



Sub-10 ps Minimum Ionizing Particle Detection With Geiger-Mode APDs

Francesco Gramuglia^{1†*}, Emanuele Ripiccini^{1†}, Carlo Alberto Fenoglio¹, Ming-Lo Wu¹, Lorenzo Paolozzi^{2,3}, Claudio Bruschini^{1‡} and Edoardo Charbon^{1‡}

¹Advanced Quantum Architecture Laboratory, Ecole Polytechnique Fédérale de Lausanne (EPFL), Neuchâtel, Switzerland,

²Département de Physique Nucléaire et Corpusculaire, Université de Genève, Geneva, Switzerland, ³European Organization for Nuclear Research, CERN, Meyrin, Switzerland

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*Correspondence:

Francesco Gramuglia
Francesco.gramuglia@epfl.ch

[†]These authors share the first
authorship

[‡]These authors share the last
authorship

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Major advances in silicon pixel detectors, with outstanding timing performance, have recently attracted significant attention in the community. In this work we present and discuss the use of state-of-the-art Geiger-mode APDs, also known as single-photon avalanche diodes (SPADs), for the detection of minimum ionizing particles (MIPs) with best-in-class timing resolution. The SPADs were implemented in standard CMOS technology and integrated with on-chip quenching and recharge circuitry. Two devices in coincidence allowed to measure the time-of-flight of 180 GeV/c momentum pions with a coincidence time resolution of 22 ps FWHM (9.4 ps Gaussian sigma). Radiation hardness measurements, also presented here, highlight the suitability of this family of devices for a wide range of high energy physics (HEP) applications.

Keywords: avalanche photodiode, beamline, particles, sensor, time-of-flight

1 INTRODUCTION

1.1 High Timing Resolution With Silicon Pixel Detectors

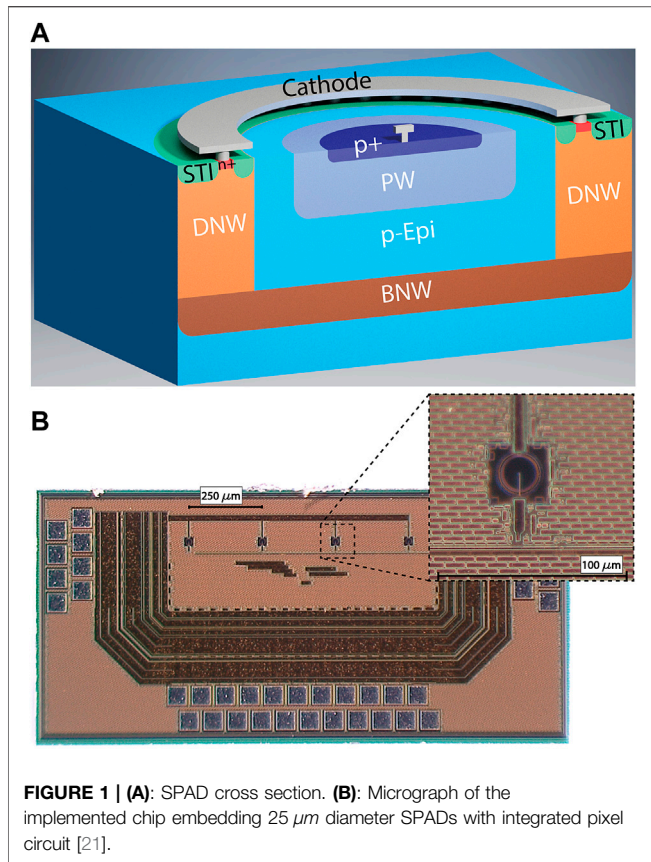
Silicon pixel detectors have been developed in high-energy physics applications to provide precise position measurements thanks to their compactness and high spatial granularity. Recent developments have been focused on sub-100 ps timing measurements of optical photons and direct detection of charged particles.

When a particle passes through the detector, electron-hole pairs are generated. When these charges move in the depletion region, an induced current pulse is registered on one electrode. According to the Shockley-Ramo theorem [1, 2], this current is proportional to the free charge Q , to the speed of the charge carriers v , and to the weighting field, which can be expressed, to a first approximation, as $\frac{1}{d}$, where d is the thickness of the depletion region. Hence, we can calculate the induced current as:

$$i = kQv \frac{1}{d} \quad (1)$$

where k is a proportionality factor. The signal ends when all charges have been collected. Moreover, in case of a minimum ionizing particle (MIP) crossing a thin device, the charge Q is proportional to d . We thus have:

$$i = kNd v \frac{1}{d} = kNv, \quad (2)$$



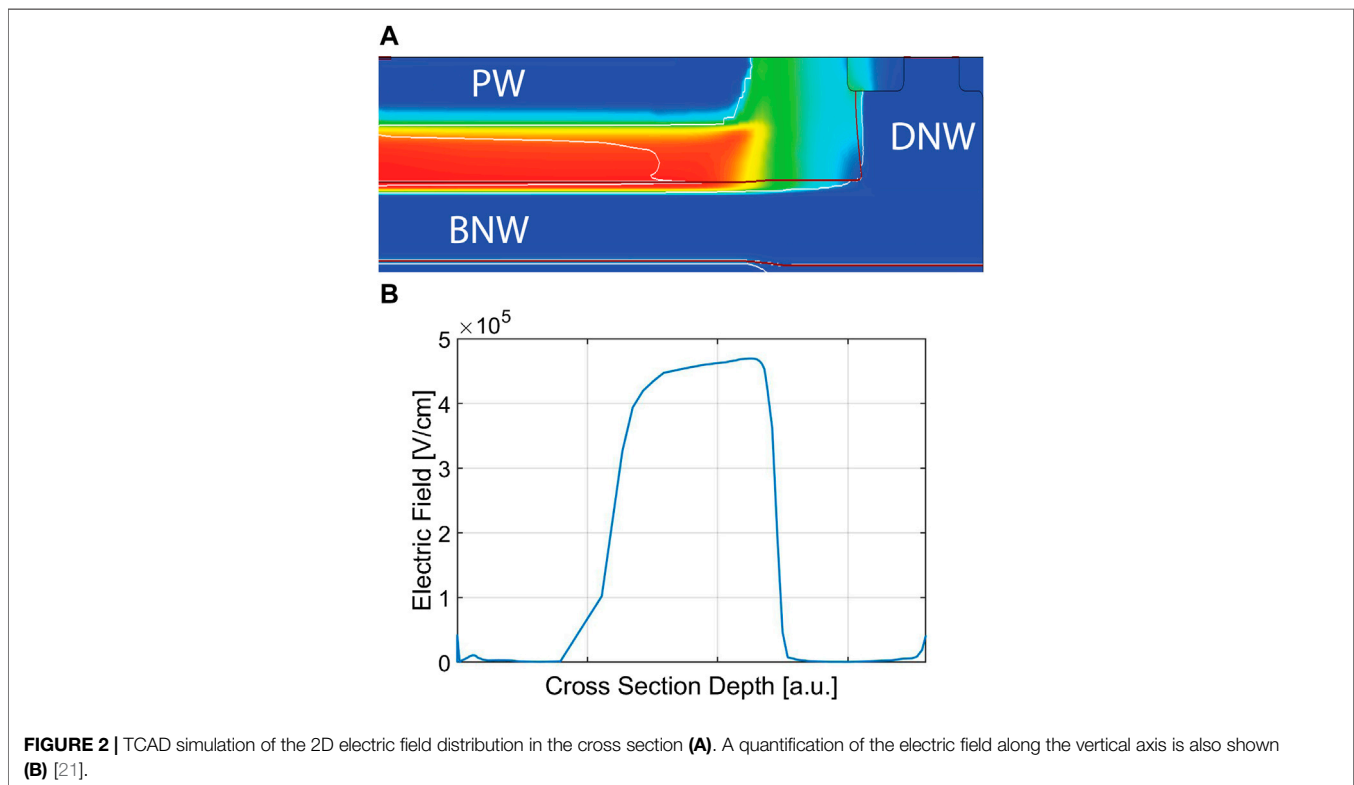
where N is the number of electron-hole pairs generated per unit length. This result shows that the initial value of the induced current is constant and does not depend on the thickness of the depletion region. When reading out this current signal on a load, behaving like an ideal transimpedance amplifier, we observe a sharp voltage pulse. The time-of-arrival of the charge is usually determined by comparing the voltage pulse with a threshold. The uncertainty of the voltage pulse σ_V is expressed as:

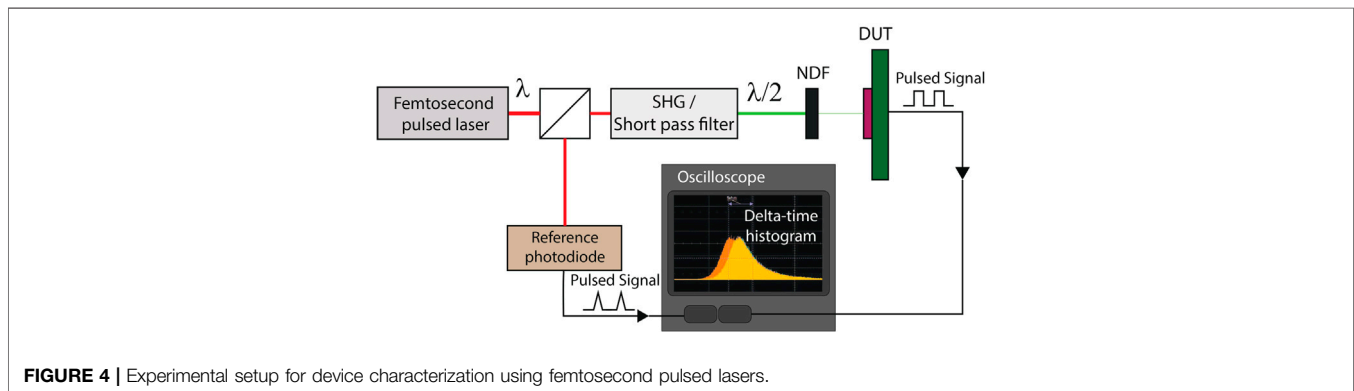
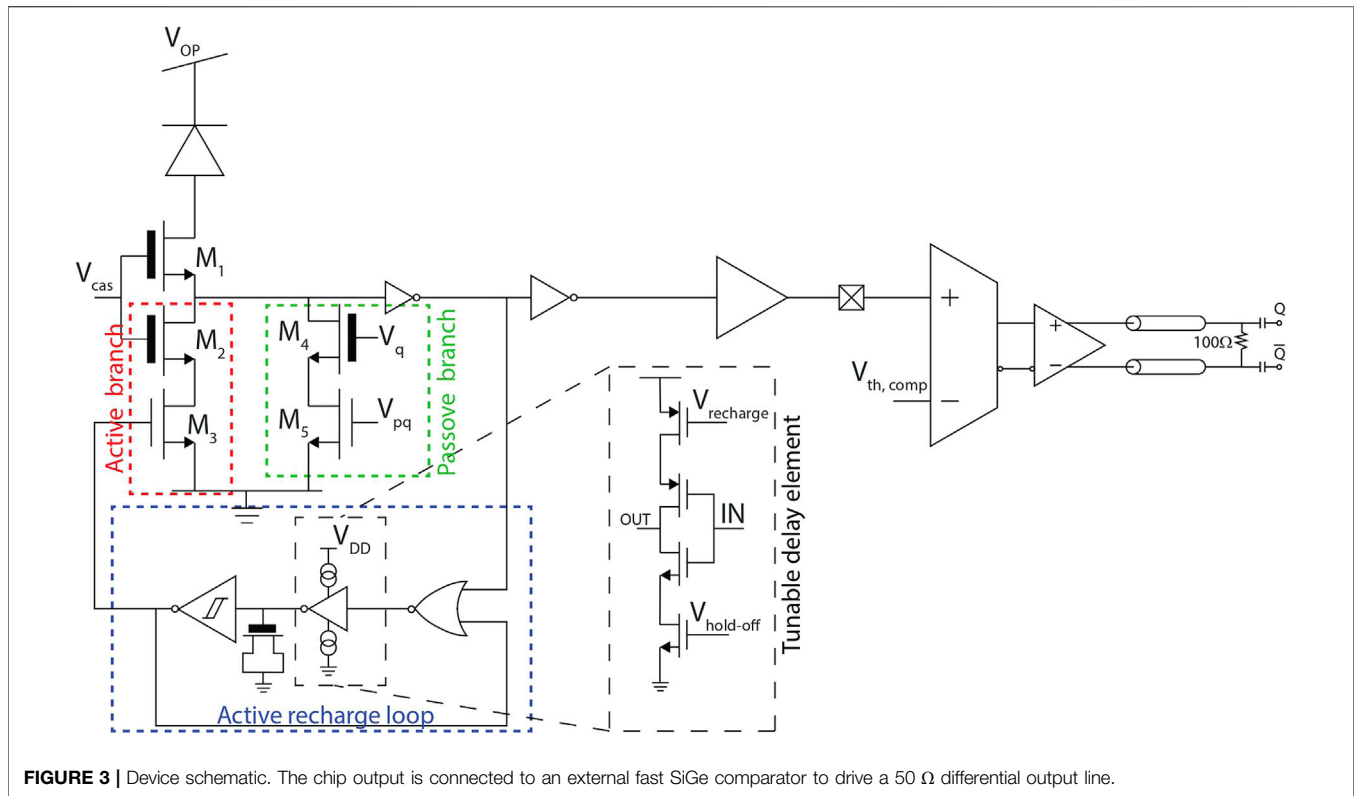
$$\sigma_V = \sigma_t \frac{dV}{dt}, \quad (3)$$

where σ_t is the timing jitter of the voltage pulse. By inverting Eq. 3, we find that:

$$\sigma_t = \frac{\sigma_V}{\frac{dV}{dt}}. \quad (4)$$

Equation 4 shows that the signal fluctuation (σ_V) should be reduced to achieve a better timing jitter σ_t and the slew rate $\frac{dV}{dt}$ should be maximized. In case of a sensor with an internal finite gain G [3–5], the slew rate is proportional to $\frac{G}{d}$. This analysis, where low gain avalanche diode (LGAD) concept is introduced, suggests that thin sensors with large internal gain will, in principle, result in a better timing jitter. As the LGAD signal needs amplification, the detector capacitance becomes crucial for the timing jitter. As reported in [6], a timing resolution of 16 ps has been achieved with a 45 μm thick and 1.7 mm^2 area LGAD. There is, however, another effect that can significantly affect the pulse shape while detecting MIPs: the charge collection noise. This phenomenon is caused by the



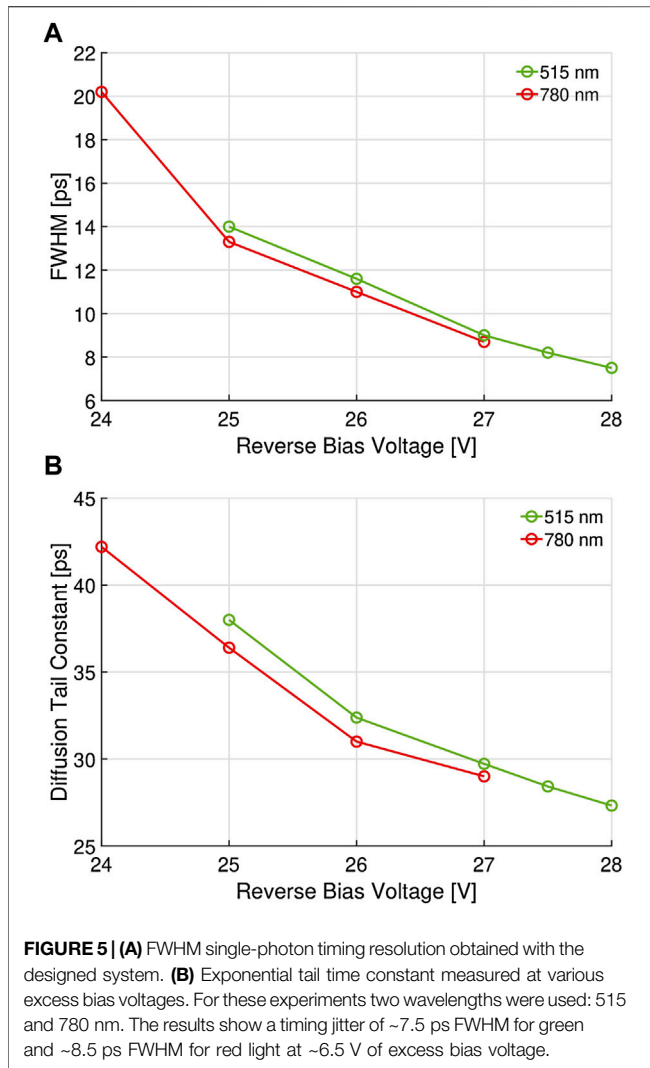


variability of the profile of the deposited charge. As shown in [7], this effect introduces a timing jitter that is non-negligible at the 10 ps scale, and which increases with the detector thickness [8]. Various solutions have been proposed to reduce the contribution of this additional source of timing jitter, such as the detectors reported in [5, 9, 10].

All the effects mentioned above call for extremely high intrinsic gain and slew rate together with thin structures. Thus, Geiger-mode silicon APDs (i.e., devices biased above breakdown), also known as single-photon avalanche diodes (SPADs), could represent promising candidates for substantial timing jitter reduction [11]. In SPADs, unlike APDs, the

avalanche is a self-sustaining process, and the timing jitter contributions are more related to the avalanche growth dynamics. In particular, the timing jitter improves, decreasing the avalanche current value needed by the frontend electronics to detect a pulse [12]. A comprehensive theoretical study of timing performance in SPADs when used in MIP detection is presented in [13]. First examples of such systems, detailed in [14–16], were following the concept proposed by [17].

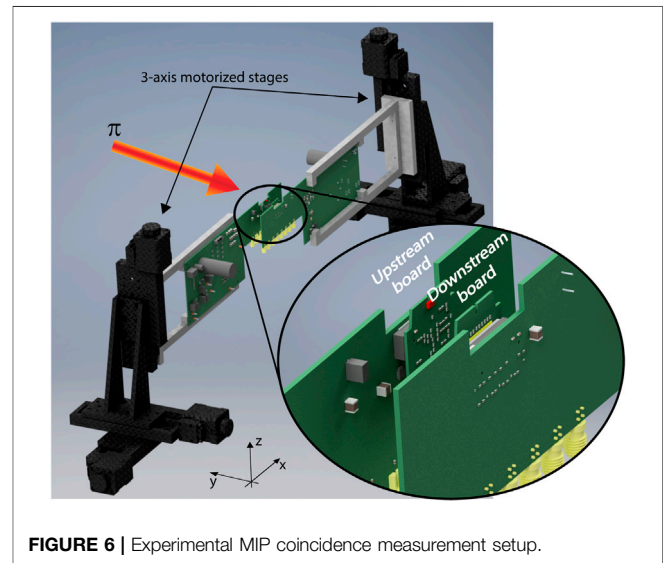
Although these potential advantages are promising, some problems usually affect Geiger-mode devices in the framework of MIP detection. Indeed, typical SPADs have a long dead time if no properly designed active quenching and recharge techniques



are used [18]. Another issue is the presence of noise in the form of spurious pulses even in the dark. This noise, known as dark count rate (DCR), could limit the suitability of SPADs for the target application because of significant degradation of the measurement signal-to-noise ratio (SNR). However, as shown by [19, 20], DCR can be drastically reduced by detecting MIPs with two SPADs operated in coincidence. Building on these elements, we present MIP time-of-flight (ToF) measurements resulting in unprecedented timing precision.

1.2 Single-Photon Avalanche Diodes Detector and System-On-Board

The detector system used in this work relies on the SPAD-based sensor presented in [21]. This device's cross-section is based on a substrate-isolated type, where a *p*-well (*PW*) layer forms the anode of the SPAD and a *buried n*-well (*BNW*) layer creates the cathode contact. The latter is connected to the high voltage through a *deep-n*-well (*DNW*). The SPAD presents a *p-i-n* structure [21]. **Figure 1A** shows the cross-



section of the SPAD, while **Figure 1B** shows a micrograph of the sensor used in this study. The guard ring has a virtual design and employs a low doping *p-Epi* region located between the *PW* and the *DNW* contact to smooth the doping transition and lower the electric field. Thus, a *p-Epi* layer between anode and cathode allows a relatively extended and uniform high-field region (**Figure 2A**).

The sensor integrates four independent SPAD pixels with a diameter of $25 \mu\text{m}$. A dedicated on-chip front-end circuitry, shown in **Figure 3**, is implemented in close proximity to each SPAD. In the SPAD front-end circuit (see **Figure 3**) the cascode transistor M_1 is used as a resistive divider and voltage clamp, along with M_2 to enable high excess bias. This comes in combination with thin-oxide MOS transistors in the remainder of the front-end to improve the timing performance. M_2 and M_3 form the active recharge branch, turned on by the feedback loop composed by the NOR gate, Schmitt trigger, and tunable delay element (see **Figure 3 right**). The circuit is designed to enable a tunable dead time, as short as 3 ns, supporting very high count rates while still maintaining very low afterpulsing [21]. Concerning the leakage current for this detector, as reported in [21], the measured value is on the order of 0.1–1 pA, which corresponds to a value of about $0.4\text{--}4 \text{ fA}/\mu\text{m}^2$.

In this work, we implemented a complete and optimized system-on-board to further improve performance. The resulting system comprises a motherboard, where all needed voltage levels are derived from a single 5 V power supply. A power management unit was designed to filter most of the electronic noise and to provide low-noise and stable voltage levels to the detector and its front-end circuits. Moreover, the full integration of a system-on-board reduces the noise picked up in cables and power cords that can act as antennas. Indeed, reducing the noise in the system is essential when the target timing precision approaches 10 ps [3]. A full system control is

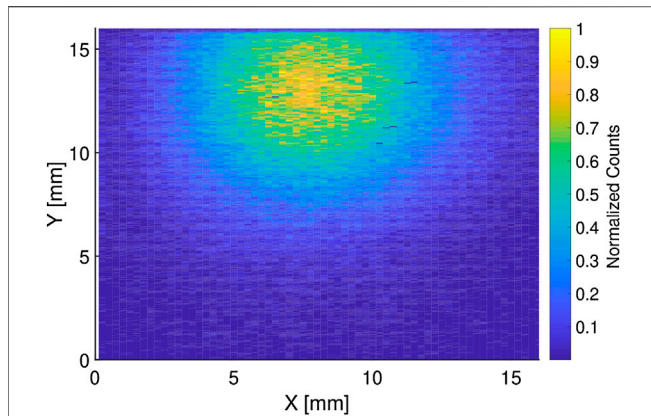


FIGURE 7 | MIP beam profile acquired with the HVC MOS telescope described in [26].

TABLE 1 | Summary of the MIP detection measurement results. The Gaussian sigma has been obtained by dividing the FWHM by $2\sqrt{2\ln(2)}$. Assuming that the response is the same for both SPADs, the σ_{single} values have been obtained by dividing the σ values by $\sqrt{2}$. The errors have been evaluated using statistical error propagation.

Bias (V)	FWHM (ps)	FWTM (ps)	σ (ps)	σ_{single} (ps)
24	27 ± 1	104 ± 4	11.5 ± 0.4	8.1 ± 0.3
27	22 ± 2	62 ± 3	9.4 ± 0.7	6.6 ± 0.5

the chip's output (high impedance node) and helps propagate the signal through a high-frequency cable to the timestamping electronics. In addition, the use of these comparators makes it possible to achieve high signal slew rate (≥ 1.6 V/ns).

2 OPTICAL DEVICE CHARACTERIZATION

In order to analyze the performance of our system, we started from an optical characterization using the setup in **Figure 4** [21, 22]. The test bench is composed of a femtosecond pulsed laser used as the controlled light source, making the pulse length contribution to the measured timing jitter negligible. The laser beam is split into two branches. One branch is captured by a fast photodiode used as an optical, rather than electrical, reference to ensure that the dominant jitter is that of the device under test (DUT). The other branch passes through a second harmonic generation (SHG) stage to generate a light pulse in the visible range (i.e., within our device sensitivity spectrum). The latter is then attenuated, employing a neutral density filter (NDF) to reach a single-photon regime, and sent to the DUT. Finally, the output signals of the photodiode and the DUT are connected to an oscilloscope to build a time-difference histogram, representing the instrument response function (IRF). An asymmetric curve characterizes the typical SPAD IRF with the main peak, generally modeled with a Gaussian profile and an exponential tail [23–25].

The experiment has been repeated for several excess bias voltages and two wavelengths, and the results are shown in **Figure 5**. The timing results are expressed as FWHM of the IRF. The timing precision shows a dependency on the bias point, and it improves when increasing the applied voltage, as expected. With this improved system, we reached a timing jitter of 7.5 ps at a reverse bias voltage of 28 V, corresponding to an excess bias (V_{ex}) of about 6.5 V. Moreover, we report in **Figure 5B** the decay time constant of the exponential tail again as a function of reverse bias voltage. These results show an improvement of almost 40% with respect to what reported in [21], where the output was directly taken from the packaged die with high impedance 4 GHz active probes. This optical characterization provides us with an estimation of the system performance when detecting a MIP. Indeed, the mean free path of a MIP in silicon is on the order of hundreds of nanometers. Therefore, considering the thin structure of the proposed

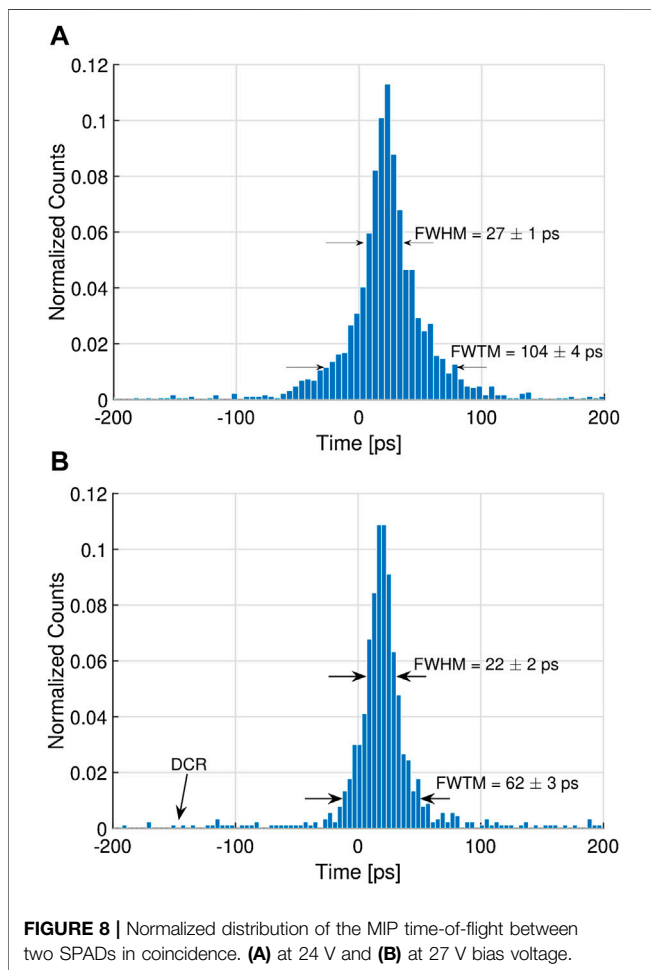
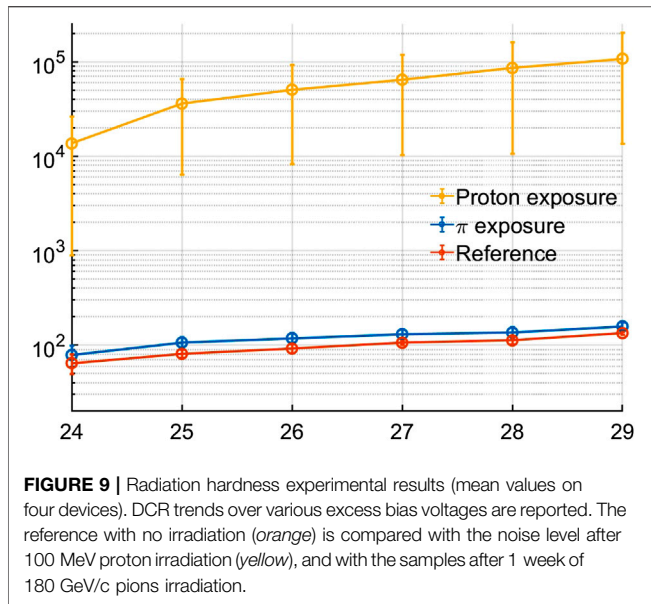


FIGURE 8 | Normalized distribution of the MIP time-of-flight between two SPADs in coincidence. (A) at 24 V and (B) at 27 V bias voltage.

achieved with a serial bus interface that allows the tuning of the device operating point from an host computer.

The output of the chip is connected to fast SiGe comparators (Analog Device ADCMP572) that drive 50 Ω lines (**Figure 3**). This solution reduces the capacitive load at



SPADs, we expect the generation of a small amount of primary charge inside the device sensitive volume. Moreover, Geiger-mode operation and a prompt avalanche detection ensure that the output signal is the same when detecting single photons or MIPs.

3 TIME-OF-FLIGHT MEASUREMENTS FOR MINIMUM IONIZING PARTICLES

The setup used for the ToF measurement of MIPs is shown in **Figure 6**. It consists of two systems-on-board (see **Section 1.2**), both mounted on motorized linear stages with sub-micrometer positioning resolution to allow a proper detector alignment and to guarantee the acquisition of coincidence measurements. We installed the setup on the H8 beamline in the CERN North Area. This beamline delivers 180 GeV/c momentum pions produced on a graphite target by the interaction of protons accelerated by the Super Proton Synchrotron (SPS).

The beam profile measurement is reported in **Figure 7**. A good alignment between the two detectors has been achieved thanks to an HVCMOS telescope [26]. The two detectors were positioned at the center of the beam, where the intensity is the highest. Coincidence events were acquired for two bias voltages, 24 and 27 V, corresponding to approximately 2.5 and 5.5 V V_{ex} , respectively. **Figure 8** shows the ToF distributions for both V_{ex} . The MIP measurement results are summarized in **Table 1**.

4 RADIATION HARDNESS

The radiation hardness of the SPAD detectors was characterized by using protons to induce ionizing damage and, more importantly, displacement damage, which causes structural permanent defects [27, 28]. The detectors were irradiated

using the Proton Irradiation Facility (PIF) at the Paul Scherrer Institute (PSI, Villigen, Switzerland). We used a 100 MeV mono-energetic beam with a fluence of 1×10^8 protons per second to reach a 300 TeV/g displacement damage dose (DDD) and 9.4 krad total ionizing dose (TID). The DCR difference was measured 2 weeks after the exposure with the aforementioned setup. The DCR comparison before and after the exposure is reported in **Figure 9**. The characterization of the radiation hardness shows that the SPAD detector can maintain its functionality under the given radiation dose. The SPADs are not saturated by the DCR induced by the radiation damage thanks to their short dead time and high count rate. Moreover, as the ToF measurement is based on coincidence, even detectors reaching a DCR value of 1×10^5 counts per second will not affect their particle detection performance, as also shown in [19, 20]. No other degradation of the device performance was observed.

5 DISCUSSION

In this work we showed how Geiger-mode devices (i.e., SPADs) can detect MIPs with a sub-10 ps timing precision. This result paves the way to the implementation of future high timing resolution particle trackers based on this kind of detector. Moreover, the radiation hardness of the device was explored up to a DDD of 300 TeV/g. After exposure, DCR increased by about three orders of magnitude, which is comparable with [29]. Nevertheless, this increment does not affect the timing performance of the device and does not cause the saturation of its output, thanks to the short dead time of 3 ns guaranteed by the integrated pixel circuit on-chip. In addition, while detecting charged particles on a beamline, the number of accidental coincidences due to DCR is strongly suppressed by the logic AND between the two SPADs used for the ToF measurement [19]. As shown in **Section 1.2**, in the proposed SPAD, the electric field is designed in order to have a uniform profile within the entire intrinsic layer, representing the multiplication region. Moreover, the small thickness of the charge collector region significantly reduces the charge collection noise. These two device features together with an improved front-end circuit and a maximization of the signal slew-rate are crucial when targeting sub-10 ps timing resolution.

When analyzing **Figure 8** and the results in **Table 1**, we notice a dependency of the performance on the applied bias voltage. In particular, we can see a lower FWTM (full width at tenth maximum) and an improvement in the FWHM for the ToF distribution when increasing the bias point from 24 to 27 V. The higher field improves the avalanche buildup and lateral spread time dispersion [30–32]. Moreover, a higher bias voltage enlarges the drift region and increases the electric field inside it. This effect reduces the size of the neutral region and helps minimize the statistical spread of the diffusion and transit time needed by the primary charge carriers to reach the multiplication region [11].

Both distributions show a negligible flat background coming from random dark count coincidences. This is indicative of the efficacy of the noise filtering provided by measurements in coincidence.

AUTHOR CONTRIBUTIONS

FG: Chip and board design, optical measurements, beam time measurements, data analysis, paper writing ER: ToF measurement with SPADs proposal, mechanical integration, data analysis, beam time measurements, paper writing CAF: Optical measurements, beam time measurements, data analysis, paper writing M-LW: radiation hardness measurements, data analysis, paper writing LP: Operation of the HV-CMOS telescope for SPADs alignment on beam, paper reviewing EC: Supervision, funding acquisition, paper reviewing CB: Supervision, funding acquisition, paper reviewing.

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