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First measurement of the CP-violating phase $\sin\,B^0_s\!\rightarrow J\!/\psi(\rightarrow\!e^+e^-)\phi\,\,\rm{decays}$

LHC_b collaboration[†]

Abstract

A flavour-tagged time-dependent angular analysis of $B_s^0 \to J/\psi \phi$ decays is presented where the J/ψ meson is reconstructed through its decay to an e^+e^- pair. The analysis uses a sample of pp collision data recorded with the LHCb experiment at centre-of-mass energies of 7 and 8 TeV, corresponding to an integrated luminosity of 3 fb^{-1} . The CP-violating phase and lifetime parameters of the B_s^0 system are measured to be $\phi_s = 0.00 \pm 0.28 \pm 0.05 \text{ rad}, \Delta\Gamma_s = 0.115 \pm 0.045 \pm 0.011 \text{ ps}^{-1}$ and $\Gamma_s = 0.608 \pm 0.018 \pm 0.011 \text{ ps}^{-1}$ where the first uncertainty is statistical and the second systematic. This is the first time that CP-violating parameters are measured in the $B_s^0 \rightarrow J/\psi \phi$ decay with an e^+e^- pair in the final state. The results are consistent with previous measurements in other channels and with the Standard Model predictions.

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¹ 1 Introduction

The phase difference ϕ_s between direct decays and decays through mixing of B_s^0 mesons to 2 ³ Charge-Parity (CP) eigenstates is a CP-violating observable. In the Standard Model (SM), 4 considering $b \rightarrow (c\bar{c})s$ transitions and neglecting subleading penguin contributions, this ⁵ phase is predicted to be $-2\beta_s$, where $\beta_s = \arg[-(V_{ts}V_{tb}^*)/(V_{cs}V_{cb}^*)]$ and V_{ij} are the elements ⁶ of the CKM quark-flavour mixing matrix [\[1\]](#page-16-0).

⁷ The precise measurement of the ϕ_s phase is potentially sensitive to new physics ⁸ (NP) processes. The measured phase could be modified if new particles were to contribute to the B_s^0 - \overline{B}_s^0 mixing amplitudes [\[2\]](#page-17-0). Measurements of ϕ_s using differ- $\overline{9}$ to ent decay channels with muons in the final state, namely $B_s^0 \rightarrow J/\psi K^+ K^-$ [\[3,](#page-17-1) [4\]](#page-17-2), $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$ [\[5\]](#page-18-0), $B_s^0 \rightarrow \psi(2S)\phi$ [\[6\]](#page-18-1), and a channel with open charm mesons, ¹² $B_s^0 \rightarrow D_s^+ D_s^-$ [\[7\]](#page-18-2), have been reported previously by the LHCb collaboration. Mea-¹³ surements of ϕ_s in $B_s^0 \to J/\psi \phi$ decays with $J/\psi \to \mu^+ \mu^-$ have also been performed by ¹⁴ the ATLAS [\[8,](#page-18-3) [9\]](#page-18-4), CMS [\[10\]](#page-18-5), CDF [\[11\]](#page-18-6) and D0 [\[12\]](#page-18-7) collaborations. The world-average ¹⁵ value of these measurements is $\phi_s = -0.051 \pm 0.023$ rad [\[13\]](#page-18-8). A precise prediction of ¹⁶ the ϕ_s phase value is available from global fits of the CKM matrix within the SM. The ¹⁷ CKMFitter group result is $\phi_s = -0.0365^{+0.0013}_{-0.0012}$ rad [\[14\]](#page-19-0) while the UTfit collaboration 18 result is $\phi_s = -0.0370 \pm 0.0010$ rad [\[15\]](#page-19-1).

19 This paper presents a measurement of ϕ_s using a flavour-tagged time-dependent angular analysis of the $B_s^0 \to J/\psi \phi$ mode with $J/\psi \to e^+e^-$ and $\phi \to K^+K^-$ decays.¹ This is the ²¹ first time that the $B_s^0 \to J/\psi (e^+e^-)\phi$ decay is used to measure CP-violating observables, 22 and in particular the phase ϕ_s . The analysis is based on a data set corresponding to an integrated luminosity of 3 fb^{-1} collected at the LHC in proton-proton (pp) collisions ²⁴ at centre-of-mass energies of 7 and 8 TeV by the LHCb experiment. The yield of the ²⁵ $B_s^0 \to J/\psi (e^+e^-)\phi (K^+K^-)$ sample amounts to about 10% of that of the previously analysed ²⁶ $B_s^0 \to J/\psi(\mu^+\mu^-)\phi(K^+K^-)$ mode using the same data set [\[16\]](#page-19-2). The analysis follows closely ²⁷ that of the two muons decay mode, reported in Refs. [\[3,](#page-17-1)[5\]](#page-18-0). Relevant changes are described ²⁸ in more detail in this paper.

 A comparison of the two results is of interest given the different main sources of systematic uncertainties induced by the markedly different reconstruction of decays with muons in the final state compared to decays with electrons. These differences arise ³² from the significant bremsstrahlung emission of the electrons and the different signatures exploited in the online trigger selection [\[17–](#page-19-3)[19\]](#page-19-4).

³⁴ The article is structured in the following way. The phenomenological description of ³⁵ the $B_s^0 \to J/\psi (e^+e^-)\phi (K^+K^-)$ decay and the relevant physics observables are described in Sec. [2.](#page-3-0) A brief description of the LHCb detector, the candidates selection and the background subtraction are outlined in Sec. [3.](#page-4-0) The relevant inputs to the analysis, namely the resolution, efficiency and the flavour tagging, are detailed in Sec. [4](#page-7-0) and [5.](#page-9-0) The maximum-likelihood fit procedure used to determine the physics parameters and the results of the fit are described in Sec. [6,](#page-10-0) while the evaluation of the systematic uncertainties is discussed in Sec. [7.](#page-11-0) Finally, conclusions are presented in Sec. [8.](#page-15-0)

¹The inclusion of charge-conjugate processes is implied throughout this paper, unless otherwise noted. For simplicity, the resonance $\phi(1020)$ is referred to as ϕ here and in the following.

Figure 1: Definition of the angles in the helicity basis. The polar angle θ_K (θ_e) is the angle between the K^+ (e^+) momentum and the direction opposite to the B^0_s momentum in the $K^+K^ (e^+e^-)$ centre-of-mass system, and the ϕ_h is the azimuthal angle between the K^+K^- and $e^+e^$ decay planes.

⁴² 2 Phenomenology

⁴³ The phenomenological aspects of the analysis are presented in Ref. [\[20\]](#page-19-5). This formalism as also holds for the $B_s^0 \to J/\psi (e^+e^-) \phi (K^+K^-)$ decay. Angular momentum conservation in ⁴⁵ the $B_s^0 \to J/\psi \phi$ decay implies that the final state is an admixture of two CP-even and ⁴⁶ one CP-odd components, with orbital angular momentum of 0 or 2, and 1, respectively. 47 Moreover, along with the three P-wave states of the $\phi \to K^+K^-$ transition, there is also a 48 CP -odd K^+K^- component in an S-wave state [\[21\]](#page-19-6). The CP-even and CP-odd components ⁴⁹ are disentangled by a time-dependent angular analysis, where the angular observables 50 $\Omega = {\cos \theta_e, \cos \theta_K, \phi_h}$ are defined in the helicity basis as shown in Fig. [1.](#page-3-1) The polar α_1 angle θ_K (θ_e) is the angle between the K⁺ (e⁺) momentum and the direction opposite ⁵² to the B_s^0 momentum in the K^+K^- (e^+e^-) centre-of-mass system. The azimuthal angle μ ₅₃ between the K^+K^- and e^+e^- decay planes is ϕ_h . A definition of the angles in terms of ⁵⁴ the particles momenta can be found in Ref. [\[20\]](#page-19-5).

⁵⁵ The differential decay rate for $B_s^0 \to J/\psi \phi$ decay as a function of the decay time and angles can be expressed as a sum of polarisation amplitudes and their interference terms. Each of these can be factorised into a part dependent on the decay time t and a part dependent on the set of angular variables Ω, as

$$
G(t,\Omega) \equiv \frac{\mathrm{d}^4 \Gamma(B_s^0 \to J/\psi \phi)}{\mathrm{d}t \,\mathrm{d}\Omega} \propto \sum_{k=1}^{10} h_k(t) f_k(\Omega). \tag{1}
$$

59 The time-dependent functions $h_k(t)$ are given as

$$
h_k(t|B_s^0) = N_k e^{-\Gamma_s t} \left[a_k \cosh \frac{\Delta \Gamma_s t}{2} + b_k \sinh \frac{\Delta \Gamma_s t}{2} + c_k \cos(\Delta m_s t) + d_k \sin(\Delta m_s t) \right], \tag{2}
$$

60

$$
h_k(t|\overline{B}_s^0) = \bar{N}_k e^{-\Gamma_s t} \left[a_k \cosh \frac{\Delta \Gamma_s t}{2} + b_k \sinh \frac{\Delta \Gamma_s t}{2} - c_k \cos(\Delta m_s t) - d_k \sin(\Delta m_s t) \right], \tag{3}
$$

61 where $\Delta\Gamma_s \equiv \Gamma_L - \Gamma_H$ is the decay width difference between the light and the heavy 62 B_s mass eigenstates, $\Delta m_s \equiv m_H - m_L$ is their mass difference, and $\Gamma_s \equiv (\Gamma_L + \Gamma_H)/2$ ⁶³ is their average width. The coefficients N_k (\bar{N}_k) and a_k, b_k, c_k, d_k can be expressed in ⁶⁴ terms of ϕ_s and four complex transversity amplitudes A_i (\bar{A}_i) at $t = 0$, as detailed in 65 Table [1.](#page-4-1) The label i takes the values $\{\perp, \parallel, 0\}$ for the three P-wave amplitudes and 66 S for the S-wave amplitude. The amplitudes are parameterised by $|A_i|e^{i\delta_i}$ with the

\boldsymbol{k}	$f_k(\theta_K,\theta_e,\phi_h)$	N_k	N_k	a_k	b_k	c_k	d_k
	$2\cos^2\theta_K\sin^2\theta_e$	$ A_0 ^2$	$ \bar{A}_0 ^2$		D	\mathcal{C}	$-S$
	$\sin^2\theta_K(1-\sin^2\theta_e\cos^2\phi_h)$	$ A_{\parallel} ^2$	$ \bar{A}_{\parallel} ^2$		D		$-S$
3	$\sin^2\theta_K(1-\sin^2\theta_e\sin^2\phi_h)$	$ A_\perp ^2$	$A_{\perp} ^2$		$-D$		S
	$\sin^2\theta_K \sin^2\theta_e \sin 2\phi_h$	$ A_\parallel A_\perp $	$A_{\parallel}A_{\perp}$	$C \sin(\delta_{\perp} - \delta_{\parallel})$	$S\cos(\delta_{\perp}-\delta_{\parallel})$	$\sin(\delta_{\perp}-\delta_{\parallel})$	$D\cos(\delta_{\perp}-\delta_{\parallel})$
5	$\frac{1}{2}\sqrt{2}\sin 2\theta_K\sin 2\theta_e\cos \phi_h$	$ A_0A_{\parallel} $	$ A_0A_{\parallel} $	$\cos(\delta_{\parallel}-\delta_0)$	$D\cos(\delta_{\parallel}-\delta_0)$	$C\cos(\delta_{\parallel}-\delta_0)$	$-S\cos(\delta_{\parallel}-\delta_0)$
6	$-\frac{1}{2}\sqrt{2}\sin 2\theta_K\sin 2\theta_e\sin \phi_h$	$ A_0A_\perp $	$ A_0A_+ $	$C \sin(\delta_{\perp} - \delta_0)$	$S\cos(\delta_{\perp}-\delta_0)$	$\sin(\delta_{\perp}-\delta_0)$	$D\cos(\delta_{\perp}-\delta_0)$
	$rac{2}{3}$ sin ² θ_e	$ A_{\rm S} ^2$	$ A_{\rm S} ^2$		$-D$	$\,C$	
8	$\frac{1}{3}\sqrt{6}\sin\theta_K\sin 2\theta_e\cos\phi_h$	$ A_{\rm S}A_{\rm II} $	$ A_{\rm S}A_{\rm } $	$C\cos(\delta_{\parallel}-\delta_{\rm S})$	$S\sin(\delta_{\parallel}-\delta_{\rm S})$	$\cos(\delta_{\parallel}-\delta_{\rm S})$	$D\sin(\delta_{\parallel}-\delta_{\rm S})$
9	$-\frac{1}{3}\sqrt{6}\sin\theta_K\sin 2\theta_e\sin\phi_h$	$ A_{\rm S} A_{\perp} $	$ A_{\rm S}A_{\perp} $	$\sin(\delta_{\perp}-\delta_{\rm S})$	$-D\sin(\delta_{\perp}-\delta_{\rm S})$	$C \sin(\delta_{\perp} - \delta_{\rm S})$	$S\sin(\delta_{\perp}-\delta_{\rm S})$
10	$\frac{4}{3}\sqrt{3}\cos\theta_K\sin^2\theta_e$	$ A_{\rm S}A_0 $	$ A_{\rm S}A_0 $	$C\cos(\delta_0-\delta_{\rm S})$	$S\sin(\delta_0-\delta_{\rm S})$	$\cos(\delta_0-\delta_{\rm S})$	$D\sin(\delta_0-\delta_{\rm S})$

Table 1: Definition of angular and time-dependent functions for B_s^0 and \overline{B}_s^0 mesons.

⁶⁷ conventions $\delta_0 = 0$ and $|A_{\perp}|^2 + |A_0|^2 + |A_{\parallel}|^2 = 1$. The S-wave fraction is defined as 68 $F_{\rm S} = |A_{\rm S}|^2 / (|A_{\rm S}|^2 + |A_{\perp}|^2 + |A_0|^2 + |A_{\parallel}|^2)$. In contrast to Ref. [\[3\]](#page-17-1), the S-wave parameters 69 are measured in a single range of $m(K^+K^-)$ within ± 30 MeV/ c^2 of the known ϕ mass [\[13\]](#page-18-8). ⁷⁰ For a particles produced in a B_s^0 and \bar{B}_s^0 flavour eigenstates, the coefficients in Eqs. [\(2\)](#page-3-2) 71 and [\(3\)](#page-3-3), respectively are given in Table [1](#page-4-1) together with the angular functions $f_k(\Omega)$, where τ_2 the S, D, C coefficients are defined as

$$
S = -\frac{2|\lambda|}{1 + |\lambda|^2} \sin(\phi_s), \quad D = -\frac{2|\lambda|}{1 + |\lambda|^2} \cos(\phi_s) \quad \text{and} \quad C = \frac{1 - |\lambda|^2}{1 + |\lambda|^2}.
$$
 (4)

 73 The parameter λ is related to CP violation in the interference between mixing and decay. ⁷⁴ and is defined by $\lambda = \eta_i(q/p)(\bar{A}_i/A_i)$ where the polarisation states i have the CP eigenvalue τ_5 $\eta_i = +1$ for $i \in \{0, \parallel\}$ and $\eta_i = -1$ for $i \in \{\perp, S\}$. The complex parameters p and q relate ⁷⁶ the mass eigenstates to the flavour eigenstates, $|B_{L,H}\rangle = p|B_s^0\rangle \pm q|\overline{B}_s^0\rangle$. The CP-violating τ_7 phase is defined by $\phi_s \equiv -\arg(\lambda)$ and is assumed here to be the same for all polarisation ⁷⁸ states. The value of $|\lambda|$ equals unity in the absence of CP violation in decay [\[22](#page-19-7)[–24\]](#page-19-8). In ⁷⁹ this paper, the CP violation in B_s meson mixing is assumed to be negligible, following $\frac{1}{80}$ the measurements in Refs. [\[25,](#page-19-9) [26\]](#page-19-10).

81 3 Detector, data set and selection

⁸² The LHCb detector [\[27\]](#page-19-11) is a single-arm forward spectrometer covering the pseudorapidity 83 range $2 < \eta < 5$, designed for the study of particles containing b or c quarks. The detector ⁸⁴ includes a high-precision tracking system consisting of a silicon-strip vertex detector ⁸⁵ surrounding the pp interaction region, a large area silicon-strip detector located upstream ⁸⁶ of a dipole magnet with a bending power of about 4 Tm, and three stations of silicon-strip ⁸⁷ detectors and straw drift tubes placed downstream of the magnet. The tracking system $\frac{88}{188}$ provides a measurement of momentum, p, of charged particles with a relative uncertainty ⁸⁹ that varies from 0.5% at low momentum to 1.0% at 200 GeV/c. The minimum distance of \bullet a track to a primary pp collision vertex (PV), the impact parameter (IP), is measured 91 with a resolution of $(15 + 29/p_T)$ µm, where p_T is the component of the momentum $\frac{92}{2}$ transverse to the beam in GeV/c. Different types of charged hadrons are distinguished ⁹³ using information from two ring-imaging Cherenkov detectors (RICH). Photons, electrons,

and hadrons are identified by a calorimeter system consisting of scintillating-pad and

preshower detectors, an electromagnetic calorimeter (ECAL), and a hadronic calorimeter.

 Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers.

 Samples of simulated events are used to optimise the signal selection, to derive the ₉₉ angular efficiency and to correct the decay-time efficiency. The simulated pp collisions are generated using Pythia [\[28\]](#page-20-0) with a specific LHCb configuration [\[29\]](#page-20-1). The decays of hadronic particles are described by EvtGen [\[30\]](#page-20-2), in which final-state radiation is generated using Photos [\[31\]](#page-20-3). The interaction of the generated particles with the detector and its response are implemented using Geant4 toolkit [\[32\]](#page-20-4), as described in Ref. [\[33\]](#page-20-5).

 The online candidate selection is performed by a trigger [\[34\]](#page-20-6), which consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, which applies a full decay reconstruction. At the hardware stage, events are required to have a hadron or electron with a high transverse-energy deposit in 108 the calorimeters, $E_T > 3$ GeV and $E_T > 3.68$ GeV, respectively. The subsequent software trigger is implemented as two separate levels that further reduce the event rate. The first level is designed to select decays which are displaced from all PVs. At the second level, ¹¹¹ $B_s^0 \to J/\psi \phi$ candidates are selected by identifying events containing a pair of oppositely ₁₁₂ charged kaons with an invariant mass within ± 30 MeV/ c^2 of the known φ-meson mass [\[13\]](#page-18-8) or by using topological b-hadron triggers. These topological triggers require a two-, three- $_{114}$ or four-track secondary vertex with a large sum of the p_T of the charged particles and significant displacement from all PVs. A multivariate algorithm [\[35\]](#page-20-7) is used for the $_{116}$ identification of secondary vertices consistent with the decay of a b hadron. The trigger signals are associated with reconstructed particles in the offline selection. The candidate selection is devised in order to minimise the impact on the decay-time efficiency.

 Electrons radiate bremsstrahlung photons when travelling through the detector material. For events where the photons are emitted upstream of the spectrometer magnet, the photon and the electron deposit their energy in different ECAL cells, and the electron momentum measured by the tracking system is underestimated. Neutral energy deposits in the ECAL compatible with being emitted by the electron are used to correct for this effect. The limitations of the recovery technique degrade the resolution of the reconstructed ¹²⁵ invariant masses of both the di-electron pair and the B_s^0 candidate [\[17\]](#page-19-3).

 In the offline selection, J/ψ candidates are formed from two oppositely charged tracks identified as electrons, and ϕ candidates from pairs of oppositely charged tracks identified as kaons. The pairs of tracks need to form a good quality vertex. The electron candidates are required to have $p_T > 0.5 \,\text{GeV}/c$ and di-electron invariant mass $m(e^+e^-) \in [2.5, 3.3] \,\text{GeV}/c^2$, where a wider range compared to the dimuon mode analysis is chosen to account for the 131 radiative tail arising due to bremsstrahlung. The p_T of the ϕ candidate is required to be $_{132}$ larger than $1 \text{ GeV}/c$.

133 The J/ψ and ϕ candidates that are consistent with originating from a common vertex ¹³⁴ are combined to form B_s^0 candidates. The mass of the B_s^0 candidates is required to be in the range $m(e^+e^-K^+K^-) \in [4.7, 5.6] \text{ GeV}/c^2$. The reconstructed decay time of the B_s^0 ¹³⁶ candidate, t, is obtained from a kinematic fit with the J/ψ mass constrained to its known ¹³⁷ value [\[13\]](#page-18-8) and the B_s^0 candidate constrained to originate from the associated PV. Each ¹³⁸ B_s⁰ candidate is associated with the PV that yields the smallest χ^2_{IP} , where χ^2_{IP} is defined as the difference in the vertex-fit χ^2 of a given PV reconstructed with and without the ¹⁴⁰ particle under consideration. The B_s^0 candidates are selected if they have decay times in

141 the range $0.3 < t < 14$ ps and decay-time uncertainty estimates $\sigma_t < 0.12$ ps. The fraction ¹⁴² of events containing more than one B_s^0 candidate within the $m(e^+e^-K^+K^-)$ range is ¹⁴³ 2.6%. All candidates are retained in the subsequent analysis. The impact of allowing ¹⁴⁴ multiple candidates per event is negligible.

¹⁴⁵ The main sources of background are partially reconstructed b-hadron decays and ¹⁴⁶ combinatorial background. The first of these arises from the $B_s^0 \to \chi_{c1}(1P)(\to J/\psi\gamma)\phi$ ¹⁴⁷ and $B_s^0 \to \psi(2S) (\to J/\psi \ X) \phi$ decay.² The combinatorial background is due to random ¹⁴⁸ combination of tracks in the event that pass the candidate selection. In addition, possible background contributions to the signal region originate from $\Lambda_b^0 \to J/\psi pK^-$ and $B^0 \to$ ¹⁵⁰ $J/\psi K^*(892)^0$ decays, where the proton or the π^- meson from the $K^*(892) \to K^+\pi^-$ decay ¹⁵¹ is misidentified as a K^+ or K^- meson, respectively.

 The combinatorial background is suppressed using a boosted decision tree (BDT) [\[36\]](#page-20-8) analysis, trained using the TMVA toolkit [\[37\]](#page-20-9). The BDT discriminant is trained using a ¹⁵⁴ signal sample of simulated $B_s^0 \to J/\psi \phi$ decays, and a sample of background from data. For the background same-sign combinations of electron and/or kaon pairs are chosen with the same selection criteria as for signal. The simulation is corrected to match the distributions observed in data for variables used in the identification of electrons and kaons. The eight variables used for the training of the BDT discriminant are the transverse momenta of the ¹⁵⁹ J/ ψ and ϕ candidates, the vertex χ^2 of the B_s^0 candidate, the χ^2 of the kinematic fit of the ¹⁶⁰ B_s^0 candidate with the J/ψ mass constrained to its known value and the electron and kaon identification probability as provided mainly from the RICH and calorimeter systems. The optimal working point for the BDT discriminant is determined using a figure of merit 163 that optimises the statistical power of the selected data sample for the analysis of ϕ_s by taking the number of signal and background candidates into account [\[38\]](#page-20-10).

The candidates are rejected if the K^+ candidate can also be identified as a proton by a ¹⁶⁶ dedicated neural network [\[39\]](#page-20-11) to suppress any possible contamination from $\Lambda_b^0 \to J/\psi p K^-$ ¹⁶⁷ decays. The remaining misidentified background contribution is estimated using simulated ¹⁶⁸ samples and amounts to 1% of the expected signal yield for Λ_b^0 decays and is negligible 169 for B^0 decays.

Figure [2](#page-7-1) shows the distribution of $m(e^+e^-K^+K^-)$ for the selected $B_s^0 \to J/\psi \phi$ can- 171 didates. In order to describe better the left tail of the $m(e^+e^-K^+K^-)$ distribution, the ¹⁷² sample is split into three categories by the number of electron candidates: zero, one ¹⁷³ or both electrons of the pair that received bremsstrahlung corrections. An extended m_1 ¹⁷⁴ maximum-likelihood fit is made to the unbinned $m(e^+e^-K^+K^-)$ distribution.

 In the fit the signal component is described by the sum of two Crystal Ball (CB) functions [\[40\]](#page-20-12) and the combinatorial background by an exponential function. The partially ¹⁷⁷ reconstructed background components from $B_s^0 \to \chi_{c1}(1P)\phi$ and $B_s^0 \to \psi(2S)\phi$ decays are modelled using a Gaussian function and the sum of two Gaussian functions, respec- tively. The parameters that describe the shape of the signal candidates and the partially reconstructed background are fixed to values obtained from simulation. The core widths and the common mean of the CB functions are left free in the fit. The fit to the three ¹⁸² categories gives a yield of $(1.27 \pm 0.05) \times 10^4$ signal candidates where the uncertainty is statistical only.

 184 The fit results are used to assign per-candidate weights via the *sPlot* technique with $m(e^+e^-K^+K^-)$ as the discriminating variable [\[41\]](#page-20-13). This is used to subtract the background

²The symbol X stands for unreconstructed particles.

Figure 2: Distribution of $m(e^+e^-K^+K^-)$ for selected $B^0_s \to J/\psi \phi$ candidates divided into three categories: (a) zero, (b) one and (c) both electrons with bremsstrahlung correction. The blue solid line shows the total fit which is composed of (red short-dashed line) the signal and the background contributions. The combinatorial background is indicated by the green long-dashed line while the partially reconstructed background from the $B_s^0 \to \psi(2S)\phi$ and $B_s^0 \to \chi_{c1}(1P)\phi$ decays are indicated by pink and purple dash-dotted lines, respectively.

¹⁸⁶ contribution in the maximum-likelihood fit described in Sec. [6.](#page-10-0) As the three categories ¹⁸⁷ are statistically independent further steps of the analysis are performed on the combined ¹⁸⁸ sample.

189 4 Detector resolution and efficiency

¹⁹⁰ The finite decay-time resolution is a diluting factor that will affect the relative precision of ϕ_s and has to be accounted for. The way this is introduced into the analysis is described 192 in Sec. [6.](#page-10-0) The assumed decay-time resolution model, \mathcal{R} , consists of a sum of two Gaussian ¹⁹³ distributions with their widths depending on the per-candidate decay-time uncertainty ¹⁹⁴ determined by the vertex fit as detailed in Ref. [\[16\]](#page-19-2). The parameters of this model are ¹⁹⁵ loosely constrained in the fit of the $B_s^0 \to J/\psi (e^+e^-)K^+K^-$ decay to the values determined 196 using an identical model from a sample of $J/\psi \to \mu^+\mu^-$ candidates produced at the ¹⁹⁷ PV. They are allowed to vary within a Gaussian constraint of twice the difference of ¹⁹⁸ their values between the electron and muon modes as extracted from simulation. The ¹⁹⁹ parameters are determined from the unbinned maximum-likelihood fit, as described in 200 Sec. [6.](#page-10-0) Taking into account the σ_t distribution of the B_s^0 signal, the resulting effective 201 resolution is 45.6 ± 0.5 fs.

²⁰² Due to the displacement requirements made on signal tracks in the trigger and offline 203 selections, the reconstruction efficiency depends on the decay time of the B_s^0 candidate.

Figure 3: Distribution of $m(e^+e^-K^+\pi^-)$ for selected $B^0 \to J/\psi K^*(892)^0$ candidates divided into three categories: (a) zero, (b) one and (c) both electrons with bremsstrahlung correction. The blue solid line shows the total fit which is composed of (red short-dashed line) the signal and the background contributions. The combinatorial background is indicated by the green long-dashed line while the partially reconstructed background from the $B^0 \to \psi(2S)K^*(892)^0$, $B^0 \to \chi_{c1}(1P)K^*(892)^0$ and $B^0 \to J/\psi K_1(1270)^0$ decays are indicated by pink, purple and yellow dash-dotted lines, respectively.

- ²⁰⁴ The efficiency is determined with the same method as described in Ref. [\[6\]](#page-18-1), by using the ²⁰⁵ control channel $B^0 \to J/\psi K^*(892)^0$, with $J/\psi \to e^+e^-$ and $K^*(892)^0 \to K^+\pi^-$ decays.
- ²⁰⁶ The decay-time dependence of the signal efficiency is determined as

$$
\varepsilon_{\text{data}}^{B_s^0}(t) = \varepsilon_{\text{data}}^{B^0}(t) \times \frac{\varepsilon_{\text{sim}}^{B_s^0}(t)}{\varepsilon_{\text{sim}}^{B^0}(t)},\tag{5}
$$

²⁰⁷ where $\varepsilon_{data}^{B^0}(t)$ is the efficiency of the control channel, determined on data, and $\varepsilon_{sim}^{B^0}(t)/\varepsilon_{sim}^{B^0}(t)$ ²⁰⁸ is the ratio of efficiencies of the simulated signal and control modes after the selection. The efficiencies are extracted by normalisation to the known lifetimes of $\tau_{B_s^0} = 1.527 \pm 0.011$ ps 210 and $\tau_{B^0} = 1.520 \pm 0.004$ ps [\[13\]](#page-18-8). The second term accounts for the small differences in ²¹¹ the decay time and kinematics between the signal and the control modes. The control 212 channel efficiency is defined as $\varepsilon_{data}^{B^0}(t) = N_{data}^{B^0}(t)/N_{gen}^{B^0}(t)$ where $N_{data}^{B^0}(t)$ is the number of 213 the $B^0 \to J/\psi K^*(892)^0$ decays in a given time bin as determined using *sPlot* technique [\[41\]](#page-20-13) 214 with $m(e^+e^-K^+\pi^-)$ as discriminating variable. The $N_{\text{gen}}^{B^0}(t)$ is the number of events 215 generated from an exponential distribution with lifetime τ_{B0} [\[13\]](#page-18-8). The analysis is not ²¹⁶ sensitive to the absolute scale of the efficiency.

217 The $B^0 \to J/\psi K^*(892)^0$ decay is selected using trigger, selection and BDT requirements ²¹⁸ similar to those used for the signal, adapted to the different final states. The background ²¹⁹ contribution to the control sample from the misidentification of final-state particles from

Figure 4: Signal efficiency as a function of the decay time, $\varepsilon_{data}^{B_s^0}(t)$, scaled by the average efficiency.

²²⁰ the $\Lambda_b^0 \to J/\psi p \pi^-$ decay is estimated to be 0.06% of the expected signal yield, while the 221 background contribution from $B_s^0 \to J/\psi \phi$ decays is negligible.

222 The $m(e^+e^-K^+\pi^-)$ invariant-mass distribution is shown in Fig. [3](#page-8-0) divided into ²²³ the three bremsstrahlung categories, as for the signal sample. The contribution 224 from $B^0 \to J/\psi K^*(892)^0$ decays is described by the sum of two CB functions while ²²⁵ an exponential function is used to describe the combinatorial background. Simi-226 larly to the signal sample, partially reconstructed background arises from B^0 decays ²²⁷ where one or more particles are not reconstructed; background components stem- γ_{228} ming from $B^0 \to \chi_{c1}(1P)(\to J/\psi\gamma)K^*(892)^0$, $B^0 \to \psi(2S)(\to J/\psi X)K^*(892)^0$ and ²²⁹ $B^0 \to J/\psi K_1(1270)^0 (\to K^*(892)^0 \pi^0)$ decays² are described using a single Gaussian func-²³⁰ tion, the sum of two Gaussian functions and the sum of two CB functions, respectively. ²³¹ The $B^0 \to J/\psi K^*(892)^0$ yield is found to be $(5.45 \pm 0.05) \times 10^4$ signal candidates.

232 The decay-time efficiency for the $B_s^0 \to J/\psi \phi$ signal is shown in Fig. [4.](#page-9-1) The efficiency ²³³ is relatively uniform at high values of decay time but decreases at low decay times due to ²³⁴ the selection criteria that require displaced tracks.

235 The efficiency as a function of the $B_s^0 \to J/\psi \phi$ helicity angles is not uniform due to the forward geometry of the LHCb detector and the requirements imposed on the final-state 237 particle momenta. Projections of the three-dimensional efficiency, $\varepsilon(\Omega)$, to the three helicity angles are shown in Fig. [5.](#page-10-1) The angular efficiency correction is introduced in the analysis through normalisation integrals in the probability density function describing the signal decays in the fit described in Sec. [6.](#page-10-0) The integrals given in Table [2](#page-10-2) are calculated using simulated candidates that are subject to the same trigger and selection criteria as the data, following the same technique as in Ref. [\[20\]](#page-19-5). The relative efficiency is constant for 243 the azimuthal angle ϕ_h . A dependence of up to 15% is observed for $\cos \theta_e$ and $\cos \theta_K$. The finite angular resolution has small impact on the results of the analysis and is neglected. A systematic uncertainty is assigned to account for this effect.

²⁴⁶ 5 Flavour tagging

 247 The B_s candidate flavour at production is determined by two independent categories of ²⁴⁸ flavour tagging algorithms, the opposite-side (OS) taggers [\[42\]](#page-20-14) and the same-side kaon ²⁴⁹ (SSK) tagger [\[43\]](#page-21-0), which exploit specific features of the production of $b\bar{b}$ quark pairs in

	k_1	I_k/I_0
1	(00)	0.9801 ± 0.0014
$\overline{2}$	()	1.0200 ± 0.0017
3	$(\perp\perp)$	1.0209 ± 0.0016
4	$(\Vert \perp)$	0.0003 ± 0.0018
5	(0)	0.0008 ± 0.0012
6	$(0\perp)$	0.0015 ± 0.0012
7	(SS)	0.9983 ± 0.0011
8	$(S\)$	0.0004 ± 0.0016
9	(S_+)	0.0012 ± 0.0016
10	(S0)	-0.0067 ± 0.0036

Table 2: Angular acceptance integrals for the simulated sample. The I_k integrals are normalised with respect to the I_0 integral.

Figure 5: Efficiency projected onto (left) $\cos \theta_K$, (middle) $\cos \theta_e$ and (right) ϕ_h obtained from a simulated $B_s^0 \rightarrow J/\psi \phi$ sample, scaled by the average efficiency.

²⁵⁰ pp collisions, and their subsequent hadronisation. Each tagging algorithm assigns a tag 251 decision and a mistag probability. The tag decision, q, takes values $+1$, -1 , or 0, if the ²⁵² signal candidate is tagged as B_s^0 , \overline{B}_s^0 , or is untagged, respectively. The fraction of events ²⁵³ in the sample with a nonzero tagging decision gives the efficiency of the tagger, ε_{tag} . The $_{254}$ mistag probability, η , is estimated event-by-event, and represents the probability that ²⁵⁵ the algorithm assigns a wrong tag decision. It is calibrated using data samples of two ²⁵⁶ flavour specific decays, $B^{\pm} \to J/\psi (e^+e^-)K^{\pm}$ for the OS taggers and $B_s^0 \to D_s^- \pi^+$ for the 257 SSK tagger, resulting in a corrected mistag probability, $\omega(\bar{\omega})$, for a candidate with initial ²⁵⁸ flavour B_s^0 (\overline{B}_s^0). In case of the SSK algorithm, the calibrated sample of $B_s^0 \to D_s^- \pi^+$ decays is weighted to match the kinematics of the $B_s^0 \to J/\psi \phi$ signal decays. A linear 260 relationship between η and ω is used for the calibration. The effective tagging power ²⁶¹ is given by $\varepsilon_{\text{tag}}(1-2\omega)^2$ and for the combined taggers in the $B_s^0 \to J/\psi(e^+e^-)\phi$ signal ²⁶² sample a value of $(5.07 \pm 0.16)\%$ is obtained.

²⁶³ 6 Maximum-likelihood fit and results

²⁶⁴ The CP observables are determined by an unbinned maximum-likelihood fit to the $_{265}$ background-subtracted candidates in four-dimensions, namely the B_s^0 decay time and ₂₆₆ the three helicity angles, with a probability density function (PDF) describing $B_s^0 \rightarrow$ $_{267}$ J/ψ(e^+e^-) ϕ signal decay. The negative log-likelihood function to be minimised is given by

$$
-\ln \mathcal{L} = -\alpha \sum_{i=1}^{N} w_i \ln \mathcal{P}, \qquad (6)
$$

₂₆₈ where N is the total number of candidates. The w_i coefficients are the *sPlot* weights [\[41\]](#page-20-13) computed using $m(e^+e^-K^+K^-)$ as discriminating variable, and the fac-²⁷⁰ tor $\alpha = \sum w_i / \sum w_i^2$ is used to account for the correct signal yield in the sample. The ²⁷¹ PDF, $\mathcal{P} = \mathcal{S}/\int \mathcal{S} dt d\Omega$, is normalised over the four-dimensional space where

$$
\mathcal{S}(t,\Omega,\mathfrak{q}^{OS},\mathfrak{q}^{SSK}|\eta^{OS},\eta^{SSK}) = \mathcal{T}(t',\Omega,\mathfrak{q}^{OS},\mathfrak{q}^{SSK}|\eta^{OS},\eta^{SSK}) \otimes \mathcal{R}(t-t'|\sigma_t) \times \varepsilon_{\text{data}}^{B_s^0}(t), \tag{7}
$$

 $_{272}$ with the decay-time resolution function, \mathcal{R} , defined in Sec. [4](#page-7-0) and

$$
\mathcal{T}(t',\Omega,\mathfrak{q}^{OS},\mathfrak{q}^{SSK}|\eta^{OS},\eta^{SSK}) = (1+\mathfrak{q}^{OS}(1-2\omega^{OS})) (1+\mathfrak{q}^{SSK}(1-2\omega^{SSK})) G(t,\Omega) + (1-\mathfrak{q}^{OS}(1-2\bar{\omega}^{OS})) (1-\mathfrak{q}^{SSK}(1-2\bar{\omega}^{SSK})) \bar{G}(t,\Omega),
$$
 (8)

²⁷³ which allows for the inclusion of the information from both tagging algorithms in the computation of the decay rate. The function $G(t, \Omega)$ is defined in Eq. [\(1\)](#page-3-4) and $\bar{G}(t, \Omega)$ ²⁷⁵ is the corresponding function for \bar{B}_s^0 decays. The angular efficiency is included in the 276 normalisation of the PDF via the ten integrals, $I_k = \int d\Omega \, \varepsilon(\Omega) f_k(\Omega)$. The integrals are ²⁷⁷ pre-calculated using simulation as described in Sec. [4.](#page-7-0)

²⁷⁸ When using weights from the *sPlot* method, the standard uncertainty estimate based on the Hessian matrix will generally not give asymptotically correct confidence inter- vals [\[44\]](#page-21-1). A bootstrap method [\[45\]](#page-21-2) is used to obtain a correct estimate of the statistical uncertainty. The weights are recalculated for each bootstrap sample. In the fit, Gaussian constraints are included for certain nuisance parameters, namely the mixing frequency ²⁸³ $\Delta m_s = 17.757 \pm 0.021 \,\text{ps}^{-1}$ [\[13\]](#page-18-8), the tagging calibration parameters, and the time res- olution parameters. The fitting procedure is validated using pseudoexperiments and ²⁸⁵ simulated $B_s^0 \to J/\psi (e^+e^-) \phi$ decays.

 The results of the fit to the data are shown in Table [3](#page-12-0) while the projections of the fit results on the decay time and helicity-angle distributions are reported in Fig. [6.](#page-12-1) The correlation matrix of statistical uncertainties is reported in Table [5](#page-17-3) of Appendix [A.](#page-16-1) The results are consistent with previous measurements of these parameters [\[3,](#page-17-1)8[–12\]](#page-18-7), and the 290 SM predictions for ϕ_s [\[22–](#page-19-7)[24\]](#page-19-8). They show no evidence of CP violation in the interference between B_s^0 meson mixing and decay, nor for direct CP violation in $B_s^0 \to J/\psi (e^+e^-) \phi$ decays, as the parameter $|\lambda|$ is consistent with unity within uncertainties.

²⁹³ 7 Systematic uncertainties

 Systematic uncertainties for each of the measured parameters are reported in Table [4.](#page-13-0) They are evaluated by observing the change in the physics parameters after repeating the likelihood fit with a modified model assumption, or through pseudoexperiments, in case of uncertainties originating from the limited size of calibration samples.

²⁹⁸ The decay-time and angular efficiencies obtained independently in the three ²⁹⁹ bremsstrahlung categories are compatible within statistical uncertainties. While the

Table 3: Results of the maximum-likelihood fit, described in Sec. [6,](#page-10-0) to the $B_s^0 \to J/\psi (e^+e^-) \phi$ decays including all acceptance and resolution effects. The first uncertainty is statistical and the second is systematic.

	Parameter	Fit result and uncertainty
	Γ_s [ps ⁻¹] $\Delta\Gamma_s$ [ps ⁻¹] $ A_\perp ^2$	$0.608 \pm 0.018 \pm 0.011$ $0.115 \pm 0.045 \pm 0.011$ $0.234 \pm 0.034 \pm 0.008$
	$ A_0 ^2$ δ_{\parallel} [rad]	$0.530 \pm 0.029 \pm 0.013$ $3.11^{+0.08}_{-0.07} \pm 0.06$
	δ_{\perp} [rad]	$2.41_{ -0.42}^{ +0.43} \pm 0.10$
	ϕ_s [rad] $ \lambda $	$0.00 \pm 0.28 \pm 0.05$
	$F_{\rm S}$	$\begin{array}{l} 0.877^{+0.112}_{-0.116} \pm 0.031 \\ 0.062^{+0.042}_{-0.051} \pm 0.022 \\ 0.01^{+0.25}_{-0.27} \pm 0.04 \end{array}$
	$\delta_{\rm S}$ [rad]	
Candidates / (0.274 ps) $10^3\,$ 10^2 $10\,$ ⊷Data Total CP-even 1 -CP-odd --S-wave 10^{-1}	$\mathop{\hbox{\rm LHCb}}\limits_3$ fb^-1 5 10 Decay time [ps]	$\frac{1}{2}$ Candidates / 0.1 $\frac{1}{2}$ 8 80 $\frac{1}{400}$ $LHCb$ 3 fb ⁻¹ 400 200 $\boldsymbol{0}$ -0.5 $\overline{0}$ 0.5 $\cos\theta_e$
Candidates / 0.1 Candidates / 0.0 $\frac{80}{400}$ 400 200 $^{0}_{-1}$ -0.5	$LHCb$ 3 fb ⁻¹ $\boldsymbol{0}$ 0.5	LHCb $3 fb^{-1}$ $\boldsymbol{0}$ $\mathbf{0}$ -2 $\stackrel{2}{\phi}_h$ [rad] 1 $cos\theta_{K}$

Figure 6: Decay time and helicity-angle distributions for (data points) $B_s^0 \to J/\psi (e^+e^-) \phi$ decays with the one-dimensional projections of the PDF extracted in the maximum-likelihood fit. The solid blue line shows the total signal contribution, which is composed of (long-dashed red) CP-even, (short-dashed green) CP-odd and (dash-dotted purple) S-wave contributions.

³⁰⁰ effective decay-time resolution differs for the three categories, it was verified with simula-³⁰¹ tions that the result of a weighted average of three independent maximum-likelihood fits ³⁰² is consistent with the default one.

³⁰³ Repeating the mass fit in bins of the decay time and helicity angles shows that the 304 mass resolution depends on $\cos \theta_e$ and $\cos \theta_K$. As the *sPlot* technique assumes that the ³⁰⁵ discriminating variable is independent of the observables of interest, the effect of this

Source	Γ_s	$\Delta\Gamma_s$	A_{\perp}^2	A_0^2	δ_{\parallel}	δ_{\perp}	ϕ_s	$ \lambda $	F_S	δ_S
	$ ps^{-1} $	$\mathrm{[ps^{-1}]}$			[rad]	rad	rad			rad
Stat. uncertainty	0.018	0.045	0.034	0.029	$+0.08$ -0.07	$+0.43$ -0.42	0.28	$+0.112$ -0.116	$+0.042$ -0.051	$+0.25$ -0.27
Mass factorisation	0.003	0.003	0.005	0.007	0.01	0.03	0.02	0.011	0.017	0.01
Mass model	0.009	0.005	0.004	0.005	0.01	0.09	0.03	0.011	0.007	0.03
Ang. acceptance			0.002	0.001	$\overline{}$	0.02	0.01	0.005	0.003	0.02
Time resolution	0.002	0.008	0.004	0.002	0.06	0.02	0.03	0.003	0.002	0.01
Time acceptance	0.003	0.003	0.001	0.001				0.001		
MC (time acc.)	0.001	0.001	0.001							
MC (ang. acc.)		$\qquad \qquad -$	0.001	0.001	0.01	0.01	0.02	0.017	0.003	
Λ_h^0 background	0.001	0.001	0.001	0.001	0.01	$\overline{}$	0.01	0.005	0.01	
Ang. resolution		0.002	0.002	0.003		0.01			0.005	
B_c^+ background	0.003									
Fit bias				0.009				0.020		
Syst. uncertainty	0.011	0.011	0.008	0.013	0.06	0.10	0.05	0.031	0.022	0.04
Total uncertainty	0.021	0.046	0.035	0.032	0.10	0.44	0.28	$+0.117$ -0.121	$+0.047$ -0.056	$+0.25$ -0.27

Table 4: Statistical and systematic uncertainties. A dash corresponds to systematic uncertainties that are negligible. Systematic uncertainties from different sources are added in quadrature.

306 correlation is quantified. The data sample is divided in intervals of $\cos \theta_e$ and $\cos \theta_K$ and ³⁰⁷ new weights are computed with fits to $m(e^+e^-K^+K^-)$. The four-dimensional likelihood ³⁰⁸ fit is evaluated with modified weights. The variation of each physics parameter is assigned 309 as a systematic uncertainty. For the decay time and azimuthal ϕ_h angle the effect is ³¹⁰ negligible.

 The mass model is tested in two ways. For the first test a new set of weights using a sum of two Ipatia functions [\[46\]](#page-21-3) is computed to describe the signal component of the $m(e^+e^-K^+K^-)$ distribution. For the second test a set of pseudoexperiments is used by fluctuating the default mass model parameters within their uncertainties (accounting for correlations), providing a new set of weights. The width of the obtained physics parameters distributions from the pseudoexperiments or the difference between the default and Ipatia based result is assigned as systematic uncertainty, whichever is larger.

 The statistical uncertainty on the angular efficiency is propagated by repeating the fit using new sets of the ten integrals, I_k , systematically varied according to their covariance matrix. The width of the obtained distributions for each physics parameter is taken as the systematic uncertainty. The angular resolution is neglected in the maximum-likelihood fit. The effect of this assumption is studied using pseudoexperiments, where the helicity angles are smeared according to the experimental resolution. There is a small effect on the polarisation amplitudes, strong phase and decay width difference while all other parameters are unaffected.

 A systematic contribution is evaluated to take into account the effect of the finite decay-time resolution by comparing pseudoexperiments with fixed and constrained decay- time resolution parameters. A sample of pseudoexperiments with the four-dimensional $B_s^0 \to J/\psi (e^+e^-)\phi$ PDF including time and angular efficiencies is used. The procedure is evaluated for two scenarios: the former with decay-time resolution parameters fixed

 to generated values, and the latter with parameters constrained to twice the difference 332 between values obtained from signal simulation with $J/\psi \to e^+e^-$ and $J/\psi \to \mu^+\mu^-$ decays. The quadratic difference between the uncertainties of pseudoexperiments with fixed and constrained parameters is assigned as a systematic uncertainty. In addition tests with decay-time resolution parameters fixed in the fit to the data sample are performed. The 336 parameters are fixed to values obtained from the time angle fit at ϕ_s value fixed to 0 or $\pi/2$. 337 or to values from a sample of $J/\psi \rightarrow \mu^+\mu^-$ candidates produced at the PV corrected for 338 the difference between e^+e^- and $\mu^+\mu^-$ simulation samples. The test results are compatible within statistical uncertainties to the default fit results.

³⁴⁰ The decay-time efficiency introduces a systematic uncertainty from three different sources. First, the contribution due to the statistical uncertainty on the determination of the decay-time efficiency from the control channel is obtained by evaluating the fit multiple times after randomly varying the parameters of the time efficiency within their statistical uncertainties. The statistical uncertainty is dominated by the size of the $B^0 \to J/\psi K^*(892)^0$ control sample. Second, a sum of two Ipatia functions is used as an atternative mass model for the $m(e^+e^-K^+\pi^-)$ distribution and a new decay-time efficiency $_{347}$ function is produced. Finally, the efficiency function is computed with the $B⁰$ lifetime 348 modified by $\pm 1\sigma$. In all cases the difference in the fit results arising from the use of the new efficiency function is taken as a systematic uncertainty.

 The sensitivity to the BDT selection is studied by adjusting the working point around the optimal position for the signal channel where the difference of the number of signal candidates is within 10% between the default and varied BDT criteria. The effect of applying the modified BDT requirement in the likelihood fit is studied using pseudoexper- iments. The mass model parameters for each BDT requirement are varied within their uncertainties (accounting for correlations) and the weights are re-evaluated based on the alternative model. The fit is repeated using a new set of weights and a new efficiency function. The observed variations in the physics parameters are compatible with statistical fluctuations. This is verified by pseudoexperiments with 10% of candidates removed at random.

 A systematic uncertainty is assigned to account for the differences in the final-state kinematics between data and simulated samples. The simulated signal events are weighted using a multidimensional BDT-based algorithm [\[47\]](#page-21-4). The procedure is repeated for the ³⁶³ control sample $B^0 \to J/\psi (e^+e^-) K^* (892)^0$. The reweighted simulation samples of both channels are used to obtain new angular and decay-time acceptances. The difference with the default fit result is assigned as a systematic uncertainty.

³⁶⁶ The fraction of $\Lambda_b^0 \to J/\psi pK^-$ candidates contributing to the signal sample is estimated to be 1% using simulation. The impact of neglecting this contribution is evaluated for the 368 data sample by fitting the $m(e^+e^-K^+K^-)$ distribution with an additional component to account for, namely the sum of two CB functions, the shape of which is fixed to a fit to ³⁷⁰ simulated $Λ_b^0$ \rightarrow J/ ψpK^- candidates. In addition, the decay-time efficiency is redetermined ³⁷¹ including a component for background from $\Lambda_b^0 \to J/\psi p \pi^-$ decays. This component is modelled by the sum of two CB functions, the shape of which is fixed to a fit to simulated $\Lambda_b^0 \to J/\psi p \pi^-$ candidates. The fraction of the $\Lambda_b^0 \to J/\psi p \pi^-$ decays is estimated from the simulation to be at most 0.06% [\[48\]](#page-21-5). The differences of physics parameters obtained from the fit with modified weights and efficiency function is assigned as a systematic uncertainty.

³⁷⁷ A small fraction of $B_s^0 \to J/\psi \phi$ decays comes from the decays of B_c^+ mesons. The

 fraction is estimated as 0.8% in Ref. [\[49\]](#page-21-6) and pseudoexperiments are used to assess the ³⁷⁹ impact of ignoring such a contribution on the extraction of the physics parameters. Only Γ_s is observed to be affected, with a bias on its central value corresponding to 20% of the statistical uncertainty, which is assigned as a systematic uncertainty.

 A possible bias in the fitting procedure is investigated through many pseudoexperiments of equivalent size to the data sample. For each pseudoexperiment the physics parameters are fluctuated in the underlying PDF and then compared to the obtained fit results. The resulting deviations are small and those that are not compatible with zero within three standard deviations are quoted as systematic uncertainties.

 Inclusion of a result with a constraint on the Δm_s into a global analysis leads to trouble- some treatment of systematic effects introduced by choice of the constraint. Therefore we ³⁸⁹ provide a result with the mixing frequency fixed to the PDG value, $\Delta m_s = 17.757 \,\text{ps}^{-1}$ [\[13\]](#page-18-8), as reported in Appendix [B.](#page-16-2) No significant difference is observed with respect to the default result.

 The systematic uncertainties associated to the mass model and mass factorisation can be treated as uncorrelated between this result and that of Ref. [\[16\]](#page-19-2). More details on the systematic effects for the studied channel are given in Ref. [\[50\]](#page-21-7).

395 8 Conclusion

396 Using a data set corresponding to an integrated luminosity of 3 fb^{-1} collected by the LHCb experiment in pp collisions at centre-of-mass energies of 7 and 8 TeV, a flavour-tagged 398 decay-time-dependent angular analysis of $(1.27 \pm 0.05) \times 10^4$ $B_s^0 \rightarrow J/\psi (e^+e^-) \phi$ decays is 399 performed. A number of physics parameters including the CP-violating phase ϕ_s , average ⁴⁰⁰ decay width Γ_s and decay width difference $\Delta\Gamma_s$ as well as the polarisation amplitudes and strong phases of the decay are determined. The effective decay-time resolution 402 and effective tagging power are 45.6 ± 0.1 fs and $(5.07 \pm 0.16)\%$, respectively. The CP parameters are measured to be

$$
\phi_s = 0.00 \pm 0.28 \pm 0.05 \,\text{rad},
$$

\n
$$
\Delta\Gamma_s = 0.115 \pm 0.045 \pm 0.011 \,\text{ps}^{-1},
$$

\n
$$
\Gamma_s = 0.608 \pm 0.018 \pm 0.011 \,\text{ps}^{-1}
$$

 where the first uncertainty is statistical and the second is systematic. The dominant sources of the systematic uncertainty are the imperfect mass and decay-time resolution 406 models. This is the first measurement of the CP content of the $B_s^0 \to J/\psi (e^+e^-) \phi$ decay and first time that ϕ_s has been measured in the final state containing electrons. These results constitute an important check for the results with muons in the final state because the systematic uncertainties of the measurements are independent, while the studied mechanism of the CP violation is the same. The results are consistent with previous measurements [\[3,](#page-17-1)[8](#page-18-3)[–12\]](#page-18-7), the SM predictions [\[22–](#page-19-7)[24\]](#page-19-8), and show no evidence of CP violation $_{412}$ in the interference between B_s^0 meson mixing and decay. In addition, no evidence for 413 direct CP violation in $B_s^0 \to J/\psi (e^+e^-) \phi$ decays is observed.

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(United Kingdom).

Appendices

A Correlation matrix

⁴³⁷ The CP observables are determined by an unbinned maximum-likelihood fit to the background-subtracted candidates with a probability density function (PDF) describing ⁴³⁹ $B_s^0 \to J/\psi (e^+e^-)\phi$ signal decay. The correlation matrix of their statistical uncertainties is presented in Table [5.](#page-17-3) It is obtained using the bootstrap method.

441 B Fit results with fixed Δm_s

⁴⁴² The fit is repeated with a fixed value of the mixing frequency $\Delta m_s = 17.757 \text{ ps}^{-1}$ [\[13\]](#page-18-8) instead of a Gaussian constraint. The fit results are presented in Table [6](#page-17-4) and corresponding correlation matrix in Table [7.](#page-18-9)

References

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	Γ_s	$\Delta\Gamma_s$	$ A_\perp ^2$	$ A_0 ^2$	δ_{\parallel}	δ_{\perp}	ϕ_s	$ \lambda $	F_S	δ_S
Γ_s	1.00	-0.31	0.41	-0.38	-0.01	-0.03	0.0	-0.09	-0.08	-0.03
$\Delta\Gamma_s$		1.00	-0.68	0.63	0.01	-0.02	0.01	-0.01	-0.04	-0.02
$ A_\perp ^2$			1.00	-0.66	-0.06	0.10	-0.06	-0.14	-0.26	0.03
$ A_0 ^2$				1.00	0.08	-0.17	0.07	0.24	0.36	-0.05
δ_{\parallel}					1.00	-0.03	0.13	-0.06	0.14	-0.20
δ_{\perp}						1.00	0.08	-0.11	-0.28	-0.05
ϕ_s							1.00	0.15	0.26	-0.05
$ \lambda $								1.00	0.52	-0.03
F_S									1.00	-0.06
δ_S										1.00

Table 5: Correlation matrix of statistical uncertainties.

Table [6](#page-10-0): Results of the maximum-likelihood fit described in Section 6 to the $B_s^0 \to J/\psi (e^+e^-) \phi$ decays including all acceptance and resolution effects and with the mixing frequency fixed to the PDG value, $\Delta m_s = 17.757 \,\text{ps}^{-1}$ [\[13\]](#page-18-8). The first uncertainty is statistical and the second is systematic, which is discussed in Section [7.](#page-11-0)

Parameter	Fit result and uncertainty
Γ_s [ps ⁻¹]	$0.608 \pm 0.018 \pm 0.011$
$\Delta\Gamma_s$ [ps ⁻¹]	$0.115 \pm 0.043 \pm 0.011$
$ A_{\perp} ^2$	$0.234 \pm 0.033 \pm 0.008$
$ A_0 ^2$	$0.53^{+0.026}_{-0.027} \pm 0.013$
δ_{\parallel} [rad]	$3.11^{+0.07}_{-0.08}\pm 0.06$
δ_{\perp} [rad]	$2.41^{+0.45}_{-0.46}\pm 0.10$
ϕ_s [rad]	$0.00 \pm 0.30 \pm 0.05$
$ \lambda $	$0.877_{ -0.126}^{ +0.104} \pm 0.031$
$F_{\rm S}$	$0.062^{+0.045}_{-0.052} \pm 0.022$
$\delta_{\rm S}$ [rad]	$0.01 \pm 0.29 \pm 0.04$

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	Γ_s	$\Delta\Gamma_s$	$ A_{\perp} ^2$	$ A_0 ^2$	δ_{\parallel}	δ_{\perp}	ϕ_s	$ \lambda $	F_S	δ_S
Γ_s	1.00	-0.25	0.37	-0.32	-0.01	-0.04	0.01	-0.04	-0.05	-0.03
$\Delta\Gamma_s$		1.00	-0.65	0.60	0.04	-0.05	0.06	-0.01	-0.09	0.05
$ A_\perp ^2$			1.00	-0.61	-0.13	0.09	-0.09	-0.17	-0.25	0.01
$ A_0 ^2$				1.00	0.14	-0.16	0.07	0.17	0.31	0.0
δ_{\parallel}					1.00	-0.05	0.10	-0.01	0.17	-0.22
δ_{\perp}						1.00	0.20	-0.07	-0.26	-0.10
ϕ_s							1.00	0.20	0.20	-0.07
$ \lambda $								1.00	0.51	-0.03
F_S									1.00	-0.05
δ_S										1.00

Table 7: Correlation matrix of statistical uncertainties for a fit with fixed Δm_s .

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LHCb collaboration

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