

EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

# The Sensitivity of a Meander Coupler to Particle Displacement

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**Abstract:** The sensitivity of a 80 cm long meander pickup to particle displacement has been theoretically obtained. The pickup is a travelling wave coupler, and its phase velocity is designed to synchronize a 60 MeV/c beam, aiming at betatron cooling at LEAR. Based on the calculated pickup sensitivity, cooling time is estimated with an acceptable result.

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## 1. Meander pickup under examination

The coupling impedance of the meander coupler discussed here is derived from theory [1]. In the calculation, the geometrical structure of the coupler, other than the length, is set same as that of the test piece installed in LEAR in September 1986 (see Fig. 1). The length of the test piece is 20 cm; in this note, we will discuss also for other lengths.

In the actual set up of a pickup for betatron cooling, two identical couplers sandwiches the beam as in Fig. 2(a) and are used in difference mode. In the calculation, however, the characteristics of the coupler (phase velocity, characteristic impedance, and coupling impedance) are obtained for the structure as in Fig. 2(b), where a ground plate is set on the equilibrium orbit. This model is equivalent to the actual setup in difference mode. The differential coupling impedance obtained from the half geometry is transformed to that of the actual full geometry by dividing by a factor of two. The explanation is as follows. Applying the Lorentz reciprocity theorem to the diagrams in Figs. 3(a) and (b), we can calculate voltage induced by the beam.

$$V_{\ell} = -\sqrt{\frac{Z_c}{8 P_s}} \int_{vol} \vec{E}_s \cdot \vec{J}_{\ell} dV, \quad (1.1)$$

where  $P_s$  and  $E_s$  are power flow and electric field generated by an external power source, respectively, and  $J_{\ell}$  density of the beam current [2,3,4]. For the half geometry (Fig. 3(a)), where a ground plate is set on the median plane, the voltage is given by

$$V_{\ell}^H = -\sqrt{\frac{Z_L}{8 P_s^H}} \int_{vol} \vec{E}_s \cdot \vec{J}_{\ell} dV, \quad (1.2)$$

where  $Z_L$  is the characteristic impedance of the pickup. For the full geometry (Fig. 3(b)), the voltage is

$$V_{\ell}^F = -\sqrt{\frac{Z_L/2}{8 P_s^F}} \int_{vol} \vec{E}_s \cdot \vec{J}_{\ell} dV. \quad (1.3)$$

Putting  $P_s^H = P_s^F/2$ , we have

$$\frac{Z_p^F}{Z_p^H} = \frac{V_{\ell}^F}{V_{\ell}^H} = \frac{1}{2}. \quad (1.4)$$

The phase velocity  $\beta_w$  of the coupler is about 0.06, and the characteristic impedance is about 50  $\Omega$  both in theory and experiment. The overall length of the pickup discussed here is 80 cm; we examine

the three configurations as shown in Fig. 4: a) four pairs of couplers of 20 cm long each, b) two pairs of couplers of 40 cm long each, and c) one pair of couplers of 80 cm long each. The reason for the examination of such configurations is that a long coupler gives a high coupling impedance for a beam with a velocity close to the phase velocity of the coupler, whereas a shorter coupler has more "broad-band" and hence more efficient for beam velocities different from the phase velocity [5].

## 2. Total differential coupling impedance of pairs of couplers

Coupling impedance of one pickup, consisting of a pair of couplers, is a function of the beam position  $x_b$ , which is measured from the equilibrium orbit, 30 mm far from the meander line in our case. In this note, we define the coupling impedance of one pickup  $Z_p(x_b)$  by the ratio of the voltage at the output of a differential power combiner to the beam current. Figure 5 shows  $dZ_p/dx_b$  of a pickup consisting of a pair of 80 cm long single couplers for a 60 MeV/c beam. At an ideal pickup  $dZ_p/dx_b$  is constant, or  $Z_p$  is proportional to  $x_b$ , but at our pickup  $dZ_p/dx_b$  has a large value at large  $|x_b|$ , especially at high frequencies. In the calculation of cooling time to be discussed later, the coupling impedance is approximated by

$$Z_p = Z_p' \cdot x_b \quad , \quad (2.1)$$

where

$$Z_p' = \left. \frac{dZ_p}{dx_b} \right|_{x_b=0} \quad . \quad (2.2)$$

We consider a pickup system consisting of  $n_{pu}$  pairs of couplers as shown in Fig. 6. The output signals from  $n_{pu}$  differential power combiners are fed into a sum power combiners. For this system, the total differential coupling impedance  $Z'_{pt}$  is given by

$$Z'_{pt} = \sqrt{n_{pu}} Z_p' \quad (2.3)$$

Figure 7 shows  $Z'_{pt}$  for the three coupler configurations and for beam momenta of 60 MeV/c ( $\beta_b = 0.06382$ ) and 100 MeV/c ( $\beta_b = 0.1060$ ). For the 60 MeV/c beam (the top figure), of which the velocity is close to the coupler's phase velocity, the single pair of 80 cm long couplers has the highest peak value at 90 MHz, but its bandwidth is narrow (up to 150 MHz). In contrast, the four pairs of 20 cm long couplers have the broadest band, but its peak value is low. At present we cannot conclude which coupler configuration is best, because we have not determined the system bandwidth, which is to be determined not only by the coupling impedance but also by the mixing between the pickup and the kicker, to be discussed in Sect. 3.2. For the 100 MeV/c beam (the bottom of Fig. 7), the four pairs of 20 cm couplers have the highest peak value and the broadest band; therefore, this configuration will be best.

### 3. Cooling time

#### 3.1 Differential equation for the cooling process

We will estimate the cooling time using the following equation [6]:

$$\begin{aligned} \frac{1}{\tau} &= -\frac{1}{\epsilon} \frac{d\epsilon}{dt} \\ &= \sum_n \frac{1}{\tau_n} \quad , \end{aligned} \quad (3.1)$$

$$\frac{1}{\tau_n} = \frac{f_0}{N} \left[ 2 g_n |\sin \mu| \cos n \omega_0 \delta T_{PK} - g_n^2 (M_n + U_n) \right] \quad , \quad (3.2)$$

where  $f_0$  is the revolution frequency,  $N$  the number of particles,  $\mu$  the phase advance of betatron oscillation between the pickup and the kicker,  $M_n$  the mixing factor between the kicker and the pickup,  $U_n$  the noise to signal ratio, and  $\delta T_{PK}$  time-of-flight (T.O.F.) error of a particle caused by its momentum error. The cosine term in Eq.(3.2) can be replaced with an value averaged over the momentum distribution. Assuming a flat momentum distribution, we have

$$\langle \cos n \omega_0 \delta T_{PK} \rangle = \text{sinc} \frac{n \omega_0 \Delta T_{PK}}{2} \quad , \quad (3.3)$$

$$\text{sinc } \alpha \equiv \frac{\sin \alpha}{\alpha} . \quad (3.4)$$

Here  $\Delta T_{PK}$  is the full width of T.O.F. error and is related with the full momentum spread  $\Delta p_0/p_0$  of the beam:

$$\frac{\Delta T_{PK}}{T_{PK}} = \left| \frac{\Delta L_{PK}}{L_{PK}} - \frac{1}{\gamma^2} \frac{\Delta p_0}{p_0} \right| , \quad (3.5)$$

where  $L_{PK}$  is the orbit length from the pickup to the kicker. At LEAR we can approximate

$$\frac{\Delta T_{PK}}{T_{PK}} = \frac{1}{\gamma^2} \frac{\Delta p_0}{p_0} . \quad (3.6)$$

Putting this into Eq.(3.3), we have

$$\langle \cos m\omega_0 \delta T_{PK} \rangle = \text{sinc } m\alpha , \quad (3.7)$$

$$\alpha = \frac{\pi}{\gamma^2} \frac{T_{PK}}{T_0} \frac{\Delta p_0}{p_0} . \quad (3.8)$$

The condition that the coherent correction term in Eq.(3.2) is positive for any  $\delta T_{PK}$  and at any harmonic leads to

$$m\omega_0 \frac{\Delta T_{PK}}{2} < \frac{\pi}{2} , \quad (3.9)$$

or

$$m < m_c = \left( \frac{2}{\gamma^2} \frac{T_{PK}}{T_0} \frac{\Delta p_0}{p_0} \right)^{-1} \quad (3.10)$$

At this harmonic number,  $\text{sinc } m\alpha$  in Eq.(3.7) is

$$\text{sinc } m_c \alpha = \frac{2}{\pi} . \quad (3.11)$$

In Eq.(3.2)  $U_n$  is inversely proportional to beam emittance, as will be shown later. Let  $U_n(0)$  be the initial value of  $U_n$ , then

$$U_n(t) = \frac{U_n(0)}{\sigma(t)} , \quad (3.12)$$

where  $\sigma$  is beam emittance normalized by its initial value:

$$\sigma(t) \equiv \frac{\epsilon(t)}{\epsilon(0)} . \quad (3.13)$$

Using Eqs.(3.7) and (3.12), we have

$$\frac{1}{\tau_n} = \frac{f_0}{N} \left[ 2g_n |\sin \mu| \text{sinc } m\alpha - g_n^2 \left( M_n + \frac{U_n(0)}{\sigma} \right) \right] . \quad (3.14)$$

At  $t = 0$ ,  $\tau_n$  takes a minimum value  $\tau_{0n}$

$$\frac{1}{\tau_{on}} = \frac{f_0}{N} \frac{(\sin \mu \operatorname{sinc} m\alpha)^2}{M_n + U_n(0)}, \quad (3.15)$$

with

$$\begin{aligned} g_n &= g_{on} \\ &\equiv \frac{|\sin \mu| \operatorname{sinc} m\alpha}{M_n + U_n(0)}. \end{aligned} \quad (3.16)$$

For another gain, we write as

$$g_n = G g_{on}; \quad (3.17)$$

then,

$$\frac{1}{\tau_n} = \frac{G}{\tau_{on}} \left[ \frac{(2-G)M_n + 2U_n(0)}{M_n + U_n(0)} - \frac{G U_n(0)}{M_n + U_n(0)} \frac{1}{\sigma} \right]. \quad (3.18)$$

Defining the following parameters

$$\begin{aligned} \frac{1}{\tau_0} &= \sum \frac{1}{\tau_{on}}, \\ A &= \sum \frac{1}{\tau_{on}} \frac{U_n(0)}{M_n + U_n(0)}, \\ B &= \sum \frac{1}{\tau_{on}} \frac{M_n}{M_n + U_n(0)}, \end{aligned} \quad (3.19)$$

we have

$$\frac{d\sigma}{dt} = -G \left( \frac{2}{\tau_0} - GB \right) \sigma + G^2 A. \quad (3.20)$$

This yields a solution

$$\sigma = (1 - \sigma_\infty) e^{-t/\tau'} + \sigma_\infty, \quad (3.21)$$

$$\frac{1}{\tau'} = G \left( \frac{2}{\tau_0} - GB \right), \quad (3.22)$$

$$\sigma_\infty = G^2 A \tau'. \quad (3.23)$$

The cooling time  $\tau_g$  to attain a goaled emittance  $\sigma_g (> \sigma_\infty)$  is

$$\tau_g = \tau' \ln \frac{1 - \sigma_\infty}{\sigma_g - \sigma_\infty}. \quad (3.24)$$

### 3.2 Parameter setting

In order to solve the differential equation, the needed parameters are evaluated here for beams of 60 MeV/c ( $\beta_b = 0.06382$ ,  $f_0 = 244$  kHz) and 100 MeV/c ( $\beta_b = 0.1060$ ,  $f_0 = 405$  kHz) circulating in LEAR, of which the circumference is 78.5 m. The number of particles  $N$  is set at  $1 \times 10^9$ , and the initial beam radius  $\sqrt{\beta\epsilon}$  at 3 cm. For the location of the pickup and the kicker, we examine two cases as shown in Fig. 8. The PU-K distances and the phase advances are as follows.

$$L_{PK} = \begin{cases} 11.3 \text{ m} & (\text{Location I}) \\ 25.6 \text{ m} & (\text{Location II}) \end{cases},$$

$$\mu = \begin{cases} 97.2^\circ & (\sin \mu = 0.992) & (\text{Location I}) \\ 292^\circ & (\sin \mu = -0.927) & (\text{Location II}) \end{cases}$$

The system bandwidth is determined to meet the following two conditions. First, the pickup has high coupling impedance in the frequency range. The result in Chapt. 2 (see Fig. 7) gives the answer. Second, the coherent correction term must be positive, as mentioned above. The critical harmonic number defined by Eq.(3.10) depend strongly on the PU-K distance. For a momentum spread of  $\Delta p_0/p_0 = 6\%$  in full width,

$$m_c = \begin{cases} 579 & (\text{Location I}) \\ 256 & (\text{Location II}) \end{cases}$$

The resulting upper limit of the frequency is

$$f_c = \begin{cases} 141 \text{ MHz} & (\text{Location I}) \\ .62 \text{ MHz} & (\text{Location II}) \end{cases}$$

for the 60 MeV/c beam, and

$$f_c = \begin{cases} 234 \text{ MHz} & (\text{Location I}) \\ 103 \text{ MHz} & (\text{Location II}) \end{cases}$$

for the 100 MeV/c beam. These frequency limit infers that the Location II with the long PU-K distance is appreciably disadvantageous.

The mixing factor  $M_n$  is approximated by

$$M_n = \begin{cases} \frac{m_s}{2m} & (m \leq m_s/2) \\ 1 & (m > m_s/2) \end{cases}, \quad (3.25)$$

where  $n_s$  is defined by

$$m_s = \frac{f_o}{\Delta f_o} = \frac{1}{\eta_f} \frac{p_o}{\Delta p_o}, \quad (3.26)$$

( $\eta_f \approx 1/\gamma^2$  at LEAR) .

Noise to signal ratio  $U_n$  at the input of the kicker is given by

$$U_n = \frac{k T_{amp} f_o}{\frac{1}{50} (e f_o \Sigma_{pt}(m f_o))^2 N \langle A^2 \rangle}, \quad (3.27)$$

where  $\langle A^2 \rangle$  is the rms value of amplitude of betatron oscillation. If we assume the phase space density is uniform in the ellipse

$$\gamma x_\ell^2 + 2\alpha x_\ell x_\ell' + \beta x_\ell'^2 = \epsilon, \quad (3.28)$$

$\langle A^2 \rangle$  is given by

$$\langle A^2 \rangle = \frac{1}{2} \beta \epsilon. \quad (3.29)$$

Therefore,  $U_n$  is inversely proportional to emittance, as assumed above (Eq.(3.12)).

### 3.3 Resulting cooling time

We have obtained the parameters necessary to calculate the cooling time. The result of the calculation is summarized in Table I. Comparing the PU-K locations of  $L_{PK} = 11.3$  m and 25.6 m, the cooling time is appreciably long at the 25.6 m distance because of the limited bandwidth. Therefore, this location should be excluded. In the case of  $L_{PK} = 11.3$  m,  $p_o = 60$  MeV/c,  $\Delta p_o/p_o = \pm 3\%$  and  $T_{amp} = 400$  K (a conventional amplifier), the coupler configuration of  $1 \times 80$  cm is best: the goal emittance  $\sigma_g = 0.33$  is attained in 1 min. The conventional amplifier is good enough, though the cooling time is reduced to 35 s with a cryogenic amplifier of  $T_{amp} = 100$  K. The cryogenic amplifier is useful for a pessimistic momentum spread of  $\pm 6\%$ . For a 100 MeV/c beam, the coupler



configuration of  $4 \times 20$  cm is best. With the cryogenic amplifier, the cooling time is around 1 min for the both momentum spreads of  $\pm 3$  and  $\pm 6$  %.

The decrease of beam emittance with time is graphically shown in Figs. 9(a) and (b) for the 60 MeV/c beam (PU :  $1 \times 80$  cm) and the 100 MeV/c one (PU :  $4 \times 20$  cm). Figure 10(a) shows  $\tau_n$ ,  $U_n(0)$ ,  $g_n$  as a function of frequency (harmonic number) for the 60 MeV/c beam ( $T_{\text{amp}} = 400$  K,  $\Delta p_0/p_0 = \pm 3$  %). Cooling time  $\tau_n$  is large at the edge regions of the bandwidth [0 MHz, 142 MHz] because of small pickup coupling impedance. Therefore, a narrower bandwidth, say [15 MHz, 140 MHz], does not lengthen the cooling time  $\tau_g$ . A similar result is obtained for the 100 MeV/c beam ( $T_{\text{amp}} = 400$  K,  $\Delta p_0/p_0 = \pm 3$  %) as shown in Fig. 10(b). A bandwidth of [15 MHz, 150 MHz] is acceptable instead of [0 MHz, 168 MHz].

#### 4. Discussion

The total length of the pickup system discussed here is 80 cm, and the phase velocity is designed to synchronize a 60 MeV/c beam. In order to gain a capability to a 100 MeV/c beam, the pickup should be divided into four couplers, 20 cm long each, as shown in Fig. 4(a). When the divided pickup is used to a 60 MeV/c beam, for which a pair of 80 cm long single couplers is better, the couplers can be connected in series, i.e., the output signal from a downstream coupler is injected to the upstream one.

This configuration is in principle equivalent to the 80 cm long single coupler. But there is a problem in dividing a pickup into short couplers. That is an edge field effect. In the theory for the calculation of the coupler's characteristics, the structure is assumed to be infinitely long, and the fields at the input and the output end are not considered. In an actual pickup, some edge fields may appear and kill the travelling wave signal. The coupling impedance of the 20 cm long test piece installed in LEAR was measured with a 100 MeV/c and a 200 MeV/c beam. The measured impedance is a half of a theoretical value at 100 MeV/c, and a fourth at 200 MeV/c. This discrepancy could be attributed to the edge field effect. A new pair 60 cm long single couplers are now prepared and to be installed in LEAR. (Estimation of cooling time with this new pickup is presented in Appendix.) The measure-

ment with this long pickup will be useful to solve this problem; at a long pickup, the edge field effect will be smaller than the travelling wave signal. If it will be evident that the edge field effect spoils a 20 cm long coupler, a pickup of two pairs of 40 cm long couplers would be better.

The gain  $g_n$  discussed in this note is a relative value. To know the actual amplifier gain, we must express  $g_n$  with the transfer functions of the feedback system, i.e., pickup impedance, amplifier gain, kicker impedance, etc.. It is a subject of another note.

### Acknowledgment

The author thanks D. Möhl for his discussion and suggestion to improve this note.

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Table I. Summary of cooling time  $\tau_g$  ( $\sigma_g = 1/3$ ) for a beam of  $\Delta p_0/p_0 = \pm 3$  or  $\pm 6\%$ ,  $N = 1 \times 10^9$ ,  $\sqrt{\beta\epsilon} = 3\text{cm}$ , and  $T_{\text{amp}} = 100$  or  $400$  K. The values of bandwidth with "PK" are limited by the mixing between the pickup and the kicker, and those with "P" are limited by the pickup coupling impedance.

$L_{\text{PK}}$	Momentum (MeV/c)	Coupler configuration	$\Delta p_0/p_0$ (%)	W (MHz)	$T_{\text{amp}}=400\text{K}$	$T_{\text{amp}}=100\text{K}$
					$\tau_g$ (s)	$\tau_g$ (s)
11.3 m $\mu = 97.2$ deg $\sin\mu = 0.992$	60	4 × 20 cm	±3	142 (PK)	112 (0.90)	50 (0.70)
			±3	142 (PK)	73 (0.80)	39 (0.64)
		1 × 80 cm	±3	142 (PK)	61 (0.78)	35 (0.62)
			±6	70 (PK)	199 (0.83)	95 (0.70)
	100	4 × 20 cm	±3	168 (P)	106 (0.91)	42 (0.75)
			±6	118 (PK)	163 (0.90)	65 (0.75)
		2 × 40 cm	±3	97 (P)	241 (0.93)	86 (0.80)
			1 × 80 cm	±3	52 (P)	789 (0.95)
25.6 m $\mu = 292$ deg $\sin\mu = -0.927$	60	4 × 20 cm	±3	62 (PK)	933 (0.95)	302 (0.85)
			±3	62 (PK)	500 (0.91)	190 (0.77)
		1 × 80 cm	±3	62 (PK)	302 (0.90)	136 (0.70)
			±6	31 (PK)	1752 (0.95)	576 (0.84)
	100	4 × 20 cm	±3	104 (PK)	228 (0.91)	90 (0.75)
			±6	52 (PK)	1047 (0.95)	341 (0.85)
		2 × 40 cm	±3	97 (P)	326 (0.93)	117 (0.80)
			1 × 80 cm	±3	52 (P)	946 (0.95)

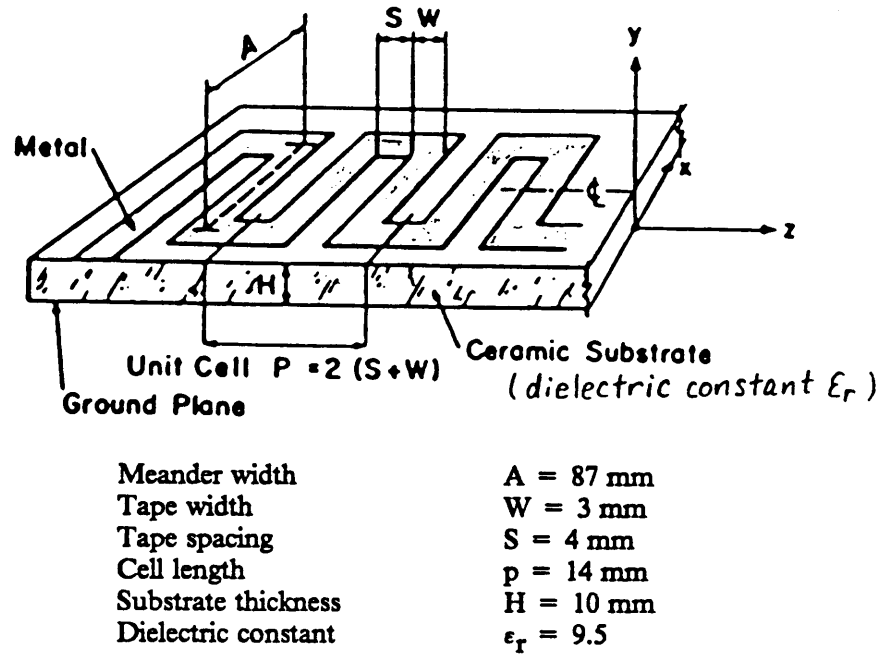


Fig. 1. Geometry of the meander coupler.

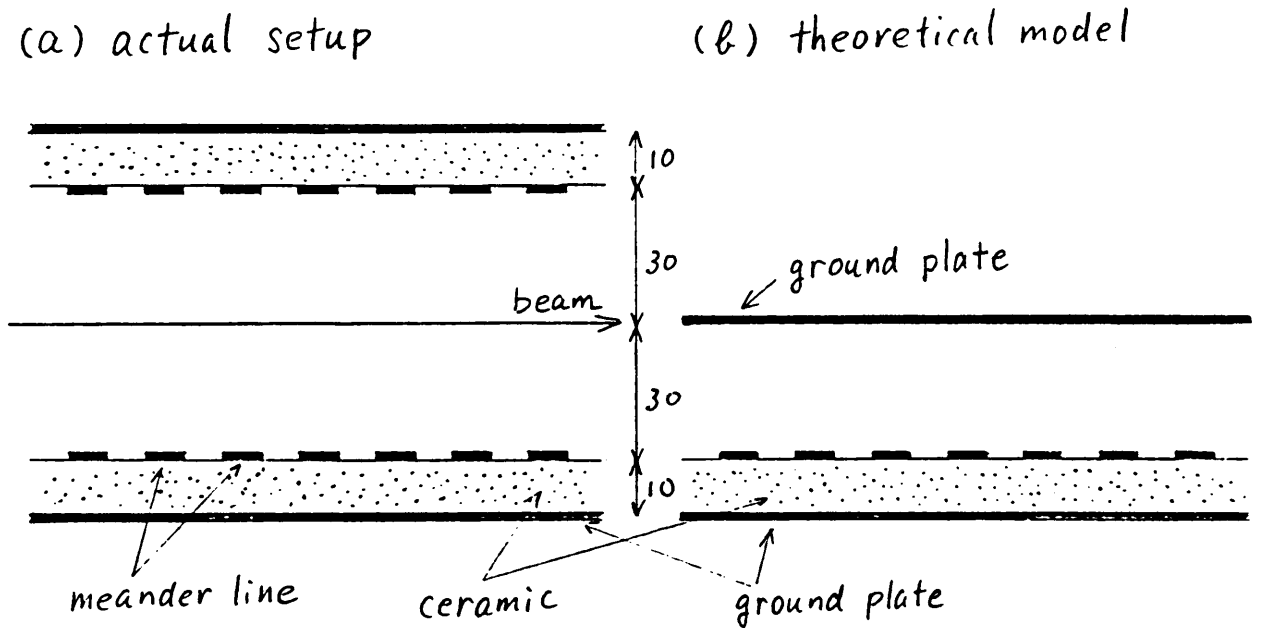
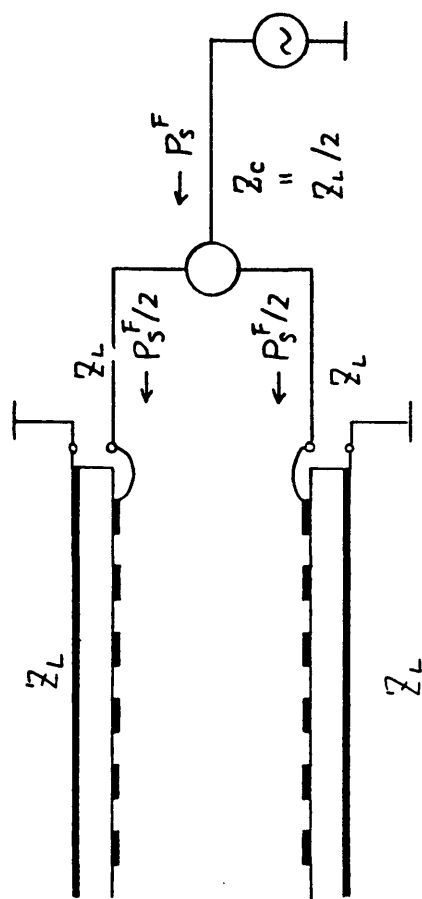
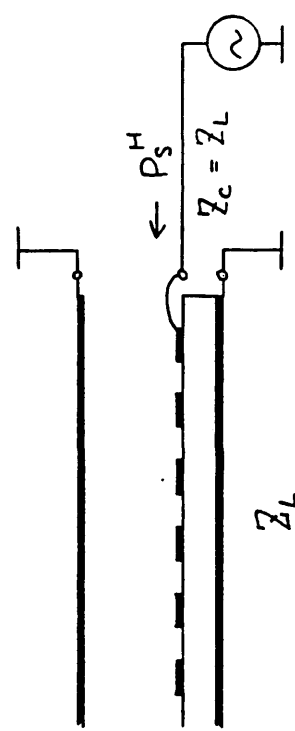


Fig. 2. (a) Actual setup of a meander pickup made up by two identical couplers sandwiching the beam, and (b) its theoretical model with a ground plate on the equilibrium orbit.



a) half geometry



b) full geometry

Fig. 3. Schematic diagrams for the application of the Lorentz reciprocity theorem. The coupling impedance is calculated for the half geometry and transformed to that for the full geometry.

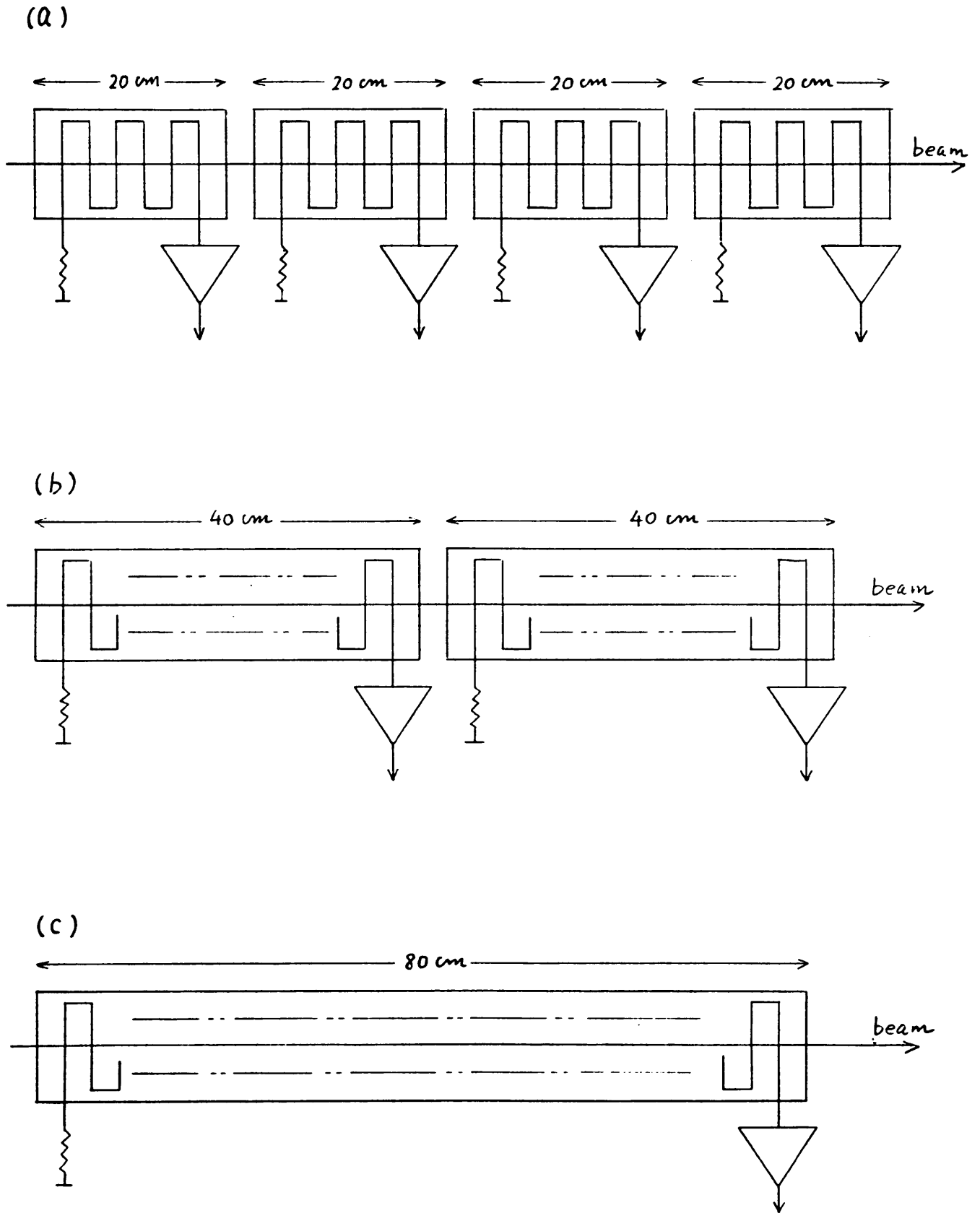


Fig. 4. Configurations of couplers.

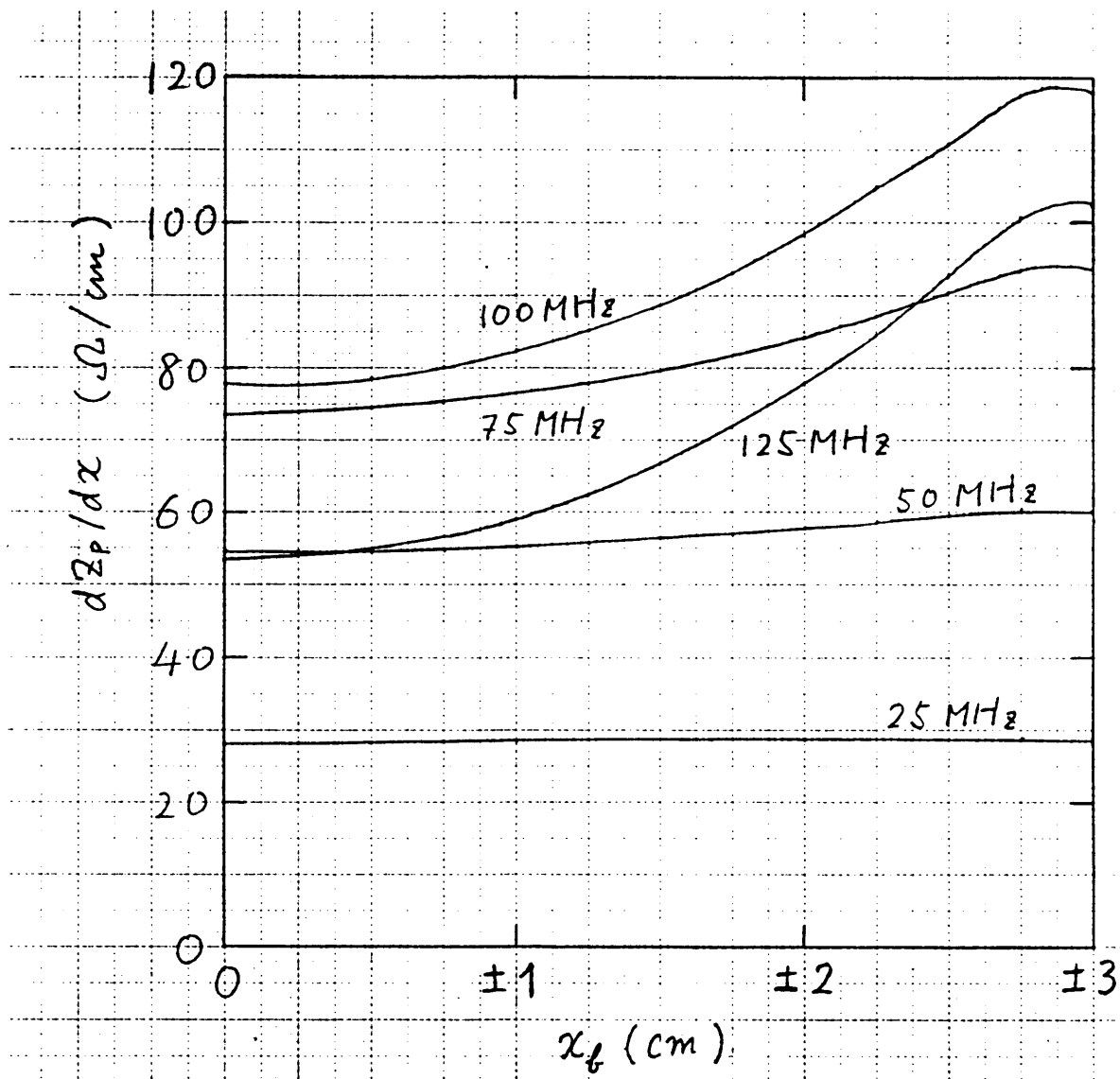


Fig. 5. Differential coupling impedance  $dZ_p/dx_b$  of a pickup consisting of a pair of 80 cm-long single couplers for a 60 MeV/c beam.

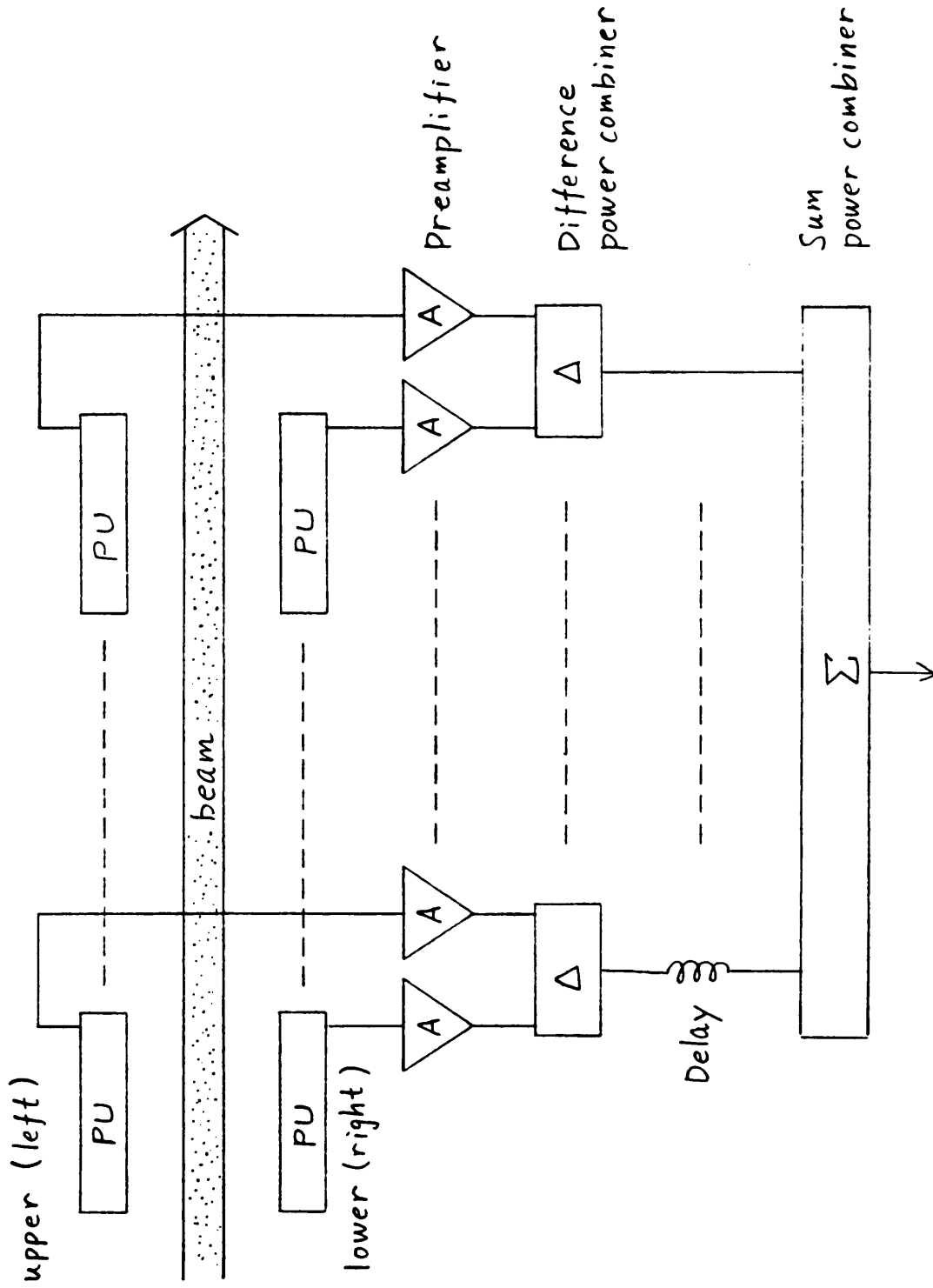


Fig. 6. Pickup system consisting of plural pairs of meander couplers, difference power combiners, delay lines, and a sum power combiner.



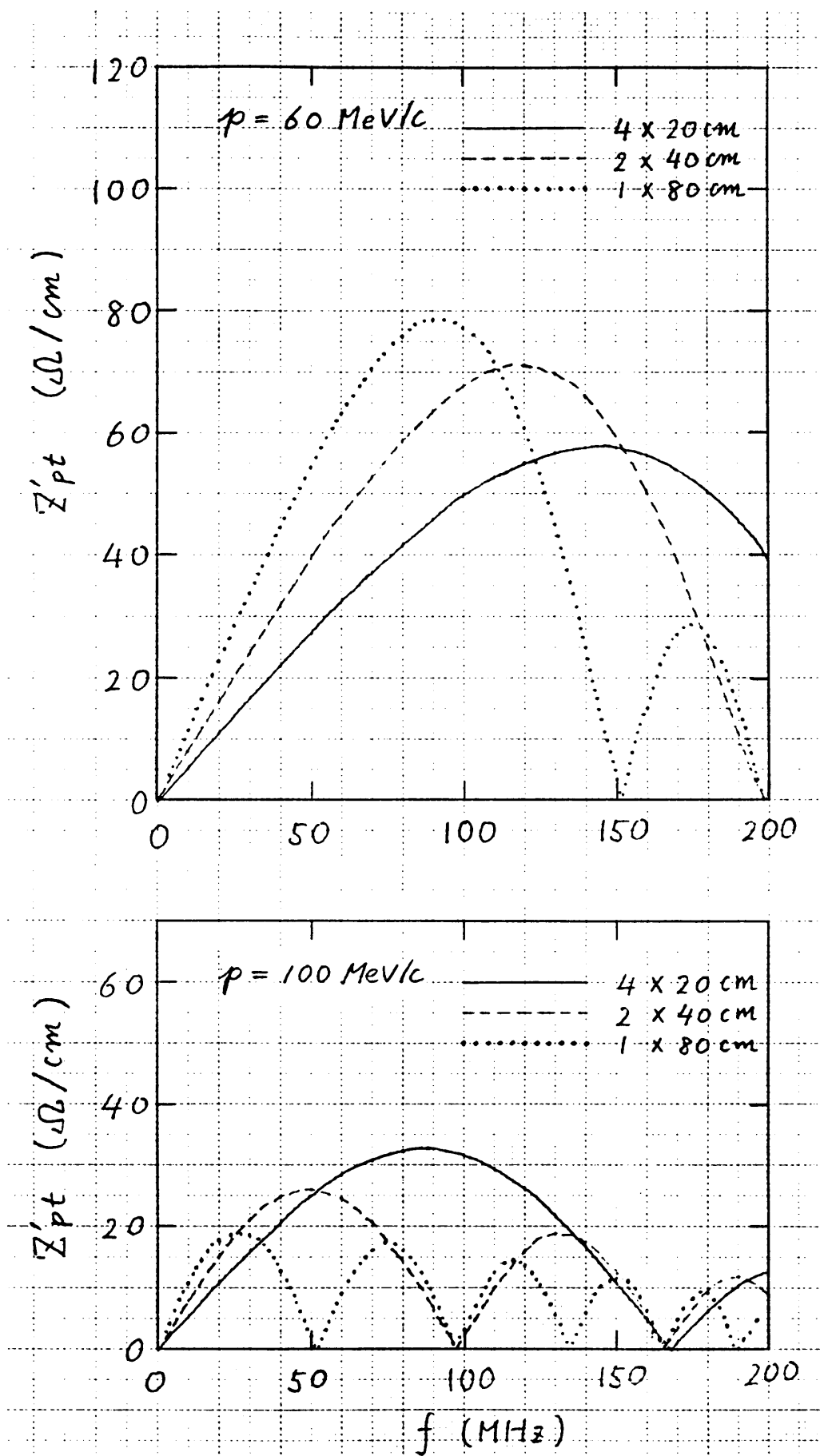


Fig. 7. Differential coupling impedance  $Z'_{pt}$  of the whole pickup system for a 60 MeV/c beam (top) and a 100 MeV/c one (bottom).

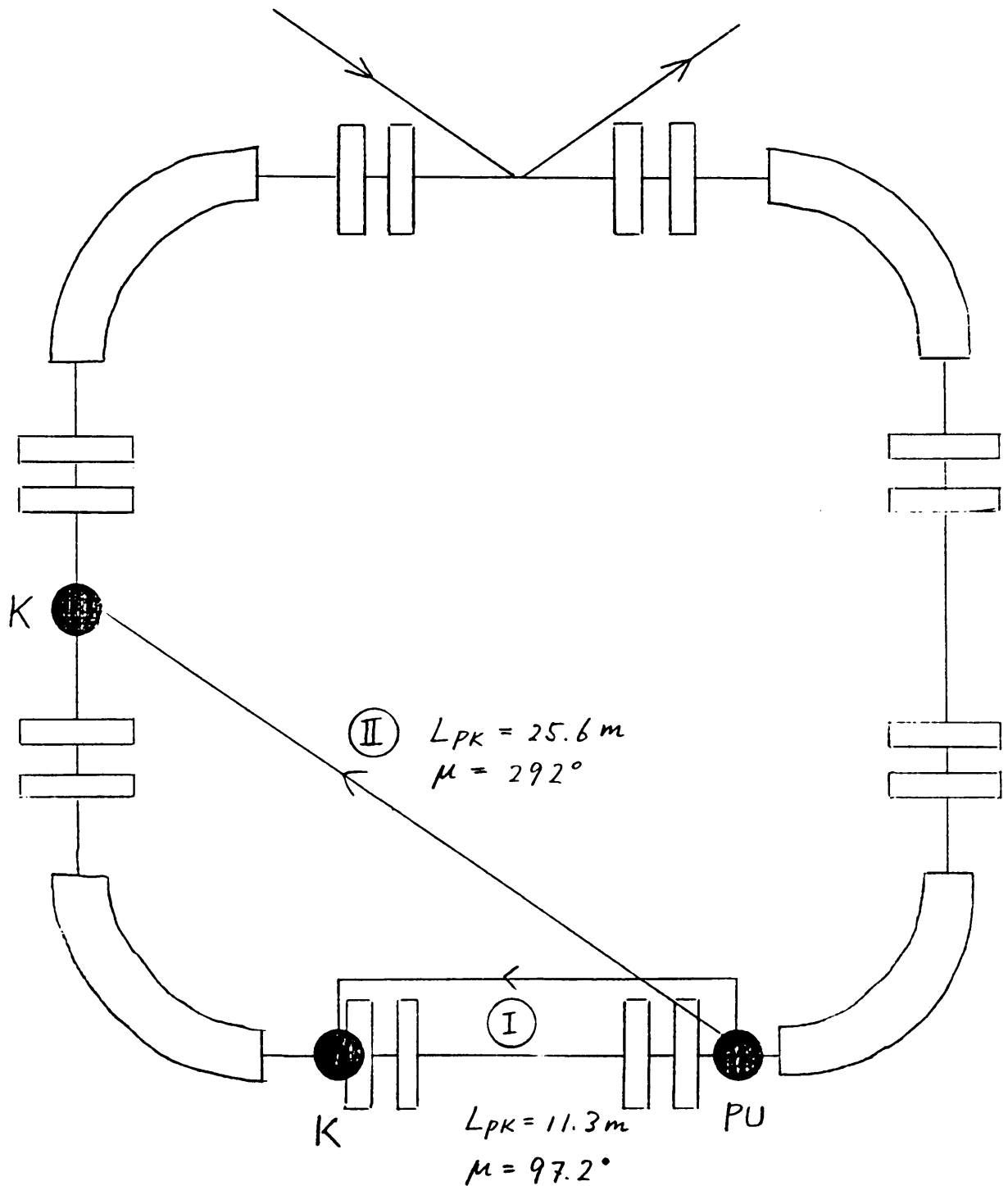


Fig. 8. Locations of the pickups and the kickers in LEAR. At the location I, the orbit length  $L_{PK}$  from the pickup to the kicker is 11.3 m, and phase advance  $\mu$  of betatron oscillation is  $97.2^\circ$  ( $\sin\mu = 0.992$ ); at the location II,  $L_{PK} = 25.6 \text{ m}$ , and  $\mu = 292^\circ$  ( $\sin\mu = -0.927$ ).

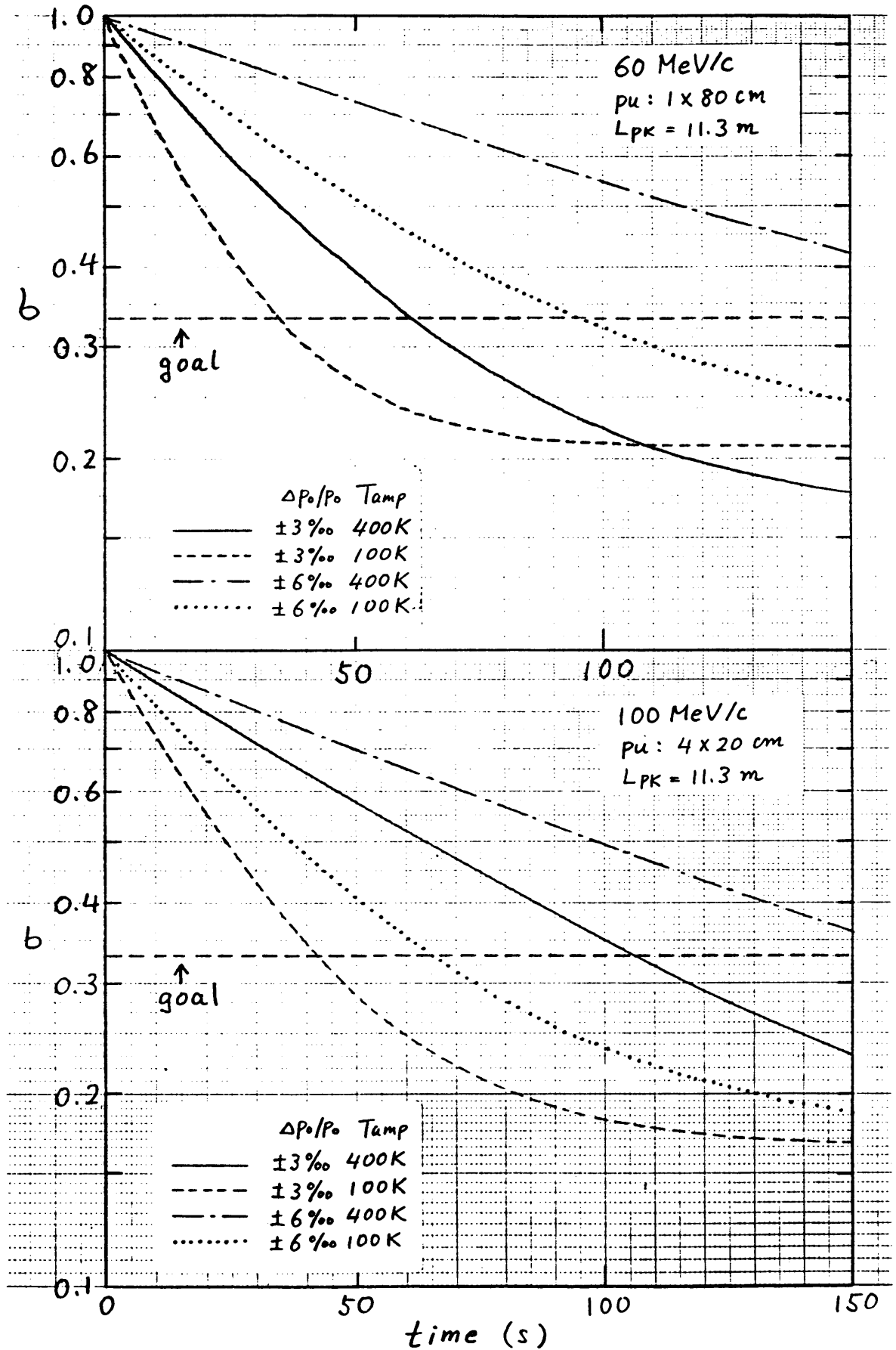


Fig. 9. Emittance decrease with time for a 60 MeV/c beam (top) and a 100 MeV/c one (bottom) under the condition of  $N = 1 \times 10^9$ ,  $\sqrt{\langle \beta \epsilon \rangle} = 3 \text{ cm}$ ,  $\Delta p_0/p_0 = \pm 3\text{‰}$ . The gain  $G$  is optimized to minimize the cooling time to attain the goaled emittance ( $\sigma_g = 0.33$ ).

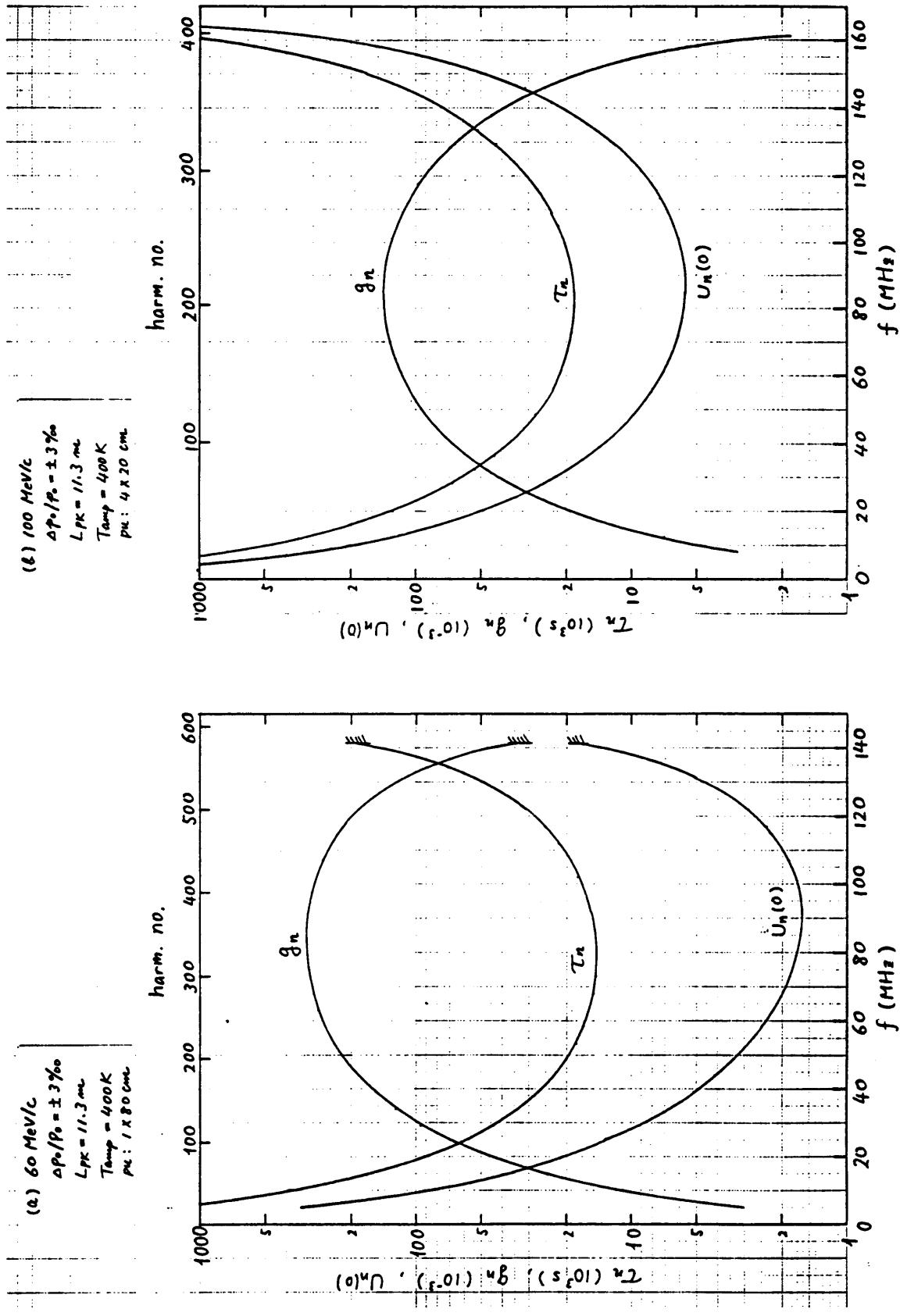


Fig. 10.  $\tau_n$ ,  $g_n$  and  $U_n(0)$  for the 60 MeV/c beam (a) and the 100 MeV/c one (b).

## APPENDIX

### COOLING TIME WITH A PAIR OF 60 CM LONG SINGLE COUPLERS

A pair of 60 cm long single couplers are installed in LEAR in July of 1987. The geometry, except the length, of the meander coupler is same as that in the text. The cooling time is estimated, and the result is summarized in Table AI and Figs. A1 and A2.

Table AI. Summary of cooling time  $\tau_g$  ( $\sigma_g = 1/3$ ) for a pair of 60 cm long single couplers. (cf. Table I in the text.)

$L_{PK}$	Momentum (MeV/c)	$\Delta p_0/p_0$ (%)	W (MHz)	$T_{amp} = 400K$	$T_{amp} = 100K$
				$\tau_g$ (G) (s)	$\tau_g$ (G) (s)
11.3 m $\mu = 97.2$ deg $\sin\mu = 0.992$	60	$\pm 3$	142 (PK)	77 (0.82)	39 (0.65)
		$\pm 6$	71 (PK)	305 (0.90)	125 (0.74)
	100	$\pm 3$	69 (P)	593 (0.96)	188 (0.90)
		$\pm 6$	69 (P)	622 (0.96)	192 (0.90)
25.6 m $\mu = 292$ deg $\sin\mu = -0.927$	60	$\pm 3$	62 (PK)	474 (0.91)	183 (0.76)
		$\pm 6$	31 (PK)	2643 (0.97)	783 (0.90)
	100	$\pm 3$	69 (P)	738 (0.96)	235 (0.90)
		$\pm 6$	52 (PK)	1028 (0.96)	319 (0.90)

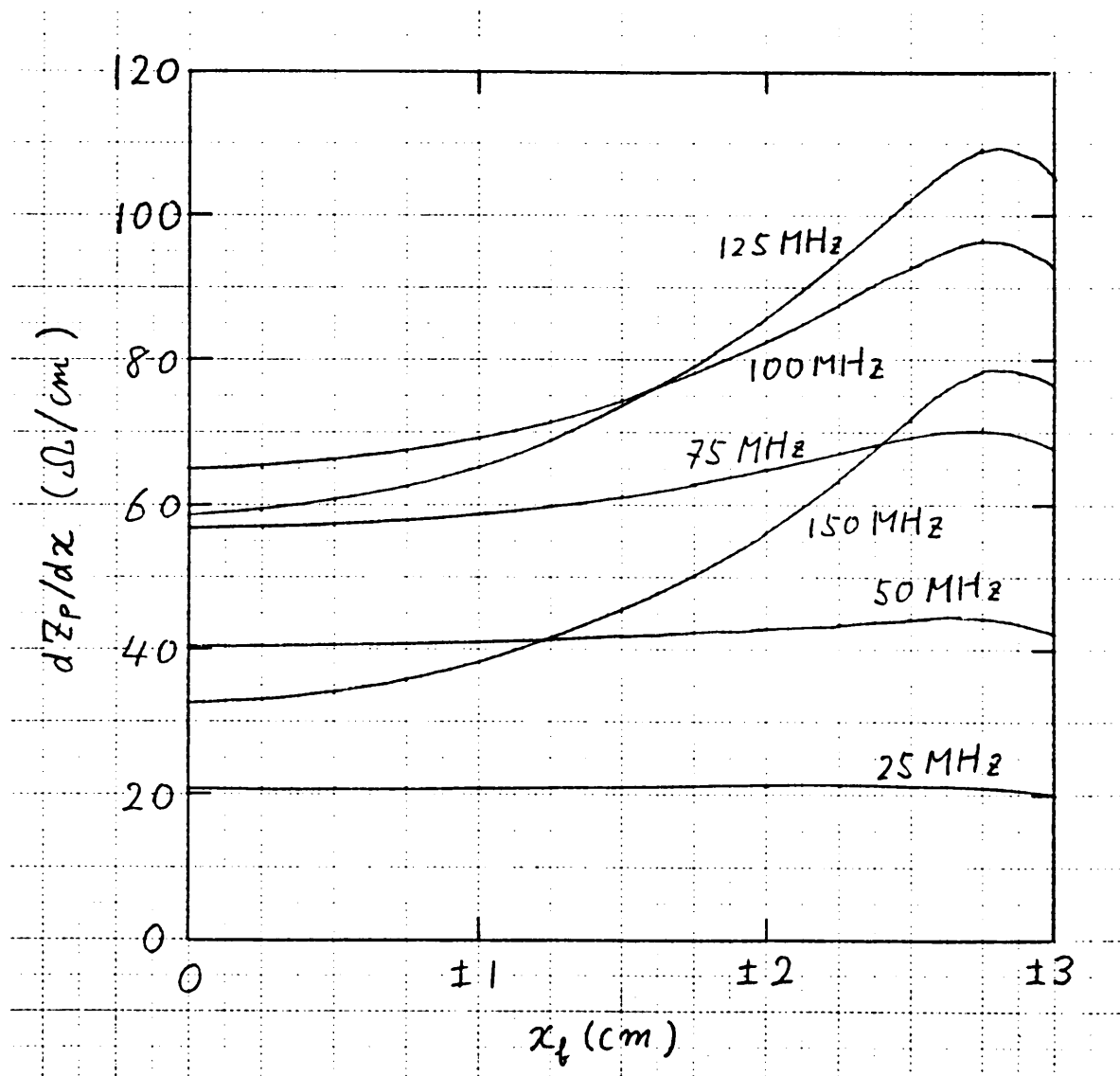


Fig. A1. Differential coupling impedance  $dZ_p/dx_b$  of a pair of 60 cm-long single couplers for a 60 MeV/c beam (cf. Fig. 5).

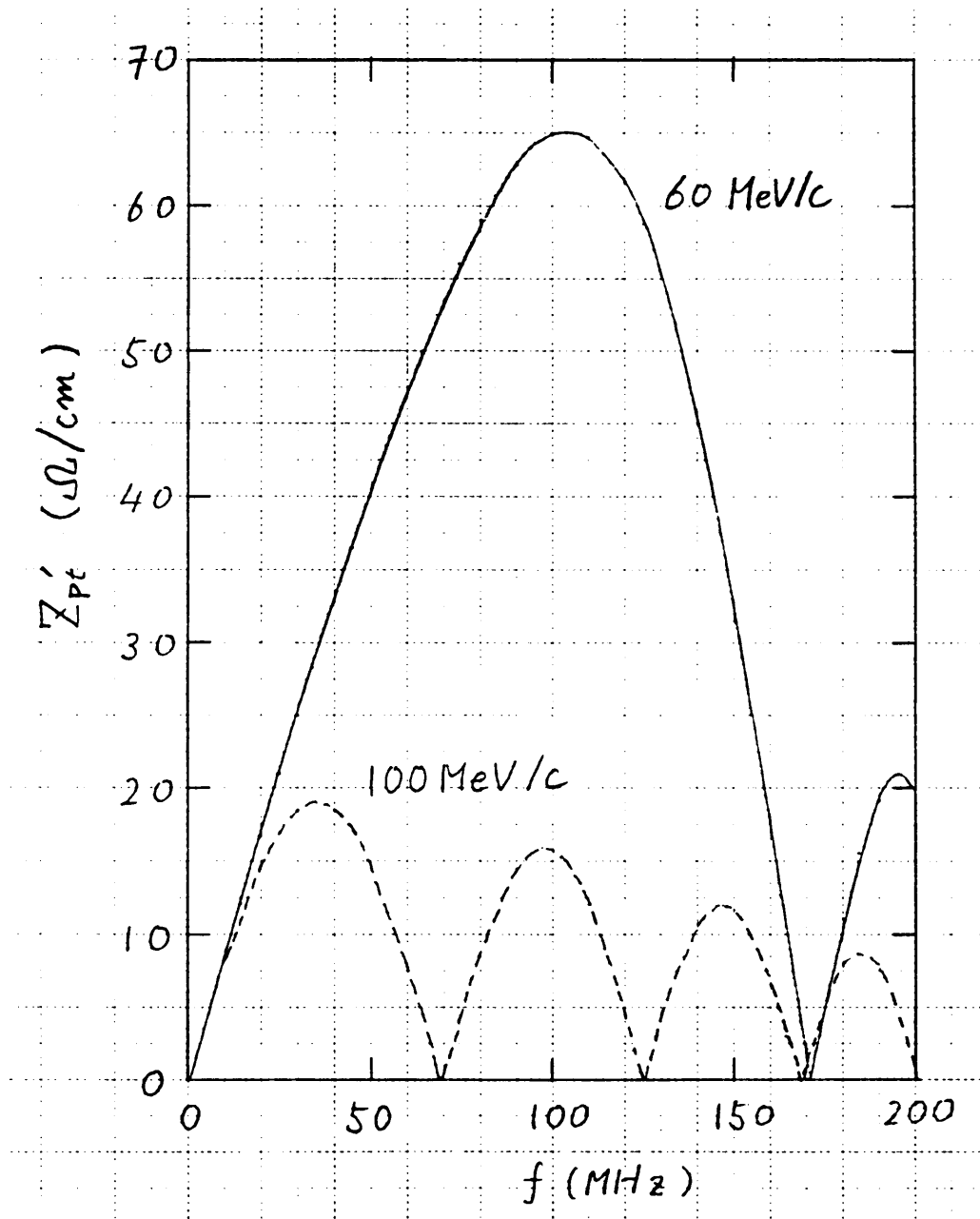


Fig. A2. Differential coupling impedance  $Z'_{pt}$  of a pair of 60 cm long single couplers (cf. Fig. 7).