda$$

Fragmentation  
Functions



Single hadron

Classic  
Jet Shapes



All hadrons

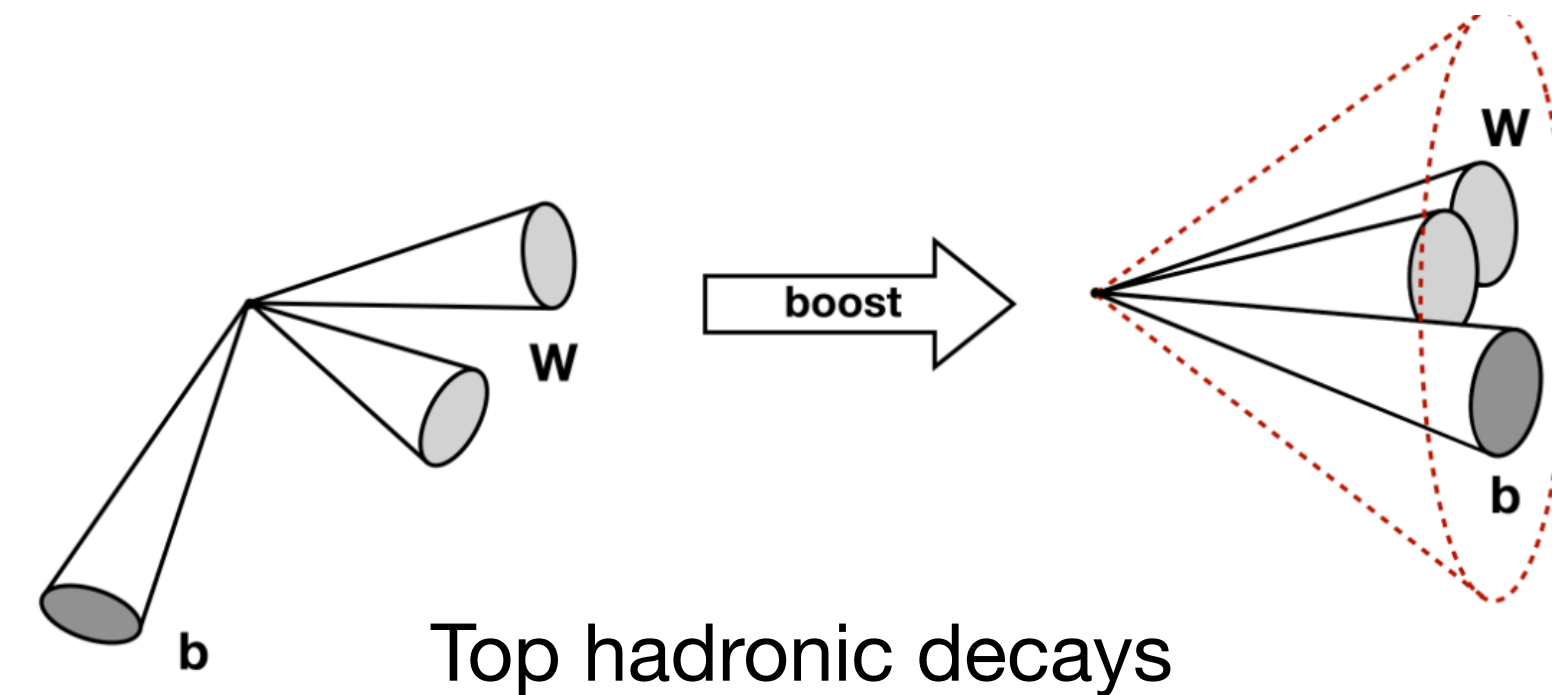
Groomed  
Observables



Subset of hadrons

Sketch by Jesse Thaler

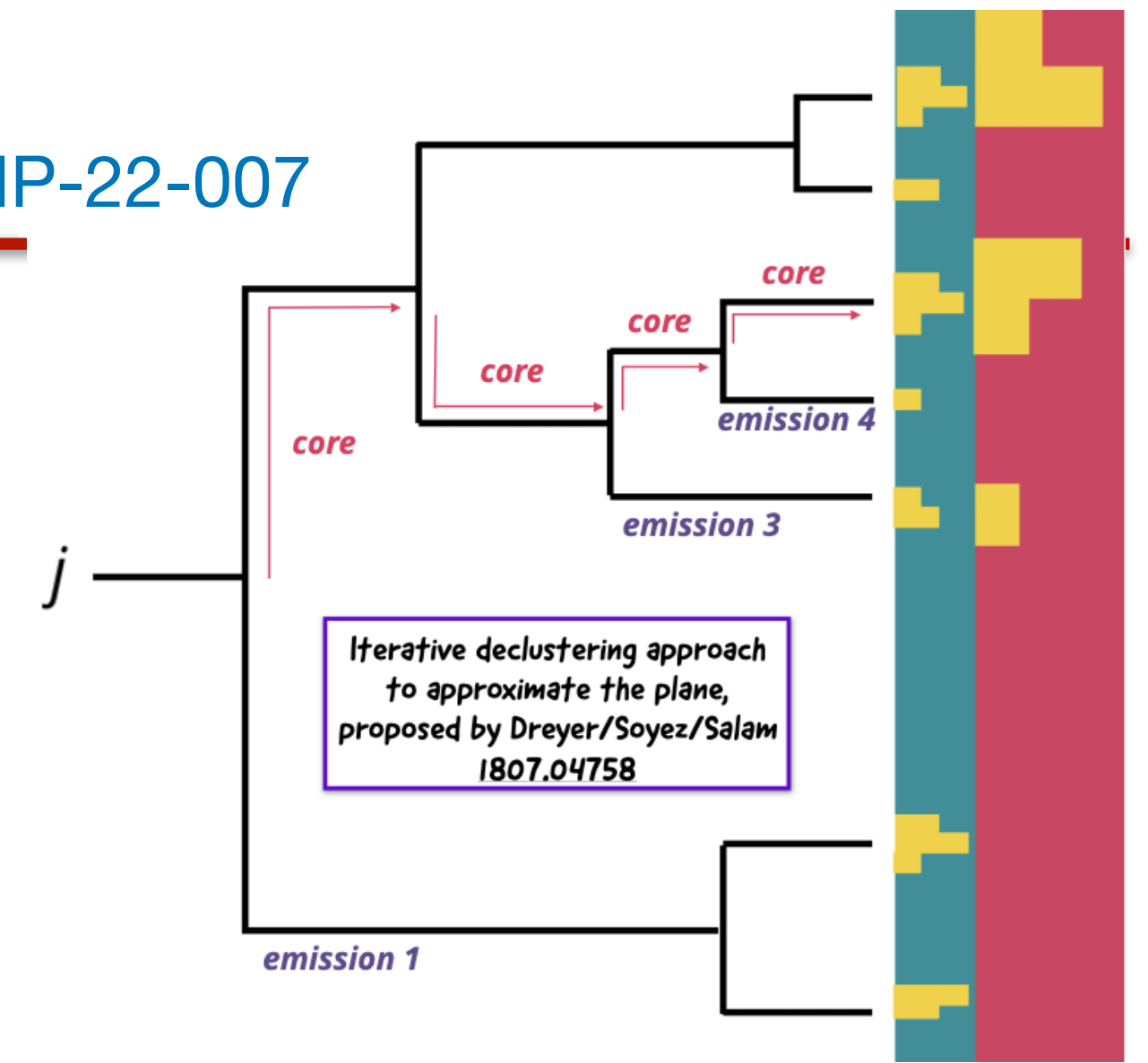
- Jet substructure reveal information about
  - Parton shower modelling
  - Flavour tagging (quark/heavy quark/gluon)
  - Large-R jets - particle content in boosted jet topologies
  - Fragmentation and non-perturbative effects
  - ...



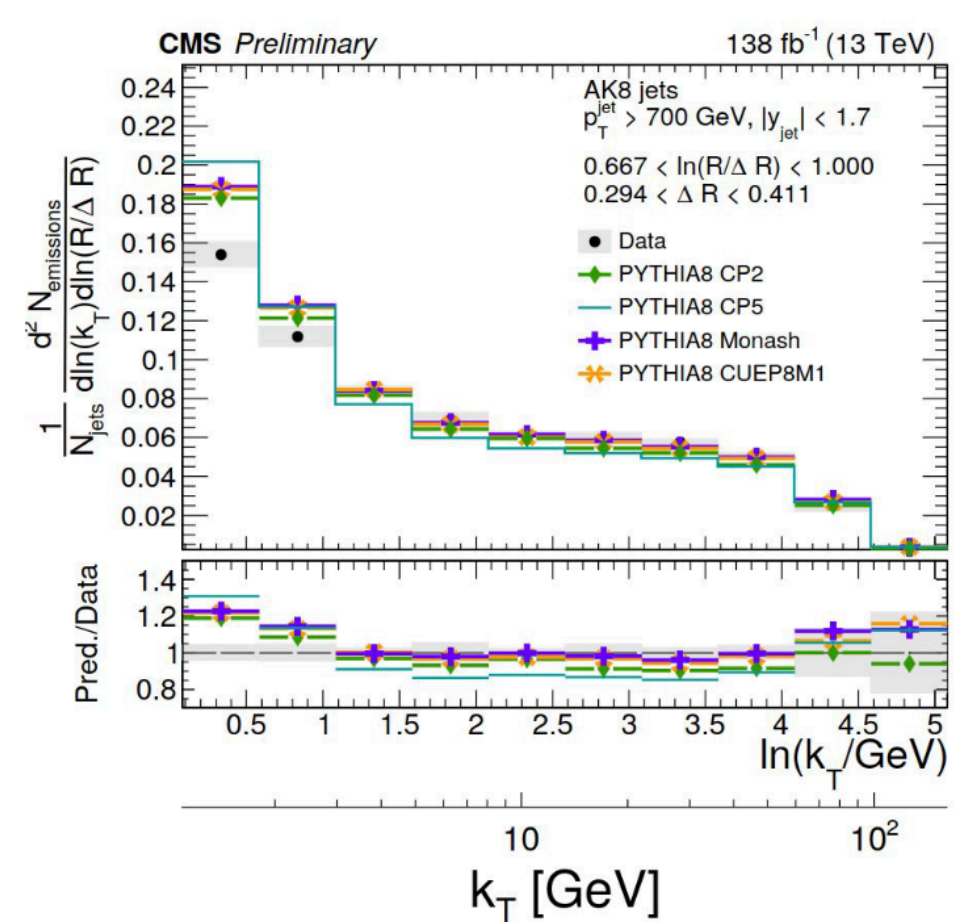
# Lund jet plane at 13 TeV

CMS-PAS-SMP-22-007

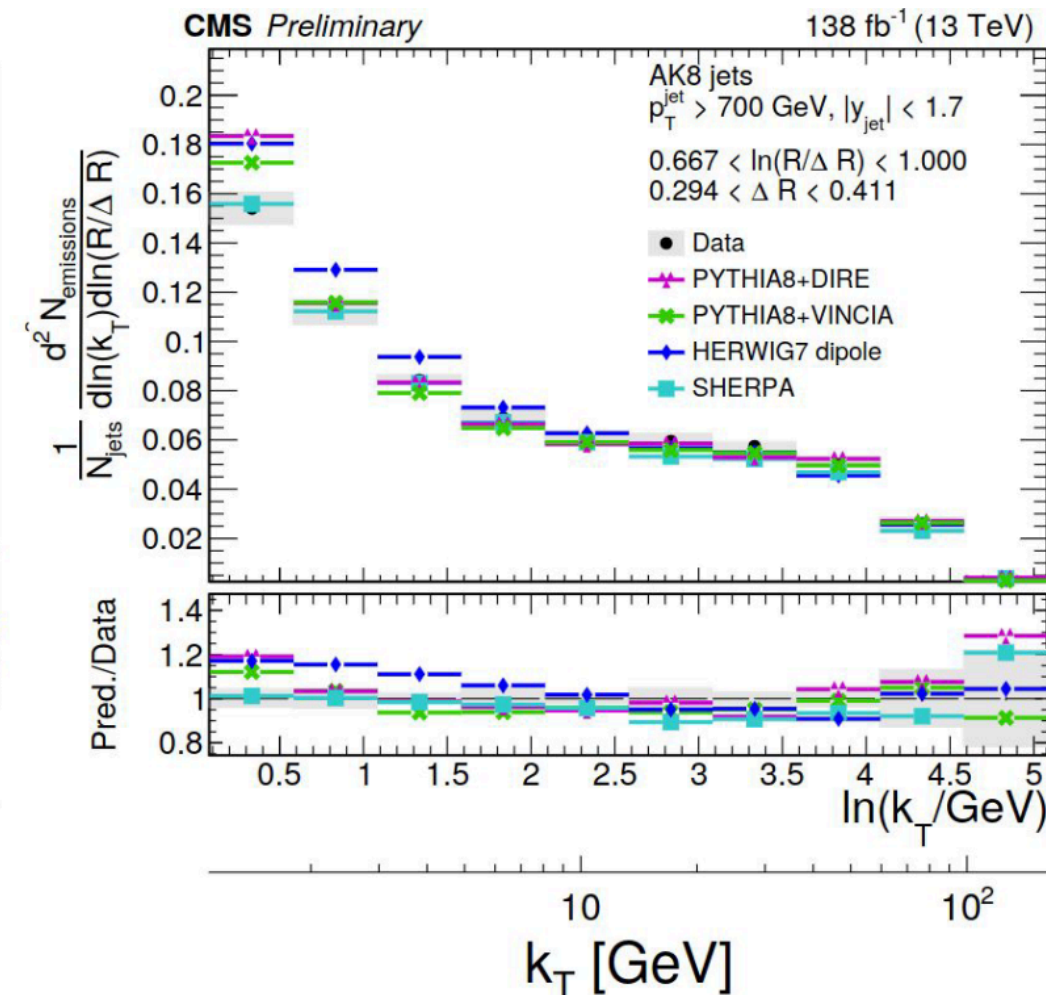
- A jet is approximated as soft emissions around a hard core which represents the original quark or gluon
  - Recluster jets with C/A algorithm and unwind widest angles first
- ‘Radiography’ of jets - 10-20% mismodelling of the data
  - Crucial input for new NLL parton shower developments and MC tuning



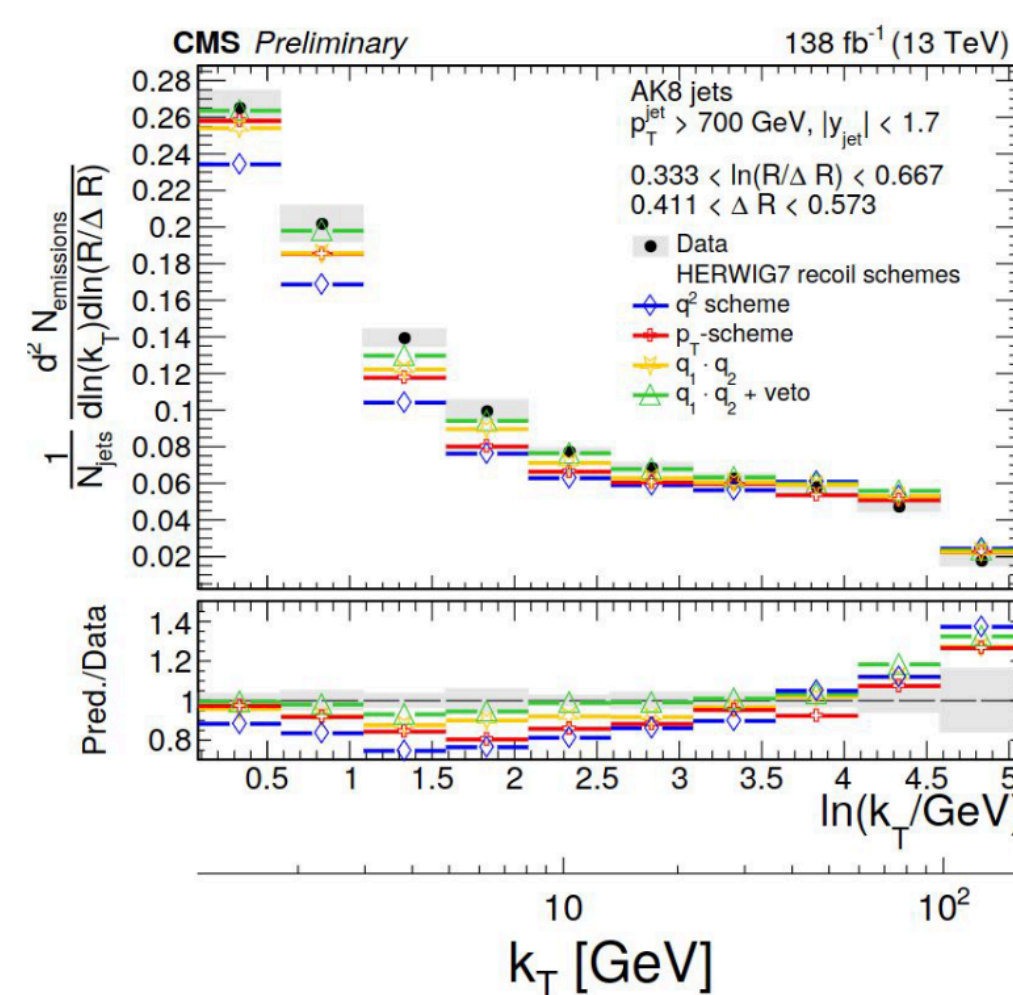
M. LeBlanc, adapted



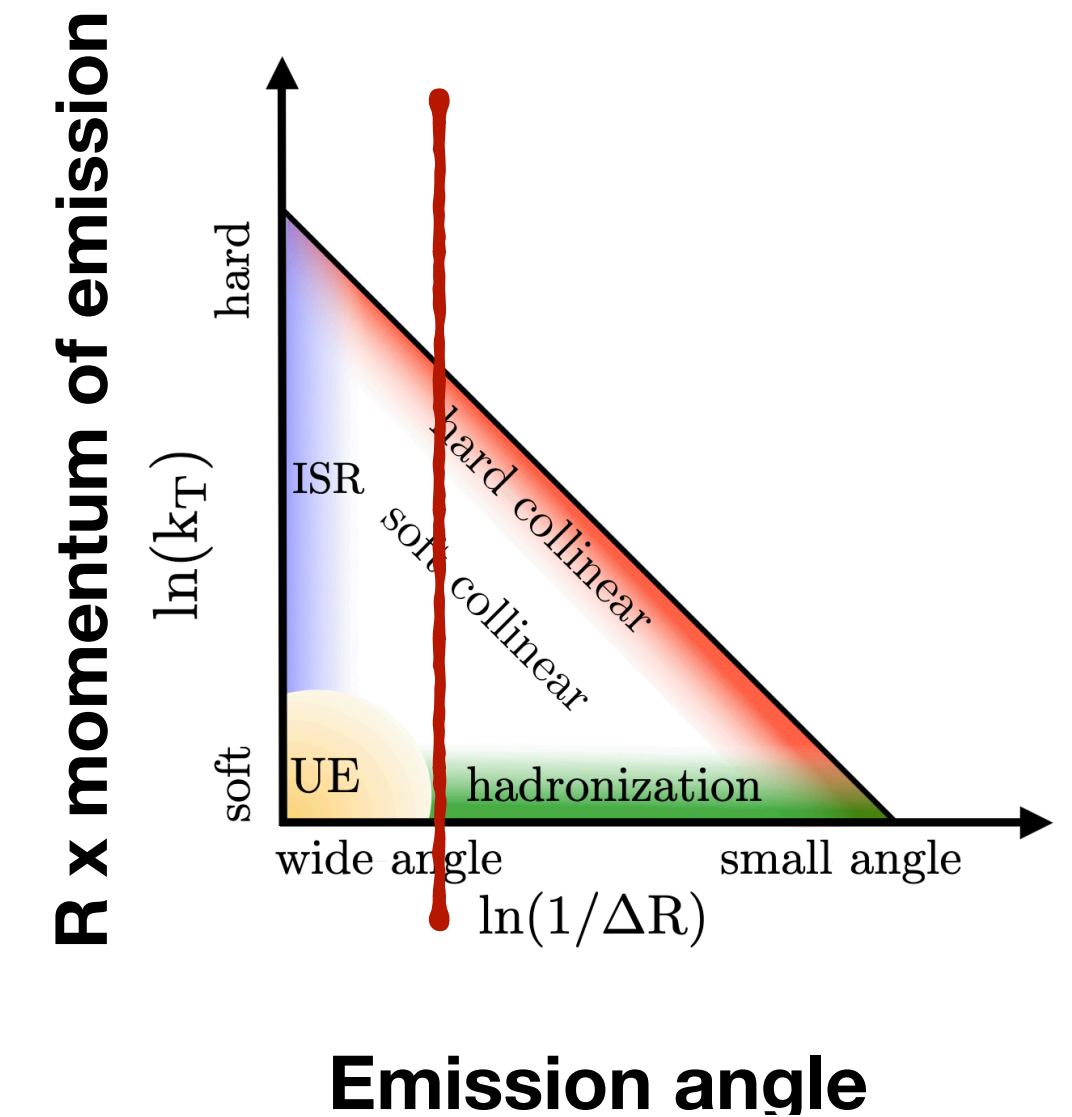
**PYTHIA8 tunes**  
(CP2, CP5, Monash, CUEP8m1)



**Dipole showers**  
(Vincia, Dire, Herwig7 dipole, Sherpa)

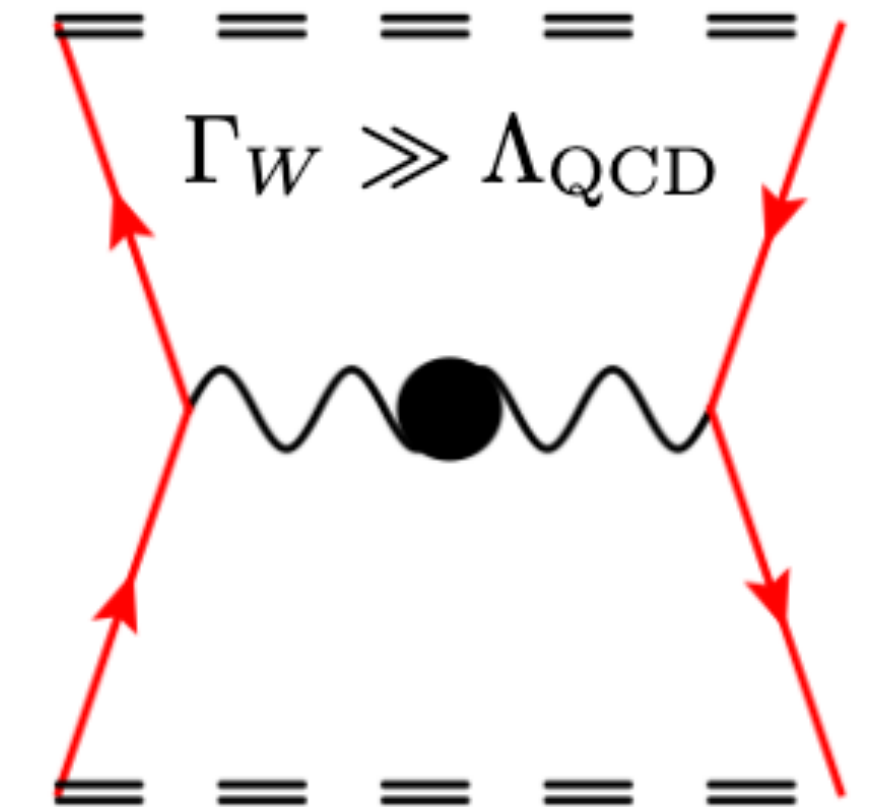
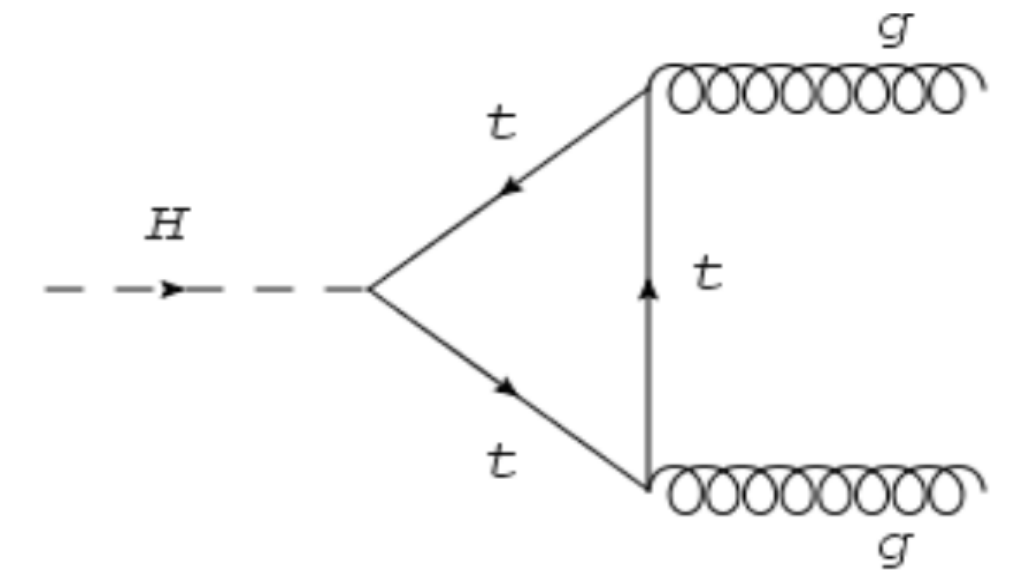


**Herwig7 recoil schemes**  
(angle-ordered)





- **Expect new generation of highly accurate MC models in the next decade**
  - NNLO calculations matched and merged with next-generation showers
  - ILC/FCC-ee/CEPC clean events to test PS/hadronization developments
  - Disentangling perturbative from non-perturbative corrections
- **High-precision quark and gluon substructure and fragmentation studies**
  - Current PS models differ on the gluon radiation pattern (less for quark)
  - Clean gluon  $H \rightarrow gg$  factory, compare with  $Z \rightarrow qq(g)$
  - $q/s/c/b$ /gluon tagging
- **Colour reconnection studies** - CR is an uncertainty on  $m_{\text{top}}$ 
  - String drag effect on  $W$  mass, No-CR excluded at 99.5% CL at LEP
  - Use threshold scan + huge sample of semi-leptonic  $WW$  to measure  $m_W$ 
    - input as constraint to make sensitive measurements of CR in hadronic  $WW$



# Summary

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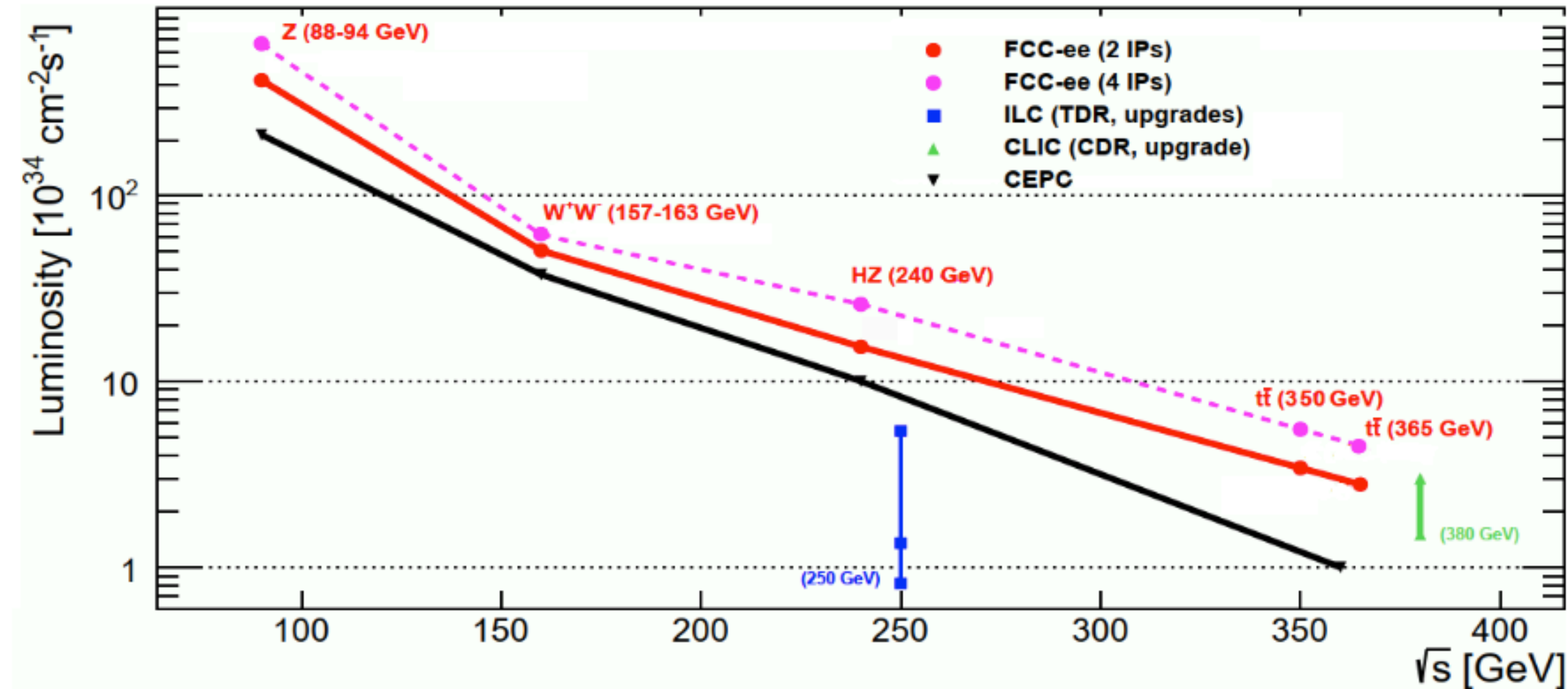
- **QCD physics at the LHC has entered % precision era both in terms of theory and experimental measurements**
- Accurate pQCD predictions are indispensable (NNLO computations are available for many processes)
- Parton showers is a fast developing field - showers uncertainties are often the dominant uncertainties in EWK measurements

**Future lepton colliders will play an instrumental role to scrutinise ongoing theory developments on the way to the future hadron-hadron collider**



# Backup

# QCD opportunities at future lepton colliders



- FCC-ee

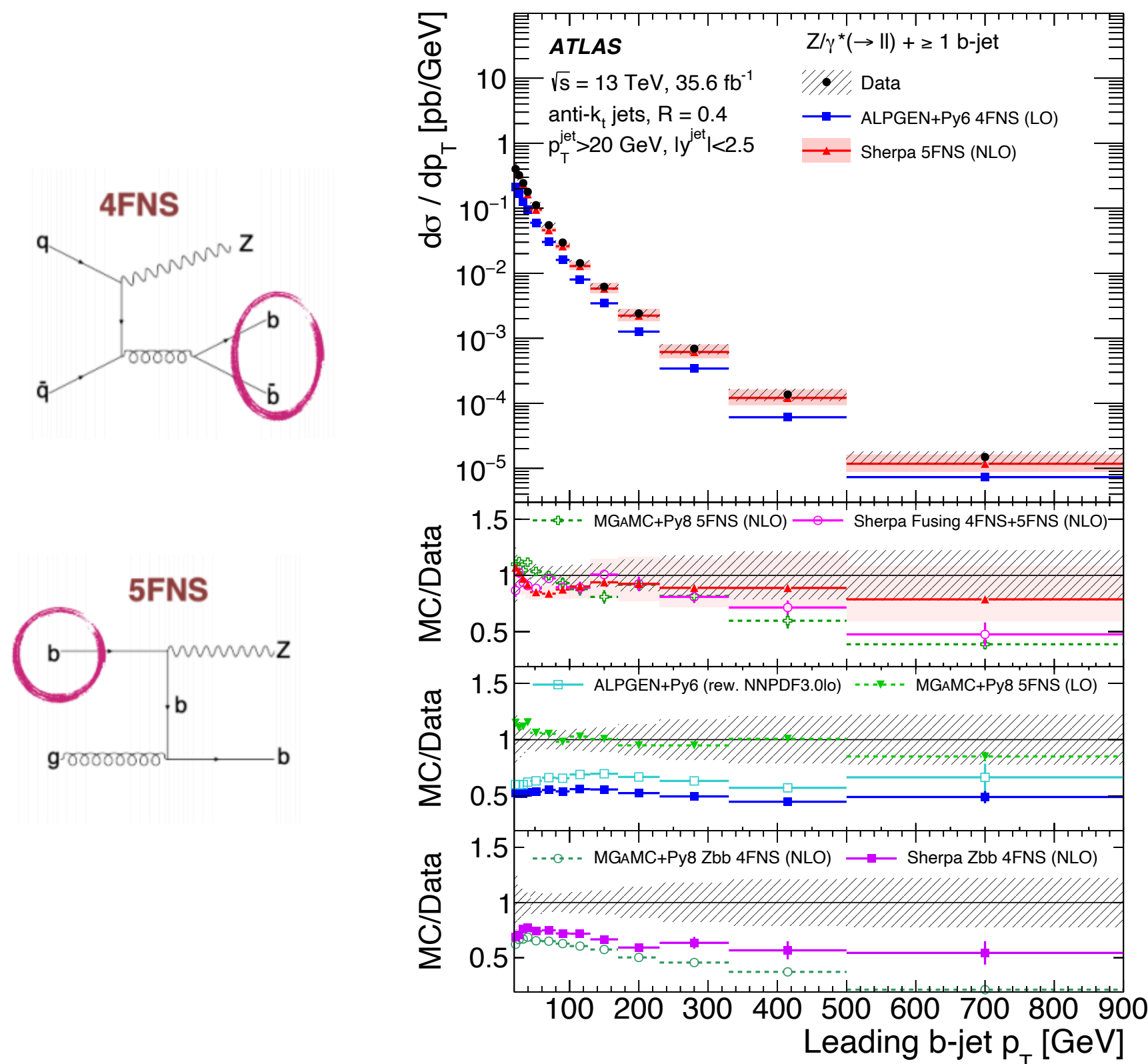
ZH maximum	$\sqrt{s} \sim 240$ GeV	3 years
$t\bar{t}$ threshold	$\sqrt{s} \sim 350$ GeV	5 years
Z peak	$\sqrt{s} \sim 91$ GeV	4 years
WW threshold+	$\sqrt{s} \geq 161$ GeV	2 years
[s-channel H	$\sqrt{s} = 125$ GeV	? Years

$10^6$	$e^+e^- \rightarrow ZH$
$10^6$	$e^+e^- \rightarrow t\bar{t}$
$5 \times 10^{12}$	$e^+e^- \rightarrow Z$
$> 10^8$	$e^+e^- \rightarrow W^+W^-$
$\sim 5000$	$e^+e^- \rightarrow H$

Never done	2 MeV
Never done	5 MeV
LEP $\times 10^5$	$< 50$ keV
LEP $\times 10^3$	$< 200$ keV
Never done	$< 100$ keV

# W/Z associated with charm and beauty

- **Z+b measurements** discriminate the effect of b quark PDF, important for VH-> bbl and BSM searches
  - test of pQCD: gluon splitting, HF mass effects, NLO effects
- **W+D measurements** reveal details of the strange parton density
  - $s - \bar{s}$  asymmetry constrained via ration of  $W^+ + \bar{c}/W^- + c$

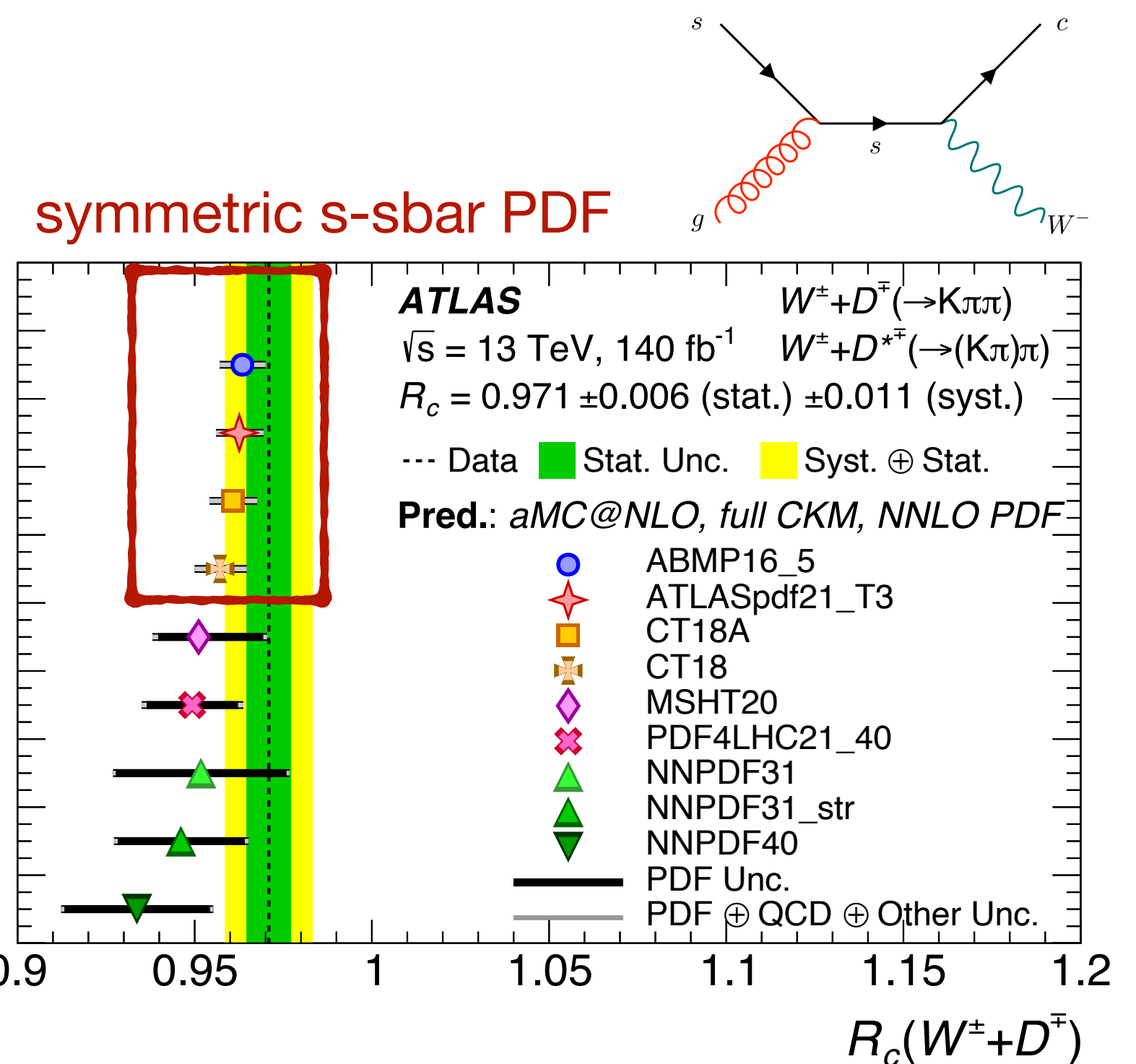


new Sherpa  
4F+5F @ NLO  
predictions

all 4F predictions  
underestimate  
the Z+1b xsection

Suggests small s-sbar asymmetry

**Outstanding challenge for PDF fits**  
 predictions at NNLO with charm  
 fragmentation included needed



# Jet response

- Particle response depends on the parton shower and hadronization
  - driven by the energy fraction of kaons and baryons in a jet

