

A search for axion-like particles in light-by-light scattering at the CLIC

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Abstract

The virtual production of axion-like particles (ALPs) in the light-by-light scattering at the CLIC collider is studied. Both differential and total cross sections are calculated, assuming interaction of the ALP with photons via CP-odd term in the Lagrangian. The 95% C.L. exclusion regions for the ALP mass and its coupling constant are given. By comparing our results with existing collider bounds, we see that the ALP search at the CLIC has a great physics potential of searching for the ALPs, especially, in the mass region 1 TeV – 2.4 TeV, with the collision energy $\sqrt{s} = 3000$ GeV and integrated luminosity $L = 5000 \text{ fb}^{-1}$ for the Compton backscattered initial photons. In particular, our limits are stronger than recently obtained bounds for the ALP production in the light-by-light scattering at the LHC.

1 Introduction

The notion of the QCD axion is closely related to the strong CP problem, which means the absence of the CP violation in the strong interactions. In

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its turn, the CP problem arises as a possible solution to the $U(1)$ problem. The QCD Lagrangian in the limit of vanishing masses of u and d quarks has a global symmetry $U(2)_V \times U(2)_A = SU(2)_I \times U(1)_Y \times SU(2)_A \times U(1)_A$. The non-zero quark condensates $\langle \bar{u}u \rangle$ and $\langle \bar{d}d \rangle$ break down the axial symmetry $SU(2)_A \times U(1)_A$ spontaneously. As a result, four Nambu-Goldstone bosons should appear. But besides light pions, no another light state is present in the hadronic spectrum since $m_\eta \gg m_\pi$. It is called the $U(1)$ problem [1].

The $U(1)_A$ symmetry is connected with a transformation of the fermion fields $\psi \rightarrow e^{i\alpha\gamma_5}\psi$, $\bar{\psi} \rightarrow \bar{\psi}e^{i\alpha\gamma_5}$. One possible resolution of the $U(1)$ problem is provided by the Adler-Bell-Jackiw chiral anomaly for the axial current $J_\mu^5 = \bar{\psi}\gamma_\mu\gamma_5\psi$ [2].

Although the axial anomaly is a total divergency, $U(1)_A$ is not a symmetry of the strong interaction for gluon fields A_μ which are pure gauges at spatial infinity [3]. They are classified by the integer n , $A_\mu = (-i/g)\partial_\mu\omega\omega^{-1}$, where $\omega \rightarrow \omega_n = \exp(i2\pi n)$ as $r \rightarrow \infty$. This condition is a definition of a classical vacuum of the gauge field $|n\rangle$. The true or θ -vacuum becomes a superposition of the vacua $|n\rangle$, $|\theta\rangle = \sum_n \exp(-in\theta)|n\rangle$ [4].

As a result, an effective QCD action acquires so-called θ -term. It breaks P- and T-invariance but conserves C-invariance, so CP-invariance is violated. Thus, it contributes to the neutron electric dipole moment d_n . The current experimental limit $d_n < 0.021 \times 10^{-23}$ e cm [5] requires θ to be less than 10^{-9} . The smallness of the angle $\bar{\theta}$ is known as *strong CP problem*.

The elegant solution of the CP mystery of the SM is provided by the Peccei-Quinn (PQ) mechanism with a new, spontaneously broken approximate global $U(1)_{\text{PQ}}$ symmetry [6]. As it is shown in [7, 8] it leads to a light neutral pseudoscalar particle, the *axion* a , which is the Nambu-Goldstone boson of the broken $U(1)_{\text{PQ}}$ symmetry. The idea is to replace the CP-violating term θ by the CP-conserving axion. Namely, the axion field can be redefined to absorb the parameter θ . In fact, the axion replaces the QCD theta parameter by a dynamical quantity, thereby explaining of non-observation of the strong CP violation. Thus, the PQ mechanism is a compelling solution to the strong CP problem.

In the PQWW scheme [6]-[8] an extra Higgs doublet is used, and the axion mass is related to the electroweak symmetry breaking scale. There are two models in which the PQ symmetry is decoupled from the electroweak (EW) scale and is spontaneously broken. It results in axions with extremely weak couplings (“invisible” axion). One of the models is the KSVZ model [9]-[10] with one Higgs doublet in which the axion is introduced as the phase

of an EW singlet scalar field. This scalar is coupled to an additional heavy quark, and its coupling is induced by the interaction of the heavy quarks with other fields. In the DFSZ model [11]-[12] two Higgs doublets are used, as well as an additional EW singlet scalar. The latter is coupled to the SM fields through its interaction with the Higgs doublets.

The axion also appears in the context of the string theory [13]-[15]. In the string theory, spin-zero particles must couple to a photon field since all couplings are defined by the expectation value of scalar fields. This implies the existence of the P-odd term in the Lagrangian proportional to

$$-\frac{1}{4}g_{a\gamma\gamma}aF_{\mu\nu}\tilde{F}^{\mu\nu} = g_{a\gamma\gamma}a\vec{E}\cdot\vec{B}, \quad (1)$$

where $F_{\mu\nu}$ is the electromagnetic tensor, $\tilde{F}_{\mu\nu} = (1/2)\varepsilon_{\mu\nu\rho\sigma}F^{\rho\sigma}$ its dual, and a is the QCD axion or axion-like particle (ALP) [16]. ALPs can also appear in theories with spontaneously broken symmetries [17]-[18] or in GUT [19]. Lately, a number of new theoretical schemes with the axion as a basic quantity was developed [21]-[28]. For a review on the axions and ALPs, see [29]-[32] and references therein.

Both theory and phenomenology of the axions were also studied in large [33]-[36] and warped [37]-[39] extra dimensions (EDs). In an ED framework, the mass of the axion becomes independent of the scale associated with the breaking of the PQ symmetry. It means that the axion mass can be treated independently of its couplings to the SM fields.

The very low mass and small coupling axion and/or ALP are a leading dark matter (DM) candidate, since their properties, allow them to be stable and difficult-to-detect. Both axions and ALPs can be produced in the early Universe and therefore constitute most of the cold DM in the Universe [40]-[42] (see also recent papers [43]-[50]). The relevance of the QCD axion and, more generally, of ALPs in astrophysics and cosmology is of particular interest [51]-[56]. Many axion DM experiments are in progress [57]-[64] (see also [65]).

The axion phenomenology involves phenomena such as stellar evolution, axion mediated forces, dark matter detection, axion decays, axion-photon conversion, so-called “light shining trough the wall”, etc.

There is a broad experimental program aiming to search for the QCD axion via its coupling to the SM. On the other hand, many ALP searches assume their strong couplings to the electromagnetic term $F_{\mu\nu}\tilde{F}^{\mu\nu}$ as in eq. (1). In terrestrial experiments, bounds on very low mass axions and small mass

axions were obtained [66]-[74]. The coupling of the ALPs to other gauge bosons is also studied (see, for instance, [75]). Note that the ALPs are not directly relevant for the QCD axion. Therefore, heavy ALPs can be detected at colliders, in particular, in a light-by-light scattering [76]-[79]. As it was shown in [80], searches at the LHC with the use of the proton tagging technique can constrain the ALP masses in the region 0.5 TeV–2 TeV.

Compact Linear Collider (CLIC) is the linear collider that is planned to accelerate and collide electrons and positrons at maximally 3 TeV center-of-mass energy [81]. In the CLIC, it is possible to obtain accelerating gradients of 100 MV/m. Three energy states are considered to operate CLIC at maximum efficiency [82]. The $\sqrt{s} = 380$ GeV is the first one and it is possible to reach the integrated luminosity $L = 1000 \text{ fb}^{-1}$. This energy stage covers Higgs boson, top quark, and gauge sectors. It is planned to examine such SM particles with high precision [83]. The second one has $\sqrt{s} = 1500$ GeV center-of-mass energy and 2500 fb^{-1} integrated luminosity. At this stage, it is enabled to investigate beyond the SM physics. Also, a detailed analysis of the Higgs boson can be made, such as the Higgs self-coupling, the top-Yukawa coupling, and rare Higgs decay channels. [84]. The third stage of the CLIC has a maximum center-of-mass energy value $\sqrt{s} = 3000$ GeV and integrated luminosity value $L = 5000 \text{ fb}^{-1}$. At this stage, the most precise examinations of the SM are possible. Moreover, it is enabled to discover beyond the SM heavy particles of mass greater than 1500 GeV [83]. The new physics search potential of the CLIC is presented in [85].

At the CLIC, it is possible to study $\gamma\gamma$ and $e\gamma$ collisions with real photons. These γ beams are gotten by the Compton backscattering of laser photons off linear electron beams. Another options for the $\gamma\gamma$ and $e\gamma$ collisions are photon-induced processes at the CLIC. In this type of process, the photons are emitted from the incoming electron beams. The photons scatter at tiny angles from the beam pipe. Hence, they have very low virtuality; that is why these photons are called “almost-real”.

The first evidence of the subprocess $\gamma\gamma \rightarrow \gamma\gamma$ was observed by the Collaboration ATLAS in high-energy ultra-peripheral PbPb collisions [86]. The same process was also reported by the CMS Collaboration [87]. Recently, the Collaboration ATLAS have published the evidence of the light-by-light scattering with the certainty of 8,2 sigma [88]. The analysis of the exclusive and diffractive $\gamma\gamma$ production in PbPb collisions was done in [89]. We have examined a possibility to constrain the parameters of the model with a warped ED in the photon-induced process $pp \rightarrow p\gamma\gamma p \rightarrow p'\gamma\gamma p'$ at the

LHC [90]. Previously, the photon-induced processes in EDs were studied in [91]-[92].

In the present paper, we propose to search for the ALP a in the exclusive light-by-light scattering at the lepton collider CLIC.

In the next section differential and total cross sections are calculated as functions of the ALP mass m_a and its coupling f . It enables us to estimate the CLIC exclusion regions for both types of the initial photons.

2 Light-by-light virtual production of ALP

The pseudoscalar ALP couples to the SM photons via

$$\mathcal{L}_a = \frac{1}{2} (\partial_\mu a)(\partial^\mu a) - \frac{1}{2} m_a^2 a^2 + \frac{a}{f_a^{(-)}} F_{\mu\nu} F^{\mu\nu} + \frac{a}{f_a^{(+)}} F_{\mu\nu} \tilde{F}^{\mu\nu} , \quad (2)$$

were $(f_a^{(-)})^{-1}$ and $(f_a^{(+)})^{-1}$ are the ALP-photon couplings in CP-odd and CP-even terms of the interaction Lagrangian. Note that, in contrast to the true QCD axion, the mass and couplings of the ALP are independent parameters. In what follows, we assume that only the last term is realized in (2) with $f_a^{(+)} = f$. As for a possible contribution from the third term in (2), it is discussed in the section Conclusions.

The explicit expressions for the photon spectrum are given below. The differential cross section is the following sum of helicity amplitudes squared [78]

$$\frac{d\sigma}{d\Omega} = \frac{1}{128\pi^2 s} (|M_{++++}|^2 + |M_{+--+}|^2 + |M_{-++-}|^2 + |M_{+-+-}|^2) . \quad (3)$$

Here and below s , t and u are the Mandelstam variables of the diphoton system. Each of the helicity amplitudes is a sum of the ALP and SM terms,

$$M = M_a + M_{\text{ew}} . \quad (4)$$

The explicit expressions of the pure ALP amplitudes can be found in [78]. In particular,

$$\begin{aligned} \Re M_{++++}^{(a)} &= -\frac{4}{f_a^2} \frac{s^2(s - m_a^2)}{(s - m_a^2)^2 + m_a^2 \Gamma_a^2} , \\ \Im M_{++++}^{(a)} &= \frac{4}{f_a^2} \frac{s^2 m_a \Gamma_a}{(s - m_a^2)^2 + m_a^2 \Gamma_a^2} , \end{aligned} \quad (5)$$

where Γ_a is the total width of the ALP

$$\Gamma_a = \frac{\Gamma(a \rightarrow \gamma\gamma)}{\text{Br}(a \rightarrow \gamma\gamma)}, \quad (6)$$

and

$$\Gamma(a \rightarrow \gamma\gamma) = \frac{m_a^3}{4\pi f^2} \quad (7)$$

is its decay width into two photons. Correspondingly, we have [78]

$$\Re M_{+--+}^{(a)} = -\frac{4}{f_a^2} \frac{u^2}{u - m_a^2}, \quad \Im M_{+--+}^{(a)} = 0, \quad (8)$$

$$\Re M_{+--+}^{(a)} = -\frac{4}{f_a^2} \frac{t^2}{t - m_a^2}, \quad \Im M_{+--+}^{(a)} = 0, \quad (9)$$

$$\begin{aligned} \Re M_{++--}^{(a)} &= \frac{4}{f_a^2} \left(\frac{s^2(s - m_a^2)}{(s - m_a^2)^2 + m_a^2 \Gamma_a^2} + \frac{t^2}{t - m_a^2} + \frac{u^2}{u - m_a^2} \right), \\ \Im M_{++--}^{(a)} &= -\frac{4}{f_a^2} \frac{s^2 m_a \Gamma_a}{(s - m_a^2)^2 + m_a^2 \Gamma_a^2}, \end{aligned} \quad (10)$$

$$M_{++++}^{(a)} = 0. \quad (11)$$

An account of the ALP width Γ_a is mainly important in a vicinity of the point $s \sim m_a^2$. That is why, it is omitted in the denominators in eqs. (8), (9), as well as in the last two terms in the first row of eq. (10).

The SM (electroweak) amplitude is a sum of the fermion and W boson one-loop amplitudes

$$M_{\text{ew}} = M^f + M^W. \quad (12)$$

The amplitudes $M_{++++}^f(s, t, u)$ and $M_{++++}^W(s, t, u)$ are calculated in [93]-[94] (see also [92])

$$\begin{aligned} \frac{1}{\alpha_{\text{em}}^2 e_f^4} \Re M_{++++}^f(s, t, u) &= -8 - 8 \left(\frac{u-t}{s} \right) \ln \left(\frac{u}{t} \right) \\ &\quad - 4 \left(\frac{t^2 + u^2}{s^2} \right) \left[\ln^2 \left(\frac{u}{t} \right) + \pi^2 \right], \\ \Im M_{++++}^f(s, t, u) &= 0, \end{aligned} \quad (13)$$

where e_f is the fermion electric charge in units of the proton charge,

$$\begin{aligned}
\frac{1}{\alpha_{\text{em}}^2} \Re M_{++++}^W(s, t, u) &= 12 + 12 \left(\frac{u-t}{s} \right) \ln \left(\frac{u}{t} \right) \\
&+ 16 \left(1 - \frac{3tu}{4s^2} \right) \left[\ln^2 \left(\frac{u}{t} \right) + \pi^2 \right] \\
&+ 16 \left[\frac{s}{t} \ln \left(\frac{s}{m_W^2} \right) \ln \left(\frac{-t}{m_W^2} \right) + \frac{s}{u} \ln \left(\frac{s}{m_W^2} \right) \ln \left(\frac{-u}{m_W^2} \right) \right. \\
&\left. + \frac{s^2}{tu} \ln \left(\frac{-t}{m_W^2} \right) \ln \left(\frac{-u}{m_W^2} \right) \right], \\
\frac{1}{\alpha_{\text{em}}^2} \Im M_{++++}^W(s, t, u) &= -16\pi \left[\frac{s}{t} \ln \left(\frac{-t}{m_W^2} \right) + \frac{s}{u} \ln \left(\frac{-u}{m_W^2} \right) \right]. \tag{14}
\end{aligned}$$

The amplitudes $M_{+--+}^{f,W}(s, t, u)$ and $M_{+--+}^{f,W}(s, t, u)$ can be obtained with the use of the following relations

$$\begin{aligned}
M_{+--+}(s, t, u) &= M_{++++}(u, t, s), \\
M_{+--+}(s, t, u) &= M_{++++}(t, s, u) = M_{++++}(t, u, s). \tag{15}
\end{aligned}$$

Note that $M_{++++}(s, t, u) = M_{++++}(s, u, t)$, since it depends only on s . In particular, we get

$$\begin{aligned}
\frac{1}{\alpha_{\text{em}}^2 e_f^4} \Re M_{+--+}^f(s, t, u) &= -8 - 8 \left(\frac{s-t}{u} \right) \ln \left(\frac{s}{-t} \right) \\
&- 4 \left[\left(\frac{t^2 + s^2}{u^2} \right) \ln^2 \left(\frac{s}{-t} \right) + \pi^2 \right], \\
\frac{1}{\alpha_{\text{em}}^2 e_f^4} \Im M_{+--+}^f(s, t, u) &= 8\pi \left[\frac{s-t}{u} + \frac{t^2 + s^2}{u^2} \ln \left(\frac{s}{-t} \right) \right], \tag{16}
\end{aligned}$$

and

$$\begin{aligned}
\frac{1}{\alpha_{\text{em}}^2 e_f^4} \Re M_{+--+}^f(s, t, u) &= -8 - 8 \left(\frac{u-s}{t} \right) \ln \left(\frac{-u}{s} \right) \\
&- 4 \left[\left(\frac{s^2 + u^2}{t^2} \right) \ln^2 \left(\frac{-u}{s} \right) + \pi^2 \right], \\
\frac{1}{\alpha_{\text{em}}^2 e_f^4} \Im M_{+--+}^f(s, t, u) &= -8\pi \left[\frac{u-s}{t} + \frac{s^2 + u^2}{t^2} \ln \left(\frac{-u}{s} \right) \right]. \tag{17}
\end{aligned}$$

The explicit formulas for $M_{+--+}^W(s, t, u)$ have been already derived in [92]

$$\begin{aligned}
\frac{1}{\alpha_{\text{em}}^2} \Re M_{+--+}^W(s, t, u) &= 12 + 12 \left(\frac{s-t}{u} \right) \ln \left(\frac{s}{-t} \right) \\
&+ 16 \left(1 - \frac{3ts}{4u^2} \right) \ln^2 \left(\frac{s}{-t} \right) \\
&+ 16 \left[\frac{u}{t} \ln \left(\frac{-u}{m_W^2} \right) \ln \left(\frac{-t}{m_W^2} \right) + \frac{u}{s} \ln \left(\frac{-u}{m_W^2} \right) \ln \left(\frac{s}{m_W^2} \right) \right. \\
&\left. + \frac{u^2}{ts} \ln \left(\frac{-t}{m_W^2} \right) \ln \left(\frac{s}{m_W^2} \right) \right], \\
\frac{1}{\alpha_{\text{em}}^2} \Im M_{+--+}^W(s, t, u) &= -\pi \left[12 \left(\frac{s-t}{u} \right) + 32 \left(1 - \frac{3ts}{4u^2} \right) \ln \left(\frac{s}{-t} \right) \right. \\
&\left. + 16 \frac{u}{s} \ln \left(\frac{-u}{m_W^2} \right) + 16 \frac{u^2}{ts} \ln \left(\frac{-t}{m_W^2} \right) \right]. \tag{18}
\end{aligned}$$

The explicit expressions for $M_{+--+}^f(s, t, u)$ and $M_{+--+}^W(s, t, u)$ are also known [93]-[94]

$$\begin{aligned}
\Re M_{+--+}^f(s, t, u) &= 8\alpha_{\text{em}}^2 e_f^4, & \Im M_{+--+}^f(s, t, u) &= 0, \\
\Re M_{+--+}^W(s, t, u) &= -12\alpha_{\text{em}}^2, & \Im M_{+--+}^W(s, t, u) &= 0. \tag{19}
\end{aligned}$$

Finally, neglecting terms m_f^2/s , m_f^2/t and m_f^2/u , we have

$$M_{++++}^f(s, t, u) \simeq M_{++++}^W(s, t, u), \tag{20}$$

$$M_{++++}^W(s, t, u) \simeq M_{++++}^W(s, t, u). \tag{21}$$

2.1 Compton backscattered photons

In addition to e^+e^- collisions, $e\gamma$ and $\gamma\gamma$ interactions with real photons can be examined at the CLIC. For this purpose, real photons could be constructed by the Compton backscattering of laser photons off linear electron beam. In this process, a laser photon which has E_0 energy interacts with an electron. This electron has very high energy E_e , and it collides with the laser photon at a tiny collision angle α (almost head-on). The scattered photon energy E_γ can be determined as follows [96]

$$E_\gamma = \frac{x_{\text{max}} E_e}{1 + (\theta/\theta_0)^2}, \quad x_{\text{max}} = \frac{\zeta}{\zeta + 1}, \quad \theta_0 = \frac{m_e}{E_e} \sqrt{\zeta + 1}. \tag{22}$$

Here θ is the photon scattering angle from an initial direction of the electron, $x_{\max} = E_{\gamma, \max}/E_e$, where $E_{\gamma, \max}$ is the maximum energy of the scattered photons, and

$$\zeta = \frac{4E_e E_0}{m_e^2} \left[\cos\left(\frac{\alpha}{2}\right) \right]^2 \simeq \frac{4E_e E_0}{m_e^2} = 15.3 \left(\frac{E_e}{\text{TeV}} \right) \left(\frac{E_0}{\text{eV}} \right). \quad (23)$$

The photon energy E_γ grows, with an increase of ζ . Hence the energy spectrum gets to be narrower. At the same time, if ζ value is greater than 4.8; high energy photons may be lost due to e^+e^- pair creation in interactions of unscattered laser photons with backscattered photons. The invariant energy of the $\gamma\gamma$ -system is equal to $s = 4x_1x_2E_e^2 = 4E_{\gamma_1}E_{\gamma_2}$, $x_i = E_{\gamma_i}/E_e$, where E_{γ_i} ($i = 1, 2$) is defined by eqs. (22), (23).

Most of these real scattered photons have high energy. These Compton backscattered (CB) photons give a spectrum which is defined as follows [95]-[96]

$$f_{\gamma/e}(x) = \frac{1}{g(\zeta)} \left[1 - x + \frac{1}{1-x} - \frac{4x}{\zeta(1-x)} + \frac{4x^2}{\zeta^2(1-x)^2} \right], \quad (24)$$

where

$$g(\zeta) = \left(1 - \frac{4}{\zeta} - \frac{8}{\zeta^2} \right) \log(\zeta + 1) + \frac{1}{2} + \frac{8}{\zeta} - \frac{1}{2(\zeta + 1)^2}. \quad (25)$$

Note that x_{\max} reaches 0.83 when $\zeta = 4.8$. We will use the cut on the final state photon rapidity $|\eta_{\gamma\gamma}| < 2.5$. The cross section of the diphoton production with the CB photon at the CLIC can be found as the integration,

$$d\sigma = 2 \int_{z_{\min}}^{z_{\max}} dz z \int_{z^2/y_{\max}}^{y_{\max}} \frac{dy}{y} f_{\gamma/e}(y) f_{\gamma/e}(z^2/y) d\sigma(\gamma\gamma \rightarrow \gamma\gamma). \quad (26)$$

Here

$$y_{\max} = z_{\max} = 0.83, \quad z_{\min} = \frac{p_\perp}{E_e}, \quad (27)$$

where p_\perp is the transverse momentum of the final photons, $f_{\gamma/e}(y)$ is the photon spectrum, and $d\sigma(\gamma\gamma \rightarrow \gamma\gamma)$ is the unpolarized differential cross section of the subprocess $\gamma\gamma \rightarrow \gamma\gamma$. The Feynman diagrams for this process are shown in Fig. 1. Let us note that in our calculations, we take into account W -loop and fermion-loop contributions as the main SM background. The other possible background with fake photons from decays of π^0 , η , and η' is negligible in the signal region.

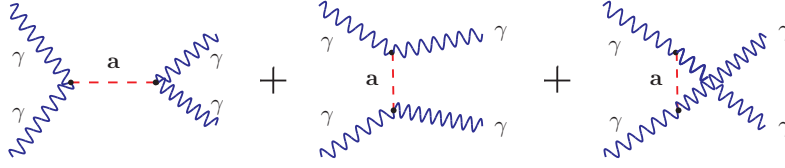


Figure 1: The Feynman diagrams describing light-by-light virtual production of the axion-like particle a .

The differential cross sections for the process $\gamma\gamma \rightarrow \gamma\gamma$ for the CB initial photons is shown in Fig. 2 as functions of the transverse momenta of the final photons p_t . The ALP mass m_a and its coupling f are chosen to be equal to 1200 GeV and 10 TeV, respectively. In order to reduce the SM background, we have imposed the cut $W = m_{\gamma\gamma} > 200$ GeV. The curves are presented for two values of the ALP branching into two photons $\text{Br} = \text{Br}(a \rightarrow \gamma\gamma)$. For this differential cross sections, the virtual production of the ALP dominates the SM light-by-light subprocess for $p_t > 100$ GeV region. The total cross sections $\sigma(p_t > p_{t,\text{min}})$ as functions of the minimal transverse momenta of the final photons $p_{t,\text{min}}$ are shown in Fig. 3. It can be seen from this figure that the deviation from the SM gets higher as the p_t -cut increases. Moreover, while the SM cross section decreases up to the value of $p_{t,\text{min}} = 500$ GeV, the total cross section remains almost unchanged.

Fig. 4 demonstrates the dependence of the total cross sections on the ALP mass for two fixed values of the ALP coupling $f = 10$ TeV (in the left panel) and $f = 100$ TeV (in the right panel). Since in the mass region $m_a = 1000 - 2500$ GeV, the dominant dependence of the cross sections scales as $1/f^2$, one can assume that it comes from the interference piece. However, it is not a case. Our calculations have shown that the pure axion matrix element M_a in (6) is dominant. Moreover, t - and u -channel terms in Eqs. (10)-(12) scale as $1/f^4$ and are negligible with respect to s -channel terms in Eqs. (7) and (12). The main contribution comes from the resonance region $s \sim m_a^2$ in the s -channel terms of M_a . As a result, in the mass region $m_a = 1000 - 2500$ GeV we get

$$\sigma \sim \frac{1}{f^2} \text{Br}(\gamma\gamma \rightarrow a), \quad (28)$$

in a qualitative agreement with Fig. 4. For more details, see Appendix A.

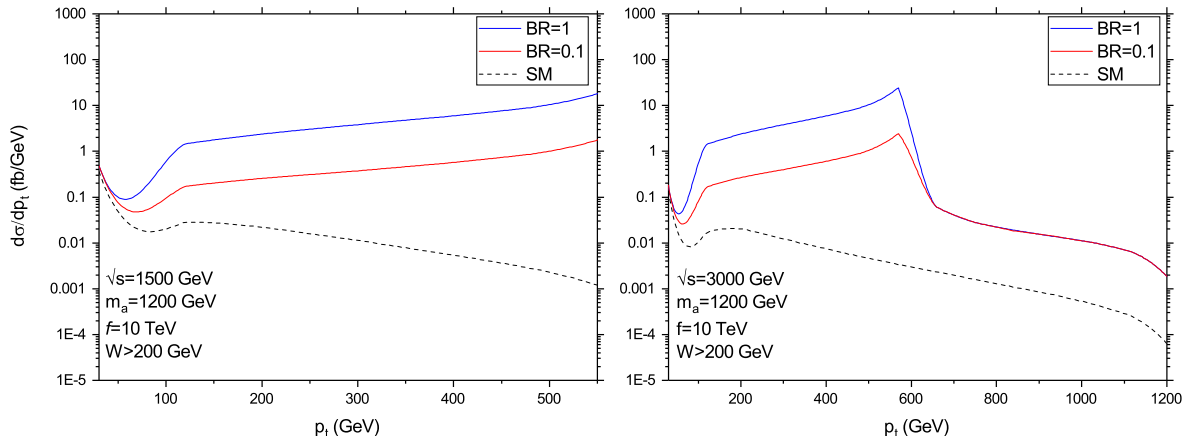


Figure 2: The differential cross sections for the process $\gamma\gamma \rightarrow \gamma\gamma$ at the CLIC for the CB initial photons with the ALP mass $m_a = 1200$ GeV, coupling constant $f = 10$ TeV, and cut $W > 200$ GeV imposed on the photon invariant mass W . The invariant energy is equal to $\sqrt{s} = 1500$ (3000) GeV in the left (right) panel. The curves both for $\text{Br}(a \rightarrow \gamma\gamma) = 1.0$ and $\text{Br}(a \rightarrow \gamma\gamma) = 0.1$ are shown. The dashed lines denote the SM contributions.

One can also see that the cross sections are very sensitive to the parameter m_a in the interval $m_a = 1000 - 2500$ GeV, in which it is approximately two orders of magnitude greater than for m_a outside of this mass range. It is not surprising that this is the region where the value of the ALP coupling constant f is mostly restricted by the light-by-light process, see Figs. 5, 6. In these figures, we have applied the cut $p_t > 500$ GeV in order to suppress SM cross sections relative to total cross sections as we analyzed from the Fig. 3. In this analysis, we have used the following statistical significance (SS) formula [97],

$$SS = \sqrt{2[(S + B) \ln(1 + S/B) - S]}. \quad (29)$$

Here S and B are the numbers of the signal and background events, respectively. It can be obtained that $SS \simeq S/\sqrt{B}$ for $S \ll B$. It is assumed that the uncertainty of the background is negligible.

Our obtained exclusion regions should be compared with the current exclusion regions on the ALP coupling and ALP mass presented in Fig. 7, especially with that obtained for the process $pp \rightarrow p(\gamma\gamma \rightarrow \gamma\gamma)p$ at the LHC

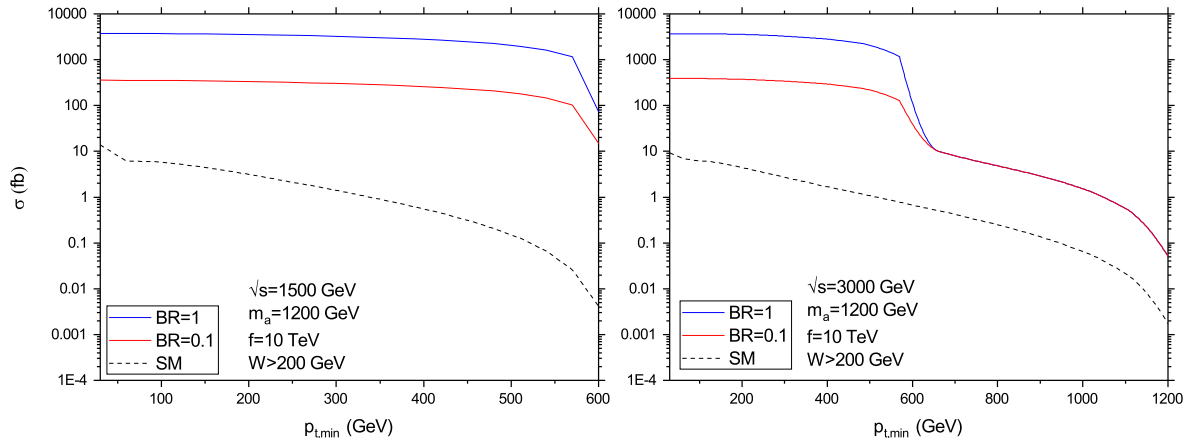


Figure 3: The same as in Fig. 2, but for the total cross sections as functions of the transverse momenta cutoff $p_{t,\min}$ of the final photons.

[78]. This comparison demonstrates the great potential of the light-by-light scattering at the CLIC. Our 95% C.L. parameter exclusion region is presented in Fig. 5 for $\sqrt{s} = 1500$ GeV and $L = 2500$ fb $^{-1}$ using $\text{Br}(a \rightarrow \gamma\gamma) = 1.0, 0.5,$ and 0.1 . The best bounds are achieved for $\text{Br}(a \rightarrow \gamma\gamma) = 1.0$. This figure shows the upper bound $f^{-1} < 5.5 \times 10^{-2}$ TeV $^{-1}$ for the ALP mass interval 10 GeV–800 GeV, while the light-by-light scattering at the LHC gives the bound $f^{-1} < 4 \times 10^{-1}$ TeV $^{-1}$ for the same mass interval. Moreover, we have obtained the very strong upper bound on f^{-1} , which is of the order of 10^{-4} TeV $^{-1}$ for the mass range $m_a = 1000 - 1200$ GeV. The best limit for the $pp \rightarrow p(\gamma\gamma \rightarrow \gamma\gamma)p$ is of the order of 10^{-2} TeV $^{-1}$ for the mass range $m_a = 600 - 800$ GeV, as seen from Fig. 7. The 95% C.L. exclusion region for $\sqrt{s} = 3000$ GeV and $L = 5000$ fb $^{-1}$ is presented in Fig. 6. It demonstrates the wider exclusion regions. In particular, one can be derived the upper bound $f^{-1} < 3 \times 10^{-2}$ TeV $^{-1}$ for the ALP mass interval 10 GeV–800 GeV. The stronger bounds on f^{-1} have been obtained, which are of the order of 10^{-4} TeV $^{-1}$ for the mass range $m_a = 1000 - 2400$ GeV and $\text{Br}(a \rightarrow \gamma\gamma) = 1.0$.

The sensitivity region in Fig. 6 is limited to a rather sharp region. It is due to the fact that the cross section is large only in the mass range 1000 – 2500 GeV, see Fig. 4. In this region the axion term dominates, while outside it the contributions from the axion and SM terms are comparable and they partially cancel each other. By comparison the exclusion region in Fig. 6 with

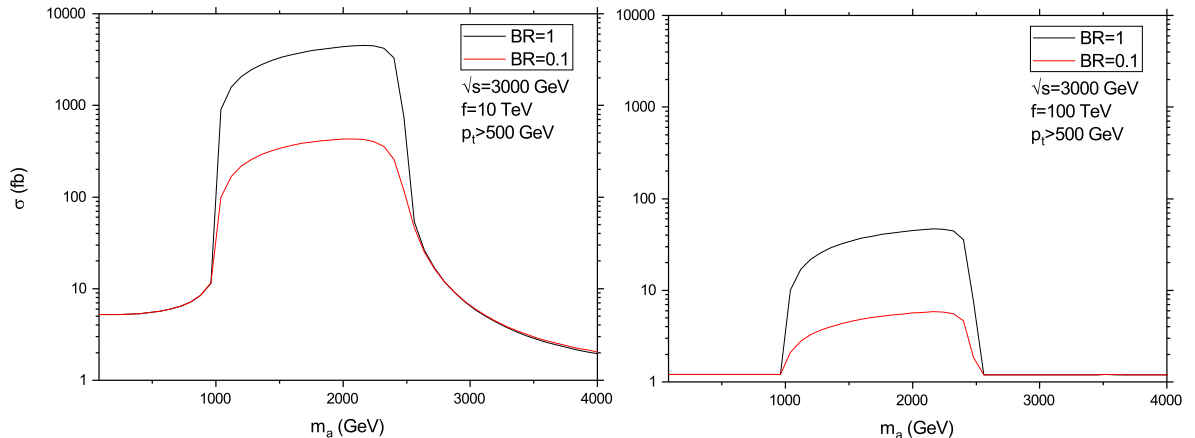


Figure 4: The total cross sections for the process $\gamma\gamma \rightarrow \gamma\gamma$ at the CLIC for the CB initial photons as functions of the ALP mass m_a for $f = 10$ TeV and $f = 100$ TeV with two values of $\text{Br}(a \rightarrow \gamma\gamma)$.

that for the process $pp \rightarrow p(\gamma\gamma \rightarrow \gamma\gamma)p$ in Fig. 7, we have to conclude that the above mentioned behavior of the sensitivity is really related to a specific dependence of the subprocess $\gamma\gamma \rightarrow \gamma\gamma$ on the axion mass as discussed in Appendix A.

2.2 Weizsäcker-Williams photons

The photon-photon interactions can be realized at the CLIC in a different way, using almost real photons emitted from incoming electron beams. These processes can be studied in the framework of the Weizsäcker-Williams approximation (WWA). [98]-[101].

In this approximation, incoming electrons scatter at very small angles. Therefore, electrons can not be caught in the main detector. If scattered electrons of the beams are observed, minimal and maximal values of scattered photon energies can be determined. Otherwise, energy or momentum cuts imposed on final state particles can be used to specify the minimum photon energy. The photon virtuality varies in the following kinematical range

$$Q_{\min}^2 \leq Q^2 \leq Q_{\max}^2, \quad (30)$$

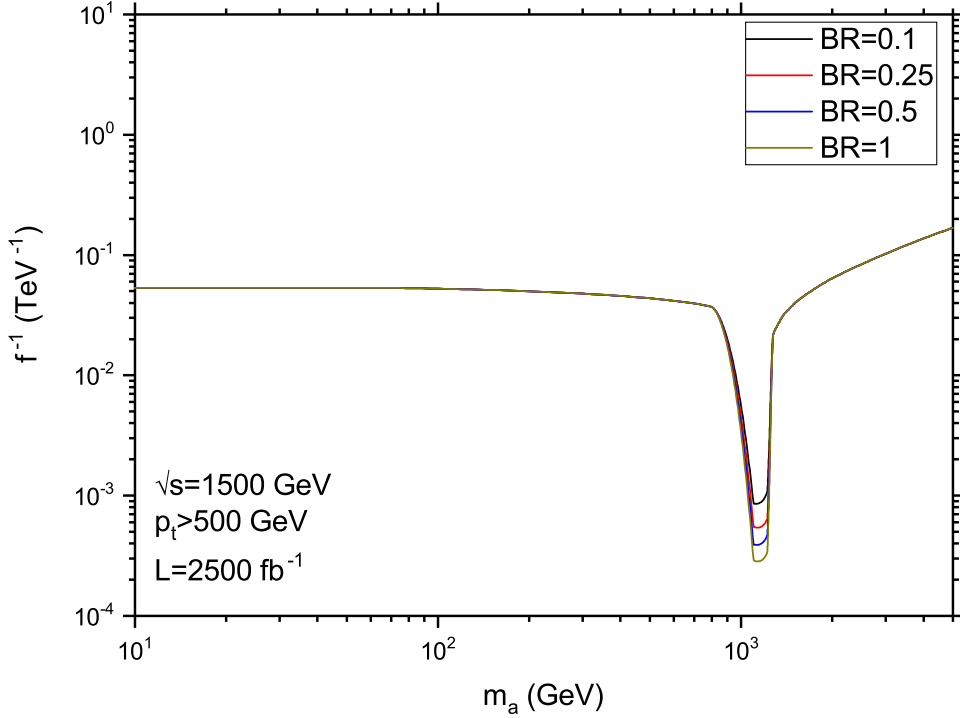


Figure 5: The 95% C.L. CLIC exclusion region for the process $\gamma\gamma \rightarrow \gamma\gamma$ for the CB initial photons with the invariant energy $\sqrt{s} = 1500$ GeV, cut $W > 200$ GeV on the photon invariant mass, integrated luminosity $L = 2500$ fb^{-1} , and different values of $\text{Br}(a \rightarrow \gamma\gamma)$.

where $Q^2 = -q^2$ (q is the photon momentum), and

$$Q_{\min}^2 = \frac{m_e^2 x^2}{1-x}, \quad Q_{\max}^2 = \frac{4E_e^2}{1-x}. \quad (31)$$

Here E_e is the energy of the incoming electron, E_γ is the photon energy and $x = E_\gamma/E_e$. The scattered electrons have very small scattering angles from the beam direction, and their transverse momenta are small. Therefore, due to momentum conservation, the transverse momenta of the emitted photons should also be very small. This means that the virtuality of the photon Q^2 in WWA is very small (almost real). In an experiment performed by the DELPHI Collaboration, it was observed that the virtualities of 90% photons are less than 1 GeV^2 using appropriate experimental techniques [102]. The

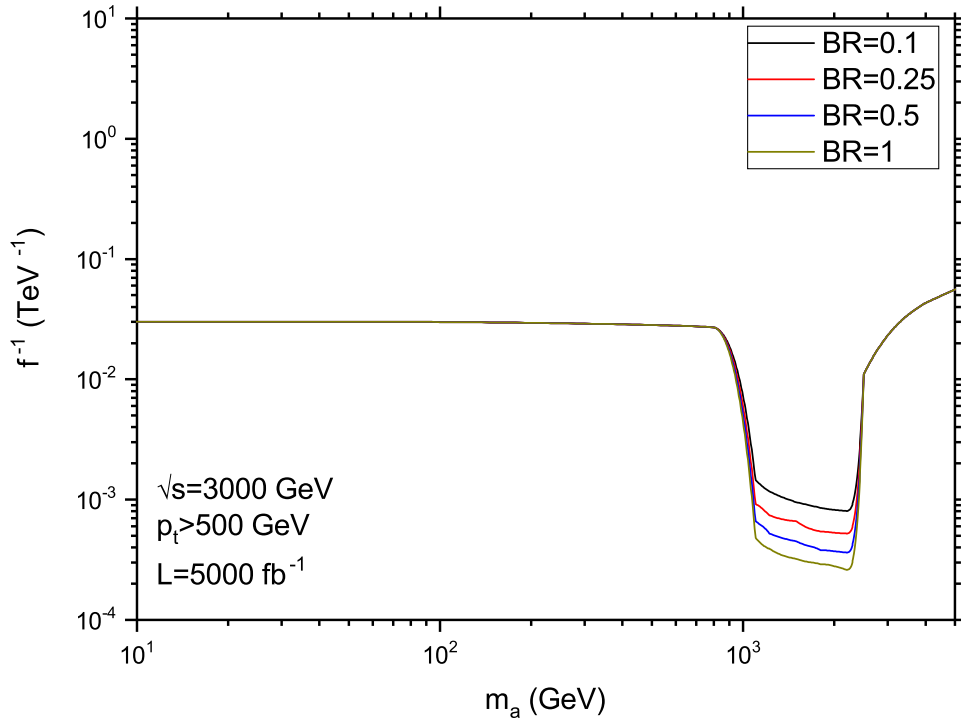


Figure 6: The as in Fig. 5, but for $\sqrt{s} = 3000$ GeV and $L = 5000$ fb $^{-1}$.

WWA is also useful for experimental studies due to it allows us to find cross sections for the process $e^-e^+ \rightarrow e^-Xe^+$ via subprocess $\gamma\gamma \rightarrow X$ [103]. In the literature, there are many papers on photon-induced processes, see, for instance, [102], [104]-[111].

In the WWA, the photons have the following spectrum

$$f_{\gamma/e}(x) = \frac{\alpha}{\pi} \left[\left(\frac{1-x+x^2/2}{x} \right) \log \frac{Q_{\max}^2}{Q_{\min}^2} - \frac{m_e^2 x}{Q_{\min}^2} \left(1 - \frac{Q_{\min}^2}{Q_{\max}^2} \right) \right]. \quad (32)$$

Here m_e is the electron mass, $x = E_\gamma/E_e$ is the ratio of the photon energy and energy of the incoming electron, and α is the fine structure constant. The cross section of the process $e^-e^+ \rightarrow e^-e^+\gamma\gamma$ can be calculated using formula (26) with the replacement $y_{\max} = z_{\max} = 1 - m_e/E_e$. In the light of above arguments, in what follows, we take $Q_{\max}^2 = 2$ GeV 2 .

In addition to the backgrounds mentioned in subsection 2.1, possible backgrounds also came from $\gamma\gamma \rightarrow e^+e^-\gamma\gamma$ and ZZ -induced processes. The first

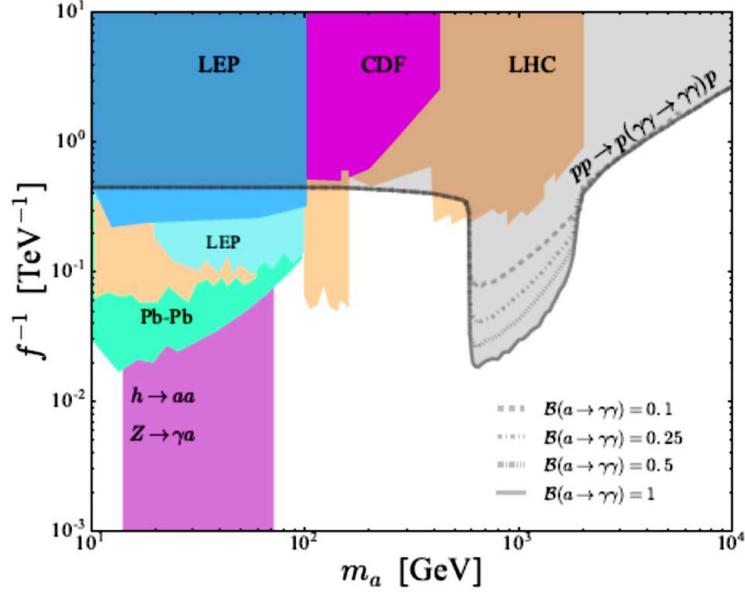


Figure 7: The 95% C.L. current exclusion regions for different values of $\text{Br}(a \rightarrow \gamma\gamma)$ [78].

one was estimated in [88] to be below 1%. The second one may not be taken into account since the ZZ luminosity is approximately 100 times smaller than the $\gamma\gamma$ luminosity [112].

The results of our calculations of the differential and total cross sections are presented in Figs. 9 and 10. They should be compared with the cross sections for the process induced by the CB photons shown in Figs. 2 and 3. The WWA cross sections have appeared to be approximately 10^4 (10^2) times smaller than the CB cross sections for $\sqrt{s} = 1500$ GeV ($\sqrt{s} = 3000$ GeV).

The same one can see in Fig. 11, where the total cross section for the process $e^+e^- \rightarrow e^+\gamma\gamma e^- \rightarrow e^+a e^- \rightarrow e^+\gamma\gamma e^-$ is shown as a function of the ALP mass m_a . For the ALP branching ratio $\text{Br}(a \rightarrow \gamma\gamma) = 1.0$, there are big bumps in the curves in the mass region 1000 GeV–3000 GeV for both values of the collision energy \sqrt{s} .

Fig. 12 gives the 95% C.L. CLIC exclusion region in the (m_a, f^{-1}) plane in the case when the subprocess $\gamma\gamma \rightarrow \gamma\gamma$ is induced by the WWA photons with $\sqrt{s} = 1500$ GeV and $L = 2500$ fb $^{-1}$. As one can see from this figure, the bounds are of the order of 10^{-1} TeV $^{-1}$ in the mass regions 10 GeV–1000

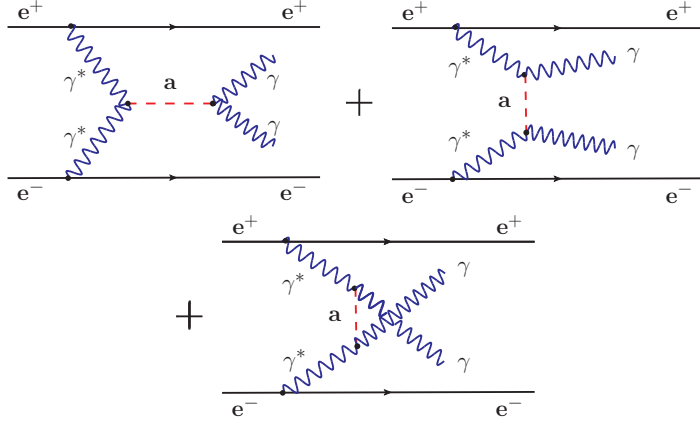


Figure 8: The Feynman diagrams describing photon-induced light-by-light virtual production of the axion-like particle a in e^+e^- collision.

GeV. In the narrow mass region 1000 GeV–1500 GeV it is obtained to be of the order of 10^{-3} TeV^{-1} . Similarly, Fig. 13 shows the 95% C.L. exclusion region in the (m_a, f^{-1}) plane for $\sqrt{s} = 3000 \text{ GeV}$ and $L = 5000 \text{ fb}^{-1}$. In the mass region 10 GeV–1000 GeV the bounds on f^{-1} are of the order of 10^{-1} TeV^{-1} . In the mass range 1000 GeV–1500 GeV, these bounds reach the value $1 \times 10^{-3} \text{ TeV}^{-1}$. For both \sqrt{s} , the bounds are much weaker than those for the CB initial photons.

3 Conclusions

We have studied the possibility to search for heavy axion-like particles in the process $\gamma\gamma \rightarrow \gamma\gamma$ with Compton backscattered initial photons and process $e^+e^- \rightarrow e^+e^-\gamma\gamma$ induced by light-by-light scattering with Weizsäcker-Williams initial photons at the CLIC. The calculations were made for the collision energy $\sqrt{s} = 1500 \text{ GeV}$ (2nd stage of the CLIC) and integrated luminosity $L = 2500 \text{ fb}^{-1}$, as well as for the energy $\sqrt{s} = 3000 \text{ GeV}$ and integrated luminosity $L = 5000 \text{ fb}^{-1}$ (3rd stage of the CLIC). It was assumed that the pseudoscalar ALP interacts with photons via CP-even term in the Lagrangian (2).

We 95% C.L. exclusion regions in the plane (m_a, f^{-1}) , where m_a is the ALP mass, f^{-1} ALP–photon coupling, are given. The results are presented

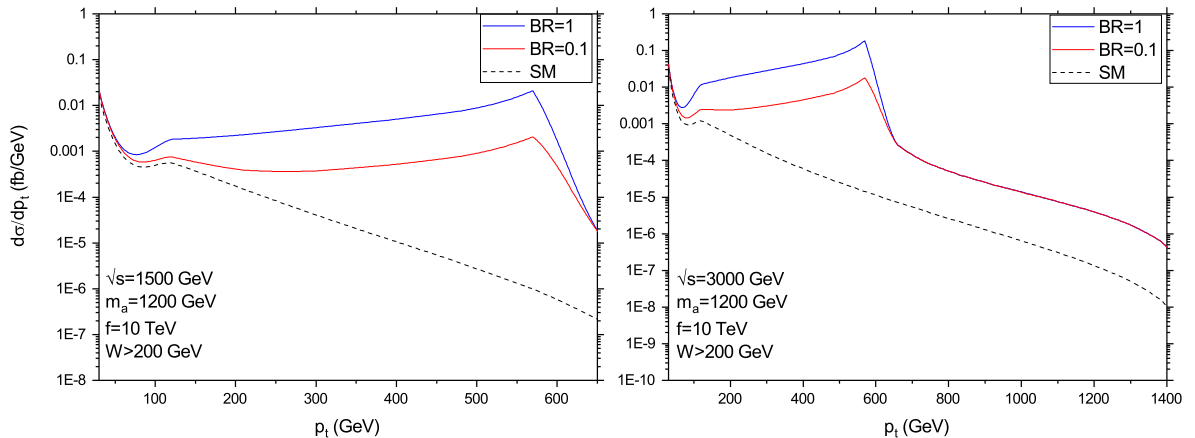


Figure 9: The differential cross sections for the process $e^+e^- \rightarrow e^+\gamma\gamma e^- \rightarrow e^+a e^- \rightarrow e^+\gamma\gamma e^-$ at the CLIC in the WWA for the initial photons in the subprocess $\gamma\gamma \rightarrow \gamma\gamma$ as functions of the transverse momenta of the final photons p_t for the ALP mass $m_a = 1200$ GeV and coupling constant $f = 10$ TeV. The invariant energy is equal to $\sqrt{s} = 1500$ (3000) GeV on the left (right) panel. The curves for both $\text{Br}(a \rightarrow \gamma\gamma) = 1.0$ and $\text{Br}(a \rightarrow \gamma\gamma) = 0.1$ are shown. The dashed lines denote the SM contributions.

for two values of \sqrt{s} and L as functions of the ALP branching ratio into photons $\text{Br}(a \rightarrow \gamma\gamma)$. The best bounds are obtained for $\text{Br}(a \rightarrow \gamma\gamma) = 1$. Our calculations have shown that the numerical results remain almost the same if we take into account the CP-odd term instead of the CP-even one in the Lagrangian (2), with the same coupling f^{-1} .

By comparing our exclusion regions with other collider exclusion regions, we may conclude that the ALP search at the CLIC has the great physics potential of searching for the ALPs, especially, in the mass region 1 TeV – 2.4 TeV, for the collision energy $\sqrt{s} = 3000$ GeV and integrated luminosity $L = 5000 \text{ fb}^{-1}$. In particular, our bounds are much stronger than recently obtained bounds for the ALP virtual production in the process $p(\gamma\gamma \rightarrow \gamma\gamma)p$ at the LHC [78].

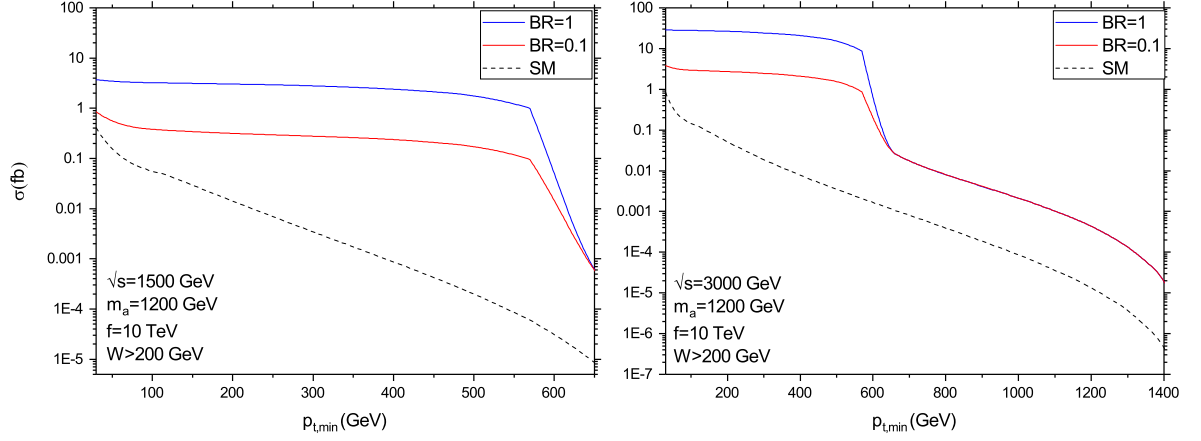


Figure 10: The same as in Fig. 9, but for the total cross sections as functions of the transverse momenta cutoff $p_{t,\min}$ of the final photons.

Appendix A

Here we obtain an approximate formula for the cross section with the CB initial photons. As it was already mentioned in the text, in the mass region 1000 – 2500 GeV the dominant contribution to the cross section comes from the s -channel terms in M_a . Let us put $M = M_{++++}$ (5)

$$M = -\frac{4}{f^2} \frac{s^2}{s - m_a^2 + im_a\Gamma_a} . \quad (\text{A.1})$$

Then

$$|M|^2 = \frac{16}{f^4} \frac{s^4}{(s - m_a^2)^2 + m_a^2\Gamma_a^2} . \quad (\text{A.2})$$

We get from (A.2) that at high energy

$$|M|^2|_{s \gg m_a^2} \sim \frac{s^2}{f^4} . \quad (\text{A.3})$$

However, simple dimensional arguments are not valid in the most important resonance region $s \sim m_a^2$ in which

$$|M|^2|_{s \sim m_a^2} \sim \frac{m_a^6}{f^4\Gamma_a^2} . \quad (\text{A.4})$$

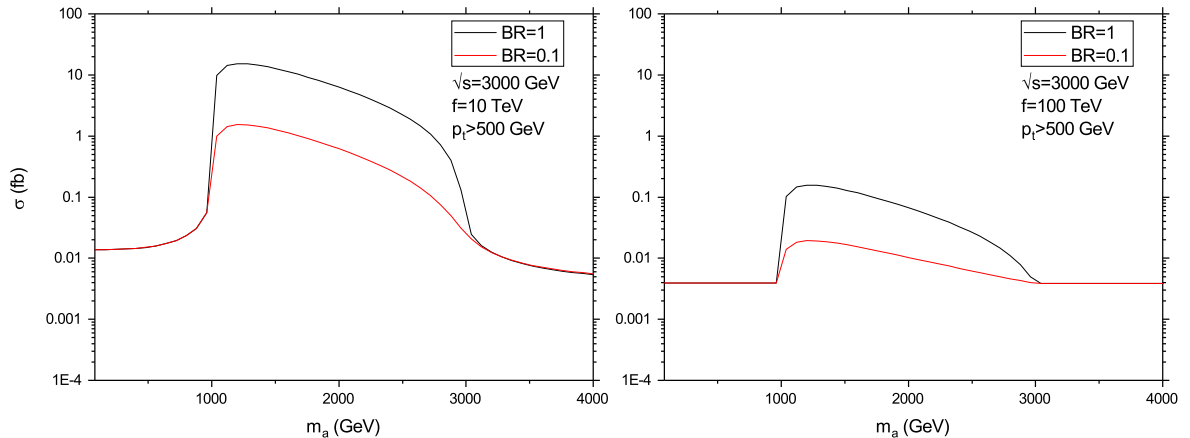


Figure 11: The total cross sections for the process $e^+e^- \rightarrow e^+\gamma\gamma e^- \rightarrow e^+a e^- \rightarrow e^+\gamma\gamma e^-$ at the CLIC in the WWA for the initial photons as functions of the ALP mass m_a for $f = 10$ TeV and $f = 100$ TeV with two values of $\text{Br}(a \rightarrow \gamma\gamma)$.

Since M depends only on s , we find from the relation

$$\frac{d\hat{\sigma}(s)}{d\Omega} = \frac{|M|^2}{64\pi^2 s} \quad (\text{A.5})$$

that the cross section of the subprocess $\gamma\gamma \rightarrow \gamma\gamma$ is equal to

$$\hat{\sigma}(s) = \frac{1}{16\pi s} |M|^2. \quad (\text{A.6})$$

The integrations in eq. (26) can be rewritten as follows

$$2z dz \frac{dy}{y} = dx_1 dx_2 \sim \frac{dx_1}{x_1} \frac{ds}{4E_e^2}. \quad (\text{A.7})$$

Then the cross section of the process under consideration is given by the integral

$$\sigma = \frac{1}{4E_e^2} \int ds \frac{1}{16\pi s} |M|^2. \quad (\text{A.8})$$

Let us estimate the contribution to σ from the resonance region

$$m_a^2 - Cm_a\Gamma_a \leq s \leq m_a^2 + Cm_a\Gamma_a, \quad (\text{A.9})$$

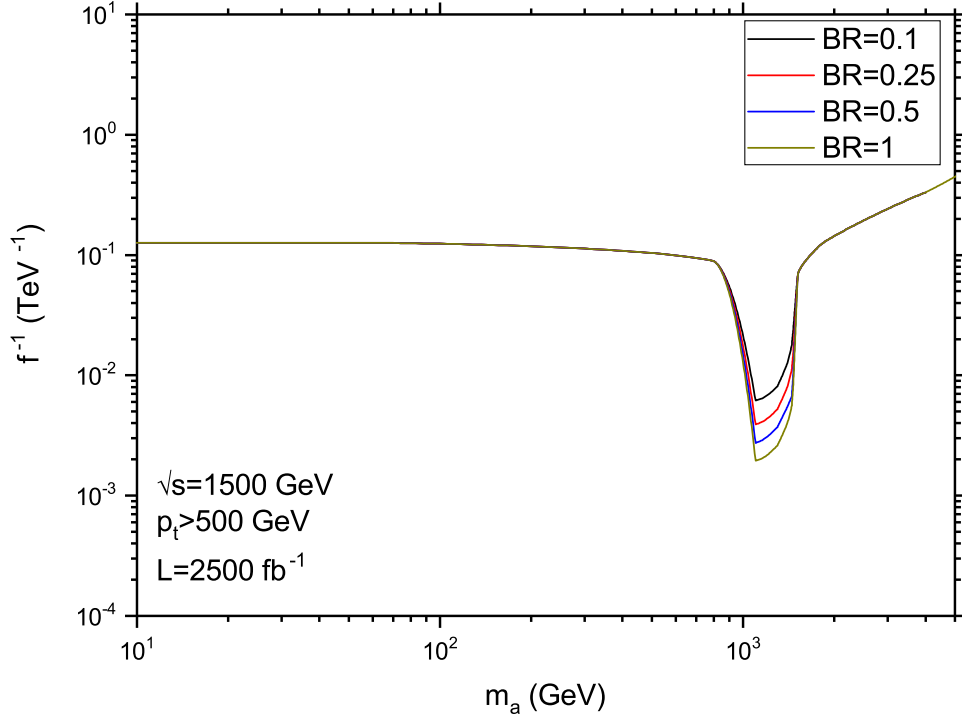


Figure 12: The 95% C.L. CLIC exclusion region for the process $e^+e^- \rightarrow e^+\gamma\gamma e^- \rightarrow e^+a e^- \rightarrow e^+\gamma\gamma e^-$ with the invariant energy $\sqrt{s} = 1500$ GeV, transverse momentum cut on the final photons $p_t = 500$ GeV, integrated luminosity $L = 2500$ fb $^{-1}$, and different values of $\text{Br}(a \rightarrow \gamma\gamma)$. The WWA for the initial photons in the subprocess $\gamma\gamma \rightarrow \gamma\gamma$ is used.

where C is a constant of order $O(1)$. After introducing variable $x = (s - m_a^2)/(m_a\Gamma_a)$, we get

$$\sigma = \frac{1}{f^2} \frac{m_a^2}{E_e^2} \text{Br}(a \rightarrow \gamma\gamma) \int_{-C}^C dx \frac{1}{x^2 + 1} . \quad (\text{A.10})$$

In order to numerically evaluate the cross section, we put $C = 1$. Then we obtain the estimate

$$\sigma \simeq 0.39 \times 10^6 \frac{\pi}{2} \left(\frac{\text{TeV}}{f} \right)^2 \left(\frac{m_a}{E_e} \right)^2 \text{Br}(a \rightarrow \gamma\gamma) \text{ fb} . \quad (\text{A.11})$$

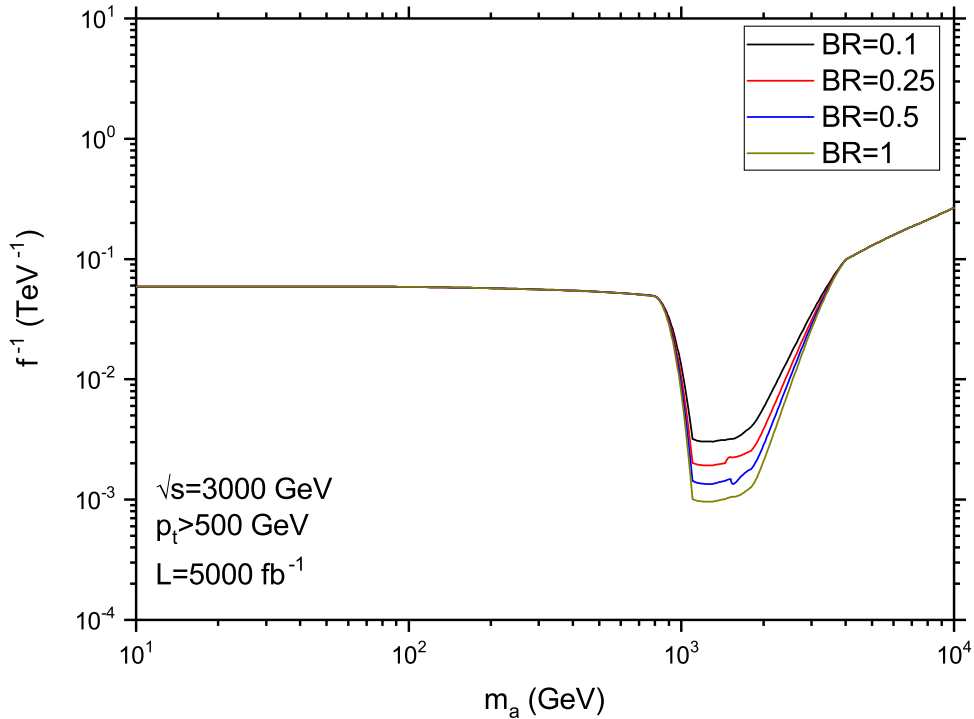


Figure 13: The same as in Fig. 12, but for $\sqrt{s} = 3000$ GeV and $L = 5000$ fb $^{-1}$.

Comparing this formula with Fig. 4, we see that it gives a correct dependence of the cross section on the parameters f , m_a and $\text{Br}(a \rightarrow \gamma\gamma)$ in the mass region 1100 – 2500 GeV. As for numerical values of σ , we find, for example, for $E_e = 3.0$ TeV, $f = 10$ TeV, $m_a = 1.5$ TeV, and $\text{Br}(a \rightarrow \gamma\gamma) = 1.0$

$$\sigma \simeq 1.6 \times 10^3 \text{ fb} . \quad (\text{A.12})$$

An accurate integration with an account of the photon spectra should modify the numerical factor in the right-hand-side of eq. (A.11). This formula must be regarded only as an illustration of how the main contribution to the cross section comes from the resonance region of the pure axion amplitude.

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