

PS/LPI Note 85-37
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EPA LATTICE MATCHING

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1. INTRODUCTION

During the design [1], the EPA lattice was optimized to fulfill the numerous constraints by using all the available parameters, mainly the positions and strengths of the quadrupoles and bending magnets.

Once the machine is built, the number of available parameters shrinks to the strength of the lattice quadrupole magnets only. In EPA, they are split in four families powered by four independent power supplies: HR.QFW, HR.QFL, HR.QFN, HR.QDN.

- Nevertheless, an operational machine needs some flexibility in order to:
- move it's transversal tunes Q_x, Q_y ,
 - adapt to different working energies where the characteristics of some elements can change mainly due to magnetic fields saturation effects.

This is the reason why an extra trimming quadrupole family, HR.QTR, has been introduced at the optimum location [2], and the highly saturated bending magnets tracked [3] then modelled [4].

In addition, due to space problems around the injection area, four over twelve quadrupoles of the HR.QFN family were replaced by another quadrupole type using an independent power supply, HR.QFI, but breaking the nice lattice symmetry (fig.1).

The goal of this note is to check the proposed matching method to serve as a basis for the on-line Configuration Update program, which as a part of the Modelling applications [5] will be used in operation to modify the EPA configuration.

2. CONSTRAINTS

With the small number of parameters available, all the numerous design constraints cannot be completely fulfilled but can be set in order of preference [6]:

- big axis symmetry: two identical cells
- transversal tunes: overall phase advances
- injection conditions: PI horizontal phase advance between injection kickers,
- stability and damping: Dispersion function = zero in the straight sections,
- slicing conditions: Equal Twiss parameters and PI vertical phase advance between Beta-Bump quadrupoles,
- Beta beating: Periodic solution in the arcs and small axis symmetry.

Remark: Although the synchrotron integrals had a considerable impact on the EPA lattice design, the matching method does not try to fit them. In fact, for a given bending magnet, they are dependent only on the local Dispersion function and Twiss parameters in the bending magnets which come as a result of the matching.

3. MATCHING METHOD

The proposed method is based on MAD matching capabilities[7] using one EPA cell (half of the ring) with three markers in positions B,C and D (fig.1) of the injection kickers and septa.

The CELL matching mode with symmetry is used in order to fulfill the first condition which consists in the big axis symmetry. Then three fitting conditions have to be fulfilled:

- a coupling of the two extremities of the cell (points A and F of fig.1) imposing (with a high weight) the corresponding phase advance (transverse tunes) as well as an equivalence (with a low weight) of the Beta function (reduction of the Beta beating and small axis symmetry).
- a constraint on the Dispersion function and it's derivative at the injection septum (point C) (damping and stability conditions).
- a coupling of the two injection kicker locations (points B and C) imposing (with an intermediate weight) the corresponding phase advance (injection conditions) as well as an equivalence (with a low weight) of the Beta function (Beta beating and slicing conditions).

4. TEST OF THE METHOD

The above method has been used to rematch the lattice with the nominal transverse tunes and using different bending magnet models corresponding to the different working energies then to adjust the lattice to different transverse tunes.

4.1 Adjustment to the bending magnet model

The Mad listing corresponding to the matching of the lattice with the nominal tunes ($Q_x = 4.46$, $Q_y = 4.38$) and the 600 MeV bending magnet model [4] is attached:

- The big and small axis symmetry are completely respected without any Beta beating in horizontal and negligible in vertical

Points A and F: $B_x = 14.705 + 1E-3$; $B_y = 3.020 + 6E-3$
Points B,C,D and E: $B_x = 13.633 + 1E-3$; $B_y = 3.135 + 6E-3$

- The dispersion functions, injection and slicing conditions are ideal;

Points B-C and D-E: $D_x = D_x' = 0$; $MU_x = MU_y = 0.025 + 1E-3$

- The maximum Beta function is reduced:

$$B_x(\max) = 15.3 \text{ m} \quad ; \quad B_y(\max) = 14.6 \text{ m}$$

Remark: Linear optics as well as chromatic functions like for example the chromaticities are derived from the parameters of the bending magnet model [4] which has been adjusted to give a representation for on and off momentum particles behaviour similar to the results of the tracking program ORBIT of M.Bell.

4.2 Adjustment to different operation energies

EPA is supposed to work at a constant operational energy, $E = 600$ MeV. Nevertheless, an energy range has been foreseen in order to cope with eventual klystron problems or energy upgrading of LIL:

$$500 \text{ MeV} < E < 650 \text{ MeV}$$

Therefore the bending magnet has been measured and modelled [4] also at these two extreme energies (fig 2). Table 1 summarizes the main parameters of the lattice after matching as well as the required quadrupole strengths.

Thanks to the trimming quadrupoles (fig 3 and table 1) located at the optimum position for this purpose [2], the lattice is easily retuned without any major modification of its characteristics. The variation with energy of the sextupole component of the bending magnet induces a small perturbation of the natural chromaticities (fig 3), which are easily compensated by the two dedicated sextupole families: HR.XNH and HR.XNV.

4.3 Adjustment to different transverse tunes:

In order to test the flexibility of the lattice as well as of the matching method, a large area of the tranverse tunes area has been covered (fig 4):

$$4.15 < Q_x, y < 4.85$$

Table 1 summarizes the main parameters of the lattice after matching with the nominal values.

In any case, the required tunes have been exactly reached with an optimum Dispersion function and horizontal phase advance between kickers. Moreover, the matching is perfect (penalty function < 5E-6) and all the constraints exactly fulfilled even for extreme tunes except for vertical tunes greater than 4.70 (cases 12,13,14). In these three cases, the horizontal parameters are acceptable but the lattice is highly mismatched in the vertical plane as shown on fig 5 which plots the maximum of the Beta function in both planes in function of the corresponding tune.

Therefore, limiting the maximum acceptable of the Beta function to 25 meters which corresponds to an EPA acceptance (with an ideal closed orbit) of:

$$\text{EPS}_x = 100 \text{ mm-mrad} ; \text{ EPS}_y = 12.5 \text{ mm-mrad}$$

the EPA lattice is perfectly matchable with the proposed method in a broad tune area:

$$4.20 < Q_x < 4.90 ; 4.15 < Q_y < 4.70$$

5. POWER SUPPLIES STRENGTH REQUIREMENTS

In any of the studied cases, the required quadrupole strengths are well inside the available power range specifications (table 1).

The HR.QTR trimming quadrupole family, implemented in order to correct locally the variation of the bending magnets characteristics with the operating energy, has been found to be extremely useful for tuning the machine to different transverse tunes specially in the cases of high vertical tunes. Their strength, limited not by the magnet (design identical to the HR.QFN, HR.QDN quadrupole magnets) but by the power supply, is still sufficient.

Finally, the rematching of the lattice by MAD needs changes of the quadrupole strengths in the arcs only, HR.QFW, HR.QFL, HR.QTR, whereas the quadrupole strengths in the straight sections, HR.QFN, HR.QFI and HR.QDN do not necessitate any modifications (at least as long as the lattice is correctly matched).

6. CONCLUSION: CONFIGURATION UPDATE

The developed matching method is proposed to serve as a basis for the modelling program, Configuration Update [8], to be used in operation to match the EPA configuration.

It has been shown to be easily usable to adapt the lattice to different bending magnets corresponding to the EPA operation energy range as well as to transverse tunes covering a large working area with a limited number of constraints.

The only bad point consists in the necessary computer time for matching (nearly 200 elements), which, still acceptable on the IBM (20 to 40 sec.) lasts as long as 4 to 5 minutes on the PRDEV computer.

REFERENCES

- [1] J.P.Delahaye,A.Krusche: The LEP Electron Positron Accumulator, Basic Parameters and Lattice Structure, PS/LPI Note 82.8
- [2] J.P.Delahaye: Effect and correction of an integrated focussing error strength in the EPA bending magnets, PS/LPI Note 83-4
- [3] M.Bell,J.P.Delahaye: Particle Tracking in the EPA Bending Magnet, PS/LPI Note 83-9
- [4] M.Bell,H.Kugler: The EPA Bending Magnet and its Representation in the Full description of the Machine; PS/LPI Note 86-01 reviewed on 23/04/86
- [5] J.P.Delahaye,H.Kugler,F.Perriollat: Proposition pour un service de "Modelling On-Line", PS/CO Note 84-22
- [6] F.Perriollat: Minute of the EPA modelling meeting no 2 (20/06/85)
- [7] F.C.Iselin: The MAD program , CERN-LEP-TH/85-15
- [8] A.Levy-Mandel: Le "Configuration Update". Cahier des charges et guide de l'utilisateur; 21 Mars 1986.

04/25/86 14:00:23 JPD MAD
 INPUT FILE: EPA600MA MAD A1 RECORDS = 102
 OUTPUT FILE: OPTICS LISTING A1
 OPA=MATCHING:LATTICE WITH OFFICIAL 600 MEV MODEL MAGNET (23 APR 1986).
 OMATCHING OF BEAM LINE "EPAH" AS A CELL, SYMM = T

O BEGIN MIGRAD MINIMIZATION, TOLERANCE = 0.10E-05
 O PENALTY FCT. CALL TIME E.D.M. PARAMETER NAME PAR. VALUE PAR. ERROR
 O 0.179191E-05 87 3.037 0.239E-06 QFWH[K1] 0.110753E+01 0.100000E-04
 O QTRH[K1] -0.668658E-01 0.100000E-04
 O QFLH[K1] 0.137569E+01 0.100000E-04
 O QFNH[K1] 0.565923E+00 0.100000E-04
 O QDNH[K1] -0.568929E+00 0.100000E-04
 O QFIH[K1] 0.533551E+00 0.100000E-04

O MIGRAD MINIMIZATION HAS CONVERGED
 O PENALTY FCT. CALL TIME E.D.M. PARAMETER NAME PAR. VALUE PAR. ERROR
 O 0.167234E-05 88 3.075 0.239E-06 QFWH[K1] 0.110753E+01 0.515467E-05
 O QTRH[K1] -0.668722E-01 -0.236619E-04
 O QFLH[K1] 0.137569E+01 -0.488435E-05
 O QFNH[K1] 0.565922E+00 -0.263501E-05
 O QDNH[K1] -0.568925E+00 0.115959E-04
 O QFIH[K1] 0.533550E+00 -0.441543E-05

1 EPA=MATCHING:LATTICE WITH OFFICIAL 600 MEV MODEL MAGNET (23 APR 1986),
 MATCHING SUMMARY FOR BEAM LINE "EPAH"

POS.	ELEMENT OCC. NO.	DIST [M]	CONDITION TYPE	QUANTITY NAME	WEIGHT	ACTUAL VALUE	MINIMUM VALUE	MAXIMUM VALUE	PENALTY CONTRIBUTION
0	0	0.000	BEGIN "EPAH"						
0	0	0.000	BEGIN COUPLE	BETX	1.000000E-01	1.463316E+01	3.037769E+00	5.580359E-17	-4.054589E-17
				BETY	1.000000E-01				
				ALFX	0.000000E+00				
				ALFY	0.000000E+00				
				DX	0.000000E+00				
				DY	0.000000E+00				
				DX'	0.000000E+00				
				DY'	0.000000E+00				
				MUX	0.000000E+00				
				MUY	0.000000E+00				
75 M	1	17.330	BEGIN COUPLE	BETX	1.000000E-01	1.363297E+01	3.140991E+00	4.452458E-03	-6.400328E-03
				BETY	1.000000E-01				
				ALFX	0.000000E+00				
				ALFY	0.000000E+00				

Annex : MAD listing after EPA Nominal matching

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DX 0.000000E+00 -2.600175E-07
DY 1.000000E+01 0.000000E+00
DX' 0.000000E+00 1.907333E-08
DY' 1.000000E+02 0.000000E+00
MUX 1.000000E+01 7.396471E-01
MUY 1.000000E+01 7.203689E-01

90 M 2 26.721 CONSTRAINT
DX 1.000000E+00 2.600288E-07
DX' 1.000000E+00 0.000000E+00
DX 1.000000E+00 2.600288E-07
DX' 1.907251E-08 0.000000E+00
DX 1.000000E+00 2.600288E-07
DX' 1.907251E-08 0.000000E+00
DX 1.000000E-01 1.363297E+01
DX' 1.000000E-01 3.140991E+00
ALFX 0.000000E+00 4.454182E-03
ALFY 0.000000E+00 -4.833625E-03
DX 0.000000E+00 2.600179E-07
DX' 0.000000E+00 2.600179E-07
DY 1.000000E+01 0.000000E+00
DY' 0.000000E+00 -1.907333E-08
MUX 1.000000E+02 0.000000E+00
MUY 1.000000E+01 1.20369E+00
MUY 1.000000E+01 1.220369E+00

105 M 3 36.111 END COUPLE
BETX BETY ALFX ALFY DX DY DX' DY' MUX MUY
1.000000E-01 1.363297E+01 1.363297E+01 1.363297E+01
1.000000E-01 3.140991E+00 3.140991E+00 3.140991E+00
0.000000E+00 4.452458E-03 4.452458E-03 4.452458E-03
0.000000E+00 -4.833625E-03 -6.400328E-03 -6.400328E-03
0.000000E+00 -2.600179E-07 -2.600179E-07 -2.600179E-07
0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00
0.000000E+00 -1.907333E-08 -1.907333E-08 -1.907333E-08
0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00
0.000000E+00 1.239647E+00 1.239647E+00 1.239647E+00
0.000000E+00 1.220369E+00 1.220369E+00 1.220369E+00
0.000000E+00 2.190000E+00 2.190000E+00 2.190000E+00

194 D1 4 62.832 END "EPAH"
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1.000000E-01 1.463336E+01 1.463336E+01 1.463336E+01
1.000000E-01 3.050700E+00 3.037769E+00 3.037769E+00
0.000000E+00 -1.956768E-15 5.580359E-17 5.580359E-17
0.000000E+00 -3.178013E-15 -4.054589E-17 -4.054589E-17
0.000000E+00 2.680492E-08 2.680492E-08 2.680492E-08
0.000000E+00 1.000000E+01 0.000000E+00 0.000000E+00
0.000000E+00 0.000000E+00 4.026253E-17 0.000000E+00
0.000000E+00 1.000000E+02 0.000000E+00 0.000000E+00
0.000000E+00 1.000000E+02 2.230000E+00 2.230000E+00
0.000000E+00 2.190000E+00 2.190000E+00 2.190000E+00
0.000000E+00 2.190000E+00 2.190000E+00 2.190000E+00

194 D1 4 62.832 END "EPAH"
BETX BETY ALFX ALFY DX DY DX' DY' MUX MUY
1.463336E+01 3.050700E+00 -1.956768E-15 -3.178013E-15
1.463336E+01 3.037769E+00 5.580359E-17 2.680492E-08
0.000000E+00 0.000000E+00 0.000000E+00 0.000000E+00
0.000000E+00 0.000000E+00 4.026253E-17 0.000000E+00
0.000000E+00 0.000000E+00 1.000000E+02 0.000000E+00
0.000000E+00 0.000000E+00 2.230000E+00 2.230000E+00
0.000000E+00 0.000000E+00 2.190000E+00 2.190000E+00
0.000000E+00 0.000000E+00 2.190000E+00 2.190000E+00

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0  FINAL VALUES FOR PARAMETERS          TOTAL = 1.672338E-06
0  PENALTY FCT.           CALL      E.D.M.    PARAMETER NAME   PAR. VALUE
0  0.167234E-05        88       0.239E-06   QFWH[K1]      0.110753E+01  0.515467E-05
0  QTRH[K1]             -0.668722E-01 -0.236619E-04
0  QFLH[K1]              0.137569E+01 -0.488435E-05
0  QFNH[K1]              0.565922E+00 -0.263501E-05
0  QDNH[K1]              0.568925E+00  0.115959E-04
0  QFIH[K1]              0.533550E+00 -0.441543E-05
1 EPA=MATCHING:LATTICE WITH OFFICIAL 600 MEV MODEL MAGNET (23 APR 1986)
1 SWISS PARAMETERS FOR BEAM LINE:EPAH'                                VERSION: 4.15
1 HORIZONTAL ELEMENT SEQUENCE 1                                     RUN: 25/04/86 14.00.27
1 PAGE 1
1 VERTICAL ELEMENT SEQUENCE 1

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POS.	ELEMENT	OCC.	DIST	I	BETAX	X'(CO)	DX	DX'	I	BETAY	ALFAY	MUY	Y'(CO)	Y(CO)	DY	DY'
NO.	NAME	NO.	[M]	I	ALFAX	[MM]	[MRAD]	[M]	I	[M]	[M]	[2P1]	[MM]	[MRAD]	[M]	[M]
BEGIN	EPAH	1	0.000	14.633	0.000	0.000	0.000	0.000	0.000	0.000	0.000	3.038	0.000	0.000	0.000	0.000
1	D1	1	2.928	15.219	-0.200	0.031	0.000	0.000	0.000	0.000	0.000	5.861	-0.964	0.122	0.000	0.000
2	QFWH	1	3.118	14.695	2.951	0.033	0.000	0.000	0.000	0.000	0.000	6.487	-2.373	0.127	0.000	0.000
3	QFWH	2	3.308	13.058	5.581	0.036	0.000	0.000	0.000	0.000	0.000	7.713	-4.166	0.131	0.000	0.000
4	D3R	1	3.647	9.563	4.748	0.040	0.000	0.000	0.000	0.000	0.000	10.805	-4.972	0.137	0.000	0.000
5	SYB	1	3.647	9.563	4.748	0.040	0.000	0.000	0.000	0.000	0.000	10.805	-4.972	0.137	0.000	0.000
6	Q2R	1	3.656	9.475	4.682	0.041	0.000	0.000	0.000	0.000	0.000	10.897	-4.944	0.137	0.000	0.000
7	D2R	1	3.668	9.363	4.653	0.041	0.000	0.000	0.000	0.000	0.000	11.017	-4.972	0.138	0.000	0.000
8	Q1R	1	3.686	9.206	4.232	0.041	0.000	0.000	0.000	0.000	0.000	11.185	-4.554	0.138	0.000	0.000
9	D1R	1	3.741	8.744	4.119	0.042	0.000	0.000	0.000	0.000	0.000	11.695	-4.662	0.139	0.000	0.000
10	B	1	4.360	5.074	2.029	0.057	0.000	0.000	0.123	0.400	0.400	14.365	0.731	0.146	0.000	0.000
11	D1R	2	4.415	4.852	1.973	0.059	0.000	0.000	0.145	0.400	0.400	14.284	0.725	0.146	0.000	0.000
12	Q1R	2	4.433	4.786	1.759	0.060	0.000	0.000	0.152	0.406	0.406	14.248	1.308	0.147	0.000	0.000
13	D2R	2	4.445	4.744	1.748	0.060	0.000	0.000	0.157	0.406	0.406	14.217	1.306	0.147	0.000	0.000
14	Q2R	2	4.454	4.712	1.719	0.060	0.000	0.000	0.160	0.406	0.406	14.192	1.369	0.147	0.000	0.000
15	SYB	2	4.454	4.712	1.719	0.060	0.000	0.000	0.160	0.407	0.407	14.192	1.369	0.147	0.000	0.000
16	D3R	2	4.792	3.645	1.435	0.073	0.000	0.000	0.298	0.407	0.407	13.288	1.300	0.151	0.000	0.000
17	QTRH	1	4.971	3.165	1.247	0.082	0.000	0.000	0.371	0.411	0.411	12.802	1.417	0.153	0.000	0.000
18	QTRH	2	5.150	2.750	1.070	0.091	0.000	0.000	0.445	0.416	0.416	12.275	1.522	0.155	0.000	0.000
19	Q3	1	5.988	1.505	0.416	0.159	0.000	0.000	0.793	0.416	0.416	9.913	1.296	0.167	0.000	0.000
20	SY	1	6.288	1.325	0.182	0.193	0.000	0.000	0.918	0.416	0.416	9.160	1.215	0.172	0.000	0.000
21	D3R	3	6.627	1.291	-0.081	0.235	0.000	0.000	1.059	0.416	0.416	8.369	1.123	0.179	0.000	0.000
22	SYB	3	6.627	1.291	-0.081	0.235	0.000	0.000	1.059	0.416	0.416	8.369	1.123	0.179	0.000	0.000
23	Q2R	3	6.636	1.293	-0.094	0.236	0.000	0.000	1.063	0.420	0.420	8.348	1.159	0.179	0.000	0.000
24	D2R	3	6.648	1.295	-0.104	0.237	0.000	0.000	1.068	0.420	0.420	8.320	1.159	0.179	0.000	0.000
25	Q1R	3	6.666	1.300	-0.171	0.239	0.000	0.000	1.075	0.464	0.464	8.273	1.490	0.179	0.000	0.000
26	D1R	3	6.721	1.321	-0.215	0.246	0.000	0.000	1.101	0.464	0.464	8.109	1.469	0.180	0.000	0.000
27	B	2	7.340	2.070	-1.040	0.308	0.000	0.000	1.577	1.088	1.088	4.777	3.437	0.196	0.000	0.000
28	D1R	4	7.395	2.188	-1.095	0.312	0.000	0.000	1.637	1.088	1.088	4.405	3.289	0.196	0.000	0.000
29	Q1R	4	7.413	2.229	-1.04	0.314	0.000	0.000	1.657	1.155	1.155	4.287	3.417	0.197	0.000	0.000
30	D2R	4	7.425	2.258	-1.218	0.315	0.000	0.000	1.671	1.155	1.155	4.205	3.382	0.199	0.000	0.000
31	Q2R	4	7.434	2.281	-1.238	0.315	0.000	0.000	1.681	1.163	1.163	4.142	3.373	0.199	0.000	0.000
32	SYB	4	7.434	2.281	-1.238	0.315	0.000	0.000	1.681	1.163	1.163	4.142	3.373	0.199	0.000	0.000
33	D3R	4	7.772	3.246	-1.614	0.335	0.000	0.000	2.075	1.163	1.163	2.202	2.362	0.217	0.000	0.000
34	QFLH	1	7.962	3.724	-0.840	0.344	0.000	0.000	2.243	0.596	0.596	1.495	1.234	0.214	0.000	0.000
35	QFLH	2	8.152	3.864	-0.908	0.352	0.000	0.000	2.300	0.600	0.600	1.087	0.763	0.258	0.000	0.000
36	D5	1	8.515	3.827	-0.004	0.367	0.000	0.000	2.300	0.600	0.600	0.725	0.235	0.325	0.000	0.000
37	SXH	1	8.665	3.832	-0.035	0.373	0.000	0.000	2.300	0.600	0.600	0.688	0.017	0.359	0.000	0.000
38	SXH	2	8.815	3.848	-0.075	0.379	0.000	0.000	2.300	0.600	0.600	0.715	-0.201	0.393	0.000	0.000
39	D5	2	9.177	3.937	-0.169	0.394	0.000	0.000	2.300	0.600	0.600	1.495	-0.729	0.462	0.000	0.000
40	Q2R	3	9.367	3.816	0.794	0.402	0.000	0.000	2.243	-0.596	-0.596	1.445	-1.372	0.486	0.000	0.000
41	QFLH	4	9.557	3.353	1.603	0.410	0.000	0.000	2.075	-1.163	-1.163	2.130	-2.293	0.504	0.000	0.000
42	D3R	5	9.896	2.390	1.243	0.429	0.000	0.000	1.681	-1.163	-1.163	4.018	-3.287	0.522	0.000	0.000
43	SYB	5	9.896	2.390	1.243	0.429	0.000	0.000	1.671	-1.163	-1.163	4.018	-3.287	0.522	0.000	0.000
44	Q2R	5	9.905	2.367	1.222	0.430	0.000	0.000	1.671	-1.155	-1.155	4.079	-3.295	0.523	0.000	0.000
45	D2R	5	9.917	2.338	1.209	0.431	0.000	0.000	1.657	-1.155	-1.155	4.159	-3.330	0.523	0.000	0.000
46	Q1R	5	9.935	2.297	1.096	0.432	0.000	0.000	1.637	-1.088	-1.088	4.274	-3.206	0.524	0.000	0.000
47	D1R	5	9.990	2.179	1.043	0.436	0.000	0.000	1.577	-1.088	-1.088	4.637	-3.352	0.526	0.000	0.000
48	B	3	10.609	1.418	0.230	0.494	0.000	0.000	1.101	-0.464	-0.464	7.901	-1.452	0.541	0.000	0.000
49	D1R	6	10.664	1.395	0.189	0.500	0.000	0.000	1.075	-0.464	-0.464	8.063	-1.474	0.542	0.000	0.000

1 EPA=MATCHING:LATTICE WITH OFFICIAL 600 MEV MODEL MAGNET (23 APR 1986),
 2 TWISS PARAMETERS FOR BEAM LINE "EPAH"
 3 DELTA(P)/P = 0.000000
 4 "MAD" VERSION : 4.15
 5 SYMM = T
 RUN: 25/04/86 14.00.27 PAGE 2

ELEMENT NO.	ELEMENT NAME	SEQUENCE OCC.	DIST I [M]	I BETAX [M]	HORI ZONTA L MUX [2P1]	HORI ZONTA L MUX [2P1]	I ALFAX [MM]	I ALFAX [MM]	V E R T I C A L		
									X'(CO) [MRAD]	DX' [M]	I BETAY [M]
50	Q1R	6	10.682	1.390	0.118	0.502	0.000	1.068	-0.420	8.109	-1.148
51	D2R	6	10.694	1.387	0.110	0.504	0.000	1.063	-0.420	8.152	-1.152
52	Q2R	6	10.703	1.385	0.097	0.505	0.000	1.059	-0.416	8.158	-1.117
53	SYB	6	10.703	1.385	0.097	0.505	0.000	1.059	-0.416	8.158	-1.117
54	D3R	6	11.041	1.403	-0.150	0.544	0.000	0.918	-0.416	8.945	-1.210
55	SY	2	11.341	1.559	-0.369	0.576	0.000	0.793	-0.416	9.696	-1.293
56	D3	2	12.179	2.688	-0.979	0.643	0.000	0.445	-0.416	12.057	-1.555
57	QTRH	3	12.358	3.069	-1.146	0.653	0.000	0.371	-0.411	12.585	-1.423
58	QTRH	4	12.537	3.510	-1.323	0.662	0.000	0.298	-0.407	13.074	-1.309
59	D3R	7	12.876	4.495	-1.588	0.676	0.000	0.160	-0.407	13.984	-1.379
60	SYB	7	12.876	4.495	-1.588	0.676	0.000	0.160	-0.407	13.984	-1.379
61	Q2R	7	12.885	4.525	-1.616	0.676	0.000	0.157	-0.406	14.009	-1.317
62	D2R	7	12.897	4.564	-1.626	0.676	0.000	0.152	-0.406	14.041	-1.320
63	Q1R	7	12.915	4.625	-1.830	0.677	0.000	0.145	-0.400	14.077	-0.745
64	D1R	7	12.970	4.830	-1.882	0.679	0.000	0.123	-0.400	14.160	-0.751
65	B	4	13.589	8.250	-3.847	0.695	0.000	0.000	0.000	11.561	4.577
66	D1R	8	13.644	8.682	-3.953	0.696	0.000	0.000	0.000	11.061	4.472
67	Q1R	8	13.662	8.828	-4.349	0.696	0.000	0.000	0.000	10.896	4.886
68	D2R	8	13.674	8.933	-4.376	0.696	0.000	0.000	0.000	10.778	4.858
69	Q2R	8	13.683	9.016	-4.438	0.696	0.000	0.000	0.000	10.687	4.886
70	SYB	8	13.683	9.016	-4.438	0.696	0.000	0.000	0.000	10.687	4.886
71	D3R	8	14.021	12.282	-5.215	0.702	0.000	0.000	0.000	7.648	4.098
72	QFWH	3	14.211	13.808	-2.712	0.704	0.000	0.000	0.000	6.443	2.324
73	QFWH	4	14.401	14.288	-0.219	0.706	0.000	0.000	0.000	5.834	0.926
74	D1	2	17.330	13.633	0.004	0.740	0.000	0.000	0.000	3.141	-0.006
75	M	1	17.330	13.633	0.004	0.740	0.000	0.000	0.000	3.141	-0.006
76	D6	1	18.087	13.668	-0.051	0.748	0.000	0.000	0.000	3.333	-0.248
77	QFNH	1	18.266	13.442	-1.306	0.751	0.000	0.000	0.000	3.494	-0.656
78	QFNH	2	18.445	12.745	2.568	0.753	0.000	0.000	0.000	3.809	-1.112
79	D7	1	20.840	3.863	1.141	0.808	0.000	0.000	0.000	12.503	-2.519
80	QDNH	1	21.019	3.539	0.677	0.816	0.000	0.000	0.000	13.186	-1.274
81	QDNH	2	21.198	3.372	0.262	0.824	0.000	0.000	0.000	13.404	0.064
82	D8	1	22.025	3.155	0.000	0.865	0.000	0.000	0.000	13.350	0.002
83	D8	2	22.853	3.372	-0.262	0.906	0.000	0.000	0.000	13.398	-0.060
84	QDNH	3	23.032	3.539	-0.677	0.914	0.000	0.000	0.000	13.179	-1.277
85	QDNH	4	23.211	3.863	-1.141	0.922	0.000	0.000	0.000	12.495	2.521
86	D9	1	25.594	12.688	-2.562	0.977	0.000	0.000	0.000	3.822	1.118
87	QFIH	1	25.784	13.428	-1.306	0.979	0.000	0.000	0.000	3.465	0.656
88	QFIH	2	25.974	13.668	0.050	0.982	0.000	0.000	0.000	3.317	-0.932
89	D10	1	26.721	13.634	-0.004	0.990	0.000	0.000	0.000	3.131	0.006
90	M	2	26.721	13.634	-0.004	0.990	0.000	0.000	0.000	3.131	0.006
91	D10	2	27.467	13.681	-0.059	0.999	0.000	0.000	0.000	3.300	-0.233
92	QFIH	3	27.657	13.444	-1.298	1.001	0.000	0.000	0.000	1.007	0.000
93	QFIH	4	27.847	12.707	2.557	1.004	0.000	0.000	0.000	3.795	-1.101
94	D9	2	30.230	3.889	1.143	1.059	0.000	0.000	0.000	12.357	-2.491
95	QDNH	5	30.409	3.565	0.677	1.066	0.000	0.000	0.000	13.033	-1.261
96	QDNH	6	30.588	3.399	0.260	1.075	0.000	0.000	0.000	13.249	0.061
97	D8	3	31.416	3.183	0.000	1.115	0.000	0.000	0.000	13.201	-0.002
98	D8	4	32.243	3.399	-0.260	1.155	0.000	0.000	0.000	13.256	1.105
99	QDNH	7	32.422	3.565	-0.677	1.164	0.000	0.000	0.000	13.041	1.258

1EPA=MATCHING:LATTICE WITH OFFICIAL 600 MEV MODEL MAGNET (23 APR 1986), TWISS PARAMETERS FOR BEAM LINE "EPAH"				"MAD" VERSION: 4.15 SYMM = T				RUN: 25/04/86 14.00.27 PAGE 3			
ELEMENT SEQUENCE		DIST [MM]	BETAX [MM]	HORI ZONT AL	MUX [2PI]	V E R T I C A L	MUY [2PI]	V(CO) [MM]	Y(CO) [MM]	DY [MMRAD]	DY [MRAD]
POS.	ELEMENT OCC. NAME NO.			X(CO) [MM]	DX [MM]	I [M]	ALFAY	I [M]	I [M]	I [M]	I [M]
100	QDNH	8	32.601	3.889	-1.143	1.171	0.000	0.000	0.000	0.000	0.000
101	D7	2	34.996	12.763	-2.563	1.227	0.000	0.000	0.000	0.000	0.000
102	QFNH	3	35.175	13.459	-1.298	1.229	0.000	0.000	0.000	0.000	0.000
103	QFNH	4	35.354	13.682	0.060	1.231	0.000	0.000	0.000	0.000	0.000
104	D6	2	36.111	13.633	0.004	1.240	0.000	0.000	0.000	0.000	0.000
105	M	3	36.111	13.633	0.004	1.240	0.000	0.000	0.000	0.000	0.000
106	D6	3	36.869	13.668	-0.051	1.248	0.000	0.000	0.000	0.000	0.000
107	QFNH	5	37.048	13.442	-1.306	1.251	0.000	0.000	0.000	0.000	0.000
108	QFNH	6	37.227	12.745	2.568	1.253	0.000	0.000	0.000	0.000	0.000
109	D7	3	39.621	3.863	1.141	1.308	0.000	0.000	0.000	0.000	0.000
110	QDNH	9	39.800	3.539	0.677	1.316	0.000	0.000	0.000	0.000	0.000
111	QDNH	10	39.979	3.372	0.262	1.324	0.000	0.000	0.000	0.000	0.000
112	D8	5	40.806	3.155	0.000	1.365	0.000	0.000	0.000	0.000	0.000
113	D8	6	41.634	3.372	-0.262	1.406	0.000	0.000	0.000	0.000	0.000
114	QDNH	11	41.813	5.539	-0.677	1.414	0.000	0.000	0.000	0.000	0.000
115	QDNH	12	41.992	3.863	-1.141	1.422	0.000	0.000	0.000	0.000	0.000
116	D7	4	44.386	12.745	-2.568	1.477	0.000	0.000	0.000	0.000	0.000
117	QFNH	7	44.565	13.442	-1.306	1.479	0.000	0.000	0.000	0.000	0.000
118	QFNH	8	44.744	13.668	0.051	1.482	0.000	0.000	0.000	0.000	0.000
119	D6	4	45.502	13.633	-0.004	1.490	0.000	0.000	0.000	0.000	0.000
120	M	4	45.502	13.633	-0.004	1.490	0.000	0.000	0.000	0.000	0.000
121	D1	3	48.430	14.288	-0.219	1.524	0.000	0.000	0.000	0.000	0.000
122	QFWH	5	48.620	13.808	2.712	1.526	0.000	0.000	0.000	0.000	0.000
123	QFWH	6	48.810	12.282	5.215	1.528	0.000	0.000	0.000	0.000	0.000
124	D3R	9	49.149	9.016	4.438	1.534	0.000	0.000	0.000	0.000	0.000
125	SYB	9	49.149	9.015	4.438	1.534	0.000	0.000	0.000	0.000	0.000
126	Q2R	9	49.158	8.933	4.376	1.534	0.000	0.000	0.000	0.000	0.000
127	D2R	9	49.170	8.828	4.349	1.534	0.000	0.000	0.000	0.000	0.000
128	Q1R	9	49.188	8.682	3.953	1.534	0.000	0.000	0.000	0.000	0.000
129	D1R	9	49.243	8.250	3.847	1.535	0.000	0.000	0.000	0.000	0.000
130	B	5	49.862	4.830	1.882	1.551	0.000	0.000	0.123	0.400	14.194
131	D1R	10	49.917	4.625	1.830	1.553	0.000	0.000	0.145	0.400	14.112
132	Q1R	10	49.935	4.564	1.626	1.554	0.000	0.000	0.152	0.406	14.075
133	D2R	10	49.947	4.525	1.616	1.554	0.000	0.000	0.157	0.406	14.044
134	Q2R	10	49.956	4.495	1.588	1.554	0.000	0.000	0.160	0.407	14.019
135	SYB	10	49.956	4.495	1.588	1.554	0.000	0.000	0.160	0.407	14.019
136	D3R	10	50.294	3.510	1.323	1.568	0.000	0.000	0.298	0.407	13.109
137	QTRH	5	50.473	3.069	1.146	1.577	0.000	0.000	0.371	0.411	12.619
138	QTRH	6	50.652	2.688	0.979	1.587	0.000	0.000	0.445	0.416	12.091
139	D3	3	51.490	1.559	0.369	1.654	0.000	0.000	0.793	0.416	9.728
140	SY	3	51.790	1.403	0.150	1.686	0.000	0.000	0.918	0.416	8.976
141	D3R	11	52.129	1.385	-0.097	1.725	0.000	0.000	1.059	0.416	8.188
142	SYB	11	52.129	1.385	-0.097	1.725	0.000	0.000	1.059	0.416	8.188
143	Q2R	11	52.138	1.387	-0.110	1.726	0.000	0.000	1.063	0.420	8.166
144	D2R	11	52.150	1.390	-0.118	1.728	0.000	0.000	1.068	0.420	8.139
145	Q1R	11	52.168	1.395	-0.189	1.730	0.000	0.000	1.075	0.420	8.092
146	D1R	11	52.223	1.419	-0.230	1.736	0.000	0.000	1.101	0.464	7.930
147	B	6	52.842	2.179	-1.043	1.794	0.000	0.000	1.577	0.000	1.664

148 DIR 12 52.897 2.297 -1.096 1.798 0.000 0.000 1.637 1.088 4.292 3.218
 149 Q1R 12 52.915 2.338 -1.209 1.799 0.000 0.000 1.657 1.155 4.176 3.343
 1EPA=MATCHING:LATTICE WITH OFFICIAL 600 MEV MODEL MAGNET (23 APR 1986).
 TWISS PARAMETERS FOR BEAM LINE "EPAH"
 DELTA(P)/P = 0.0000000

POS.	ELEMENT OCC. NO.	ELEMENT SEQUENCE			HORI	ZON	A _L	V E R T I C A L	MUX	MUX	Y'(CO)	DY'	
		I	DIST	BETAX	ALFAX	X(CO)	X(CO)	DX	I	BETAY	ALFAY	Y(CO)	DY
NAME	NO.	[M]	[M]	[2PI]	[MM]	[MM]	[MM]	[MM]	[M]	[2PI]	[MM]	[MM]	[M]
150 D2R	12	52.927	2.367	-1.222	1.800	0.000	0.000	1.671	1.155	4.096	3.308	1.668	0.000
151 Q2R	12	52.936	2.390	-1.243	1.801	0.000	0.000	1.681	1.163	4.034	3.299	1.668	0.000
152 SYB	12	52.936	2.390	-1.243	1.801	0.000	0.000	1.681	1.163	4.034	3.299	1.668	0.000
153 D3R	12	53.274	3.353	-1.603	1.820	0.000	0.000	2.075	1.163	2.139	2.302	1.686	0.000
154 QFLH	5	53.464	3.816	-0.794	1.828	0.000	0.000	2.243	0.596	1.451	1.379	1.704	0.000
155 QFLH	6	53.654	3.937	0.169	1.836	0.000	0.000	2.300	0.000	1.056	0.733	1.728	0.000
156 D5	3	54.017	3.848	0.075	1.851	0.000	0.000	2.300	0.000	0.716	0.206	1.797	0.000
157 SXH	3	54.167	3.832	0.035	1.855	0.000	0.000	2.300	0.000	0.687	-0.013	1.831	0.000
158 SXH	4	54.317	3.827	-0.004	1.863	0.000	0.000	2.300	0.000	0.687	-0.013	1.865	0.000
159 D5	4	54.679	3.864	-0.098	1.878	0.000	0.000	2.300	0.000	1.083	-0.759	1.932	0.000
160 QFLH	7	54.869	3.721	0.840	1.886	0.000	0.000	2.243	-0.596	1.489	-1.414	1.956	0.000
161 QFLH	8	55.059	3.246	1.614	1.895	0.000	0.000	2.075	-1.163	2.193	-2.354	1.973	0.000
162 D3R	13	55.398	2.281	1.238	1.915	0.000	0.000	1.681	-1.163	4.128	-3.364	1.991	0.000
163 SYB	13	55.398	2.281	1.238	1.915	0.000	0.000	1.681	-1.163	4.128	-3.364	1.991	0.000
164 Q2R	13	55.407	2.258	1.218	1.915	0.000	0.000	1.671	-1.155	4.191	-3.373	1.992	0.000
165 D2R	13	55.419	2.229	1.205	1.916	0.000	0.000	1.657	-1.155	4.272	-3.408	1.992	0.000
166 Q1R	13	55.437	2.188	1.095	1.918	0.000	0.000	1.637	-1.088	4.390	-3.280	1.993	0.000
167 D1R	13	55.492	2.070	0.40	1.922	0.000	0.000	1.577	-1.088	4.762	-3.428	1.995	0.000
168 B	7	56.111	1.321	0.215	1.984	0.000	0.000	1.681	-1.163	8.087	-1.468	2.010	0.000
169 D1R	14	56.166	1.300	0.171	1.991	0.000	0.000	1.671	-1.155	8.251	-1.489	2.011	0.000
170 Q1R	14	56.184	1.295	0.104	1.993	0.000	0.000	1.668	-0.420	8.298	-1.156	2.011	0.000
171 D2R	14	56.196	1.293	0.094	1.994	0.000	0.000	1.663	-0.420	8.326	-1.159	2.012	0.000
172 Q2R	14	56.205	1.291	0.081	1.995	0.000	0.000	1.659	-0.416	8.347	-1.124	2.012	0.000
173 SYB	14	56.205	1.291	0.081	1.984	0.000	0.000	1.681	-1.163	8.347	-1.124	2.012	0.000
174 D3R	14	56.543	1.325	-0.182	2.037	0.000	0.000	1.675	-0.464	8.251	-1.489	2.018	0.000
175 SY	4	56.843	1.505	-0.416	2.071	0.000	0.000	1.668	-0.420	8.298	-1.156	2.011	0.000
176 D3	4	57.681	2.750	-1.070	2.139	0.000	0.000	1.663	-0.420	8.326	-1.159	2.012	0.000
177 QTRH	7	57.860	3.165	-1.247	2.148	0.000	0.000	1.637	-1.088	12.256	-1.524	2.035	0.000
178 QTRH	8	58.039	3.645	-1.435	2.157	0.000	0.000	1.595	-0.416	12.271	-1.419	2.037	0.000
179 D3R	15	58.378	4.712	-1.719	2.170	0.000	0.000	1.598	-0.407	14.175	-1.371	2.043	0.000
180 SYB	15	58.378	4.712	-1.719	2.170	0.000	0.000	1.600	-0.407	14.175	-1.371	2.043	0.000
181 Q2R	15	58.387	4.744	-1.749	2.170	0.000	0.000	1.577	-0.406	14.200	-1.309	2.044	0.000
182 D2R	15	58.417	4.852	-1.973	2.171	0.000	0.000	1.52	-0.406	14.232	-1.311	2.044	0.000
183 Q1R	16	59.176	9.474	-4.682	2.189	0.000	0.000	0.000	0.000	10.890	4.937	2.044	0.000
184 D1R	15	58.472	5.074	-2.029	2.173	0.000	0.000	1.123	-0.400	14.349	-0.735	2.044	0.000
185 B	8	59.091	8.744	-4.119	2.188	0.000	0.000	0.000	0.000	11.686	4.654	2.052	0.000
186 D1R	16	59.146	9.206	-4.232	2.189	0.000	0.000	0.000	0.000	11.177	4.547	2.053	0.000
187 Q1R	16	59.164	9.363	-4.653	2.189	0.000	0.000	0.000	0.000	11.009	4.965	2.053	0.000
188 D2R	16	59.176	9.474	-4.682	2.189	0.000	0.000	0.000	0.000	10.890	4.937	2.044	0.000
189 Q2R	16	59.185	9.563	-4.748	2.190	0.000	0.000	0.000	0.000	10.798	4.964	2.053	0.000
190 SYB	16	59.185	9.563	-4.748	2.190	0.000	0.000	0.000	0.000	10.798	4.964	2.053	0.000
191 D3R	16	59.523	13.058	-5.581	2.194	0.000	0.000	0.000	0.000	7.710	4.161	2.059	0.000
192 QFWH	7	59.713	14.695	-2.921	2.197	0.000	0.000	0.000	0.000	6.486	2.368	2.063	0.000
193 QFWH	8	59.903	15.219	0.200	2.199	0.000	0.000	0.000	0.000	5.862	0.960	2.068	0.000
194 D1	4	62.832	14.633	0.000	2.230	0.000	0.000	0.000	0.000	3.051	0.000	2.190	0.000
END	1	62.832	14.633	0.000	2.230	0.000	0.000	0.000	0.000	3.051	0.000	2.190	0.000

"MAD" VERSION: 4.15
SYMM = T
RUN: 25/04/86 14.00.27
PAGE 4


```

        BMOD: LINE=(LH,B,-LH)
        ! QFW: LINE=(QFWH,QFWH)
        QTR: LINE=(QTRH,QTRH)
        QFL: LINE=(QFLH,QFLH)
        QFN: LINE=(QFNH,QFNH)
        QDN: LINE=(QDNH,QDNH)
        QFI: LINE=(QFIH,QFIH)

      50      M:
        ! MARKER

      CURVH: LINE=(D1,QFW,BMOD,QTR,D3,SY,BMOD,QFL,D5,SXH)
      CURVE: LINE=(CURVH,-CURVH,M)
      STR1H: LINE=(D6,QFN,D7,QDN,D8)
      STR2H: LINE=(D10,QFI,D9,QDN,D8)
      STR1: LINE=(STR1H,-STR2H,M)
      STR2: LINE=(STR2H,-STR1H,M)
      STR3: LINE=(STR1H,-STR1H)
      STR: LINE=(STR1,STR2,STR3)
      EPAH: LINE=(CURVE,STR,-CURVE)

      ! USE, EPAH, SYMM
      ! PRINT,#S/E
      ! TWISS!DELTAP=-0.01/0.0/0.01,CHROM

      ! MATCHING PROCEDURE
      ! CELL,EPAH,SYMM
      ! EXPANSION OF "EPAH" COMPLETE: 194 ELEMENTS, 324 POSITIONS
      ! ENTER CELL MATCHING MODE, ELAPSED CPU TIME = 0.041 SECONDS

      ! VARIABLE PARAMETERS:
      VARY,QFWH[K1],STEP=.00001,LOWER= 0.00, UPPER= 1.70
      VARY,QTRH[K1],STEP=.00001,LOWER=-0.28, UPPER=+0.28
      VARY,QFLH[K1],STEP=.00001,LOWER= 0.00, UPPER= 1.82
      VARY,QFNH[K1],STEP=.00001,LOWER= 0.00, UPPER= 0.77
      VARY,QDNH[K1],STEP=.00001,LOWER=-0.77, UPPER=-0.00
      VARY,QFIH[K1],STEP=.00001,LOWER= 0.00, UPPER=+0.71

      ! FIT AT INTERMEDIATE POINTS
      WEIGHT,BETX=0.,ALFX=0.,DX=1.,DX'=1.,BETY=0.,ALFY=0.,MUX=0.,MUY=0.
      CONSTRAI,M[2],DX=0.,DX'=0.
      75      WEIGHT,BETX=0.1,ALFX=0.,DX=0.,DX'=0.,BETY=0.1,ALFY=0.1,MUX=100.,MUY=100.
      COUPLE,M[3],M[1],M[1],M[3],MUX=0.50,MUY=0.50

      ! FIT AT THE END:
      WEIGHT,BETX=0.1,ALFX=0.,DX=0.,DX'=0.,BETY=0.,ALFY=0.1,MUX=100.,MUY=100.
      85      COUPLE,#S,#E,MUX=2.2300,MUY=2.1900
      ! PERFORM MATCH

```

FILE: EPAGOOOLI MAD

CERN CMS R4.3 V.3

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```
0... END OF "MIGRAD" COMMAND, ELAPSED CPU TIME = 3.075 SECONDS
95 !ENDMATCH
0... LAST VALUE OF THE PENALTY FUNCTION: 1.672338E-06
0... LEAVE CELL MATCHING MODE, ELAPSED CPU TIME = 3.120 SECONDS
!
! USE, EPAH, SYMM
0... EXPANSION OF "EPAH" COMPLETE: 194 ELEMENTS, 324 POSITIONS
...
END OF "USE" COMMAND, ELAPSED CPU TIME = 3.124 SECONDS
PRINT,#S/E
100 TWISS
0... SEARCHING FOR CLOSED ORBIT FOR BEAM LINE "EPAH", DELTAP = 0.000000, SYMM = T
...
... ITER: X
... 1 0.000000 0.000000 0.000000 0.000000 0.000000 0.000000 0.000000E+00
...
END OF "TWISS" COMMAND, ELAPSED CPU TIME = 3.372 SECONDS
!
STOP
**A END JOB 7612 JPD JPD ROOM PS 3.10.17 PM 25 APR 86 R51.PR1 SYS 7890 JOB 7612 CP= 1 END A*
```

Table 1: Main Parameters of the E-PA lattice matched to different tunes and operating energies

Bending magnet model	TUNES		Penalty REACHED	β_x β_y max	Function (m)	$\Delta\beta_x$ A-F (\pm mm)	$\Delta\beta_y$ A-F (\pm mm)	μ_x D S-D C	μ_y D S-D C	normalized quadrupole strength (m^{-2})
	α_x	α_y								
0	proto	4.460	4.380	4.380	4.380	2.10 ⁻⁶	1.15.3	14.6	1	500 500 0 1.10643 1.39140 .56592 .53355 .56893 -.03806
0.1	proto	4.460	4.380	4.380	4.380	2.10 ⁻⁶	15.2	14.4	0	500 500 0 1.10753 1.37569 .56592 .53355 .56892 -.06637
0.2	proto	4.460	4.380	4.380	4.380	2.10 ⁻⁶	15.0	14.4	0	500 500 0 1.10510 1.36941 .56592 .53355 .56892 -.09350
0.3	proto	4.460	4.380	4.380	4.380	2.10 ⁻⁶	14.9	14.8	0	500 500 0 1.11042 1.38035 .56592 .53355 .56892 -.05239
1	proto	4.540	4.380	4.380	4.380	1.10 ⁻⁶	14.3	14.7	0	6.5 500 0 1.13351 1.37193 .56592 .53354 .56892 -.16265
2	proto	4.600	4.380	4.380	4.380	1.10 ⁻⁵	14.3	16.1	1.5	500 500 0 1.11000 1.36968 .56593 .53355 .56893 -.14255
3	proto	4.600	4.380	4.380	4.380	2.10 ⁻⁶	14.3	18.7	0.5	2.5 500 500 0 1.14629 1.36866 .56593 .53355 .56893 -.19559
4	proto	4.540	4.380	4.380	4.380	3.10 ⁻⁷	14.9	21.9	0	3 500 500 0 1.15089 1.36823 .56593 .53356 .56893 -.18923
5	proto	4.460	4.380	4.380	4.380	3.10 ⁻⁷	16.3	21.8	0	4 500 500 3 1.12494 1.36862 .56593 .53355 .56893 -.17174
6	proto	4.360	4.380	4.380	4.380	1.10 ⁻⁶	18.7	18.3	2	1.5 500 500 0 1.08942 1.36946 .56592 .53355 .56893 -.13745
7	proto	4.360	4.410	4.380	4.460	9.10 ⁻⁶	18.2	15.7	1.5	1.5 500 500 0 1.01152 1.33096 .56593 .53355 .56892 -.10171
8	proto	4.200	4.380	4.200	4.300	9.10 ⁻⁷	27.2	14.4	0.5	4.5 500 500 0 1.02238 1.37386 .56592 .53355 .56892 -.01293
9	proto	4.300	4.180	4.300	4.180	1.10 ⁻⁶	19.0	19.3	0.5	5.5 500 500 0 1.03699 1.37493 .56592 .53355 .56893 +.02018
10	proto	4.500	4.140	4.600	4.140	2.10 ⁻⁴	15.5	14.1	0.5	6.5 500 500 0 1.06389 1.37449 .56591 .53355 .56892 +.01294
11	proto	4.600	4.200	4.600	4.200	1.10 ⁻⁴	14.4	20.0	0.5	5.5 500 500 0 1.14135 1.37244 .56592 .53355 .56892 -.03910
12	proto	4.840	4.140	4.840	4.140	8.10 ⁻¹	20.9	77.7	224.5	7.5 500 500 0 1.21138 1.37328 .59529 .56632 .20863 -.01091
13	proto	4.700	4.820	4.700	4.820	8.10 ⁻¹	17.3	78.3	126.5	1.5 501 505 0 1.16907 1.32279 .59439 -.52658 .30859 -.02773
14	proto	4.600	4.840	4.600	4.840	8.10 ⁻¹	16.4	78.4	60.0	0.5 501 505 0 1.13377 1.34311 .60063 .56662 .30663 -.01637
										1.30 1.82 0.71 0.71 0.71 ± 0.29

Maximum normalized Quadrupole Strength (600 Rev)

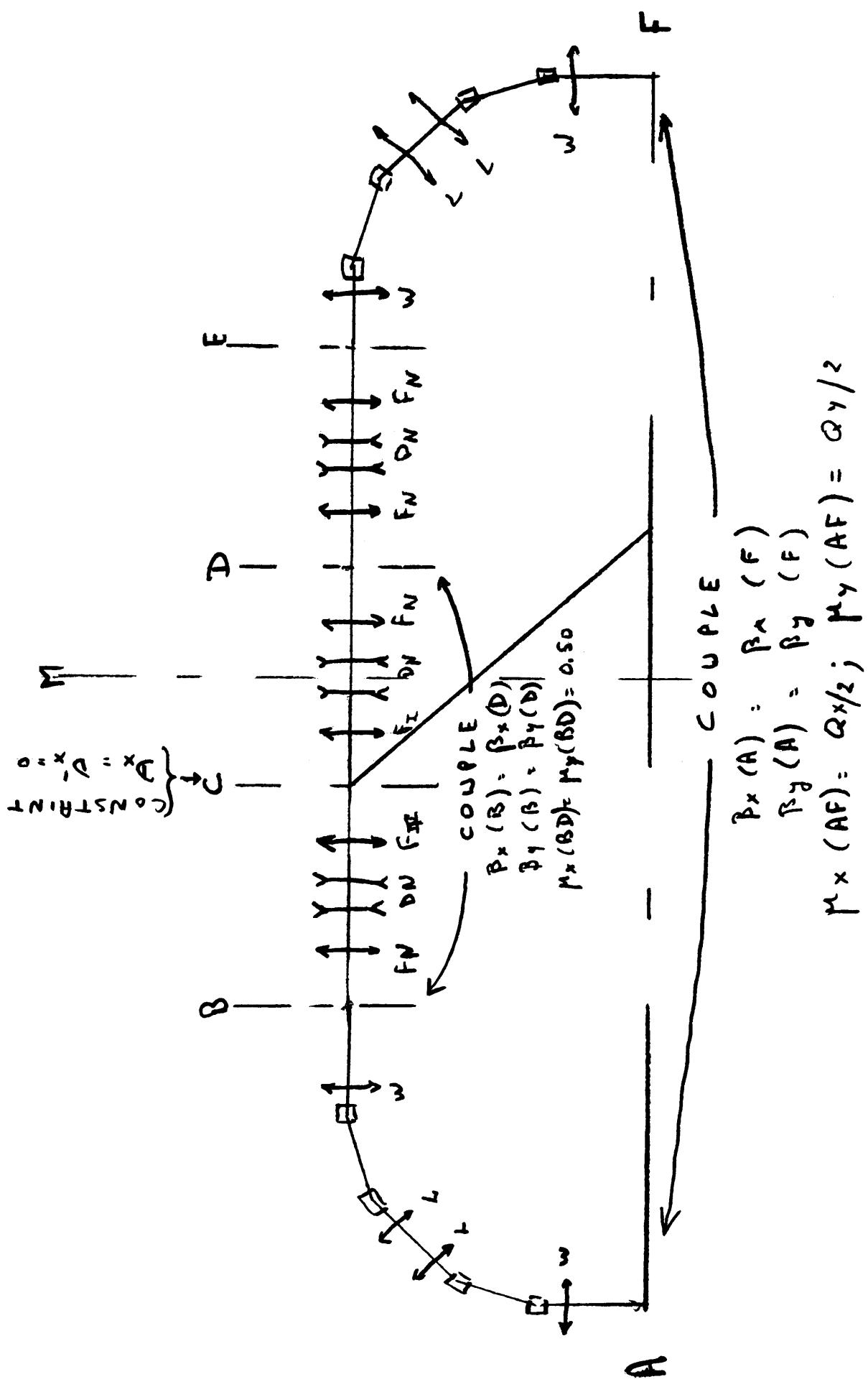
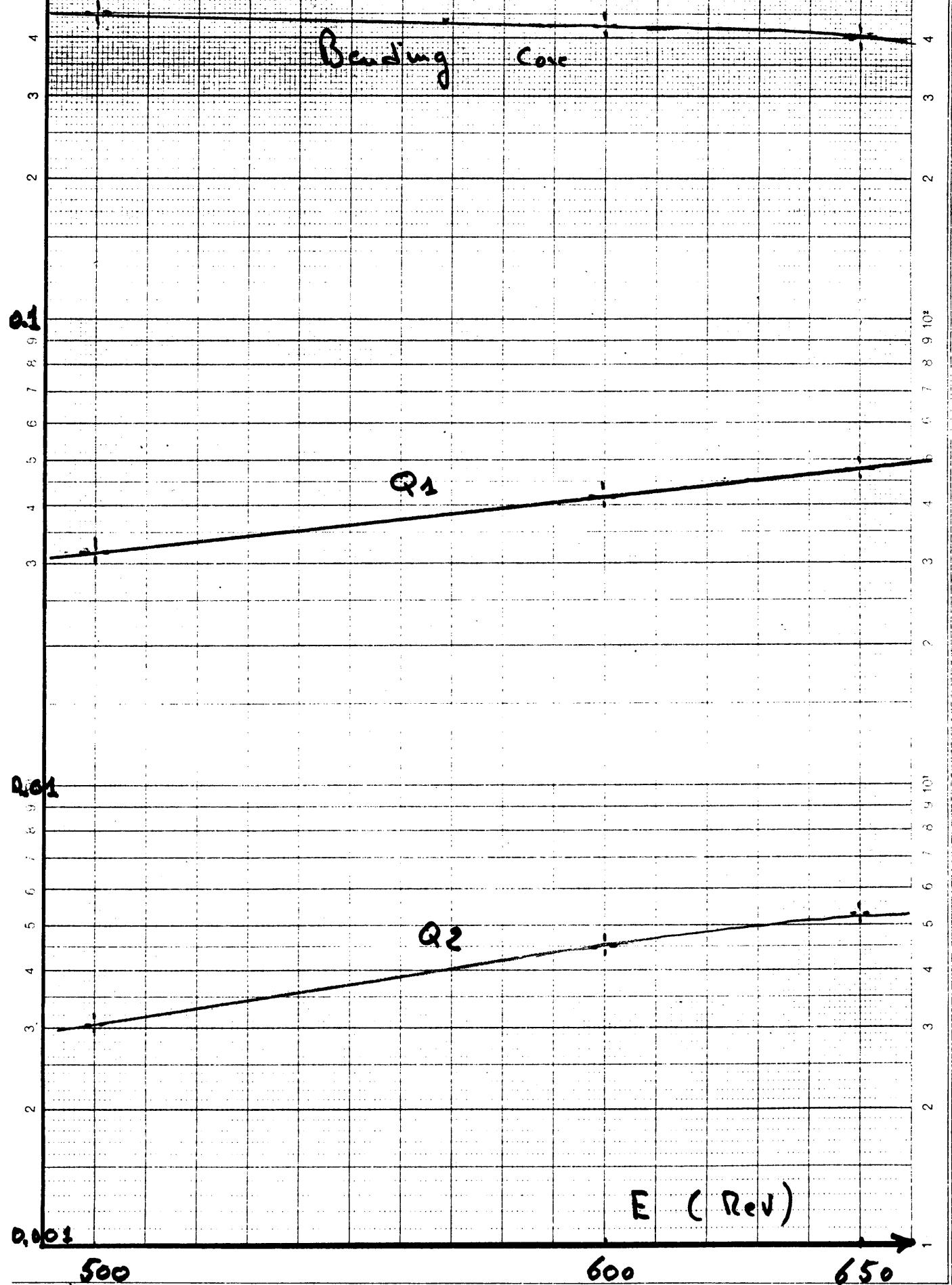


Fig 1: EPA lattice cell and matching method

$K_P (m^{-1})$

fig 2: Variation with the working energy of the
Bending flaguet model worn characteristics

(from PS/LPI Note 86-01)



$$\xi_x = \frac{dQ/a}{d\theta/\theta}$$

$$K^2 (m^{-1})$$

HR.QTR

Fig 3: Variation with the working Energy E
 of the trimming quadrupoles, HR.QTR
 strength and of the natural
 denominations: ξ_x and ξ_y

