

# Observation of associated production of top quarks with the ATLAS experiment

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on behalf of the ATLAS Collaboration

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Top quark and EW Physics

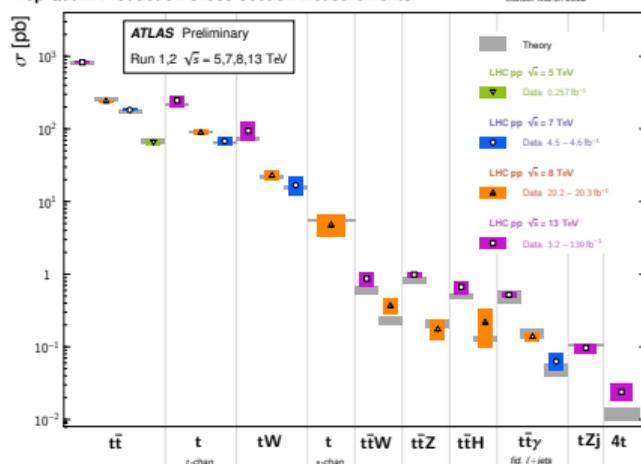
8. July 2022



- Stand-out role in the standard model due to high mass (173 GeV)
  - Decays before hadronisation ( $\tau \sim 10^{-25}$  s)  
→ direct probing through decay products
  - Yukawa coupling-strength close to unity
- Probing  $t\bar{t}V$  and  $tVq$  means probing the fundamental properties of the top quark
- Z-coupling sensitive to EW parameters: (hypercharge, weak isospin)
- Small tensor-like contributions with higher order loop corrections
- Coupling accessible through  $t\bar{t}V$  and  $tVq$  processes → probing theory predictions by measuring these rare processes
- In Run 2 we moved from discoveries to precision measurements
- Here:  
 $t\bar{t}\gamma$ : [JHEP 09\(2020\) 049](#),  $t\bar{t}Z$ : [Eur. Phys. J. C. 81 \(2021\) 737](#),  
 $tZq$ : [JHEP 07\(2020\) 124](#),  $t\gamma q$ : [ATLAS-CONF-2022-013](#),  
 $t\bar{t}t\bar{t}$  [JHEP 11 \(2021\) 118](#)



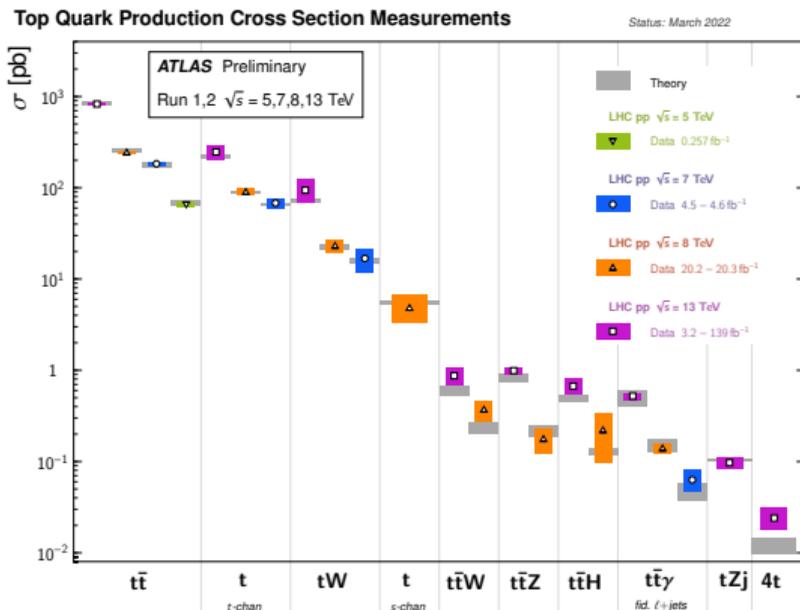
Top Quark Production Cross Section Measurements



Top cross section summary plot

# Run 2 - Observations and precision measurements with ATLAS

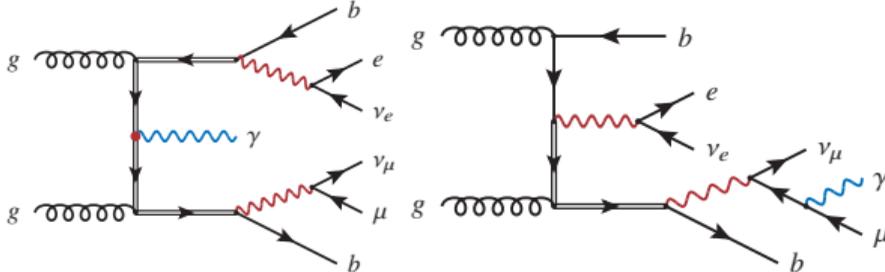
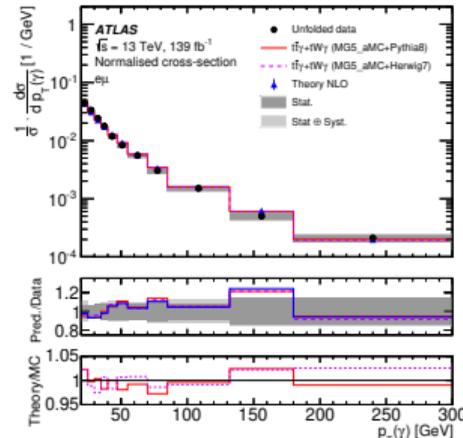
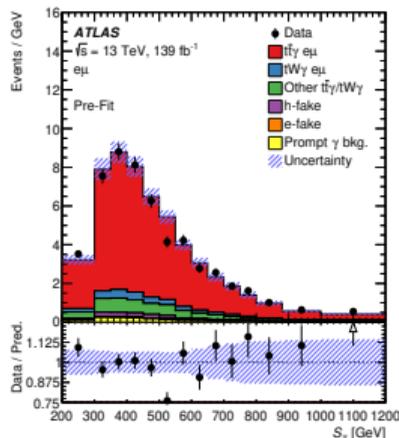
- Large Run 2 dataset allows for many precision analyses in the top-sector
- We are now able to increasingly probe rare SM processes such as  $t\bar{t}Z$ ,  $t\bar{t}\gamma$ ,  $t\gamma q$ ,  $tZq$  and even 4-tops
- $t\gamma q$  observed for the first time in ATLAS
- Able to measure inclusive **and** differential distributions
- Improved analyses techniques such as deployment of MVA techniques improve performance of several analyses



Top cross section summary plot

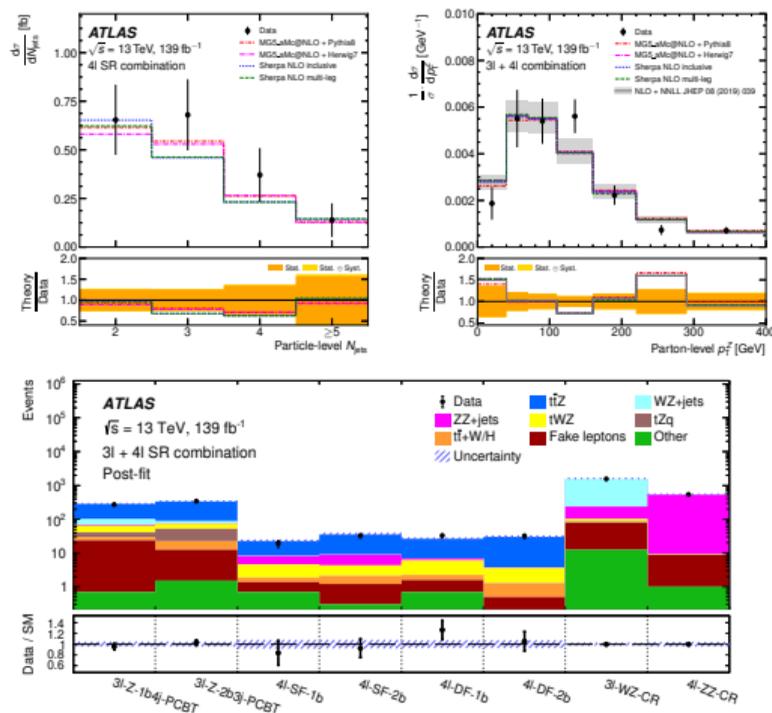
# $t\bar{t}\gamma$ -production - inclusive & differential

- $e\mu$  final state with single photon, two jets, at least one tagged
- Includes **both**  $t\bar{t}\gamma$  and  $tW\gamma \rightarrow$  check full off-shell calculations
- Measurement is performed in a fiducial volume defined at parton level
- Fiducial cross section:  
 $\sigma_{t\bar{t}\gamma}^{\text{fid.}} = 39.6 \pm 0.8(\text{stat.})_{-2.2}^{+2.6}(\text{syst.}) \text{ fb},$   
 $\sigma_{t\bar{t}\gamma}^{\text{SM, fid.}} = 38.50_{-2.18}^{+0.56}(\text{scale})_{-1.18}^{+1.04}(\text{PDF}) \text{ fb}$   
 meas. syst. limited ( $t\bar{t}\gamma/Wt\gamma$  modelling)
- Diff. cross-sections of several variables are compared with state-of-the-art MC simulations and NLO calculations
- All meas. in agreement with SM
- New  $t\bar{t}\gamma$  charge-asymmetry measurement  $\rightarrow$  Nellos talk



JHEP 09(2020) 049  
 Theory pred.: JHEP01(2019)188, JHEP10(2018)158

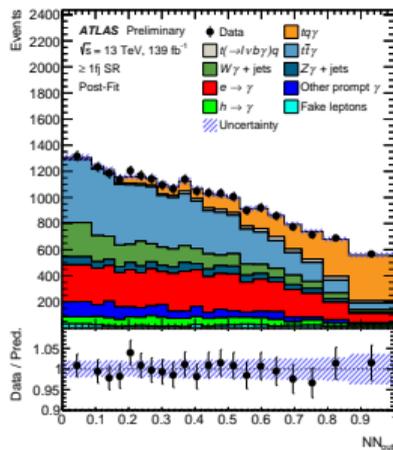
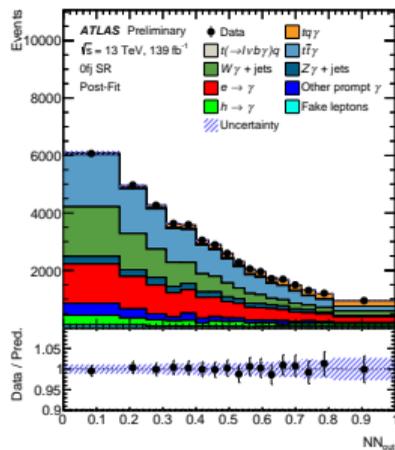
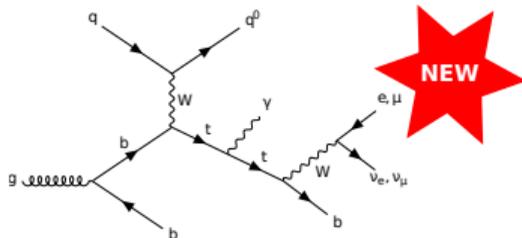
- Measurements targets  $3\ell$  and  $4\ell$  final states
- Trileptonic regions split by ( $b$ -)jet multiplicities. Tetraleptonic regions split into same-flavour/different-flavour non-Z leptons +  $b$ -jet multiplicity
- CRs to control WZ ( $3\ell$ ) and ZZ ( $4\ell$ )
- $\sigma_{t\bar{t}Z}^{\text{Incl.}} = 0.99 \pm 0.05(\text{stat.}) \pm 0.08(\text{syst.}) \text{ pb}$   
 $\sigma_{t\bar{t}Z}^{\text{NLO+NNLL}} = 863^{+8.5\%}_{-9.9\%}(\text{scale})^{+3.2\%}_{-3.2\%}(\text{PDF}+\alpha_s) \text{ fb}$   
 $\rightarrow$  relative unc. of 10%, syst. limited ( $t\bar{t}Z$  parton shower), in agreement with SM
- Diff. measurements of several variables in agreement with SM



Eur. Phys. J. C. 81 (2021) 737  
 Theory pred.: Eur. Phys. J. C 79 (2019) 249

# Observation $t\gamma q$ -production

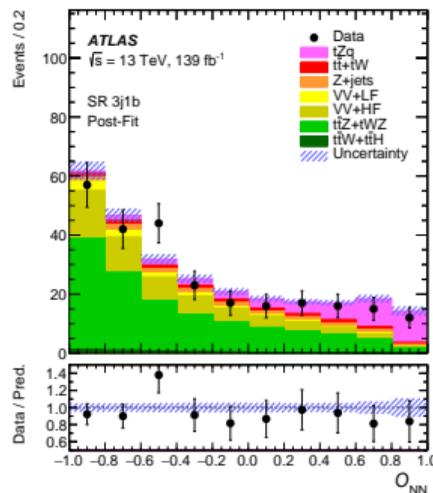
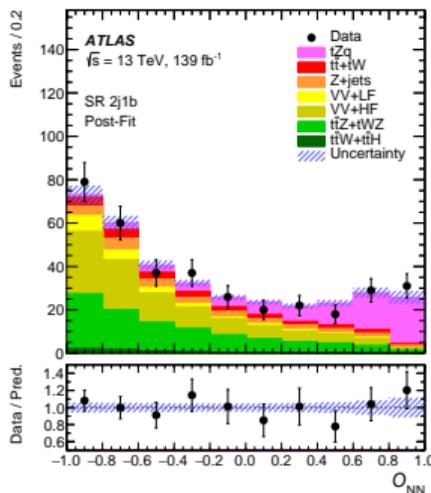
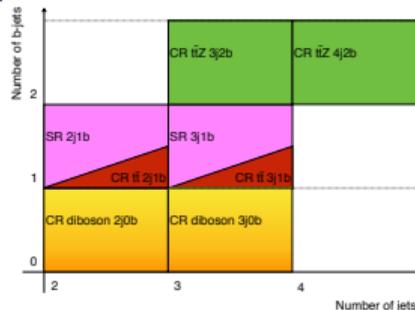
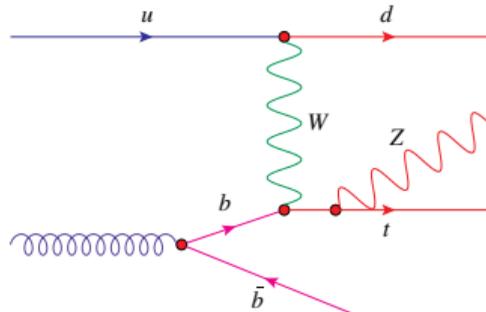
- Rare SM process sensitive to top- $\gamma$ / $W^\pm$  interaction & electric/magnetic dipole moments of top quark
- 2 SRs, requiring the presence of 1 photon, 1  $e/\mu$ , 1  $b$ -tagged jet and 1 or 0 forward jets
- Using NN to separate signal from background
- Performing profile-likelihood fit in the SRs &  $t\bar{t}\gamma$  CR with  $\mu_{t\gamma q}$ ,  $\mathcal{N}_{t\bar{t}\gamma}$ , and  $\mathcal{N}_{W+jets}$
- Observed (expected) significance is  $9.1\sigma$  ( $6.7\sigma$ )
- $\sigma_{t\gamma q}^{fid.} = 580 \pm 19(\text{stat.}) \pm 63(\text{syst.}) \text{ fb}$ ,  
syst. limited ( $t\bar{t}\gamma$  modelling)
- $\sigma_{t\gamma q}^{SM, fid.} = 406^{+25}_{-32} \text{ fb}$ . (compatible within  $2.5\sigma$ )  
 $\sim 40\%$  higher than SM, consistent with CMS



ATLAS-CONF-2022-013, Theory pred. ( $\sigma_{t\gamma q}^{SM, fid.}$ ) calculated @ NLO in QCD

# Observation of $tZq$ -production

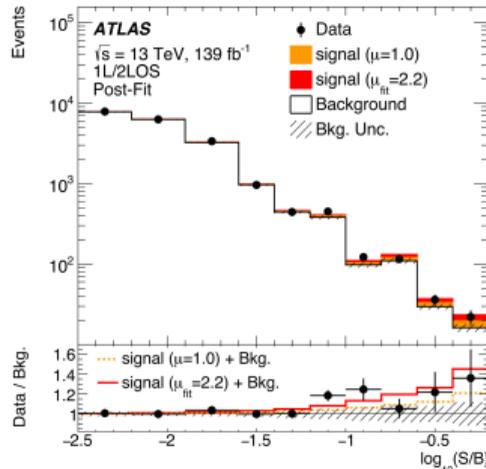
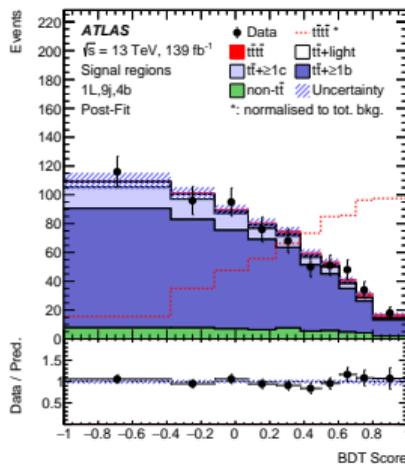
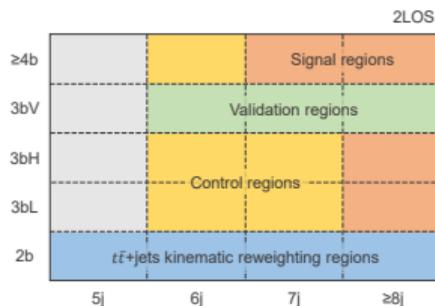
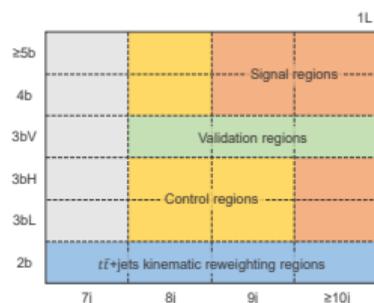
- Measured in  $3\ell$  channel with  $139 \text{ fb}^{-1}$
- $3\ell$  selections and 2 or 3 jets, one  $b$ -tagged, and one untagged
- 8 non-overlapping regions: 2 SRs, 6 CRs (constrain  $t\bar{t}Z$ ,  $t\bar{t}$ , diboson)
- NN for sig./bkg. separation
- Binned maximum-likelihood fit using SRs and CRs
- Incl.  $\sigma_{tZq}^{\text{fid.}} = 97 \pm 13(\text{stat.}) \pm 7(\text{syst.}) \text{ rel.}$  uncertainty  $\sim 14\%$  (stat. limited)
- Agrees with SM prediction:  
 $\sigma_{tZq}^{\text{SM, fid.}} = 102_{-2}^{+5} \text{ fb}$  (calculated @ NLO in QCD including non-resonant contributions with  $m_{\ell\ell} > 30 \text{ GeV}$ )



JHEP 07 (2020) 124, Theory pred. ( $\sigma_{tZq}^{\text{SM, fid.}}$ ) calculated @ NLO in QCD

# Evidence for four-tops-production

- Measuring 4-tops  $X_{\text{sec}}$  in single-lepton or opposite sign lepton pairs
- Events in  $1\ell$  and  $2\text{LOS}$  are split into 10 SRs, 11 CRs, 6 VRs
- Combining results with prev. ATLAS measurement in multi-lepton final states.
- ATLAS reports significance of  $4.7\sigma$  (2.6 expected)
- $\sigma_{\bar{t}\bar{t}\bar{t}\bar{t}} = 26 \pm 8(\text{stat.})_{-13}^{+15}(\text{syst.}) \text{ fb}$   
 $\sigma_{\bar{t}\bar{t}\bar{t}\bar{t}}^{\text{SM}} = 12.0 \pm 2.4 \text{ fb}$   
 agrees with SM within  $2\sigma$
- Meas. dominated by syst. uncertainties:  $\bar{t}\bar{t}\bar{t}\bar{t}$  &  $\bar{t}\bar{t} + \geq 1b$  modelling

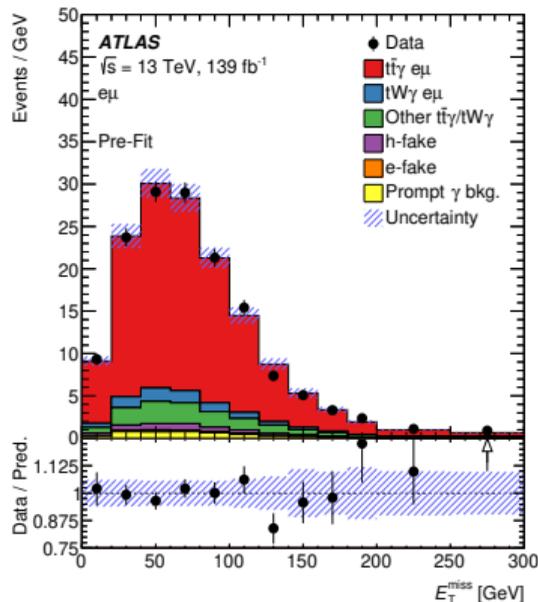
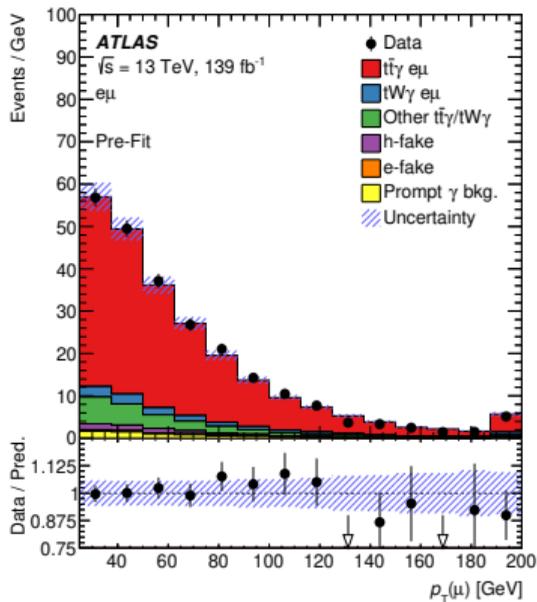
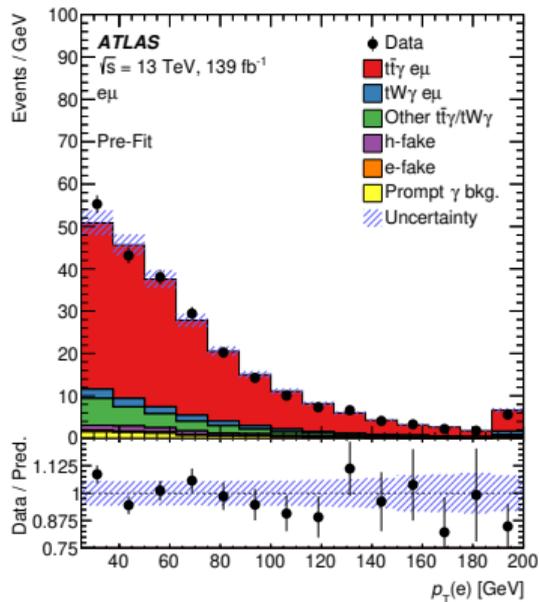


- Full Run 2 dataset allows for precision measurements in  $t\bar{t}V$  and  $tVq$  sector
- Presented today:
  - $t\bar{t}Z$  incl. and diff. measurements in  $3\ell$  and  $4\ell$
  - $t\bar{t}\gamma$  incl. and diff measurements in  $e\mu$  channel
  - $tZq$  incl. measurement
  - $t\gamma q$  incl. (brand new) measurement
  - Evidence for 4 tops production
- Presented measurements show good agreement for inclusive and differential results with SM predictions
  - Measurements are compared with state-of-the-art fixed-order computations as well as NLO+PS Monte Carlo simulations
- These analyses are the first round of ATLAS full Run 2 measurements → stringent tests of SM predictions
- Presented results are only glimpse of rich ATLAS **top-quark analysis program**
- With Run 2 measurements we have moved from discoveries to precision measurements in the  $t\bar{t}V$  and  $tVq$  sector! → Looking forward to Run 3.
- $t\bar{t}\gamma$ : [JHEP 09\(2020\) 049](#),  $t\bar{t}Z$ : [Eur. Phys. J. C. 81 \(2021\) 737](#),  
 $tZq$ : [JHEP 07\(2020\) 124](#),  $t\gamma q$ : [ATLAS-CONF-2022-013](#)  
 $t\bar{t}t\bar{t}$  [JHEP 11 \(2021\) 118](#)

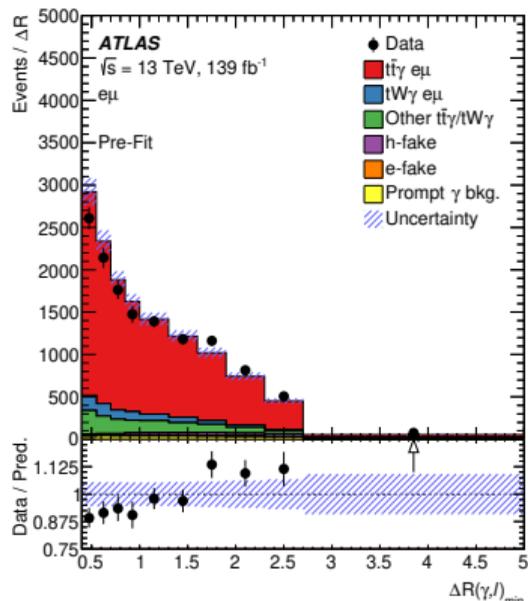
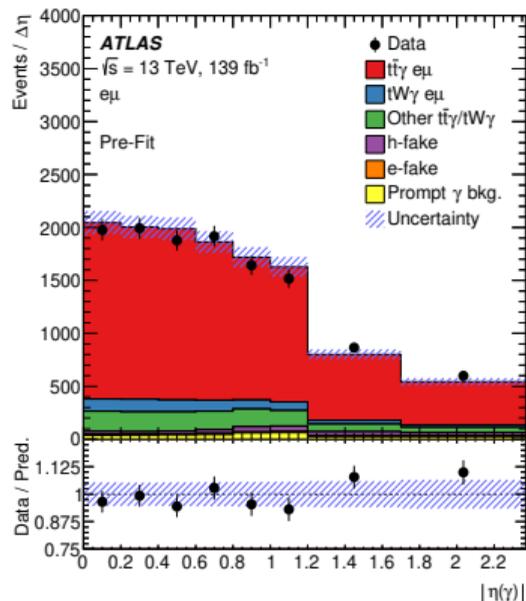
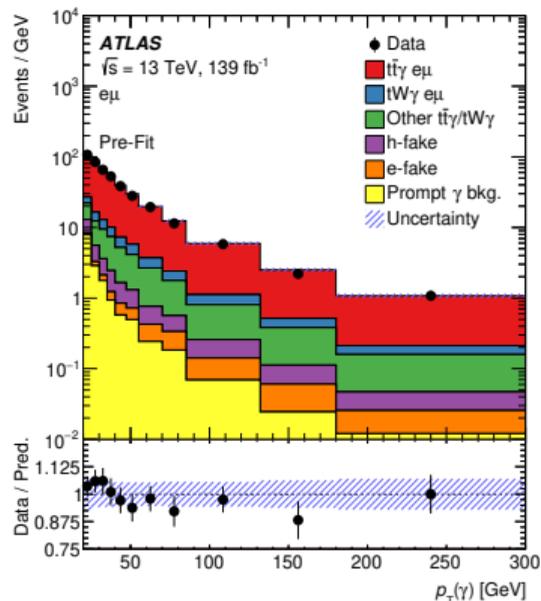


# Backup

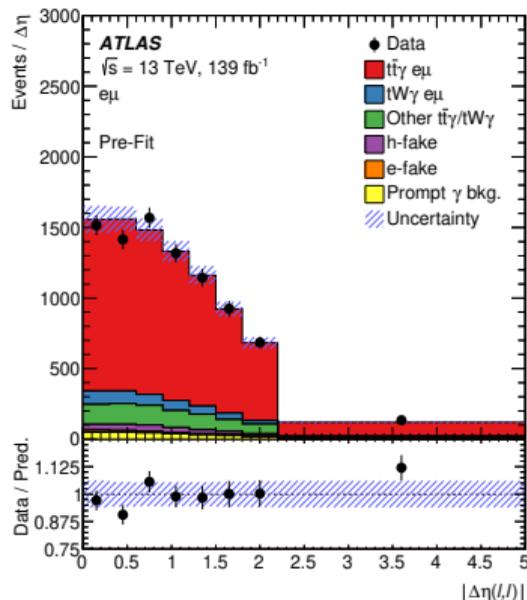
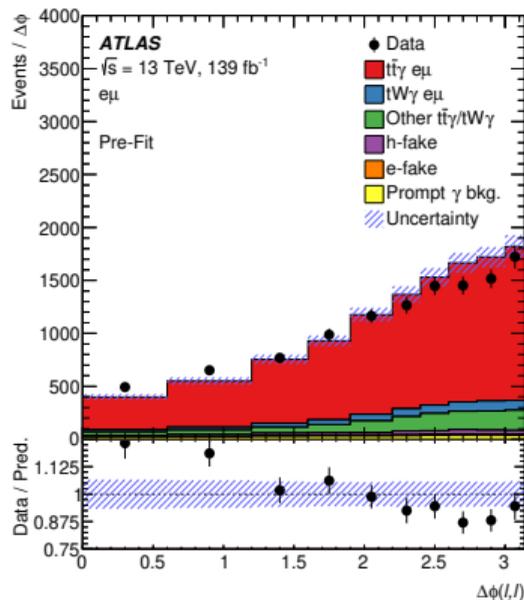
# $t\bar{t}\gamma$ – pre-fit control plots



# $t\bar{t}\gamma$ – unfolded variables pre-fit



# $t\bar{t}\gamma$ – unfolded variables pre-fit



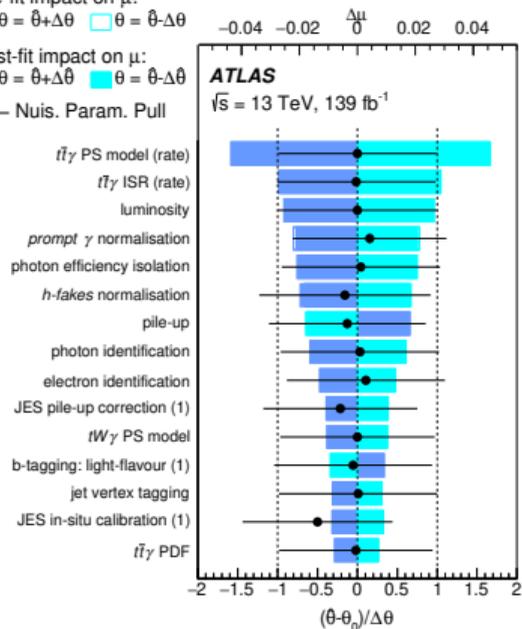
Pre-fit impact on  $\mu$ :

$\square \theta = \hat{\theta} + \Delta\theta$   $\square \theta = \hat{\theta} - \Delta\theta$

Post-fit impact on  $\mu$ :

$\blacksquare \theta = \hat{\theta} + \Delta\theta$   $\blacksquare \theta = \hat{\theta} - \Delta\theta$

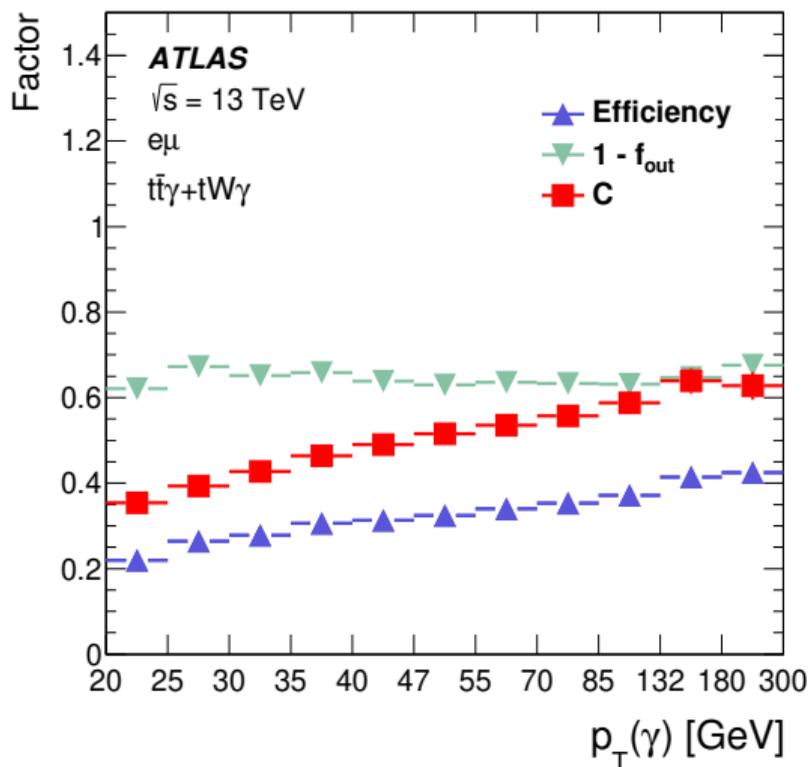
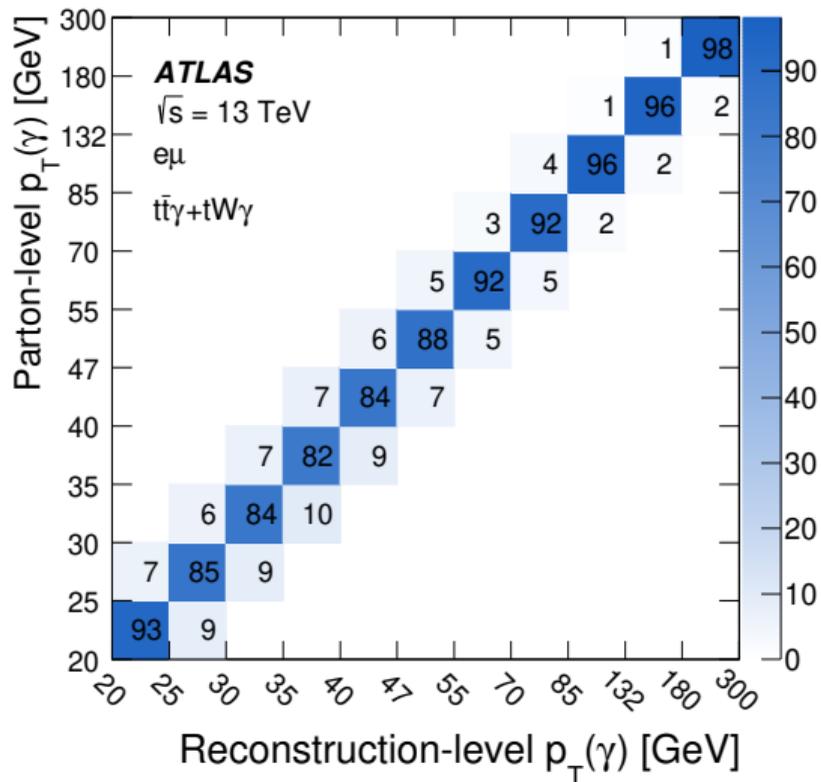
$\bullet$  Nuis. Param. Pull



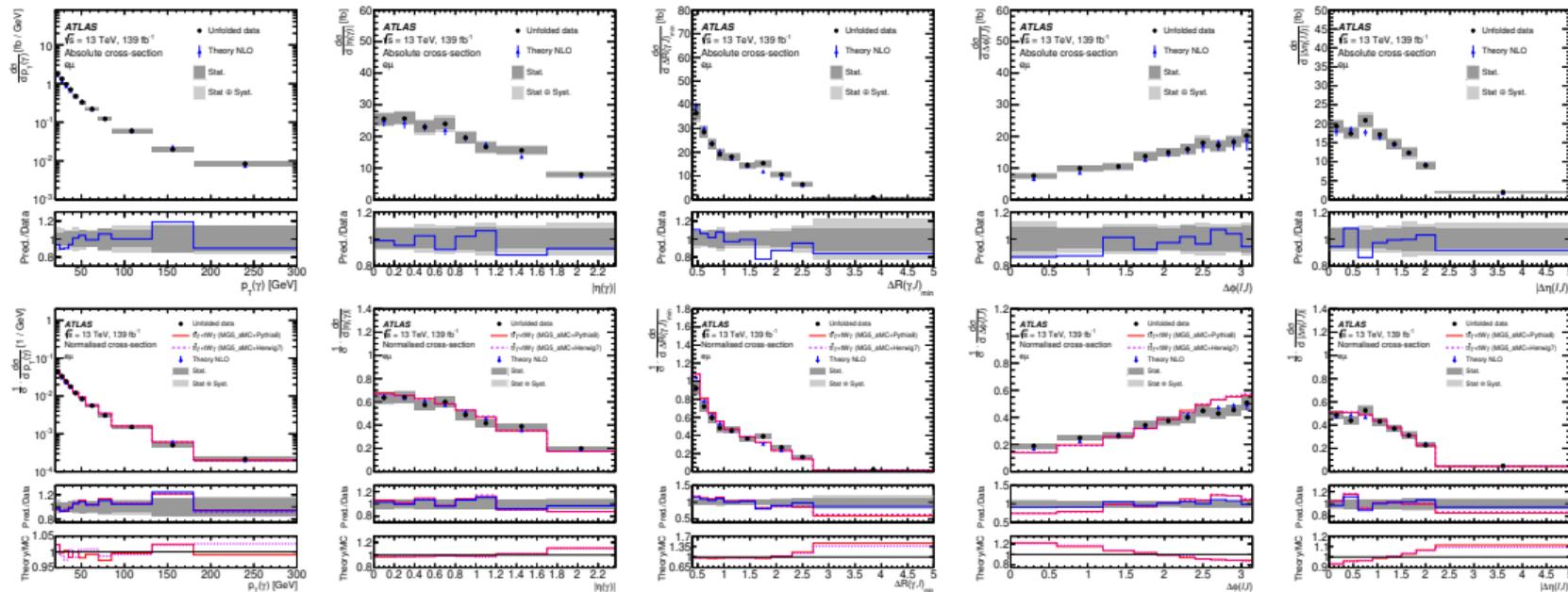
	Events
$t\bar{t}\gamma e\mu$	$2391 \pm 130$
$tW\gamma e\mu$	$156 \pm 15$
<i>Other</i> $t\bar{t}\gamma/tW\gamma$	$279 \pm 15$
h-fake	$78 \pm 40$
e-fake	$23 \pm 12$
Prompt $\gamma$ bkg.	$87 \pm 40$
<b>Total</b>	<b><math>3014 \pm 160</math></b>
<b>Data</b>	<b>3014</b>

Category	Uncertainty
$t\bar{t}\gamma/tW\gamma$ modelling	3.8%
Background modelling	2.1%
Photons	1.9%
Luminosity	1.8%
Jets	1.6%
Pile-up	1.3%
Leptons	1.1%
Flavour-tagging	1.1%
MC statistics	0.4%
Soft term $E_T^{\text{miss}}$	0.2%
$tW\gamma$ parton definition	2.8%
<b>Total syst.</b>	<b>6.3%</b>

# $t\bar{t}\gamma$ - migration matrix and efficiencies



# $t\bar{t}\gamma$ – absolute and normalised diff. cross sections



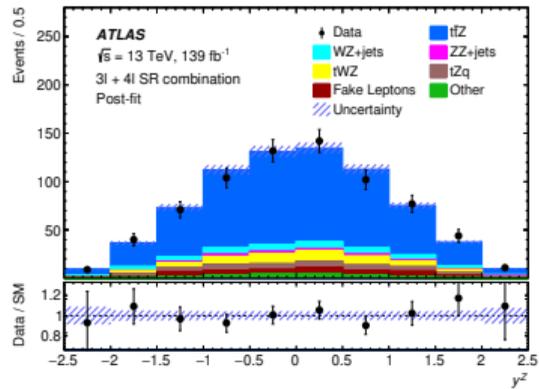
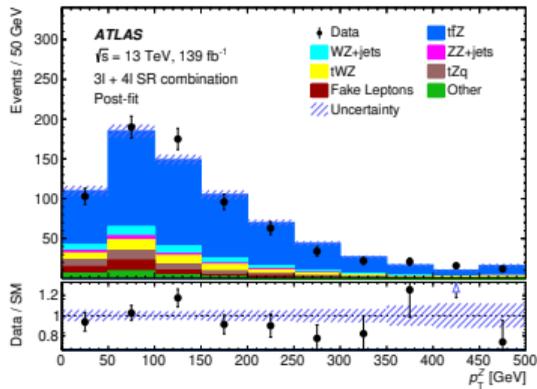
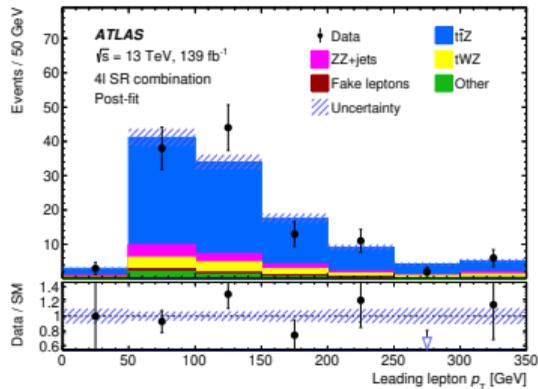
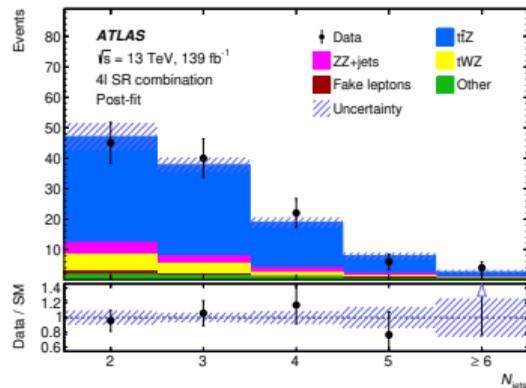
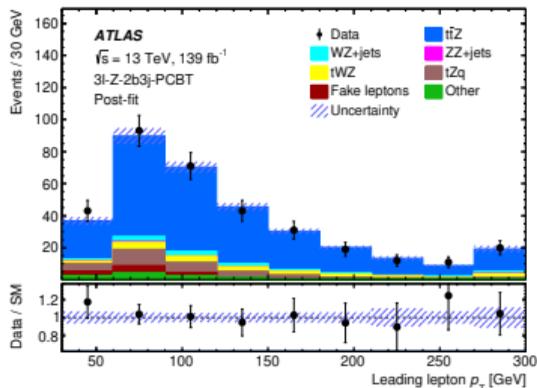
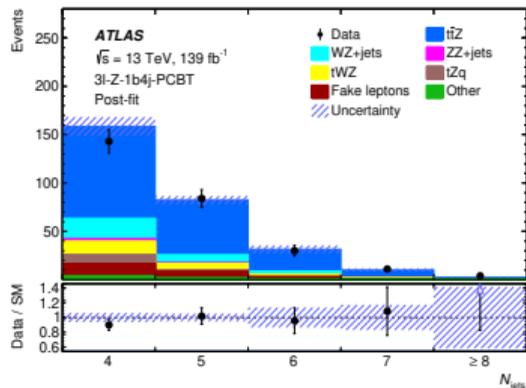
# $t\bar{t}\gamma$ - NLO calculations: $\chi^2$ & $p$ -values

Predictions	$p_T(\gamma)$		$ \eta(\gamma) $		$\Delta R(\gamma, \ell)_{\min}$		$\Delta\phi(\ell, \ell)$		$ \Delta\eta(\ell, \ell) $	
	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value
Theory NLO	6.1/11	0.87	4.5/8	0.81	11.7/10	0.31	5.8/10	0.83	6.2/8	0.62

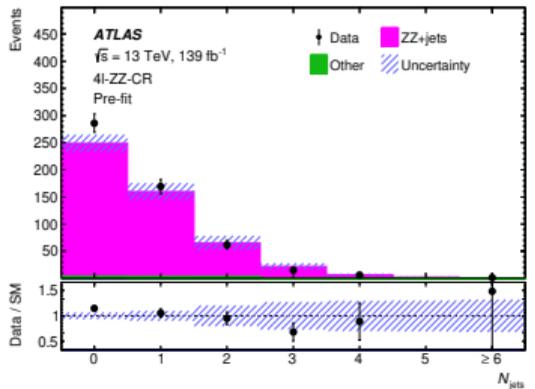
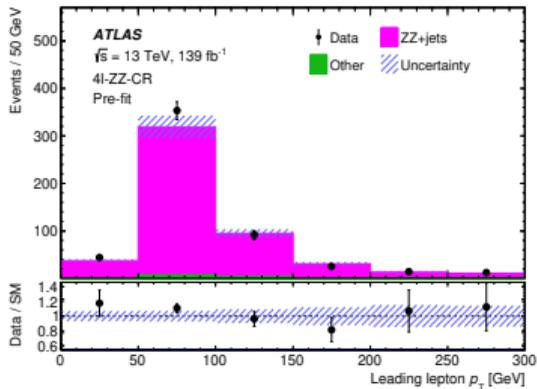
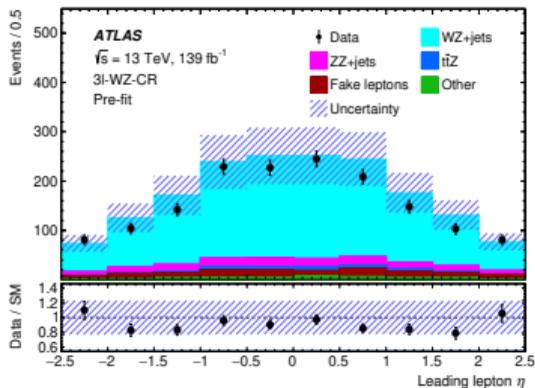
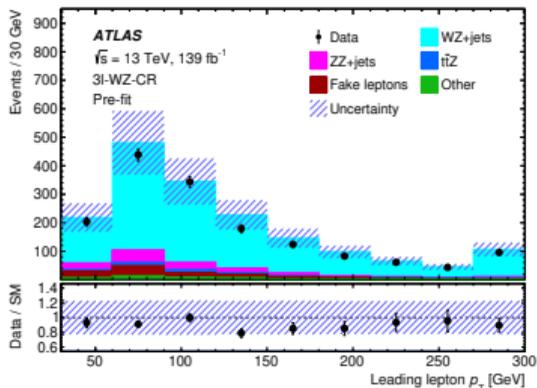
  

Predictions	$p_T(\gamma)$		$ \eta(\gamma) $		$\Delta R(\gamma, \ell)_{\min}$		$\Delta\phi(\ell, \ell)$		$ \Delta\eta(\ell, \ell) $	
	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value	$\chi^2/\text{ndf}$	$p$ -value
$t\bar{t}\gamma + tW\gamma$ (MG5_aMC+PYTHIA8)	6.3/10	0.79	7.3/7	0.40	20.1/9	0.02	30.8/9	<0.01	6.5/7	0.48
$t\bar{t}\gamma + tW\gamma$ (MG5_aMC+HERWIG7)	5.3/10	0.87	7.7/7	0.36	18.9/9	0.03	31.6/9	<0.01	6.8/7	0.45
Theory NLO	6.0/10	0.82	4.5/7	0.72	13.5/9	0.14	5.8/9	0.76	5.6/7	0.59

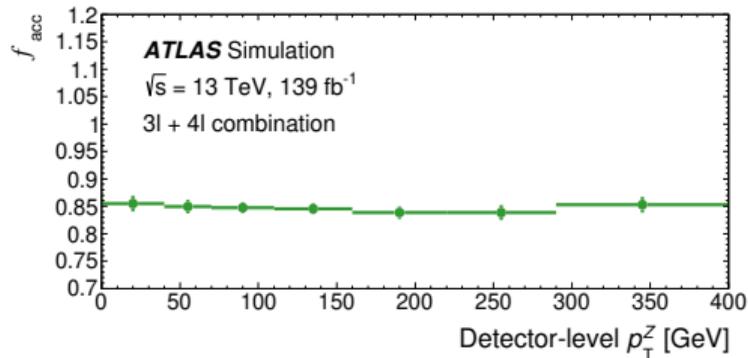
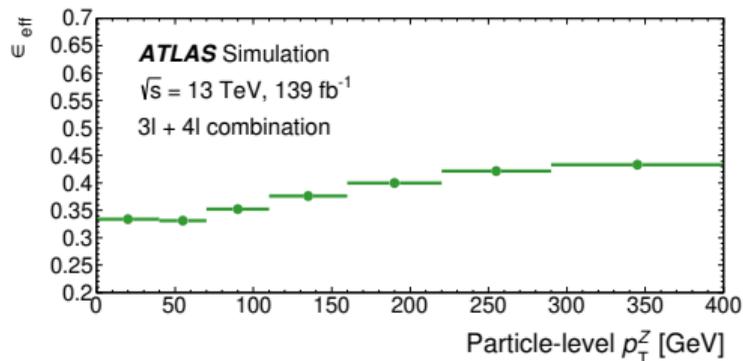
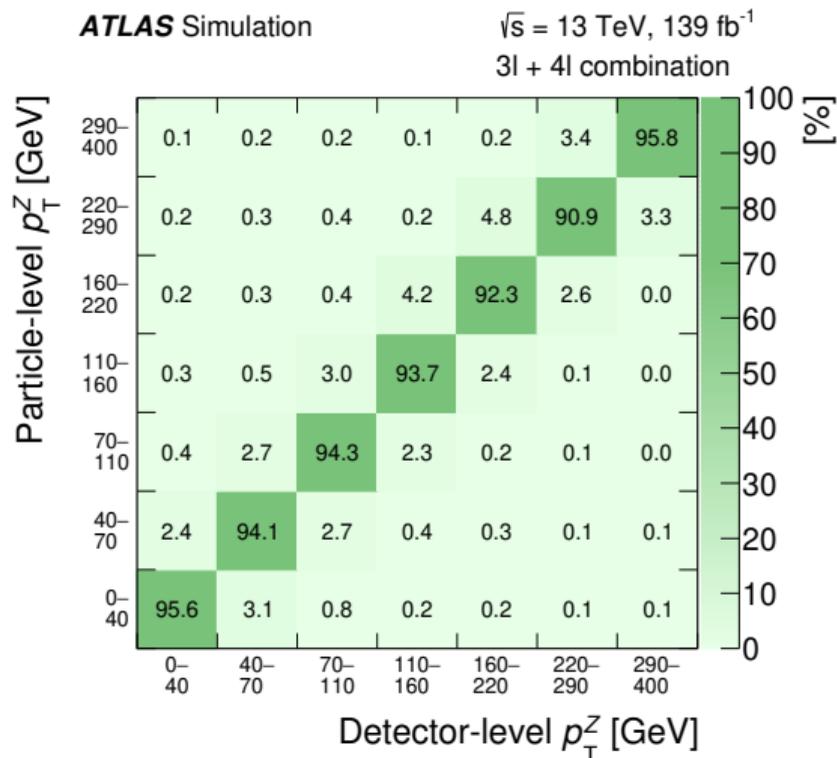
# $t\bar{t}Z$ - post fit distributions



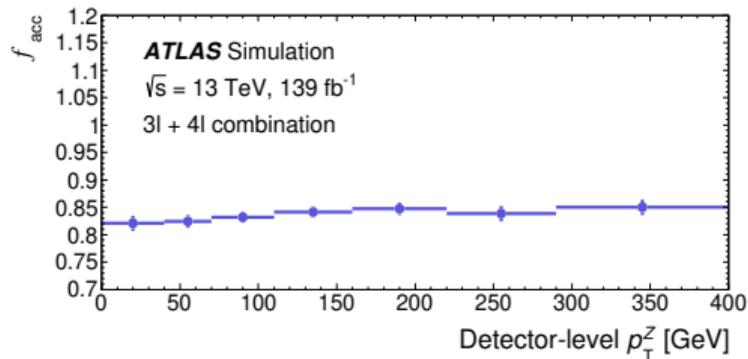
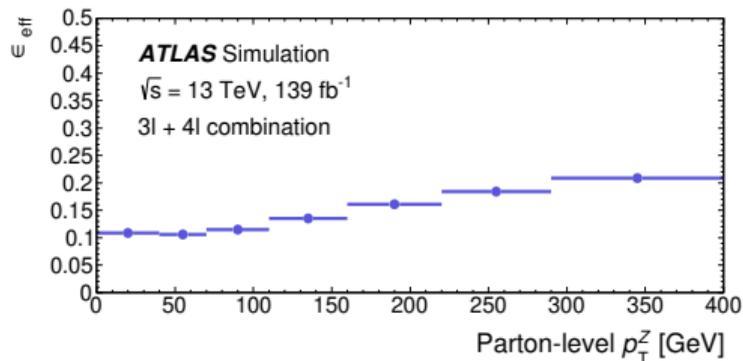
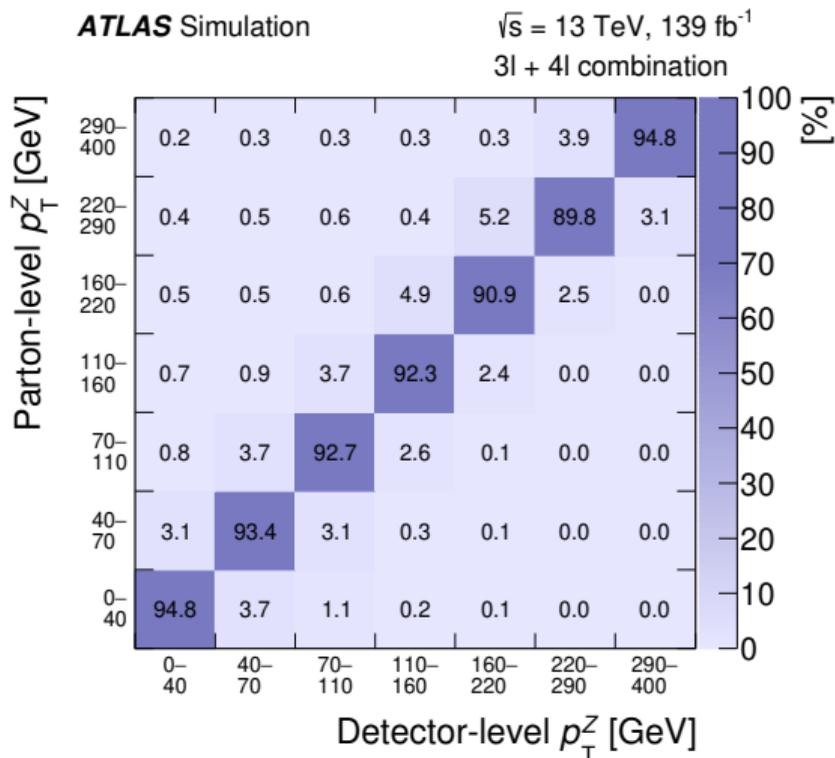
# $t\bar{t}Z$ - pre-fit CR distributions



# $t\bar{t}Z$ - Particle level migration matrix and efficiency



# $t\bar{t}Z$ - Parton level migration matrix and efficiency



# $t\bar{t}Z$ - Region definitions and $\mu_{t\bar{t}Z}$ results

Variable	3 $\ell$ -Z-1b4j-PCBT inclusive	3 $\ell$ -Z-2b3j-PCBT inclusive	3 $\ell$ -Z-2b3j differential
$N_{\ell} (\ell = e, \mu)$	= 3		
$p_T (\ell_1, \ell_2, \ell_3)$	$\geq 1$ OSSF lepton pair with $ m_{\ell\ell}^Z - m_Z  < 10$ GeV for all OSSF combinations: $m_{\text{OSSF}} > 10$ GeV		
$N_{\text{jets}}$	$\geq 4$	$\geq 3$	$\geq 3$
$N_{b\text{-jets}}$	= 1@60%	$\geq 2$ @70%	$\geq 2$ @85%
	veto add. $b$ -jets@70%		

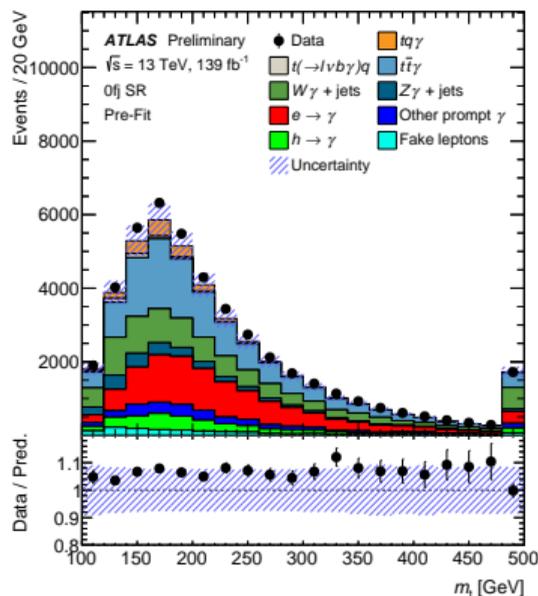
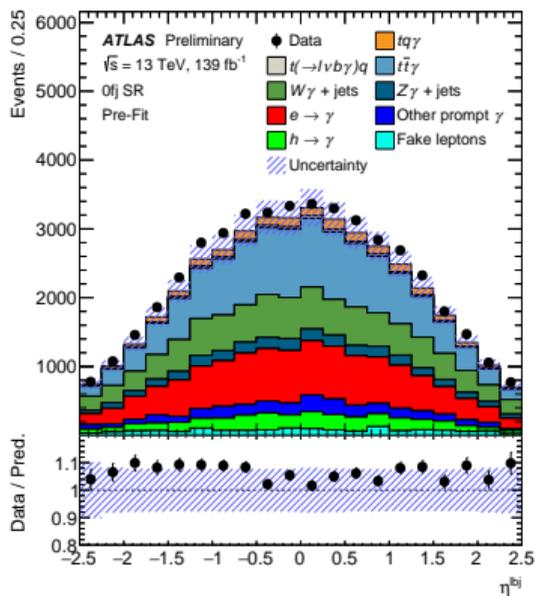
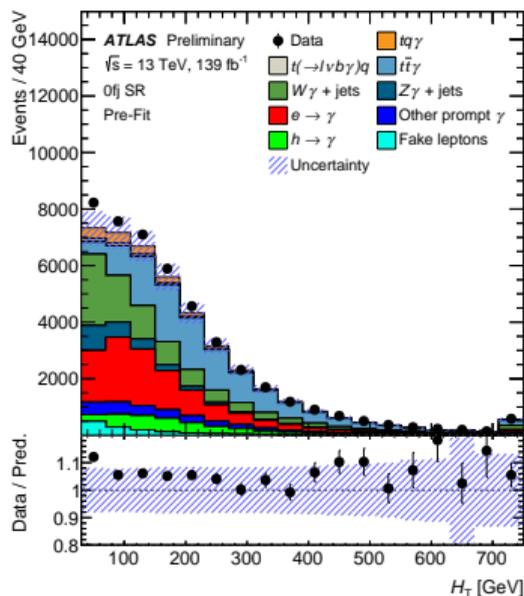
Variable	4 $\ell$ -SF-1b	4 $\ell$ -SF-2b	4 $\ell$ -DF-1b	4 $\ell$ -DF-2b
$N_{\ell} (\ell = e, \mu)$	= 4			
	$\geq 1$ OSSF lepton pair with $ m_{\ell\ell}^Z - m_Z  < 10$ GeV for all OSSF combinations: $m_{\text{OSSF}} > 10$ GeV			
$p_T (\ell_1, \ell_2, \ell_3, \ell_4)$	$> 27, 20, 10, 7$ GeV			
$\ell\ell^{\text{non-Z}}$	$e^+e^-$ or $\mu^+\mu^-$	$e^+e^-$ or $\mu^+\mu^-$	$e^\pm\mu^\mp$	$e^\pm\mu^\mp$
$E_T^{\text{miss}}$	$> 100$ GeV, if $ m_{\ell\ell}^{\text{non-Z}} - m_Z  \leq 10$ GeV	$> 50$ GeV, if $ m_{\ell\ell}^{\text{non-Z}} - m_Z  \leq 10$ GeV	-	-
	$> 50$ GeV, if $ m_{\ell\ell}^{\text{non-Z}} - m_Z  > 10$ GeV	-		
$N_{\text{jets}}$	$\geq 2$	$\geq 2$	$\geq 2$	$\geq 2$
$N_{b\text{-jets}}@85\%$	= 1	$\geq 2$	= 1	$\geq 2$

Variable	3 $\ell$ -WZ-CR	4 $\ell$ -ZZ-CR
$N_{\ell} (\ell = e, \mu)$	= 3	= 4
	1 OSSF lepton pair with $ m_{\ell\ell} - m_Z  < 10$ GeV	2 OSSF lepton pairs with $ m_{\ell\ell} - m_Z  < 10$ GeV
$p_T(\ell_1, \ell_2, \ell_3, \ell_4)$	$> 27, 20, 20$ GeV	$> 27, 20, 10, 7$ GeV
$N_{\text{jets}}$	$\geq 3$	-
$N_{b\text{-jets}}@85\%$	= 0	-
$E_T^{\text{miss}}$	-	$20 \text{ GeV} < E_T^{\text{miss}} < 40 \text{ GeV}$

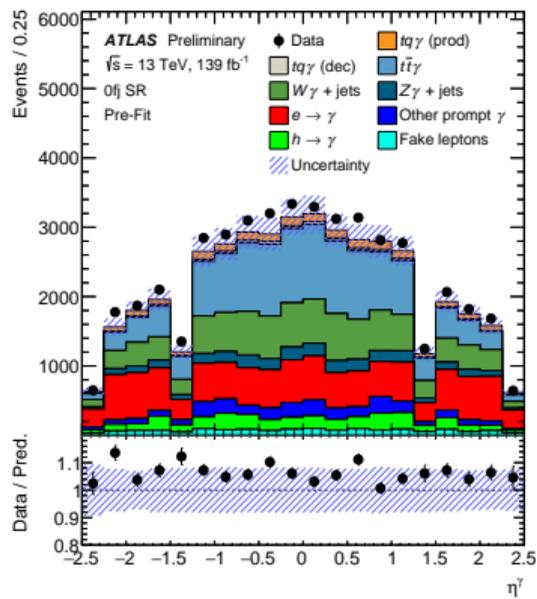
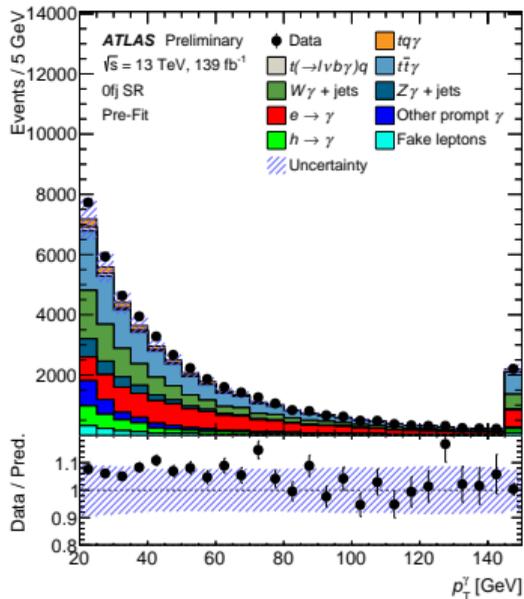
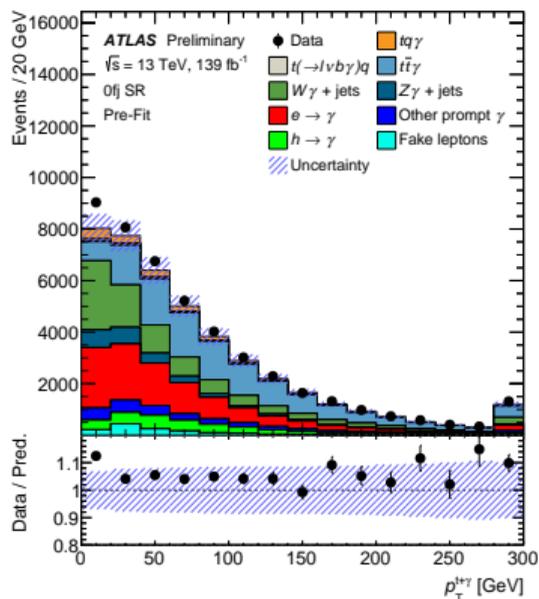
Channel	$\mu_{t\bar{t}Z}$
Trilepton	$1.17 \pm 0.07$ (stat.) $^{+0.12}_{-0.11}$ (syst.)
Tetralepton	$1.21 \pm 0.15$ (stat.) $^{+0.11}_{-0.10}$ (syst.)
Combination (3 $\ell$ + 4 $\ell$ )	$1.19 \pm 0.06$ (stat.) $\pm 0.10$ (syst.)

Region	$3\ell\text{-}Z\text{-}1b4j$ -PCBT	$3\ell\text{-}Z\text{-}2b3j$ -PCBT	$4\ell\text{-SF-}1b$	$4\ell\text{-SF-}2b$	$4\ell\text{-DF-}1b$	$4\ell\text{-DF-}2b$	$3\ell\text{-WZ-CR}$	$4\ell\text{-ZZ-CR}$
$t\bar{t}Z$	$185 \pm 16$	$247 \pm 20$	$14.5 \pm 1.7$	$26.9 \pm 2.5$	$19.3 \pm 1.8$	$26.7 \pm 2.3$	$45 \pm 11$	$0.8 \pm 0.1$
$WZ + l$	$2.4 \pm 1.8$	$0.2 \pm 0.3$	–	–	–	–	$1068 \pm 110$	–
$WZ + b$	$20 \pm 11$	$10.8 \pm 6.1$	–	–	–	–	$11.2 \pm 6.3$	–
$WZ + c$	$10.8 \pm 4.8$	$1.8 \pm 0.8$	–	–	–	–	$207 \pm 87$	–
$ZZ + l$	$0.3 \pm 0.2$	$0.02 \pm 0.02$	$1.7 \pm 0.7$	$0.9 \pm 0.5$	$0.5 \pm 0.1$	$0.02 \pm 0.01$	$121 \pm 15$	$496 \pm 26$
$ZZ + b$	$3.0 \pm 1.6$	$2.0 \pm 1.0$	$0.9 \pm 0.6$	$2.5 \pm 1.5$	$0.2 \pm 0.1$	$0.07 \pm 0.07$	$1.8 \pm 0.9$	$12.9 \pm 7.1$
$ZZ + c$	$0.7 \pm 0.2$	$0.1 \pm 0.1$	$0.9 \pm 0.5$	$1.1 \pm 0.6$	$0.2 \pm 0.1$	$0.02 \pm 0.01$	$13.0 \pm 4.1$	$19.8 \pm 7.1$
$tWZ$	$23.8 \pm 4.0$	$20.5 \pm 7.0$	$2.7 \pm 0.4$	$2.2 \pm 0.8$	$3.8 \pm 1.1$	$2.3 \pm 0.9$	$13.2 \pm 1.2$	$0.2 \pm 0.1$
$tZq$	$10.8 \pm 4.5$	$29.7 \pm 9.0$	–	–	–	–	$8.6 \pm 3.2$	–
$t\bar{t}+W/H$	$5.8 \pm 0.9$	$10.1 \pm 2.2$	$0.5 \pm 0.1$	$0.9 \pm 0.1$	$0.6 \pm 0.1$	$0.8 \pm 0.1$	$1.8 \pm 0.4$	$0.01 \pm 0.01$
Fake leptons	$23 \pm 11$	$11.0 \pm 5.3$	$0.7 \pm 0.3$	$0.9 \pm 0.4$	$0.9 \pm 0.5$	$0.3 \pm 0.1$	$65 \pm 31$	$7.9 \pm 3.1$
Other	$0.7 \pm 0.4$	$1.5 \pm 0.7$	$0.7 \pm 0.3$	$0.2 \pm 0.1$	$0.7 \pm 0.4$	$0.2 \pm 0.1$	$12.4 \pm 6.3$	$1.0 \pm 0.5$
SM total	$286 \pm 13$	$334 \pm 15$	$22.5 \pm 1.8$	$35.6 \pm 2.7$	$26.1 \pm 1.9$	$30.3 \pm 2.2$	$1569 \pm 43$	$539 \pm 23$
Data	272	343	19	33	33	32	1569	539

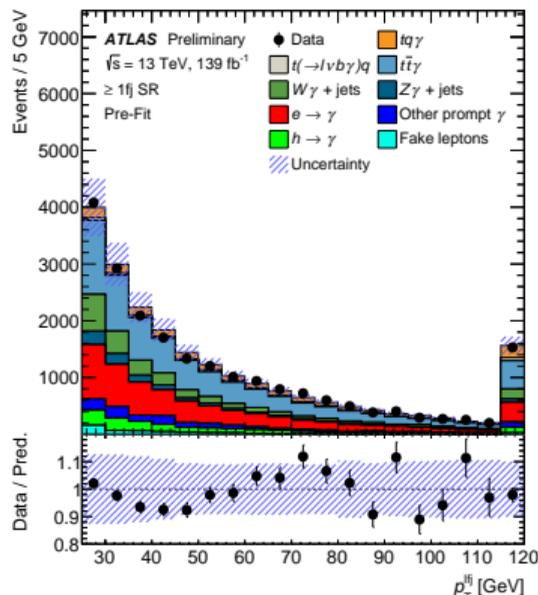
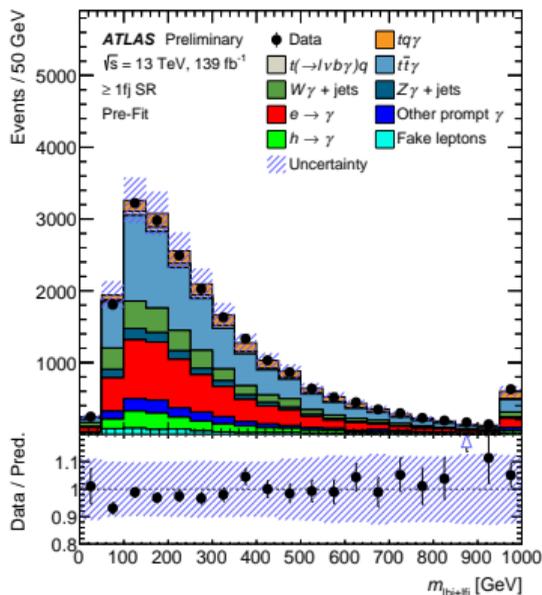
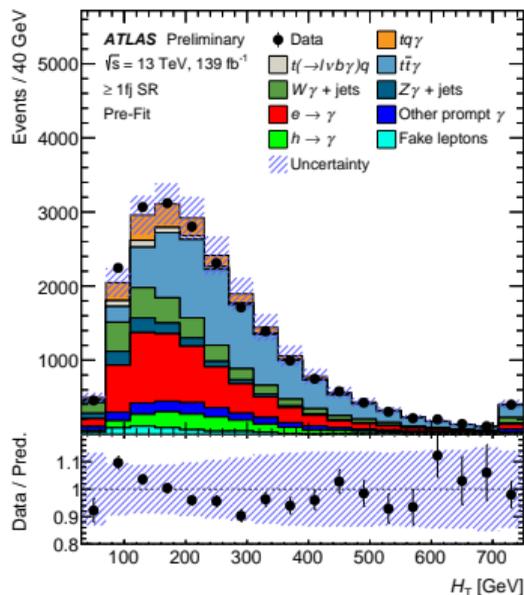
# $t\bar{t}\gamma$ - pre-fit event yields (0fj SR)



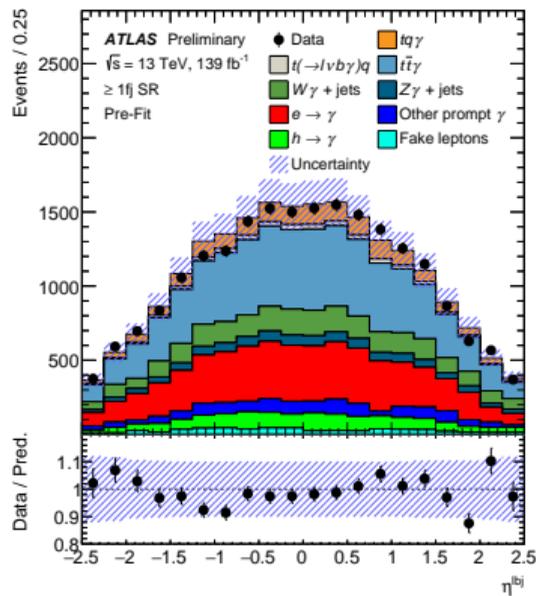
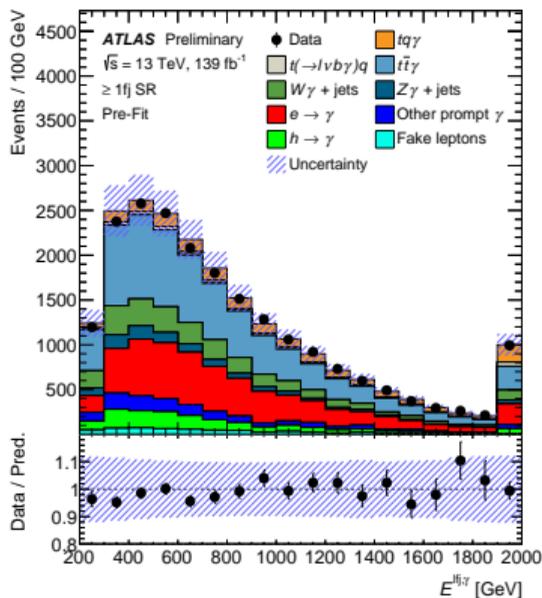
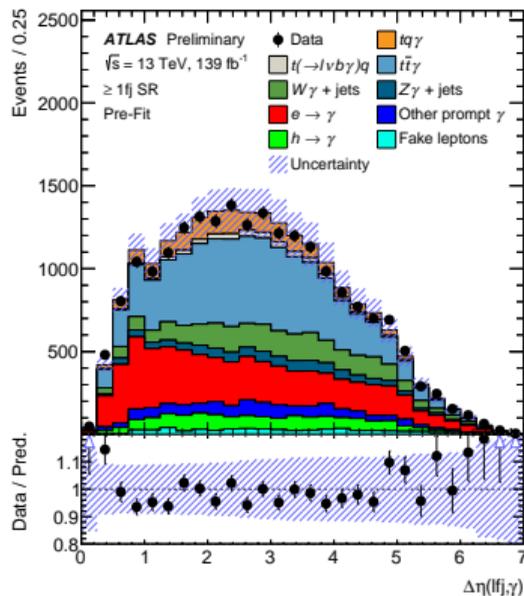
# $t\bar{t}\gamma$ - pre-fit event yields (0fj SR)



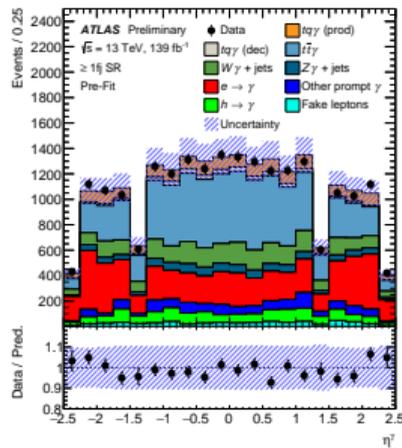
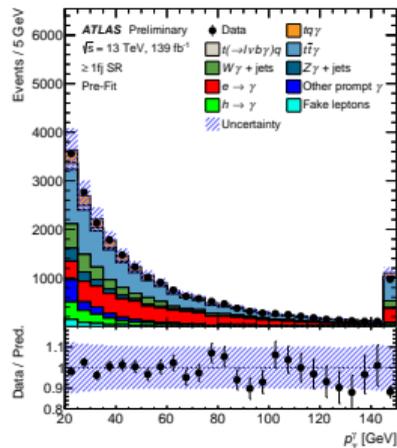
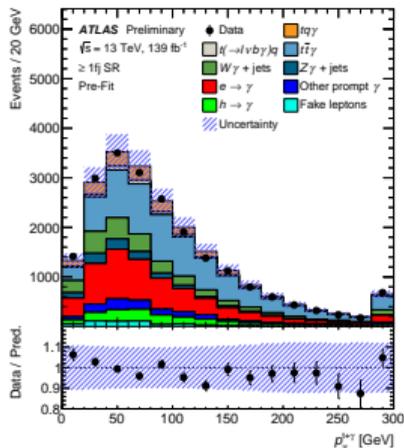
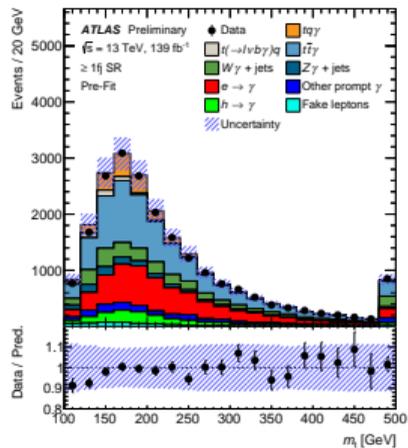
# $t\gamma q$ - pre-fit event yields ( $\geq 1fj$ SR)



# $t\gamma q$ - pre-fit event yields ( $\geq 1f_j$ SR)



# $t\gamma q$ - pre-fit event yields ( $\geq 1\text{fj SR}$ )



# $t\gamma q$ - Parton level post-fit event yields

	$\geq 1\text{fj SR}$	0fj SR	$t\bar{t}\gamma$ CR	$W\gamma$ CR
$tq\gamma$	$2390 \pm 260$	$2480 \pm 320$	$890 \pm 120$	$1280 \pm 150$
$t(\rightarrow \ell\nu b\gamma)q$	$360 \pm 150$	$460 \pm 240$	$120 \pm 50$	$230 \pm 110$
$t\bar{t}\gamma$ (production)	$3100 \pm 400$	$4800 \pm 700$	$4300 \pm 600$	$2720 \pm 350$
$t\bar{t}\gamma$ (radiative decay)	$3800 \pm 600$	$9300 \pm 1400$	$5700 \pm 600$	$4300 \pm 900$
$W\gamma$ +jets	$2500 \pm 400$	$9300 \pm 1300$	$1050 \pm 190$	$31\,900 \pm 3000$
$Z\gamma$ +jets	$990 \pm 310$	$2800 \pm 800$	$440 \pm 150$	$7900 \pm 2400$
$e \rightarrow \gamma$ fake photons	$5200 \pm 500$	$10\,300 \pm 800$	$4800 \pm 400$	$5400 \pm 500$
$h \rightarrow \gamma$ fake photons	$1100 \pm 400$	$2700 \pm 800$	$1300 \pm 500$	$2500 \pm 800$
Other prompt $\gamma$	$1360 \pm 350$	$2600 \pm 900$	$1400 \pm 400$	$4100 \pm 500$
Fake leptons	$350 \pm 170$	$900 \pm 400$	$100 \pm 50$	$3300 \pm 1600$
Total	$21\,250 \pm 150$	$45\,720 \pm 240$	$20\,180 \pm 140$	$63\,590 \pm 310$
Data	21 227	45 723	20 194	63 592

# $t\gamma q$ - Particle level post-fit event yields

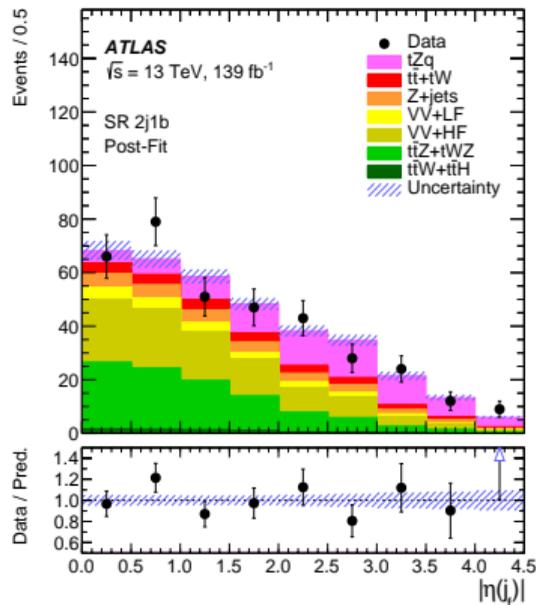
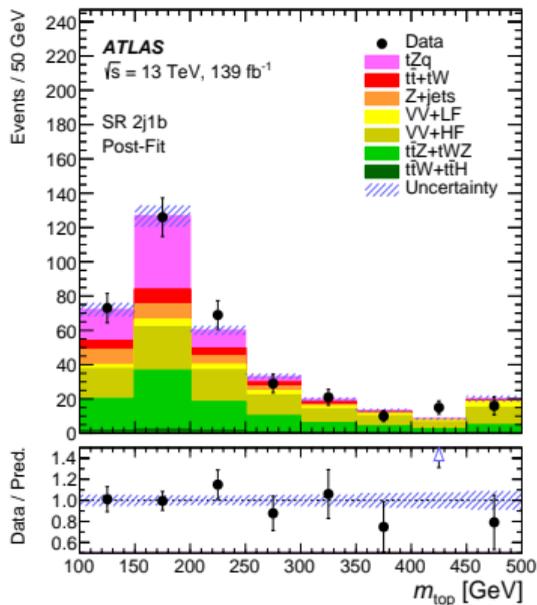
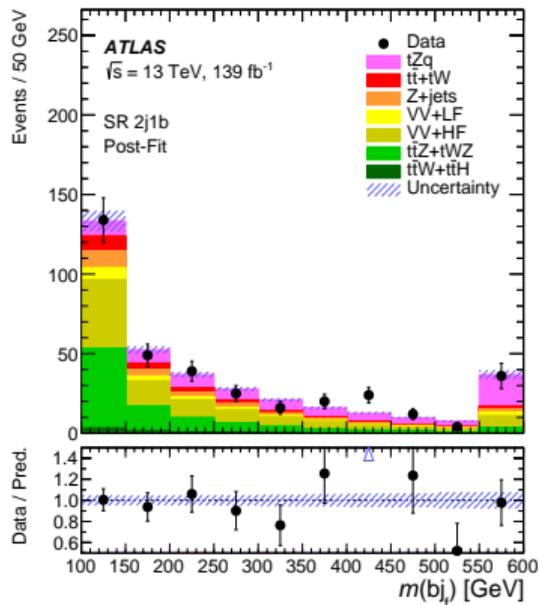
	$\geq 1\text{fj SR}$	0fj SR	$t\bar{t}\gamma$ CR	$W\gamma$ CR
$tq\gamma$	$2340 \pm 250$	$2430 \pm 310$	$880 \pm 120$	$1250 \pm 140$
$t(\rightarrow \ell\nu b\gamma)q$	$480 \pm 160$	$660 \pm 210$	$170 \pm 60$	$320 \pm 120$
$t\bar{t}\gamma$ (production)	$3100 \pm 400$	$4700 \pm 700$	$4200 \pm 600$	$2670 \pm 350$
$t\bar{t}\gamma$ (radiative decay)	$3700 \pm 600$	$9100 \pm 1300$	$5600 \pm 600$	$4200 \pm 900$
$W\gamma$ +jets	$2500 \pm 400$	$9400 \pm 1300$	$1060 \pm 190$	$31\,800 \pm 3000$
$Z\gamma$ +jets	$990 \pm 310$	$2800 \pm 800$	$440 \pm 150$	$7900 \pm 2400$
$e \rightarrow \gamma$ fake photons	$5200 \pm 500$	$10\,400 \pm 800$	$4900 \pm 400$	$5500 \pm 500$
$h \rightarrow \gamma$ fake photons	$1200 \pm 400$	$2700 \pm 800$	$1400 \pm 500$	$2600 \pm 800$
Other prompt $\gamma$	$1380 \pm 350$	$2600 \pm 900$	$1400 \pm 400$	$4100 \pm 500$
Fake leptons	$350 \pm 170$	$900 \pm 500$	$100 \pm 50$	$3300 \pm 1600$
Total	$21\,250 \pm 150$	$45\,720 \pm 240$	$20\,180 \pm 150$	$63\,590 \pm 320$
Data	21 227	45 723	20 194	63 592

# $t\gamma q$ - Systematic uncertainties for particle and parton level measurement

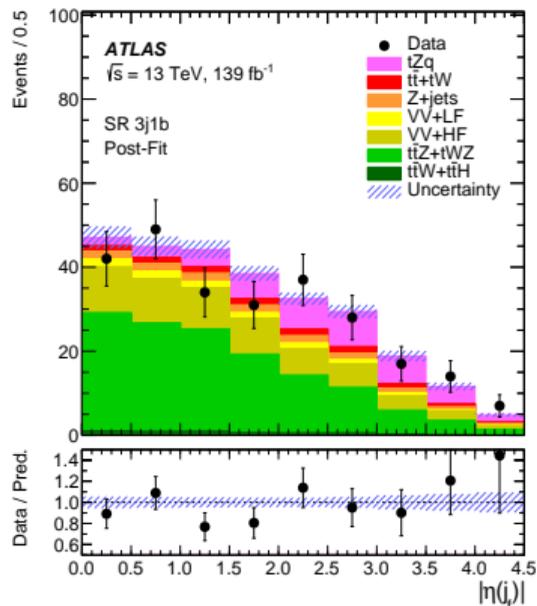
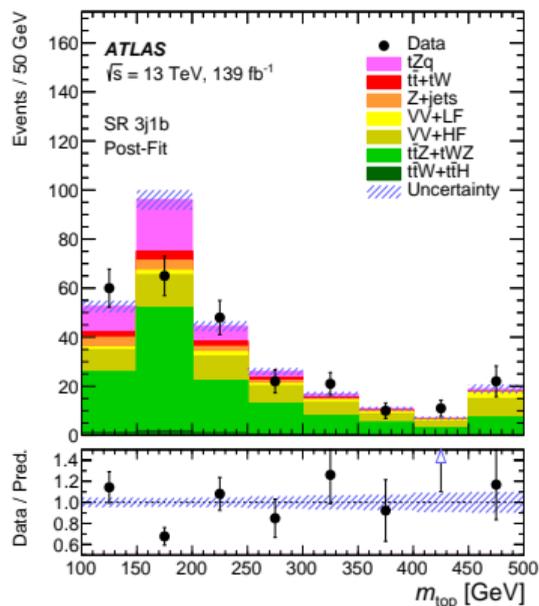
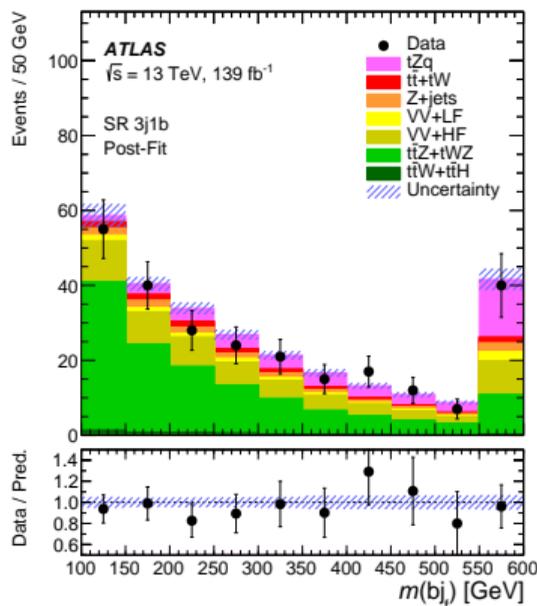
Uncertainty	$\Delta\sigma/\sigma$
$t\bar{t}\gamma$ modelling	$\pm 5.6\%$
Background MC statistics	$\pm 3.5\%$
$t\bar{t}$ modelling	$\pm 3.4\%$
$tq\gamma$ MC statistics	$\pm 3.4\%$
$t(\rightarrow \ell\nu b\gamma)q$ modelling	$\pm 1.9\%$
Additional background uncertainties	$\pm 1.9\%$
$tq\gamma$ modelling	$\pm 1.8\%$
$t(\rightarrow \ell\nu b\gamma)q$ MC statistics	$\pm 0.3\%$
Lepton fakes	$\pm 2.2\%$
$h \rightarrow \gamma$ photon fakes	$\pm 2.2\%$
$e \rightarrow \gamma$ photon fakes	$\pm 0.6\%$
Luminosity	$\pm 2.2\%$
Pileup	$\pm 1.2\%$
Jets and $E_T^{\text{miss}}$	$\pm 4.0\%$
Photons	$\pm 2.5\%$
Leptons	$\pm 0.9\%$
$b$ -tagging	$\pm 0.8\%$
Total systematic uncertainty	$\pm 10.9\%$

Uncertainty	$\Delta\sigma/\sigma$
$t\bar{t}\gamma$ modelling	$\pm 5.7\%$
Background MC statistics	$\pm 3.5\%$
$t\bar{t}$ modelling	$\pm 3.1\%$
$tq\gamma$ MC statistics	$\pm 3.1\%$
$t(\rightarrow \ell\nu b\gamma)q$ modelling	$\pm 2.2\%$
$tq\gamma$ modelling	$\pm 2.0\%$
Additional background uncertainties	$\pm 1.9\%$
$t(\rightarrow \ell\nu b\gamma)q$ MC statistics	$\pm 0.3\%$
Lepton fakes	$\pm 2.4\%$
$h \rightarrow \gamma$ photon fakes	$\pm 2.2\%$
$e \rightarrow \gamma$ photon fakes	$\pm 0.6\%$
Luminosity	$\pm 2.2\%$
Pileup	$\pm 1.3\%$
Jets and $E_T^{\text{miss}}$	$\pm 3.9\%$
Photons	$\pm 2.5\%$
Leptons	$\pm 0.9\%$
$b$ -tagging	$\pm 0.6\%$
Total systematic uncertainty	$\pm 11.0\%$

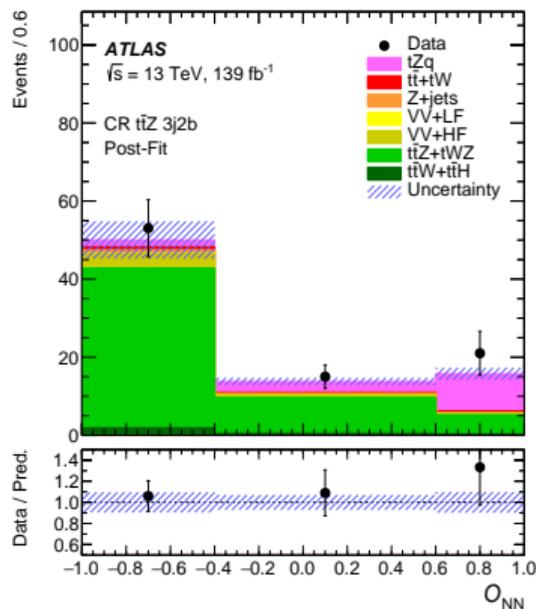
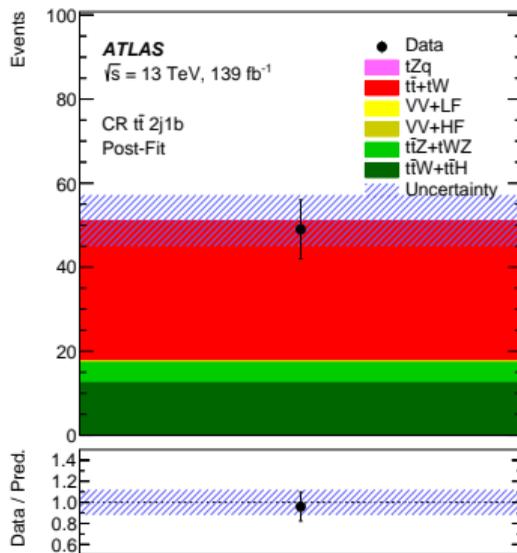
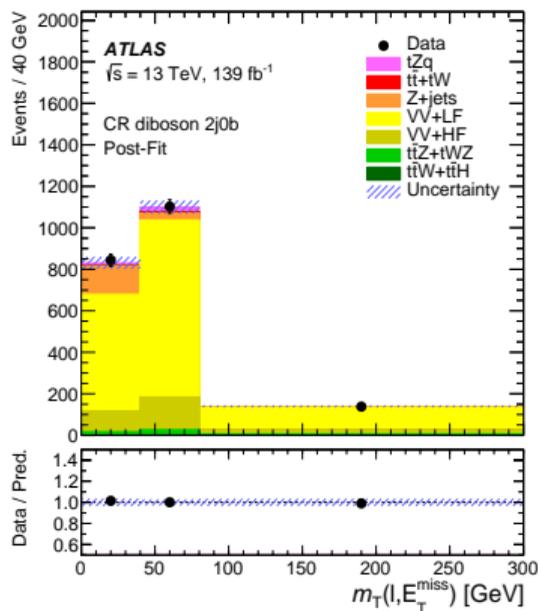
# $tZq$ - post-fit distributions



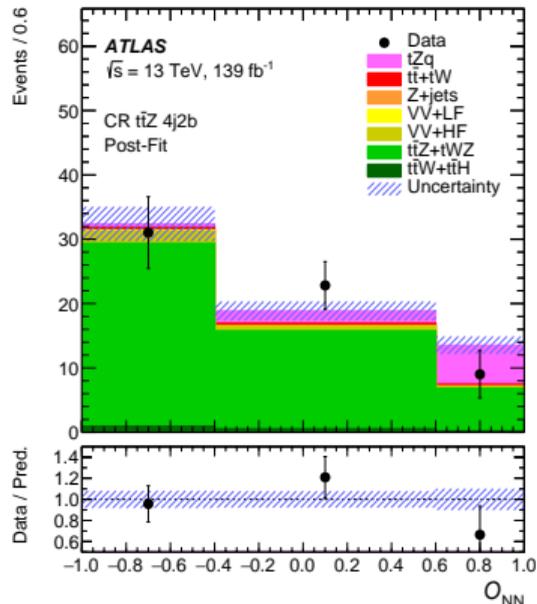
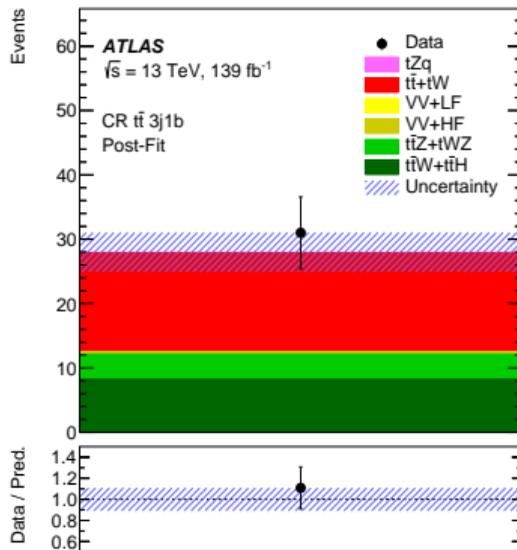
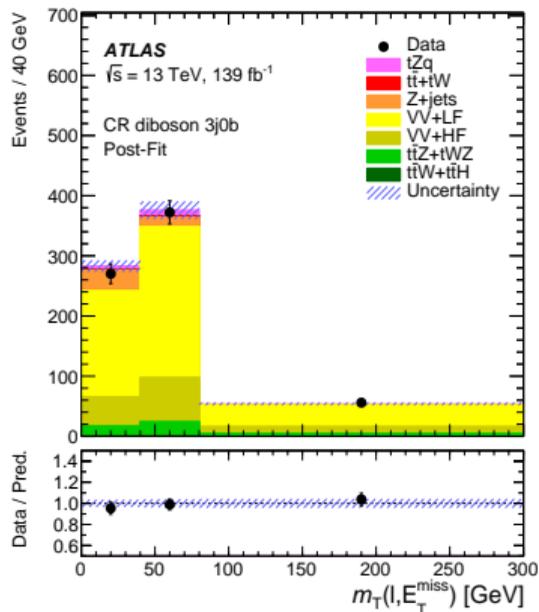
# $tZq$ - post-fit distributions



# $tZq$ - CR post-fit distributions



# $tZq$ - CR post-fit distributions

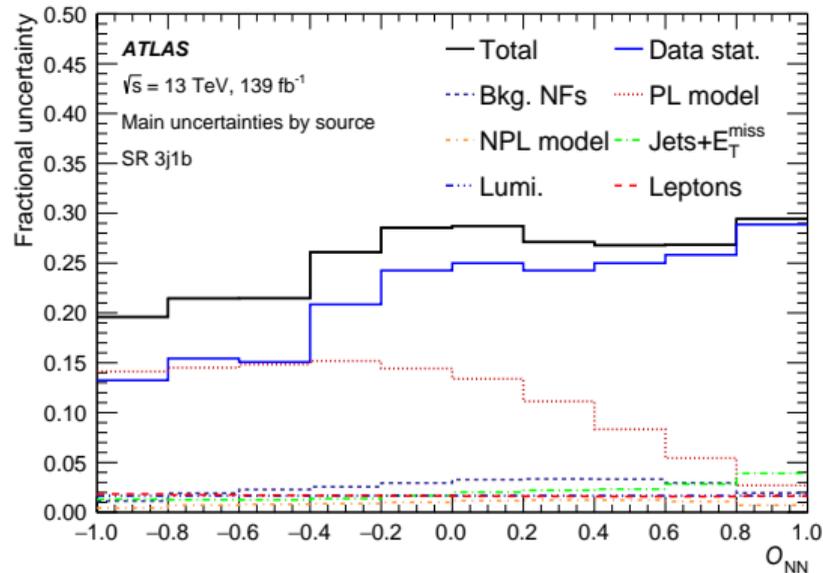
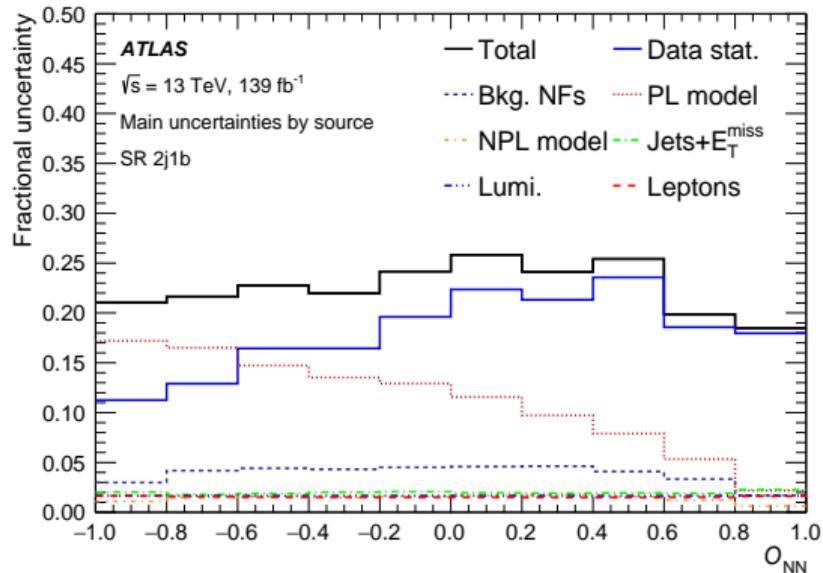


	SR 2j1b	CR diboson 2j0b	CR $t\bar{t}$ 2j1b	CR $t\bar{t}Z$ 3j2b
$tZq$	79 ± 11	53.1 ± 7.5	0.2 ± 0.1	12.9 ± 2.0
$t\bar{t} + tW$	23.8 ± 4.8	13.7 ± 2.7	33.3 ± 6.3	1.7 ± 0.3
Z+jets	28 ± 13	181 ± 82	< 0.1	1.4 ± 0.6
VV + LF	19.7 ± 7.9	2000 ± 100	< 0.1	0.1 ± 0.1
VV + HF	101 ± 22	383 ± 78	0.4 ± 0.1	5.2 ± 1.7
$t\bar{t}Z + tWZ$	96 ± 11	63.2 ± 7.0	4.8 ± 0.5	59.3 ± 7.1
$t\bar{t}H + t\bar{t}W$	6.5 ± 1.0	3.0 ± 0.5	12.4 ± 1.9	2.8 ± 0.5
Total	354 ± 16	2697 ± 56	51.1 ± 6.1	83.5 ± 6.4
Data	359	2703	49	92

	SR 3j1b	CR diboson 3j0b	CR $t\bar{t}$ 3j1b	CR $t\bar{t}Z$ 4j2b
$tZq$	43.4 ± 6.2	21.2 ± 3.3	0.2 ± 0.1	8.0 ± 1.3
$t\bar{t} + tW$	11.0 ± 2.2	6.9 ± 1.3	15.4 ± 3.1	1.0 ± 0.2
Z+jets	12.8 ± 6.0	53 ± 23	< 0.1	0.4 ± 0.2
VV + LF	10.1 ± 4.2	624 ± 53	< 0.1	0.1 ± 0.1
VV + HF	58 ± 17	186 ± 51	0.3 ± 0.1	3.4 ± 1.0
$t\bar{t}Z + tWZ$	132 ± 12	61.9 ± 6.2	3.9 ± 0.5	58.1 ± 5.3
$t\bar{t}H + t\bar{t}W$	4.7 ± 0.7	1.7 ± 0.3	8.2 ± 1.3	2.0 ± 0.3
Total	272 ± 12	955 ± 29	28.0 ± 3.0	72.8 ± 5.0
Data	259	949	31	75

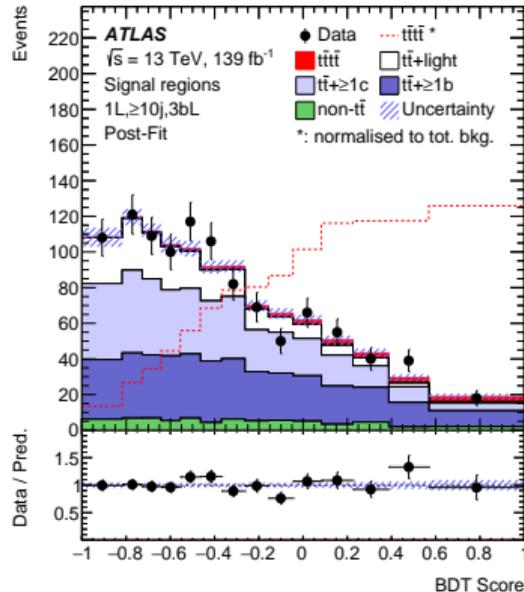
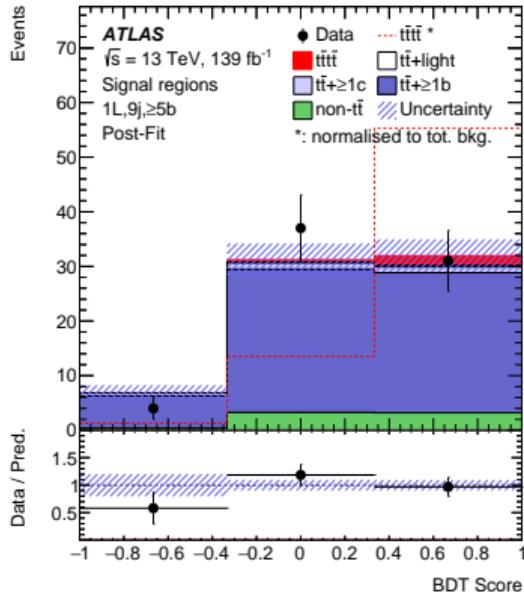
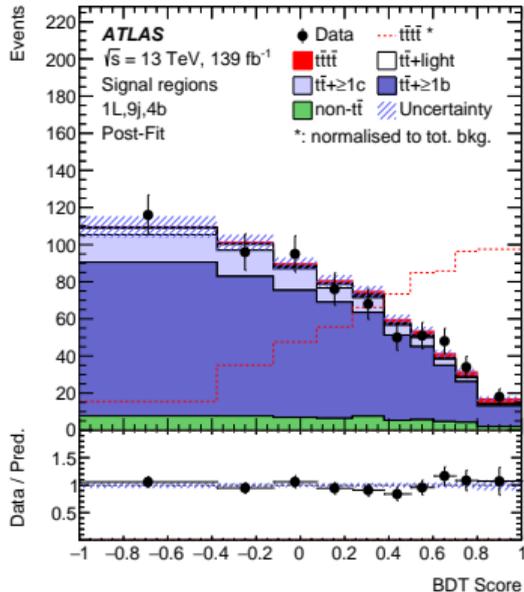
Uncertainty source	$\Delta\sigma/\sigma$ [%]
Prompt-lepton background modelling and normalisation	3.3
Jets and $E_T^{\text{miss}}$ reconstruction and calibration	2.0
Lepton reconstruction and calibration	2.0
Luminosity	1.7
Non-prompt-lepton background modelling	1.6
Pile-up modelling	1.2
MC statistics	1.0
$tZq$ modelling (QCD radiation)	0.8
$tZq$ modelling (PDF)	0.7
Jet flavour tagging	0.4
Total systematic uncertainty	7.0
Data statistics	12.6
$t\bar{t} + tW$ and Z+jets normalisation	2.1
Total statistical uncertainty	12.9

# $tZq$ - Breakdown of uncertainties

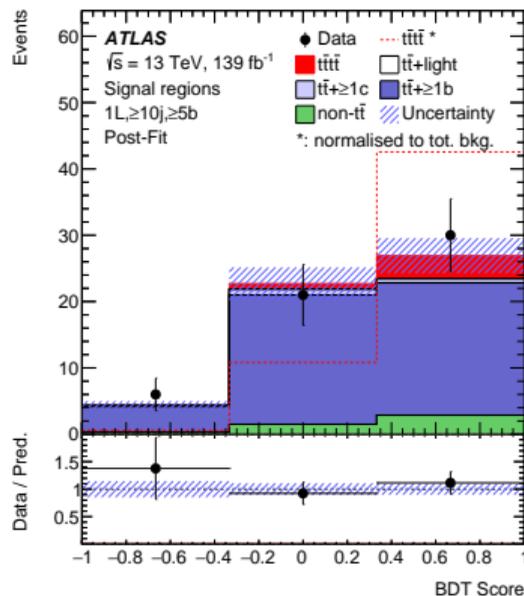
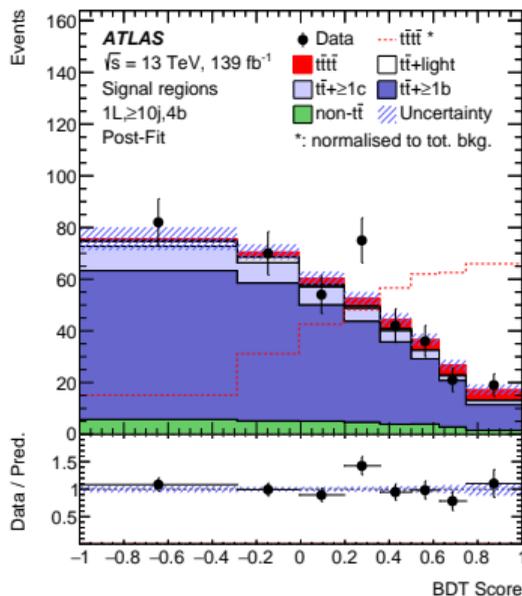
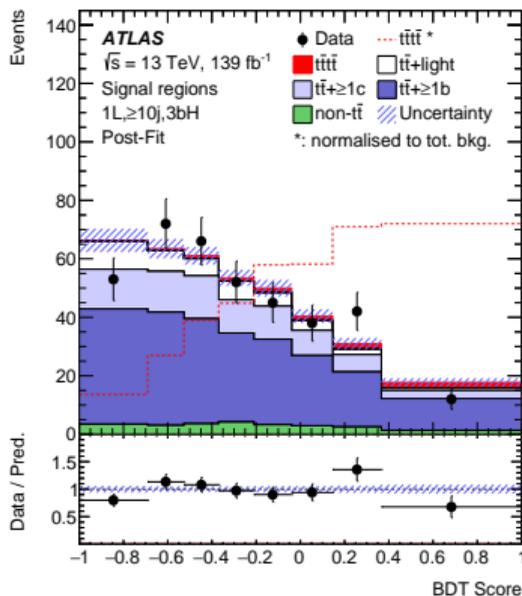


Variable	Rank		Definition
	SR 2j1b	SR 3j1b	
$m_{bj_f}$	1	1	(Largest) invariant mass of the $b$ -jet and the untagged jet(s)
$m_{\text{top}}$	2	2	Reconstructed top-quark mass
$ \eta(j_f) $	3	3	Absolute value of the $\eta$ of the $j_f$ jet
$m_T(\ell, E_T^{\text{miss}})$	4	4	Transverse mass of the $W$ boson
$b$ -tagging score	5	11	$b$ -tagging score of the $b$ -jet
$H_T$	6	–	Scalar sum of the $p_T$ of the leptons and jets in the event
$q(\ell_W)$	7	8	Electric charge of the lepton from the $W$ -boson decay
$ \eta(\ell_W) $	8	12	Absolute value of the $\eta$ of the lepton from the $W$ -boson decay
$p_T(W)$	9	15	$p_T$ of the reconstructed $W$ boson
$p_T(\ell_W)$	10	14	$p_T$ of the lepton from the $W$ -boson decay
$m(\ell\ell)$	11	–	Mass of the reconstructed $Z$ boson
$ \eta(Z) $	12	13	Absolute value of the $\eta$ of the reconstructed $Z$ boson
$\Delta R(j_f, Z)$	13	7	$\Delta R$ between the $j_f$ jet and the reconstructed $Z$ boson
$E_T^{\text{miss}}$	14	–	Missing transverse momentum
$p_T(j_f)$	15	10	$p_T$ of the $j_f$ jet
$ \eta(j_r) $	–	5	Absolute value of the $\eta$ of the $j_r$ jet
$p_T(Z)$	–	6	$p_T$ of the reconstructed $Z$ boson
$p_T(j_r)$	–	9	$p_T$ of the $j_r$ jet

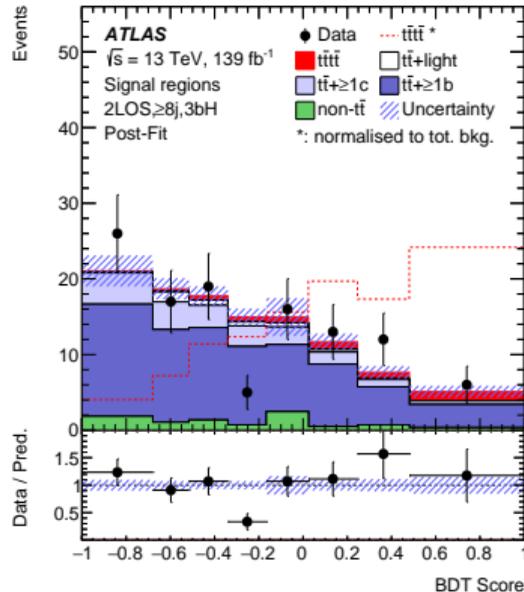
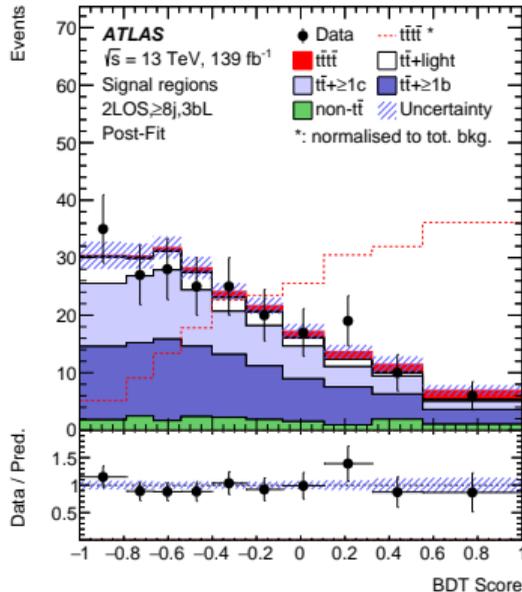
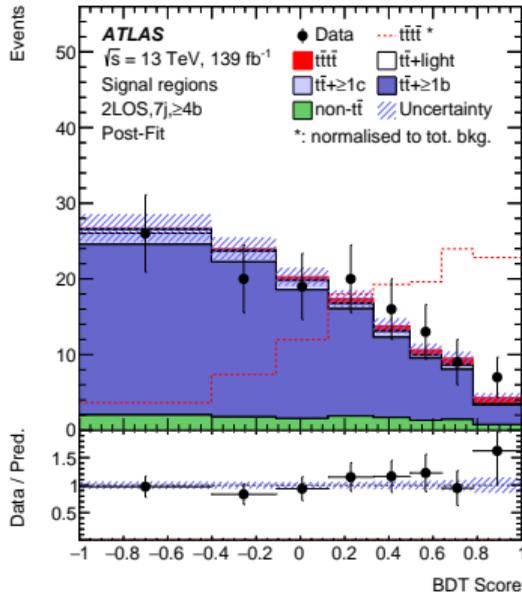
# $tZq$ - post-fit distributions



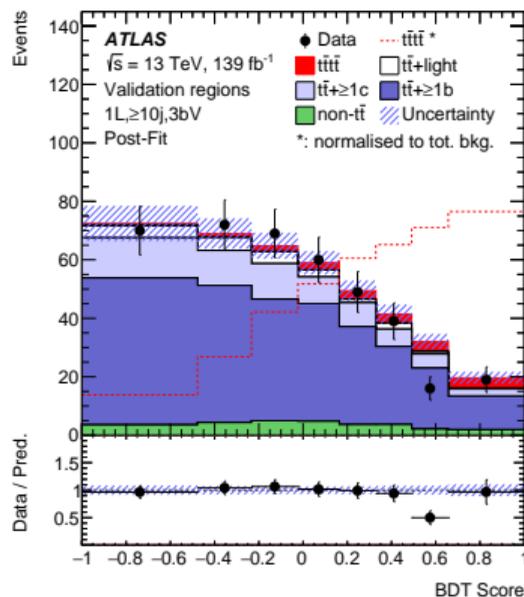
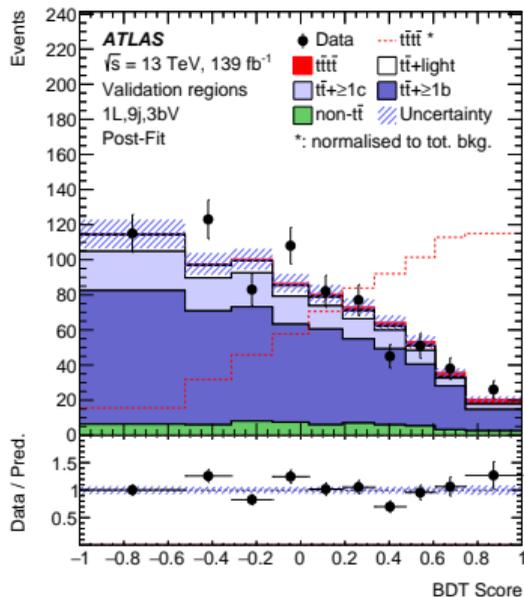
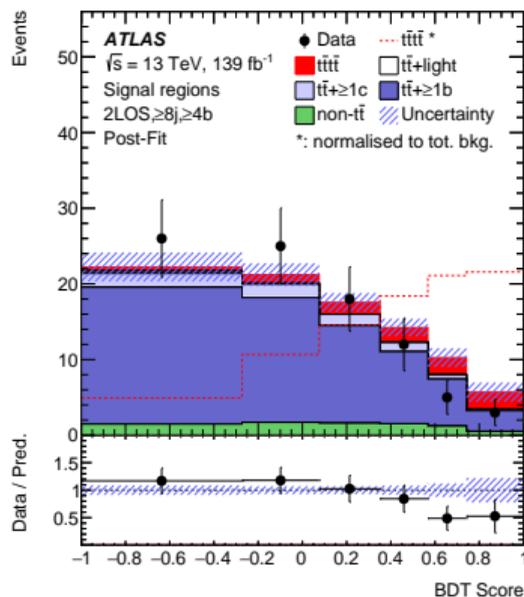
# $tZq$ - post-fit distributions



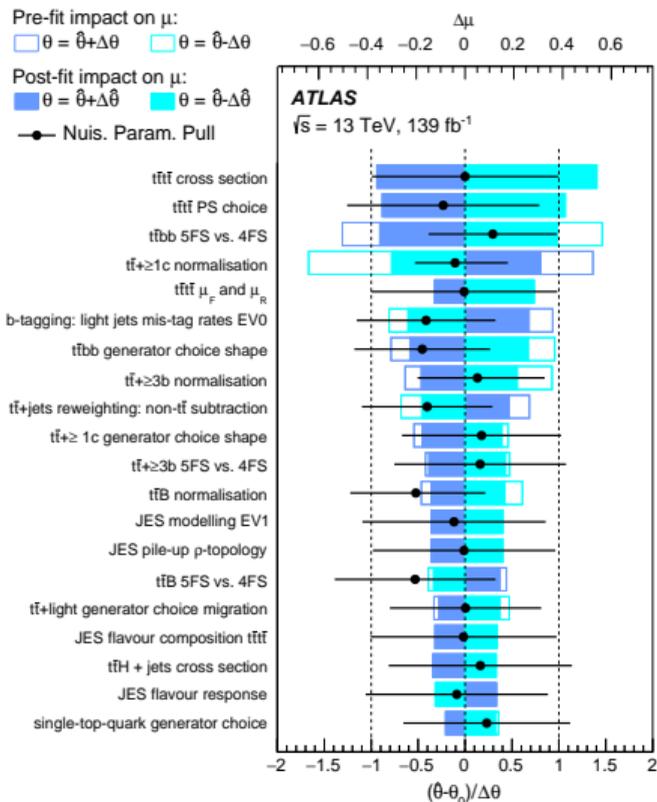
# $tZq$ - post-fit distributions



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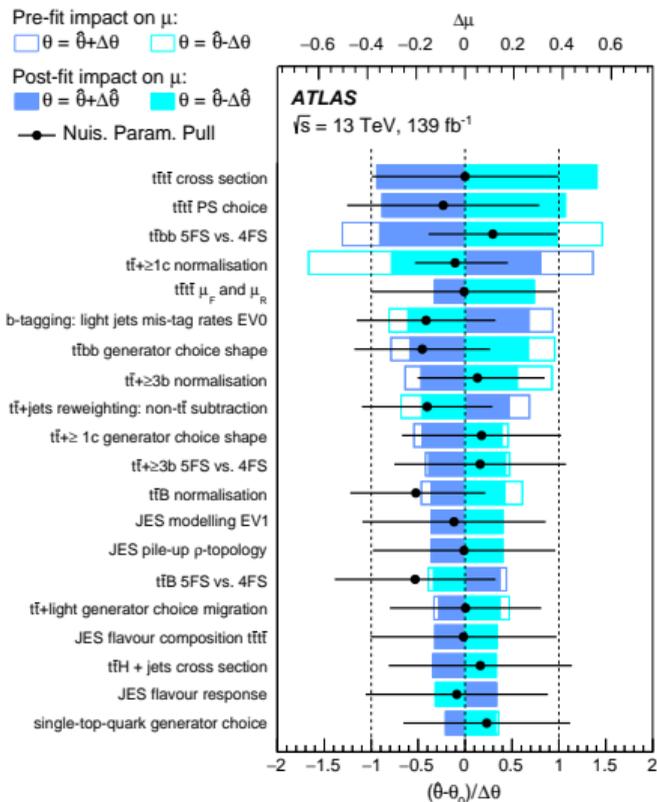


# 4 tops - Ranking and uncertainties



Uncertainty source	$\Delta\sigma_{t\bar{t}\bar{t}}$ [fb]	
<b>Signal Modelling</b>		
t $\bar{t}$ t $\bar{t}$ modelling	+8	-3
<b>Background Modelling</b>		
t $\bar{t}$ + $\geq 1b$ modelling	+8	-7
t $\bar{t}$ + $\geq 1c$ modelling	+5	-4
t $\bar{t}$ +jets reweighting	+4	-3
Other background modelling	+4	-3
t $\bar{t}$ +light modelling	+2	-2
<b>Experimental</b>		
Jet energy scale and resolution	+6	-4
b-tagging efficiency and mis-tag rates	+4	-3
MC statistical uncertainties	+2	-2
Luminosity	< 1	
Other uncertainties	< 1	
<b>Total systematic uncertainty</b>	+15	-12
<b>Statistical uncertainty</b>	+8	-8
<b>Total uncertainty</b>	+17	-15

# 4 tops - Ranking and uncertainties



Uncertainty source	$\Delta\sigma_{t\bar{t}\bar{t}}$ [fb]	
<b>Signal Modelling</b>		
<i>t<math>\bar{t}\bar{t}</math></i> modelling	+8	-3
<b>Background Modelling</b>		
<i>t<math>\bar{t}</math></i> + $\geq 1b$ modelling	+8	-7
<i>t<math>\bar{t}</math></i> + $\geq 1c$ modelling	+5	-4
<i>t<math>\bar{t}</math></i> +jets reweighting	+4	-3
Other background modelling	+4	-3
<i>t<math>\bar{t}</math></i> +light modelling	+2	-2
<b>Experimental</b>		
Jet energy scale and resolution	+6	-4
<i>b</i> -tagging efficiency and mis-tag rates	+4	-3
MC statistical uncertainties	+2	-2
Luminosity	< 1	
Other uncertainties	< 1	
<b>Total systematic uncertainty</b>	+15	-12
<b>Statistical uncertainty</b>	+8	-8
<b>Total uncertainty</b>	+17	-15

## 4 tops - $b$ -tagging requirements

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Name	$N_b^{60\%}$	$N_b^{70\%}$	$N_b^{85\%}$
2b	-	= 2	-
3bL	$\leq 2$	= 3	-
3bH	= 3	= 3	= 3
3bV	= 3	= 3	$\geq 4$
$\geq 4b$ (2LOS)	-	$\geq 4$	-
4b (1L)	-	= 4	-
$\geq 5b$ (1L)	-	$\geq 5$	-

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Uncertainty source	Description	Components (number)
$t\bar{t}+\geq 1b$ normalisation	$\pm 50\%$	$t\bar{t}+b, t\bar{t}+b\bar{b}, t\bar{t}+B, t\bar{t}+\geq 3b$ (4)
$t\bar{t}+\geq 1c$ normalisation	$\pm 50\%$	$t\bar{t}+\geq 1c$ (1)
Generator choice	POWHEG vs MADGRAPH5_AMC@NLO	$(t\bar{t}+\text{light}, t\bar{t}+\geq 1c, t\bar{t}+b, t\bar{t}+b\bar{b}, t\bar{t}+B, t\bar{t}+\geq 3b)$ $\otimes$ (shape, migration) (12)
PS choice	PYTHIA 8 vs HERWIG 7	$(t\bar{t}+\text{light}, t\bar{t}+\geq 1c, t\bar{t}+b, t\bar{t}+b\bar{b}, t\bar{t}+B, t\bar{t}+\geq 3b)$ $\otimes$ (shape, migration) (12)
Renormalisation scale	Varying $\mu_r$ in POWHEG	$t\bar{t}+\text{light}, t\bar{t}+\geq 1c, t\bar{t}+\geq 1b$ (3)
Factorisation scale	Varying $\mu_f$ in POWHEG	$t\bar{t}+\text{light}, t\bar{t}+\geq 1c, t\bar{t}+\geq 1b$ (3)
ISR	Varying $\alpha_S^{\text{ISR}}$ (PS) in PYTHIA 8	$t\bar{t}+\text{light}, t\bar{t}+\geq 1c, t\bar{t}+\geq 1b$ (3)
FSR	Varying $\mu_f$ (PS) in PYTHIA 8	$t\bar{t}+\text{light}, t\bar{t}+\geq 1c, t\bar{t}+\geq 1b$ (3)
5FS vs 4FS	POWHEGBOXRES (4FS) vs POWHEGBOX (5FS)	$t\bar{t}+b, t\bar{t}+b\bar{b}, t\bar{t}+B, t\bar{t}+\geq 3b$ (4)

Name	Description
$\sum b\text{-tag}$	Sum of pseudo-continuous $b$ -tagging score over the six jets with the highest score
$N_{\text{jets}}$	Number of jets
$\Delta R_{bb}^{\text{min}}$	Minimum $\Delta R$ between all pairs of $b$ -tagged jets
$H_{\text{T}}^{\text{all}}$	Scalar sum of all jet and lepton transverse momenta
$C^{\text{all}}$	Centrality ( $\sum_i p_{\text{T}i} / \sum_i E_i$ ) of the leptons and jets
$p_{\text{T}}^{\text{lead}}$	Transverse momentum of the leading jet
$\Delta R_{b\ell}^{\text{min}}$	Minimum $\Delta R$ between all pairs of $b$ -tagged jets and leptons
$\Delta R_{jj}^{\text{avg}}$	Average $\Delta R$ between all pairs of jets
$m_{\text{jjj}}$	Invariant mass of the closest triplet of jets
$E_{\text{T}}^{\text{miss}}$	Missing transverse momentum
$m_{\text{T}}^{\text{W}}$	$W$ reconstructed transverse mass $m_{\text{T}}(\ell, E_{\text{T}}^{\text{miss}})$ (1L)
$N_{\text{LR-jets}}$	Number of large- $R$ jets with a mass above 100 GeV
$\sum d_{12}$	Sum of the first $k_t$ splitting scale $d_{12}$ of all large- $R$ jets
$\sum d_{23}$	Sum of the second $k_t$ splitting scale $d_{23}$ of all large- $R$ jets