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Effective nucleon mass, incompressibility and third-order derivative of nuclear saturation curve in the relativistic mean field theory with vector meson self-interaction

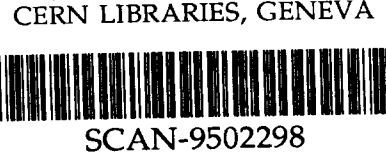
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ABSTRACT

The relations among the effective nucleon mass M_0^* , incompressibility K and the third-order derivative K' of saturation curve are studied using the relativistic mean field model which has both the scalar and the vector self-coupling interactions. The vector self-coupling makes the EOS softer at higher densities when $K \gtrsim 200\text{MeV}$. The Coulomb coefficient K_c of nucleus incompressibility is also calculated. The parameters sets of the model are determined so as to realize both the empirical K - K_c relation and $M_0^* = 0.6M$ which is consistent with the empirical spin-orbit potential. The obtained EOS with $K = 300\text{MeV}$ is successful to account for the symmetry properties and very close to the results of the Dirac-Brueckner-Hartree-Fock calculation.



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I. INTRODUCTION

One way to determine the incompressibility K of nuclear matter from the giant monopole resonance (GMR) data is using the leptodermous expansion[1] of nucleus incompressibility $K(A, Z)$ as follows.

$$K(A, Z) = K + K_{sf}A^{-1/3} + K_{vs}I^2 + K_cZ^2A^{-4/3} + \dots \quad ; \quad I = 1 - 2Z/A, \quad (1)$$

where the coefficients K_{sf} , K_{vs} and K_c are surface term coefficient, volume-symmetry coefficient and Coulomb coefficient respectively. We have omitted higher terms in eq. (1). Though there is uncertainty in the determination of these coefficients by using the present data, Pearson [2] pointed out that there is a strong correlation among K , K_c and the skewness coefficient, i.e., the third-order derivative of nuclear saturation curve. Similar observations are done by Shlomo and Youngblood [3].

According to this context, Rudaz et al. [4] studied the relation between K and the skewness coefficient using the generalized version of the relativistic Hartree approximation [5]. Recently, both of compressional and surface properties are studied by Von-Eiff et al. [6][7][8] in the framework of the mean field approximation of the σ - ω - ρ model with the nonlinear σ terms. They found that low incompressibility ($K \approx 200\text{MeV}$) and a large effective nucleon mass M_0^* at the normal density ($0.70 \leq M_0^*/M \leq 0.75$) are favorable for the nuclear surface properties [8]. On the other hand, using the same model, Bodmer and Price [9] found that the experimental spin-orbit splitting in light nuclei supported $M_0^* \approx 0.60M$. The result of the generator coordinate calculations for breathing-mode GMR by Stoitsov, Ring and Sharma [10] suggests that $K \approx 300\text{MeV}$.

In previous paper[11], we have studied the relation between K and the third-order derivative K' of nuclear saturation curve in detail, using the mean field theory with the nonlinear σ terms [12]. We found that $K = 300\text{MeV}$ is favorable to account for K , K_c , a_4 and K_{vs} , simultaneously. However, the effective nucleon mass M_0^* of the equations of state (EOS) which we found is $0.83M$. That is larger than the value of the analysis by Bodmer and Price [9], which is referred above.

In this paper, we study the effective nucleon mass, incompressibility K and K' , using the mean field theory which has the vector self-interaction as well as the scalar self-interactions [13], and compare the results with the GMR data empirically, under the assumption of scaling model[1]. It is known that the EOS of the relativistic mean field theory with vector self-coupling is very close to the result of the Dirac-Brueckner-Hartree-Fock (DBHF) calculations [14] [15] even at the higher densities [16][17]. This

paper is organized as follows. In section 2, we review the general formalism of the vector self-coupling model, briefly. In section 3, the saturation condition is investigated, and the expressions for K and K' are shown. In section 4, the relation among M_0^* , K and K' is studied. In sect. 5, the parameters of the model are determined so as to account for both the empirical K - K_c relation and the empirical spin-orbit potential [13]. Section 6 is devoted to the summary of this paper.

II. FORMALISM

We use the nonlinear relativistic mean field theory based on the σ - ω model with nonlinear σ and ω terms [13]. (For a while, we restrict our discussions to the symmetric nuclear matter and do not consider the ρ meson effects.) The lagrangian density consists of three fields, the nucleon ψ , the scalar σ -meson ϕ and the vector ω -meson V_μ , i.e.,

$$L = \bar{\psi}(i\gamma_\mu\partial^\mu - M)\psi + \frac{1}{2}\partial_\mu\phi\partial^\mu\phi - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{2}m_\omega^2V_\mu V^\mu (1 + \frac{g_\omega^2}{2}Y^2V_\mu V^\mu) + g_s\bar{\psi}\psi\phi - g_\omega\bar{\psi}\gamma_\mu\psi V^\mu - U(\phi) \quad ; \quad F_{\mu\nu} = \partial_\mu V_\nu - \partial_\nu V_\mu, \quad (2)$$

where m_ω , g_s and g_ω are ω -meson mass, σ -nucleon coupling and ω -nucleon coupling respectively. The potential $U(\phi)$ includes a nonlinear cubic-quartic terms of the scalar field ϕ ; i.e.,

$$U(\phi) = \frac{1}{2}m_s^2\phi^2 + \frac{1}{3}b\phi^3 + \frac{1}{4}c\phi^4, \quad (3)$$

where m_s is σ -meson mass, and b and c are the constant parameters which are determined phenomenologically. The constant parameter Y represents the strength of the vector self-interaction. In the mean field approximation, the effective nucleon mass M^* is given by

$$M^* = M - \Phi \quad ; \quad \Phi = g_s \langle \phi \rangle, \quad (4)$$

where $\langle \phi \rangle$ is the ground-state expectation value of the field ϕ . The baryon density ρ and scalar density ρ_s are given by

$$\rho = \frac{\lambda}{3\pi^2} k_F^3, \quad (5)$$

and

$$\rho_s = \frac{\lambda}{2\pi^2} M^* [k_F \sqrt{k_F^2 + M^{*2}} - M^{*2} \ln \left(\frac{k_F + \sqrt{k_F^2 + M^{*2}}}{M^*} \right)], \quad (6)$$

where k_F is the Fermi momentum and $\lambda = 2$ in nuclear matter. The total energy of the

system is also given by

$$\epsilon = \epsilon_N + \epsilon_v + U(\Phi). \quad (7)$$

The nucleon energy term ϵ_N in eq. (7) is given by

$$\begin{aligned} \epsilon_N(k_F, M^*) &= \frac{\lambda}{12\pi^2} [3k_F^3 E_F^* + \frac{3}{2} M^{*2} k_F E_F^* \\ &\quad - \frac{3}{2} M^{*4} \ln(\frac{k_F + E_F^*}{M^*})], \end{aligned} \quad (8)$$

where $E_F^* = \sqrt{k_F^2 + M^{*2}}$. The vector meson part ϵ_v is given by

$$\epsilon_v = W\rho - \frac{1}{2} \frac{M^2 W^2}{C_v^2} (1 + \frac{Y^2 W^2}{2}); \quad W = g_v \langle V^0 \rangle, \quad (9)$$

where $\langle V^0 \rangle$ is the ground-state expectation value of V^0 and $C_v = g_v M/m_v$. In the latter part of this paper, we write $U(\Phi)$ as

$$U(\Phi) = \frac{1}{2C_s^2} M^2 \Phi^2 + \frac{1}{3} B M \Phi^3 + \frac{1}{4} C \Phi^4, \quad (10)$$

where $C_s = g_s M/m_s$, $B = b/(g_s^3 M)$ and $C = c/g_s^4$.

The equation for the scalar field is expressed as

$$U'(\Phi) = \frac{dU(\Phi)}{d\Phi} = \frac{1}{C_s^2} M^2 \Phi + B M \Phi^2 + C \Phi^3 = \rho_s. \quad (11)$$

Using eqs. (4), (6) and (11), we can determine M^* and Φ in a self-consistent way.

The W can be determined by the equation of motion for the vector field,

$$\frac{\partial \epsilon_v}{\partial W} = 0. \quad (12)$$

The equation (12) gives [13]

$$w(1+w^2) - y' = 0, \quad (13)$$

where $w = WY$ and $y' = C_v^2 \rho Y/M^2$ are dimensionless quantities. When $y'(\geq 0)$ is

given, the equation (13) has a non-negative real solution as

$$w = \sqrt[3]{\frac{\sqrt{D} + y'}{2}} - \sqrt[3]{\frac{\sqrt{D} - y'}{2}}, \quad (14)$$

where $D = y'^2 + 4/27$. Because $d(w(1+w^2) - y')/dw = 1 + 3w^2 > 0$, eq. (14) is the unique real solution of eq. (13). In the case of $y'^2 \gg 4/27$, $w \approx y'^{1/3}$. When M^* , Φ and W are determined, we can calculate energy density of the system given by eq. (7).

III. SATURATION CONDITION, INCOMPRESSIBILITY AND THIRD-ORDER DERIVATIVE OF NUCLEAR SATURATION CURVE

At the saturation density ρ_0 , the pressure P of the system vanishes, i.e.,

$$P = \rho^2 \frac{de}{d\rho} = \rho(W + E_F^* - e) = 0; \quad e = \frac{\epsilon}{\rho}. \quad (15)$$

The saturation condition (15) gives the following relation [13]

$$W_0 = W(\rho = \rho_0) = \frac{w_0}{Y} = \frac{C_v^2 \rho_0 w_0}{M^2 y} = e_0 - E_F^* = -a_1 + M - \sqrt{k_{F0}^2 + M_0^{*2}}, \quad (16)$$

where $y = C_v^2 \rho_0 Y/M^2$ and the values with the subscript "0" are the ones at the normal density ρ_0 . We remark $y = y'(\rho = \rho_0)$. The equation (16) is written as

$$M_0^* = \sqrt{(-a_1 + M - \frac{C_v^2 \rho_0 w_0}{M^2 y})^2 - k_{F0}^2}, \quad (17)$$

or [13]

$$C_v^2 = (-a_1 + M - \sqrt{k_{F0}^2 + M_0^{*2}}) y M^2 / (w_0 \rho_0). \quad (18)$$

Putting $C_v = 0$ and $\rho_0 = 0.15 \text{fm}^{-3}$ in eq. (17), we get $M^* \approx 0.94M$ which is the upper bound for M_0^* in this model. Using eq. (18), in fig. 1, we show the relation between y and C_v^2 with several values of M_0^* . When y becomes larger, C_v becomes larger when M_0^* is fixed. From the discussion in the end of the previous section, $w_0 \approx y^{1/3}$ for the large $y(y^2 \gg 4/27)$. Then, C_v^2 is proportional to $y^{2/3}$ in the large y limit.

Fig. 1

The incompressibility K at the normal density is defined as

$$K = 9\rho_0^2 \frac{\partial^2 e}{\partial \rho^2} |_{\rho=\rho_0} = 9 \frac{\partial P}{\partial \rho} |_{\rho=\rho_0} = 9\rho_0 \frac{\partial \mu}{\partial \rho} |_{\rho=\rho_0}, \quad (19)$$

where the baryonic chemical potential μ is given by

$$\mu = E_F^* + W. \quad (20)$$

In this model, K is written as [13]

$$K = 9\rho_0 \left(\frac{C_v^2}{M^2(1+3w^2)} + \frac{k_F^2}{3\rho E_F^*} + \frac{M^*}{E_F^*} M^{*'} \right)_{\rho=\rho_0}, \quad (21)$$

where

$$M^{*'} = \frac{dM^*}{d\rho} = -\frac{M^*}{E_F^*} \frac{1}{U''(\Phi) + \partial \rho_s / \partial M^*}, \quad (22)$$

with

$$U''(\Phi) = \frac{d^2 U(\Phi)}{d\Phi^2}. \quad (23)$$

From eq. (6), $\partial \rho_s / \partial M^*$ is given by

$$\frac{\partial \rho_s}{\partial M^*} = \frac{\lambda}{2\pi^2} \left[k_F E_F^* - 3M^{*2} \ln \left(\frac{k_F + E_F^*}{M^*} \right) + 2 \frac{k_F M^{*2}}{E_F^*} \right]. \quad (24)$$

We also defined the third-order derivative K' of nuclear binding energy $E_b (= e - M)$ as

$$K' = 3\rho_0^3 \frac{d^3 E_b}{d\rho^3} |_{\rho=\rho_0} = 3\rho_0 \frac{d^2 P}{d\rho^2} |_{\rho=\rho_0} - \frac{4}{3} K = 3\rho_0^2 \frac{d^2 \mu}{d\rho^2} |_{\rho=\rho_0} - K. \quad (25)$$

In this model, K' is written as

$$K' = 3\rho_0^2 \left(-\frac{6wy}{\rho_0 M^2 (1+3w^2)^3} + \frac{d^2 E_F^*}{d\rho^2} \right)_{\rho=\rho_0} - K, \quad (26)$$

where

$$\frac{d^2 E_F^*}{d\rho^2} = \frac{1}{E_F^*} \left[\left(\frac{k_F M^*}{3\rho E_F^*} \right)^2 + \left(\frac{k_F}{E_F^*} M^{*'} \right)^2 - 2 \frac{k_F^2 M^*}{3\rho E_F^{*2}} M^{*'} - \frac{2k_F^2}{9\rho^2} + M^* M^{*''} \right]. \quad (27)$$

The $M^{*''} = \frac{d^2 M^*}{d\rho^2}$ is given by

$$\left(U'''(\Phi) + \frac{\partial \rho_s}{\partial M^*} \right) M^{*''} = -\frac{1}{E_F^*} M^{*'} + \frac{k_F^2 M^*}{3\rho E_F^{*3}} + \frac{M^{*2}}{E_F^*} M^{*'} + (M^{*'})^2 U^{(3)}(\Phi) - \frac{d}{d\rho} \left(\frac{\partial \rho_s}{\partial M^*} \right) M^{*'}, \quad (28)$$

where

$$\begin{aligned} \frac{d}{d\rho} \left(\frac{\partial \rho_s}{\partial M^*} \right) &= \frac{\lambda}{2\pi^2} \left[(3k_F - 2E_F^* + 2 \frac{M^{*2}}{E_F^*}) \frac{k_F}{3\rho} + (4k_F - 3E_F^* - 2 \frac{k_F M^{*2}}{E_F^{*2}}) \left(\frac{k_F^2}{3E_F^* \rho} + \frac{M^*}{E_F^*} M^{*'} \right) \right. \\ &\quad \left. + (3M^* + 4 \frac{k_F M^*}{E_F^*} - 6M^* \ln \left[\frac{k_F + E_F^*}{M^*} \right]) M^{*'} \right], \end{aligned} \quad (29)$$

and

$$U^{(3)} = \frac{d^3 U(\Phi)}{d\Phi^3}. \quad (30)$$

IV. THE RELATION AMONG THE EFFECTIVE NUCLEON MASS, INCOMPRESSIBILITY AND THE THIRD-ORDER DERIVATIVE OF NUCLEAR SATURATION CURVE

In our calculations, we put $M = 939\text{MeV}$, $\rho_0 = 0.15\text{fm}^{-3}$ and $a_1 = 15.75\text{MeV}$. The other independent parameters y , C_s , C_v , B and C are determined phenomenologically. Besides the two conditions for saturation, i.e., $e_0 = M - a_1$ and $P = 0$, when M_0^* , K and K' are given, we can determine the five parameters of the model. The M_0^* depends on only y and C_v as is seen in eq. (17). Therefore, we give one (two) quantity (quantities) among y , C_v and M_0^* and give two (one) quantities (quantity) among C_s , B , C , K and K' . The other quantities are automatically determined.

First, we check the sign of the quartic coefficient C of the scalar potential $U(\Phi)$, because the negative value of C may cause undesirable behaviors such as bifurcation of the solution [13]. As is pointed out in ref. [13], the vector self-coupling makes C less

negative. In fig. 2. we show the regions for $C > 0$ in the K - M_0^* plane with several values of y . The region is widened as y becomes larger. The C becomes larger (more repulsive) to cancel the attractive effect of vector self-coupling in ϵ_v (See eq. (9)). In the case of $y \geq 2$, C is positive for $M_0^* \geq 0.5M$ and $K = 150 \sim 400\text{MeV}$.

Fig. 2

Fig. 3(a),(b)

Fig. 4(a),(b)

In fig. 3, we show the $M_0^* - K'$ relations with fixed values of K both in the cases of $y = 0$ and $y = 1.0$. When $y = 1.0$, K' monotonically decreases as M_0^* increases. The cross points of curves at $M_0^* \sim 0.8M$, which appear in the case of no vector self-coupling, disappear when $y = 1.0$. In the cases with $y = 1.0$ and $M_0^* \gtrsim 0.6M$, K' is negative. When $K \geq 200\text{MeV}$, K' with $y = 1.0$ is smaller than that with $y = 0$. It seems that the vector self-coupling makes EOS of nuclear matter softer at higher densities. To confirm this observations, in fig. 4, we show the y -dependence of $K - K'$ relation when $M_0^* = 0.6M$ or $0.8M$. When $K \gtrsim 200\text{MeV}$ and $M_0^* = 0.6M$, the vector self-coupling makes K' smaller. In the case of $M_0^* = 0.8M$, K' decreases as y increases for any K . The vector self-coupling makes equations of state of nuclear matter softer at higher densities. However, the $K - K'$ relations hardly change in the larger y limit ($y > 2$).

To compare these results with experiments of GMR, we calculate the Coulomb coefficient K_c of the leptodermous expansion (1), using the scaling model, i.e., using the following equation [1],

$$K_c = -\frac{3q_{el}^2}{5r_0} \left(\frac{9K'}{K} + 8 \right), \quad (31)$$

where q_{el} is the electric charge of proton and $r_0 = (3/(4\pi\rho_0))^{1/3}$. In fig. 5, we show the $K - K_c$ relations with several values of M_0^* in the cases of $y = 0$ and $y = 1.0$. When $K \gtrsim 200\text{MeV}$, the vector self-coupling makes K_c less negative because of the decrease of the ratio K'/K . In these cases, we can account for the empirical values using the vector coupling and the smaller M_0^* . On the contrary, when $K \lesssim 200\text{MeV}$, the vector self-coupling does not make K'/K much smaller or makes K'/K larger. Therefore, it does

not make K_c much larger or makes K_c smaller. So we can not account for the empirical values for $K < 200\text{MeV}$ even we make y larger.

Fig. 5(a),(b)

V. Determinations of parameters and symmetry properties

In this section, we determined the parameters of our model, using the empirical data by Pearson [2]. In table I, we show the set of the empirical values of K and K_c in table 3 of ref. [2]. According to the conclusion of ref. [2], i.e., $K = 120 \sim 351\text{MeV}$, we only show the sets with $K = 150 \sim 350\text{MeV}$. In fig. 6, we show the $y - M_0^*$ relations which account for the sets. We could not find the parameters for sets with $K = 150\text{MeV}$ and for the set with $K = 200\text{MeV}$ and $K_c = 2.577, 2.577 + 2.06\text{MeV}$ as in the cases of $y = 0$ [11], because of the reason which is mentioned in the end of the previous section. The M_0^* decreases as y increases in any case of K .

Table I

Fig. 6

The smaller M_0^* and the larger y has the opposite effects to the larger y in the EOS. The smaller M_0^* makes the EOS stiffer, while the smaller y makes the EOS softer. In fig. 7, we show the EOS with several y , which account for the set of $K = 250\text{MeV}$ and $K_c = -0.7065\text{MeV}$. The EOS becomes softer when $y = 0.5$, because the effect of larger y is larger than the effect of smaller M_0^* . The EOS becomes stiffer again when $y = 1.0$, because, as is shown in fig. 6, the M_0^* decreases rapidly enough to overcome the larger y effect. Though we do not show a figure, two effects almost cancel each other in the case of $K = 300\text{MeV}$ and $K_c = -3.990\text{MeV}$, when y is not so large ($y \lesssim 5$).

Fig. 7

Table II

In this vector self-coupling theory, there is one more input to fix the EOS. According to ref. [13], $M_0^* \approx 0.6M$ is favorable to account for the spin-orbit potential and the optical potential. We search for the parameters sets which account for the data sets in table I and $M_0^* = 0.6M$. The results are summarized in table II. It is impossible to find the parameters for the sets of $(K, K_c) = (350, -7.274)\text{MeV}, (350, -7.274 - 2.06)\text{MeV}$, because, as shown in fig. 6, in these cases M_0^* is always smaller than $0.6M$ at any y . (For comparison, in table II we also show the EOS with the parameters set which satisfies $K = 350\text{MeV}$, $K = -7.274\text{MeV}$ and $y = 0$, whose $M_0^*(= 0.597M)$ is very close to $0.6M$. We call this parameters set EOS 6.) Also we could not find the parameter sets for $K \geq 250\text{MeV}$, except EOS 1, in the region $y < 10$. It seem to be difficult to find these parameters even if we make y larger. It is probably because, as is seen in fig. 6, M_0^* hardly decreases in the larger y region. We remark that $C > 0$ except for the cases of the EOS 4 and 6.

If we fix M_0^* , there is still uncertainty of K . To determine K , we calculate the volume-symmetry coefficient K_{vs} in the expansion (1). Because the ρ -meson effects is important in the symmetry properties [18][19], we add the following standard ρ -meson-term to the lagrangian (2)[18][19][17].

$$L_\rho = -\frac{1}{4}\mathbf{B}_{\mu\nu}\cdot\mathbf{B}^{\mu\nu} + \frac{1}{2}m_\rho^2\mathbf{b}_\mu\cdot\mathbf{b}^\mu - g_\rho\bar{\psi}\gamma_\mu\frac{\boldsymbol{\tau}}{2}\cdot\mathbf{b}^\mu\psi; \quad \mathbf{B}_{\mu\nu} = \partial_\mu\mathbf{b}_\nu - \partial_\nu\mathbf{b}_\mu - g_\rho\mathbf{b}_\mu\times\mathbf{b}_\nu, \quad (32)$$

where \mathbf{b} is the ρ meson field. Using the new lagrangian and the mean field approximation, we can calculate K_{vs} with aid of the scaling model [1]

$$K_{vs} = K_{sym} - L\left(9\frac{K'}{K} + 6\right), \quad (33)$$

where

$$L = 3\rho_0\frac{da_4}{d\rho}\Big|_{\rho=\rho_0}; \quad a_4 = \frac{1}{2}\rho\frac{\partial^2\epsilon}{\partial\rho^2}\Big|_{\rho_3=0}; \quad \rho_3 = \rho_p - \rho_n \quad (34)$$

and

$$K_{sym} = 9\rho_0^2\frac{d^2a_4}{d\rho^2}\Big|_{\rho=\rho_0}. \quad (35)$$

The results are also summarized in table II. In these calculations, we determine the ρ meson coupling g_ρ so as to realize $a_4 = 30.0\text{MeV}$ at $\rho = \rho_0$. However, the results do not depend much on the choice of g_ρ , because K_{vs} is more sensitive to the ratio K'/K

than to g_ρ . In fact, if we put $C_\rho^2 = (g_\rho M/m_\rho)^2 = 50 \sim 100$ in the EOS 3, we get $K_{vs} \approx -258 \sim -340\text{MeV}$. The difference is not larger than the length of empirical error bar (202MeV) in ref. [2]. In fig. 8, we compare these results with the empirical data in refs. [2] and [3]. From the figure, it is seen that EOS 1 and 3 are favorable to account for the empirical values of K_{vs} , though the EOS 5 could not be excluded. The EOS 3 ($K = 300\text{MeV}$) is most favorable as in the case of $y = 0$ [11], because it corresponds to the mean value of the empirical K_c .

In fig. 9, we show the k_F -dependence of nuclear binding energy using the EOS 1,3 and 5. The result of the EOS 3 is much closer to the EOS of the DBHF calculations [14] than the EOS of the mean field theories with the NL1 parameters [20] and with the NL-SH parameters [21], which do not have the vector self-coupling. This is consistent with the observations by Gmuca [16] and by Sugahara and Toki[17].

Fig. 8

Fig. 9

VI. SUMMARY

We studied the relations among the effective nucleon mass M_0^* , incompressibility K , the third-order derivative K' of nuclear saturation curve, using the mean field theory with the vector self-coupling. The results are summarized as follows.

- (1) When we fix M_0^* and $K(\gtrsim 200\text{MeV})$, the vector self-coupling makes K' smaller, i.e., makes the EOS softer at higher densities.
- (2) Using the vector self-coupling, we can account for the empirical relation between $K(\gtrsim 250\text{MeV})$ and K_c with the smaller M_0^* .
- (3) We could not find the parameters for the empirical sets $(K, K_c) = (150, 5.861 \pm 2.06)\text{MeV}, (200, 2.577)\text{MeV}$ and $(200, 2.577 + 2.06)\text{MeV}$, when $y < 10$. It is due to the fact that the vector self-coupling does not make K' much smaller when $K \lesssim 200\text{MeV}$.
- (4) It seems that $(K, K_c) = (300, -3.990)\text{MeV}$ is favorable to account for the symmetry properties besides the empirical K - K_c relations.
- (5) The EOS which is given by parameter set in (4) has very close to the RBHF's EOS at the higher densities.

In this paper, we restrict our discussions to the M_0^* , K , K' , K_c and K_{σ} , because they can be calculated in the framework of the nuclear matter and do not depend parameter m_σ . Von-Eiff et al. studied the surface properties [6][7][8] in the framework of the mean field approximation of the nonlinear σ - ω - ρ model with no vector self-coupling (i.e, in the case of $y = 0$). They found that low incompressibility ($K_{nm} \approx 200\text{MeV}$) and a large effective nucleon mass ($0.70 \leq M^*/M \leq 0.75$) are favorable for the nuclear surface properties [8]. It is interesting to study these problem using the vector self-coupling model.

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	Set 1	Set 2	Set 3	Set 4	Set 5
K	150	200	250	300	350
K_c	5.861 ± 2.06	2.577 ± 2.06	-0.7065 ± 2.06	-3.990 ± 2.06	-7.274 ± 2.06

Table I

EOS	1	2	3	4	5	6
K	250	300	300	300	350	350
K_c	$-0.7065-2.06$	$-3.990+2.06$	-3.990	$-3.990-2.06$	$-7.274+2.06$	-7.274
K'	-118.2	-179.6	-86.68	6.237	-36.72	71.69
M_0^*/M	0.600	0.600	0.600	0.600	0.600	0.597
K_{vs}	-165.2	-75.23	-299.7	-524.0	-437.5	-667.0
L	82.96	81.82	87.29	93.03	90.48	95.42
K_{sym}	-20.51	-25.18	-2.977	51.61	19.94	81.40
y	1.974	2.459	0.7096	0.2493	0.3849	0.000
C_s^2	516.45	477.19	387.91	352.63	350.30	338.39
C_v^2	464.44	519.65	303.52	246.76	261.41	235.83
B	-1.378×10^{-3}	-3.697×10^{-3}	-5.820×10^{-4}	1.207×10^{-3}	-5.019×10^{-5}	1.260×10^{-3}
C	1.177×10^{-2}	1.657×10^{-2}	5.767×10^{-3}	-3.167×10^{-4}	2.708×10^{-3}	-1.372×10^{-3}

Table II

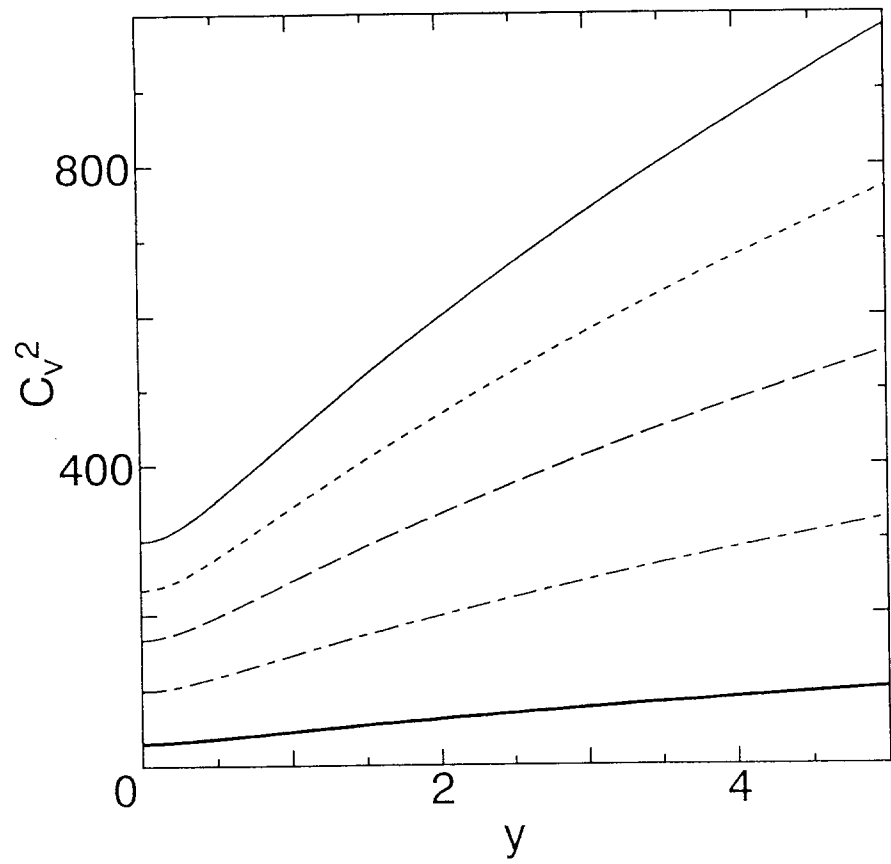


fig.1

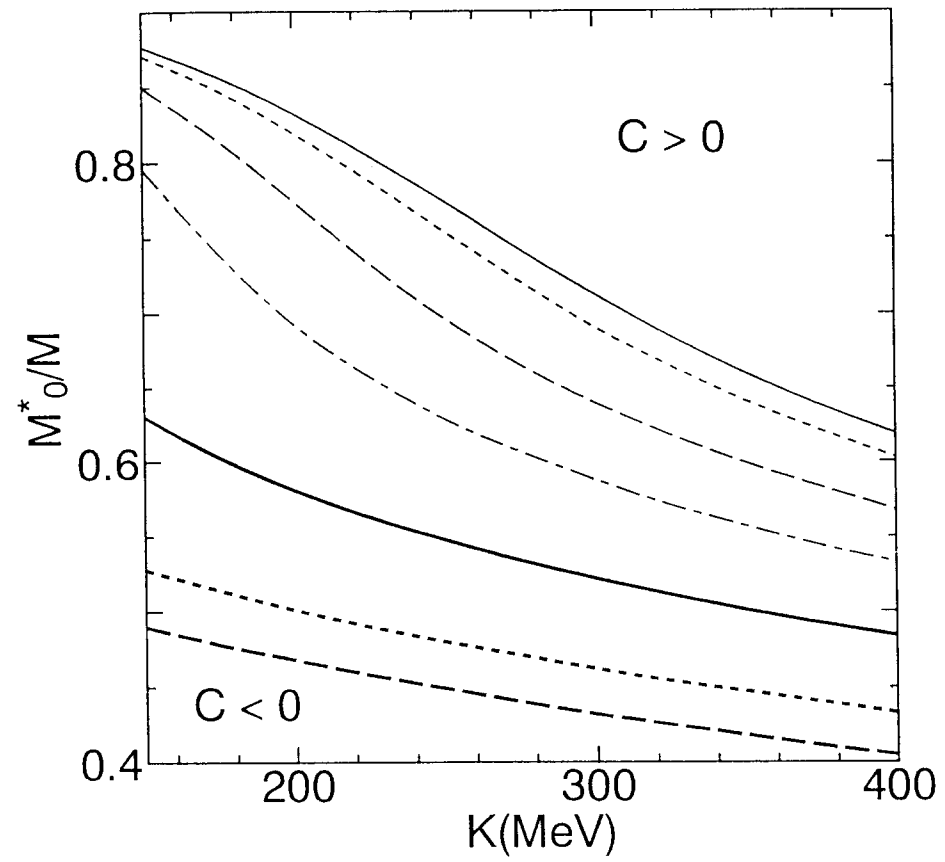


fig.2

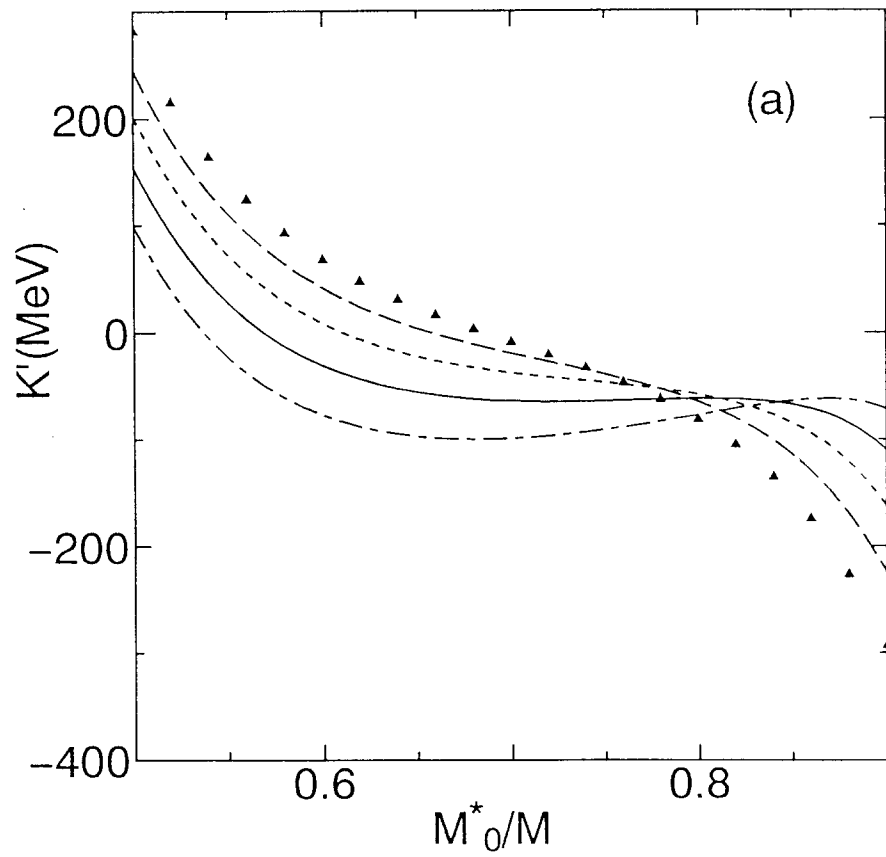


fig.3(a)

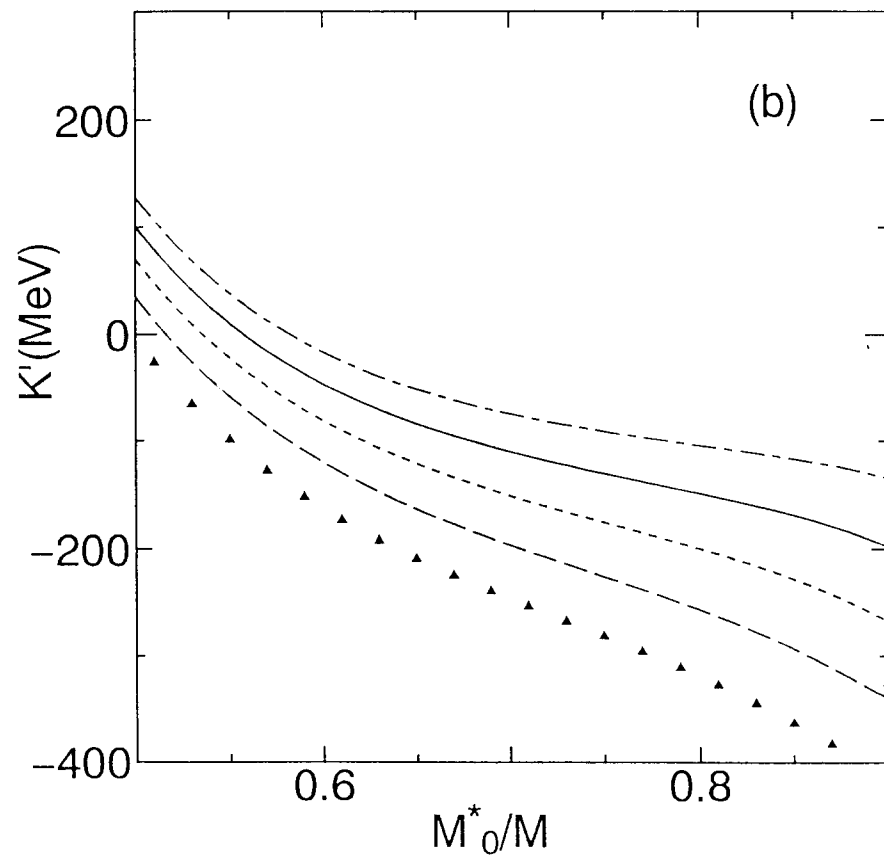


fig.3(b)

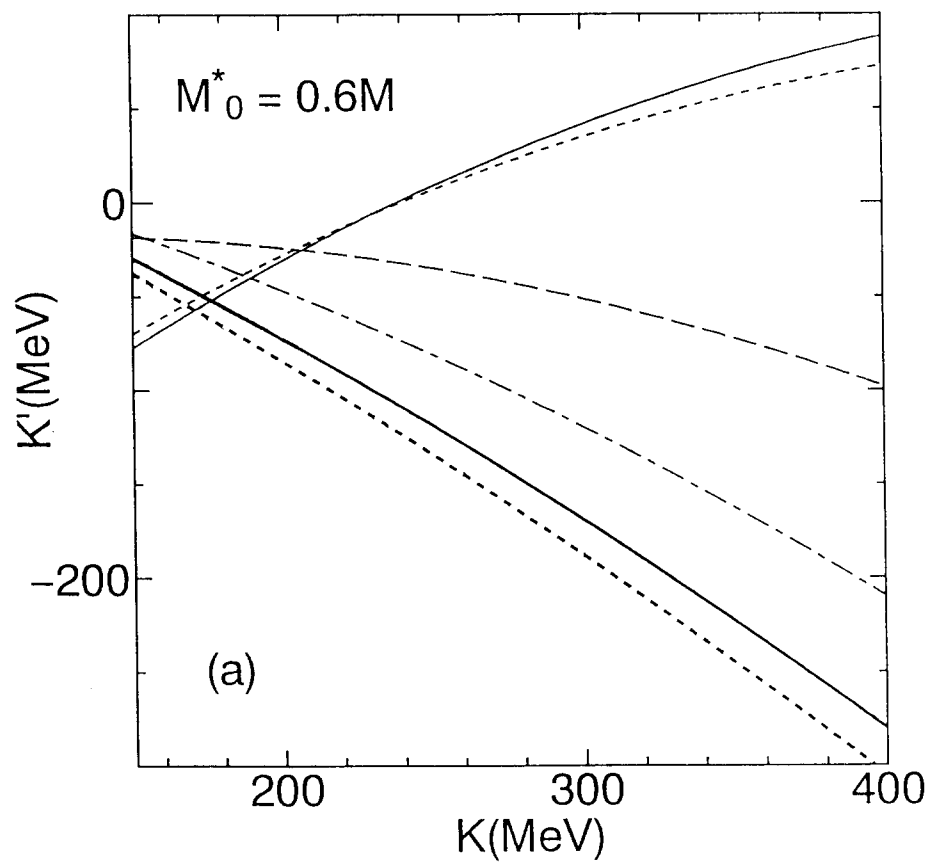


fig.4(a)

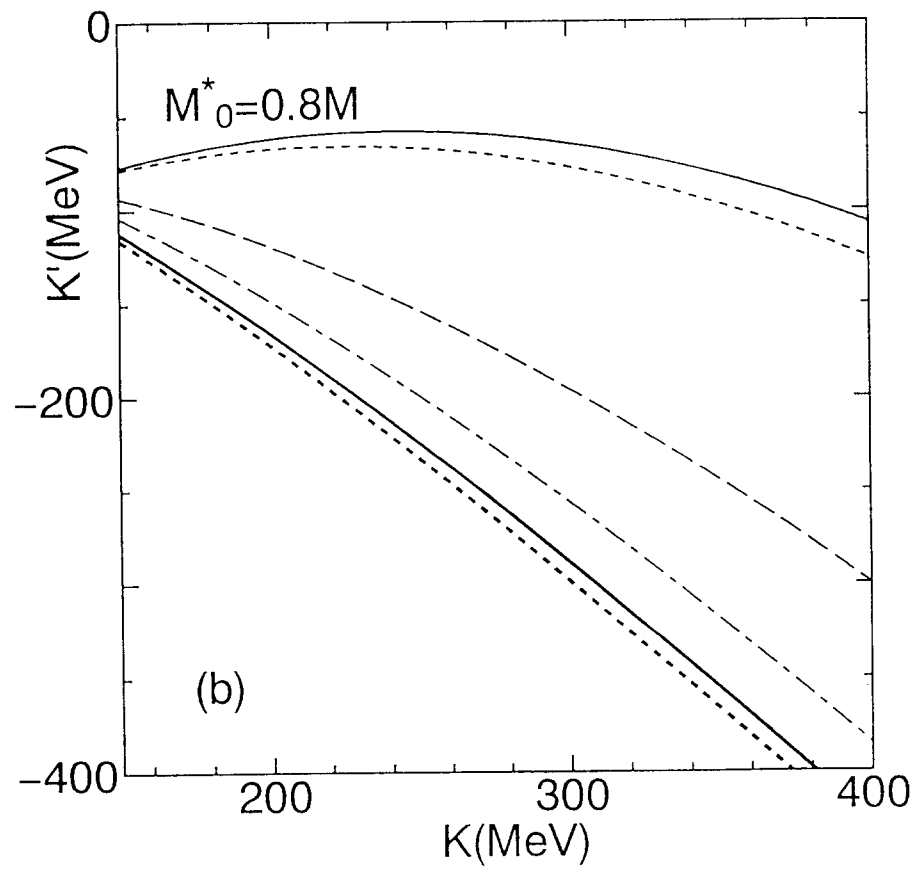


fig.4(b)

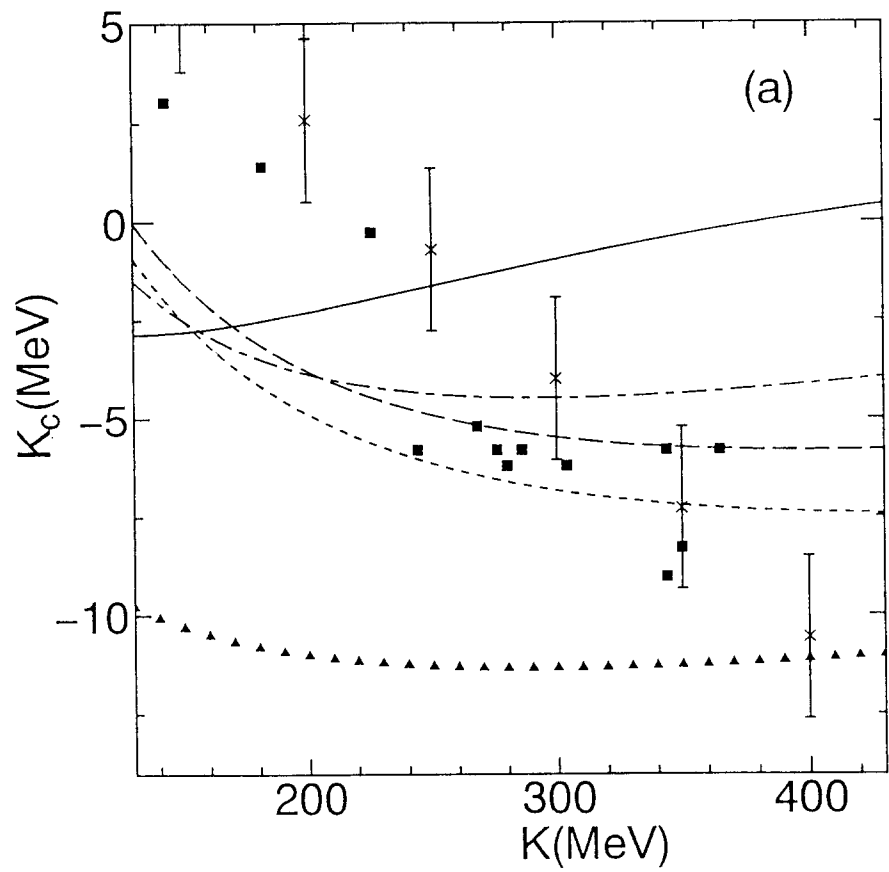


fig.5(a)

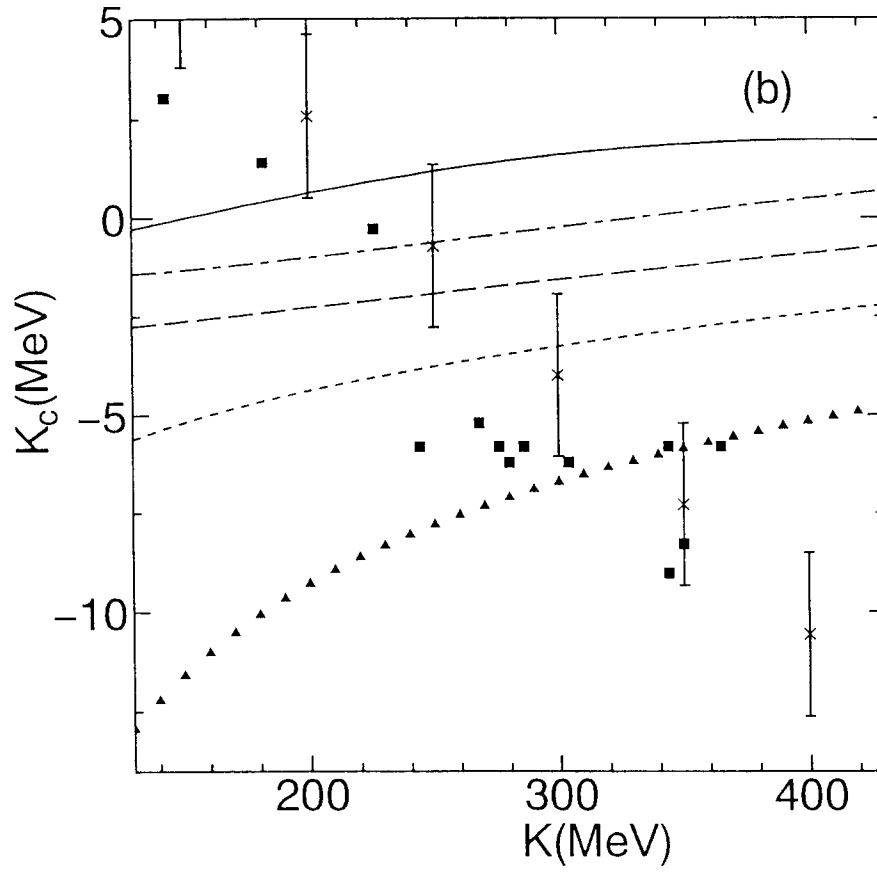


fig.5(b)

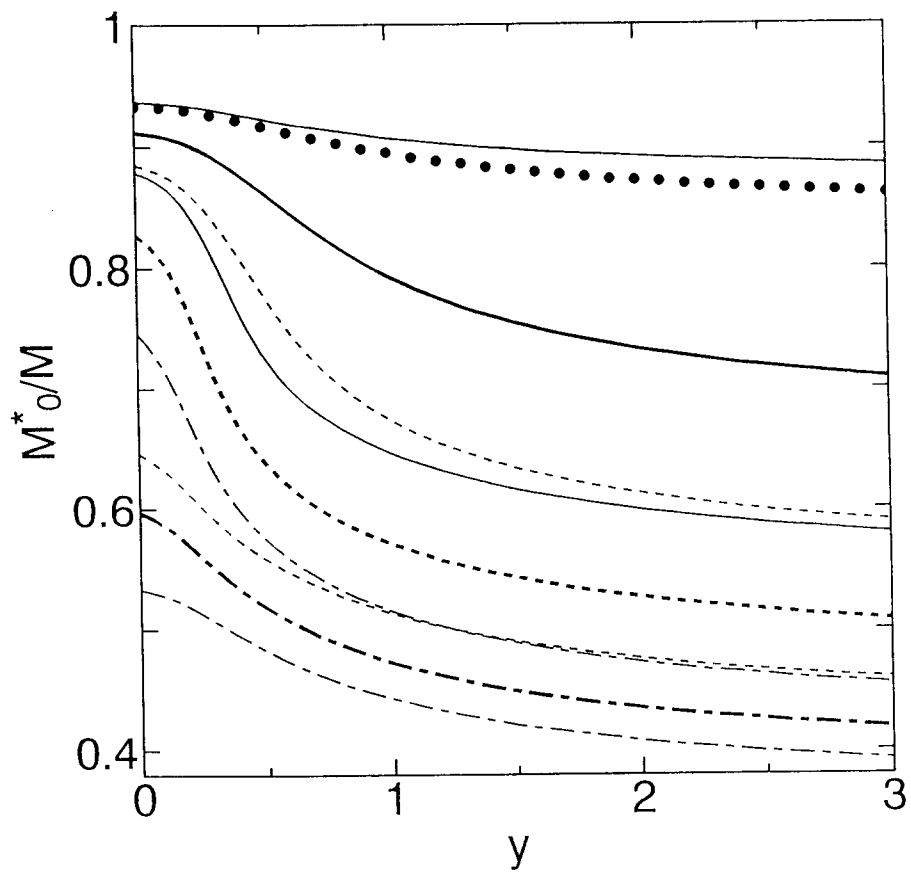


fig.6

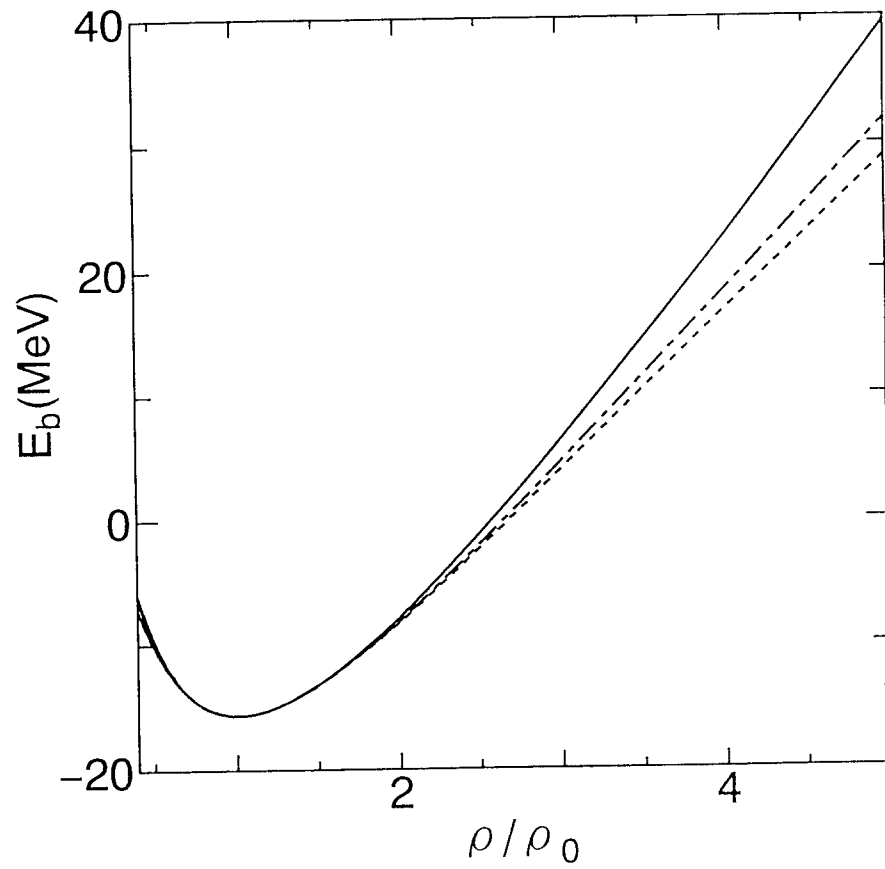


fig.7

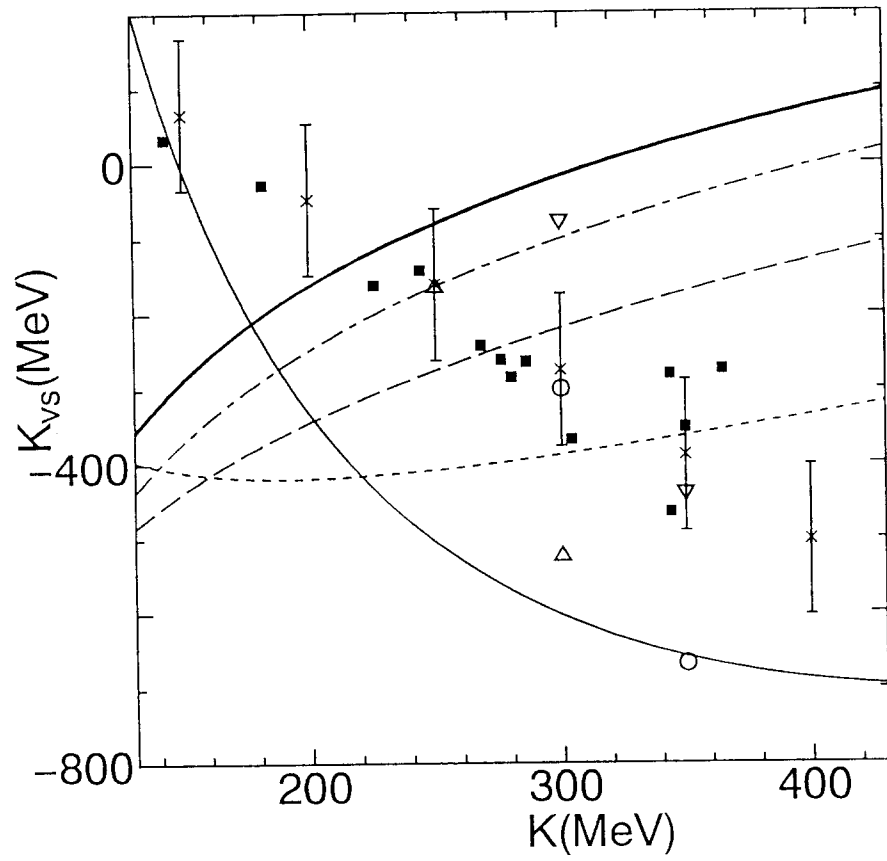


fig.8

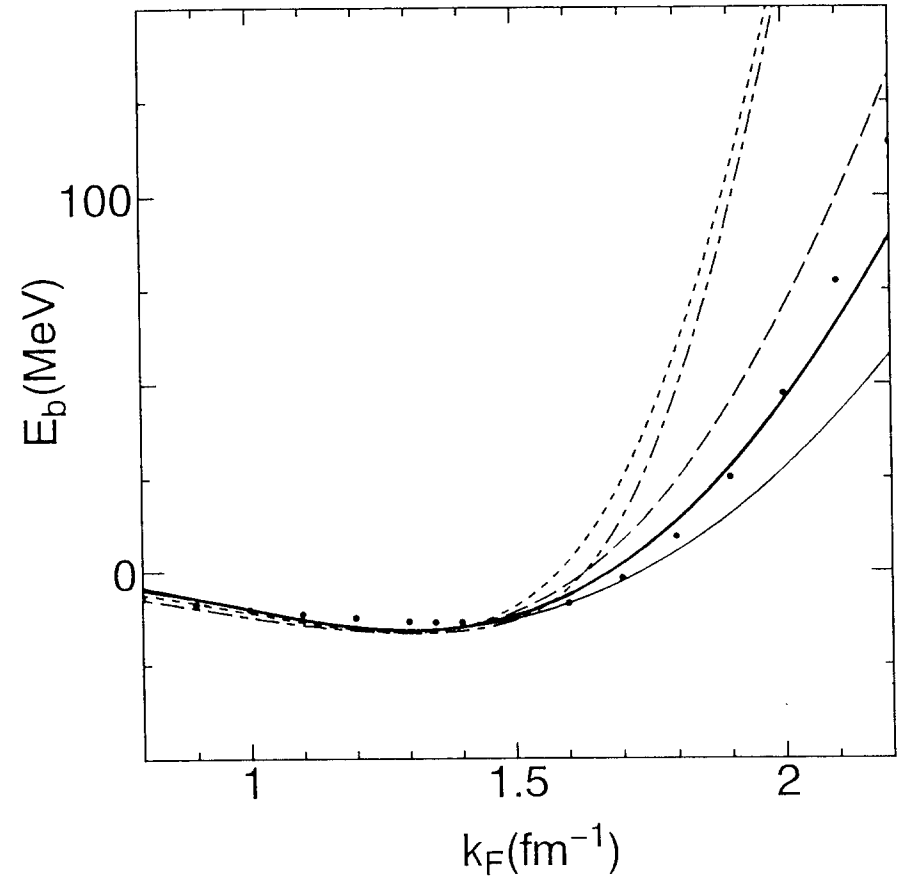


fig.9

Fig. 4 The $K-K'$ relation. (a) The $M_0^* = 0.6M$ case. (b) The $M_0^* = 0.8M$ case: The solid line, the dotted line, the dashed line, the dashed-dotted line, bold solid line and

the bold dashed lines are the DDHF results from the ref. [14].

Table and Figure Captions

Table I

The empirical K - K_c relation in the table of the ref. [2]. (Shown in MeV.)

Table II

Parameter sets fitted for the empirical value of K and K_c in the table I. The K , K_c , K' , K_{vs} , L and K_{sym} are shown in MeV. Except in EOS 6, $C_\rho^2 = g_\rho M/m_\rho = 75.17$. In EOS 6, $C_\rho^2 = 74.69$.

Fig. 1 The y - C_ρ^2 relations with several values of M_0^* : The solid line, the dotted line, the dashed line, the dashed-dotted line and the bold solid line are results with $M_0^*/M = 0.5, 0.6, 0.7, 0.8$ and 0.9 respectively.

Fig. 2 The region for $C > 0$ in the $K - M_0^*$ plane: The solid line, the dotted line, the dashed line, the dashed-dotted line, the bold solid line, the bold dotted line and the bold dashed line are results with $y = 0, 0.1, 0.2, 0.3, 0.5, 1.0$ and 2.0 respectively. In all cases, $C > 0$ above the line and $C < 0$ below the line.

Fig. 3 The $M_0^* - K'$ relation. (a)The $y = 0$ case. (b)The $y = 1.0$ case: The dashed-dotted line, the solid line, the dotted line, the dashed line and the solid triangles are the results with $K = 150, 200, 250, 300$ and 350 MeV respectively.

Fig. 4 The $K - K'$ relation. (a)The $M_0^* = 0.6M$ case. (b)The $M_0^* = 0.8M$ case: The solid line, the dotted line, the dashed line, the dashed-dotted line, bold solid line and bold dotted line are the results with $y = 0, 0.1, 0.5, 1.0, 2.0$ and 3.0 respectively.

Fig. 5 The $K - K_c$ relation. (a)The $y = 0$ case. (b)The $y = 1.0$ case: The solid triangles, the dotted line, the dashed line, the dashed-dotted line and the solid line are the results with $M_0^*/M = 0.5, 0.6, 0.7, 0.8$ and 0.9 respectively. The crosses with error bars are the data from the table 3 in ref. [2]. The solid small squares are the data from the table IV in ref. [3]. (For simplicity of the figure, we omit the error bars in the latter data.)

Fig. 6 The $y - M_0^*$ relation for the empirical $K - K_c$ relation: The solid small circles are the results for $K = 200$ MeV and $K_c = 2.577 - 2.06$ MeV. The solid lines, the dotted lines and the dashed-dotted lines are the results for $K = 250, 300, 350$ respectively. In each case, the upper line is the result with the upper bound for K_c , the lower line is the result with the lower bound for K_c and the bold line is the result with the average value of K_c .

Fig. 7 The $\rho - E_b$ relations: The solid line, dotted line and dashed-dotted line are the results with the parameters with $y = 0, 0.5$ and 1.0 respectively, when $K = 250$ MeV and $K_c = -0.7065$ MeV are satisfied.

Fig. 8 The $K - K_{vs}$ relation: The open triangles with $K = 250$ and 300 MeV are the results of EOS 1 and 4 respectively. The open inverse-triangles with $K = 300$ and 350 MeV are the results of EOS 2 and 5 respectively. The open circles with $K = 300$ and 350 MeV are the results of EOS 3 and 6 respectively. The solid line, the dotted line, the dashed line, the dashed-dotted line and the bold solid line are the results with $y = 0, 0.5, 1.0, 2.0$ and 5.0 respectively, when $M_0^* = 0.6M$. The crosses with error bars are the data from the table 3 in ref. [2]. The solid small squares are the data from the table IV in ref. [3]. (For simplicity of the figure, we omit the error bars in the latter data.)

Fig. 9 The $k_F - E_b$ relations for several EOS: The solid line, the bold solid line, the dashed line, the dashed-dotted line and dotted line are the results of EOS 1, EOS 3, EOS 5, the EOS with the NL parameters [20] and the EOS with NL-SH parameters [21], respectively. The small solid circles are the DBHF results from the ref. [14].

