



Measurement of the branching fraction of the decay $B_s^0 \rightarrow K_S^0 K_S^0$

LHCb collaboration[†]

Abstract

A measurement of the branching fraction of the decay $B_s^0 \rightarrow K_S^0 K_S^0$ is performed using proton–proton collision data corresponding to an integrated luminosity of 5 fb^{-1} collected by the LHCb experiment between 2011 and 2016. The branching fraction is determined to be

$$\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0) = [8.3 \pm 1.6 (\text{stat}) \pm 0.9 (\text{syst}) \pm 0.8 (\text{norm}) \pm 0.3 (f_s/f_d)] \times 10^{-6},$$

where the first uncertainty is statistical, the second is systematic, and the third and fourth are due to uncertainties on the branching fraction of the normalization mode $B^0 \rightarrow \phi K_S^0$ and the ratio of hadronization fractions f_s/f_d . This is the most precise measurement of this branching fraction to date. Furthermore, a measurement of the branching fraction of the decay $B^0 \rightarrow K_S^0 K_S^0$ is performed relative to that of the $B_s^0 \rightarrow K_S^0 K_S^0$ channel, and is found to be

$$\frac{\mathcal{B}(B^0 \rightarrow K_S^0 K_S^0)}{\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0)} = [7.5 \pm 3.1 (\text{stat}) \pm 0.5 (\text{syst}) \pm 0.3 (f_s/f_d)] \times 10^{-2}.$$

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1 Introduction

Flavour-changing neutral current processes, especially neutral B meson decays to kaons and excited kaons, can be used as probes of the Standard Model and of the CKM unitarity triangle angle $\beta_{(s)}$. While decays such as $B_{(s)}^0 \rightarrow K^{*0} \bar{K}^{*0}$, $B_s^0 \rightarrow K^{*0} \bar{K}^0$, and $B^0 \rightarrow K^+ K^-$ have already been measured at the LHC [1–4], decays of b hadrons to final states containing only long-lived particles, such as K_S^0 mesons or Λ baryons, have never before been reported in a hadronic production environment. A measurement of the branching fraction of $B_s^0 \rightarrow K^0 \bar{K}^0$ decays can be used as input to future SM predictions, and is a first step toward a time-dependent measurement of CP violation in this channel using future LHC data.

In the Standard Model, the decay amplitude of $B_s^0 \rightarrow K^0 \bar{K}^0$ is dominated by $b \rightarrow \bar{s} d d$ loop transitions with gluon radiation, while other contributions, including color singlet exchange, are suppressed to the level of 5% [5] in the decay amplitude. Predictions of this branching fraction within the SM lie in the range $(15 - 25) \times 10^{-6}$ [6–9], with calculations relying on a variety of theoretical approaches such as soft collinear effective theory, QCD factorisation, and perturbative leading-order and next-to-leading-order QCD. Beyond the Standard Model, possible contributions from new particles or couplings [5, 10–13] can be probed by improved experimental precision on the branching fraction measurement.

The decay $B_s^0 \rightarrow K^0 \bar{K}^0$ was first observed by the Belle collaboration in 2016 [14]. The branching fraction was determined to be $\mathcal{B}(B_s^0 \rightarrow K^0 \bar{K}^0) = (19.6_{-5.1}^{+5.8} \pm 1.0 \pm 2.0) \times 10^{-6}$, where the first uncertainty is statistical, the second systematic and the third due to the uncertainty of the total number of produced $B_s^0 \bar{B}_s^0$ pairs. The related decay $B^0 \rightarrow K^0 \bar{K}^0$ has a branching fraction of $(1.21 \pm 0.16) \times 10^{-6}$ [15–17] in the world average.

This paper presents measurements of the branching fraction of $B_{(s)}^0 \rightarrow K_S^0 K_S^0$ decays using proton-proton collision data collected by the LHCb experiment at centre-of-mass energies $\sqrt{s} = 7, 8, \text{ or } 13$ TeV. The $B_{(s)}^0 \rightarrow K_S^0 K_S^0$ branching fraction is assumed to be half of the $B_{(s)}^0 \rightarrow K^0 \bar{K}^0$ branching fraction, as the $K^0 \bar{K}^0$ final state is CP even. These $B_{(s)}^0$ branching fractions are determined relative to the $B^0 \rightarrow \phi K_S^0$ branching fraction, where the notation ϕ is used for the $\phi(1020)$ meson throughout. This normalization mode has a corresponding branching fraction equal to half of $\mathcal{B}(B^0 \rightarrow \phi K^0) = (7.3 \pm 0.7) \times 10^{-6}$ [18, 19], and is chosen for its similarity to the signal mode. Despite the smaller branching fraction, the yield of the normalization mode is much larger than that of the signal mode, because the near-instantaneous ϕ decay can be reconstructed more efficiently than a long-lived K_S^0 , and because for LHCb the production fraction of B^0 mesons is approximately four times that of B_s^0 mesons. [42, 43]. Throughout this paper, the decays $B_{(s)}^0 \rightarrow K_S^0 K_S^0$ and $B^0 \rightarrow \phi K_S^0$ are reconstructed using the decays $K_S^0 \rightarrow \pi^+ \pi^-$ and $\phi \rightarrow K^+ K^-$.

The paper is structured as follows. A brief description of the LHCb detector as well as the simulation and reconstruction software is given in Sec. 2. Signal selection and strategies to suppress background contributions are outlined in Sec. 3. The models to describe the invariant-mass components, the fitting and the normalization procedure are introduced in Sec. 4. Systematic uncertainties are discussed in Sec. 5. Finally, the results are summarized in Sec. 6.

2 LHCb detector

The LHCb detector [20, 21] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing b or c quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector (VELO) surrounding the pp interaction region [22], a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm, and three stations of silicon-strip detectors and straw drift tubes [23, 24] placed downstream of the magnet. The tracking system provides a measurement of momentum, p , of charged particles with a relative uncertainty that varies from 0.5% at low momentum to 1.0% at 200 GeV/ c . The minimum distance of a track to a primary vertex (PV), the impact parameter (IP), is measured with a resolution of $(15 + 29/p_T) \mu\text{m}$, where p_T is the component of the momentum transverse to the beam, in GeV/ c . Different types of charged hadrons are distinguished using information from two ring-imaging Cherenkov detectors [25]. Photons, electrons and hadrons are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic calorimeter and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers.

The online event selection is performed by a trigger [26], which consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, which applies a full event reconstruction. At the hardware trigger stage, events are required to contain a muon with high p_T or a hadron, photon or electron with high transverse energy in the calorimeters. In the software trigger, events are selected by a topological b -hadron trigger. At least one charged particle must have a large transverse momentum and be inconsistent with originating from any PV. A two- or three-track secondary vertex is constructed, which must have a large sum of the p_T of the charged particles and a significant displacement from any PV. A multivariate algorithm [27] is used for the identification of secondary vertices consistent with the decay of a b -hadron. This is used to collect both $B_{(s)}^0 \rightarrow K_S^0 K_S^0$ and $B^0 \rightarrow \phi K_S^0$ decays. In addition to this topological trigger and algorithm, some $B^0 \rightarrow \phi K_S^0$ decays are also collected using dedicated ϕ trigger requirements that exploit the topology of the $\phi \rightarrow K^+ K^-$ decay and apply additional particle identification requirements to the charged kaons.

Simulation is required to model the effects of the detector acceptance and the imposed selection requirements. In simulation, pp collisions are generated using PYTHIA [28] with a specific LHCb configuration [29]. Decays of hadronic particles are described by EVTGEN [30], in which final-state radiation is generated using PHOTOS [31]. The interaction of the generated particles with the detector, and its response, are implemented using the GEANT4 toolkit [32] as described in Ref. [33].

3 Event selection

The decays $B_{(s)}^0 \rightarrow K_S^0 K_S^0$ and $B^0 \rightarrow \phi K_S^0$ are reconstructed using the decay modes $K_S^0 \rightarrow \pi^+ \pi^-$ and $\phi \rightarrow K^+ K^-$.¹ The long-lived K_S^0 mesons are reconstructed in two different categories, depending on whether the K_S^0 meson decays early enough that the pions can be tracked inside the VELO, or whether the K_S^0 meson decays later and its products

¹The inclusion of charge-conjugate processes is implied throughout the paper

can only be tracked downstream. These are referred to as *long* and *downstream* track categories, and are abbreviated as L and D, respectively. The K_S^0 mesons reconstructed in the long track category have better mass, momentum and vertex resolution than the downstream track category. However, due to the boost of the B meson, the lifetime of the K_S^0 meson, and the geometry of the detector, there are approximately twice as many K_S^0 candidates reconstructed in the downstream category than in the long category, before any selections are applied.

This analysis is based on pp collision data collected by the LHCb experiment. Data collected in 2011 (2012) were recorded at a center-of-mass energy of 7 TeV (8 TeV), while in 2015 and 2016 the center-of-mass energy was increased to 13 TeV. Data recorded at center-of-mass energies of 7 and 8 TeV (Run 1) are combined and then treated separately from data recorded at 13 TeV (Run 2). Due to low trigger efficiency for B_s^0 mesons decaying into two downstream K_S^0 mesons, these are discarded from the analysis. Consequently, there are four data categories that are considered in the following—Run 1 LL, Run 1 LD, Run 2 LL and Run 2 LD—and measurements are performed separately in each of these data categories before being combined in the final fit.

Signal B_s^0 or B^0 candidates are built in successive steps, with individual K_S^0 candidates reconstructed first and then combined. The K_S^0 candidates are constructed by combining two oppositely charged pions that meet certain requirements on the minimum total momentum and transverse momentum; on the minimum χ_{IP}^2 of the K_S^0 candidate with respect to the associated PV (where χ_{IP}^2 is defined as the difference in the impact parameter χ^2 of a given PV reconstructed with and without the considered particle); on the maximum distance of closest approach (DOCA) between the two particles; and on the quality of the vertex fit. An event can have more than one PV, in which case the associated PV is defined as that with which the B candidate forms the smallest value of χ_{IP}^2 . The invariant mass of K_S^0 candidates constructed from long (downstream) tracks must be within 35 MeV/ c^2 (64 MeV/ c^2) of the known K_S^0 mass [15]. The DOCA between the two K_S^0 candidates is required to be smaller than 1 mm for the LL category and 4 mm for the LD category. Signal B_s^0 or B^0 candidates are then formed by combining two K_S^0 candidates that result in an invariant mass close to the known $B_{(s)}^0$ masses, discussed further below and in Sec. 4.

The normalization decay $B^0 \rightarrow \phi K_S^0$ is constructed in a similar way. The ϕ meson is constructed by combining two oppositely charged kaon candidates that result in an invariant mass within 50 MeV/ c^2 of the nominal ϕ mass, as a first loose selection. Due to the vanishing lifetime of the ϕ meson, the charged kaon candidates are only reconstructed from long tracks, and thus all ϕ are reconstructed in the L category. The K_S^0 meson of the normalization decay can be either L or D, so that the $B^0 \rightarrow \phi K_S^0$ decay has both LL and LD reconstructions.

The rest of the candidate selection process consists of a preselection followed by the application of a multivariate classifier, and then some additional selections are applied to further reduce combinatorial background. In the preselection, loose selection requirements are applied to remove specific backgrounds from other b -hadron decays and suppress combinatorial background. These backgrounds for the signal and normalization modes are discussed further below. Additional suppression of the combinatorial background is included using a final selection after the multivariate classifier is applied, where particle identification (PID) requirements are added such that all final-state particles must be inconsistent with the muon hypothesis based on the association of hits in the muon

stations.

Possible background decays are studied using simulated samples. For the signal channel, these include: $B_{(s)}^0 \rightarrow K_S^0 \pi^+ \pi^-$; $B_{(s)}^0 \rightarrow K_S^0 \pi^+ K^-$ with kaon–pion misidentification; $B_{(s)}^0 \rightarrow K_S^0 K^+ K^-$ with double kaon–pion misidentification; and $\Lambda_b^0 \rightarrow p K_S^0 \pi^-$ with proton–pion misidentification. Backgrounds from $K_L^0 \rightarrow \pi^+ \pi^-$ decays are negligible. Applying the K_S^0 mass window requirement to the two-hadron system originating directly from a b -hadron decay reduces the background yields by a factor of 10 to 100, depending on the decay channel. To further suppress the contribution of these modes, a requirement on the distance along the beam axis direction (the z -direction) between the decay vertices of the K_S^0 and B_s^0 candidates, $\Delta z > 15$ mm, is applied to K_S^0 candidates reconstructed from long tracks for both decay channels.

An additional background comes from the requirements used to identify K_S^0 candidates, which may also select Λ baryons due to their long flight distance. The $\Lambda \rightarrow p \pi^-$ decays are excluded by changing the mass hypothesis of one pion candidate to the proton hypothesis, reconstructing the invariant mass, $m(p \pi^-)$, and tightening the pion PID requirement in an 8 MeV/ c^2 mass window around the known Λ mass. This procedure is carried out for each pion from each K_S^0 candidate, in both the signal and normalization channels.

For the normalization channel $B^0 \rightarrow \phi K_S^0$, the decays $B_{(s)}^0 \rightarrow K_S^0 h^{(\prime)+} h^{(\prime)-}$ with $h^{(\prime)\pm} = \pi^\pm, K^\pm$ are suppressed by requiring the invariant mass of the combination of the two final-state kaons to be close to the ϕ mass. The largest contributions are expected from the decay channel $B_s^0 \rightarrow K_S^0 \pi^+ K^-$ with a fraction of about 1% compared to $B^0 \rightarrow \phi K_S^0$ decays. This is reduced to a negligible level by applying PID requirements to the kaon candidates. The partially reconstructed decays $B^0 \rightarrow \phi K^{*0}$ and $B^+ \rightarrow \phi K^{*+}$, with $K^{*0} \rightarrow K_S^0 \pi^0$ and $K^{*+} \rightarrow K_S^0 \pi^+$, share the same decay topology as the normalization channel when omitting the pion that originates from decay of the K^* resonance and have a higher branching fraction than the normalization decay. Due to the missing particle, the B candidates have a kinematic upper limit on their masses of about 5140 MeV/ c^2 . Therefore, the mass window to determine the yield of the normalization channel is set to $5150 < m(K_S^0 K^+ K^-) < 5600$ MeV/ c^2 to fully exclude these contributions.

Further separation of signal from combinatorial background is achieved using the XGBoost implementation [34] of the Boosted Decision Tree (BDT) algorithm [35]. For the training, simulated signal (normalization) decays are used as signal proxy, while the upper mass sideband $m(K_S^0 K_S^0) > 5600$ MeV/ c^2 ($m(\phi K_S^0) > 5600$ MeV/ c^2) in data is utilized as background proxy. To account for differences in data and simulation, the simulated decays are weighted in the B meson production kinematics and detector occupancy (represented by the number of tracks in the event) to match data distributions.

The BDT exploits the following observables: the flight distance, IP and χ_{IP}^2 of the B and K_S^0 candidates with respect to all primary vertices, as well as the decay time, the momentum, transverse momentum and pseudorapidity of the B candidate. This set of quantities is chosen such that they have a high separation power between signal and background and are not directly correlated to the invariant mass. The same procedure is applied to the $B^0 \rightarrow \phi K_S^0$ data samples.

In order to choose the optimal threshold on the BDT response, the figure of merit $\varepsilon_{\text{sig}}/(3/2 + \sqrt{N_{\text{bkg}}})$ [36] is used for the signal mode, where the value 3/2 corresponds to a target 3 sigma significance and ε_{sig} is the signal efficiency of the selection, determined from simulation. The figure of merit $N_{\text{sig}}/\sqrt{N_{\text{sig}} + N_{\text{bkg}}}$ is used for the normalization channel

to minimize the uncertainty on the yield. So as not to bias the determination of the signal yield, the candidates in the signal region were not inspected until the selection was finalized. Consequently, the expected background yield N_{bkg} is calculated by interpolating the result of an exponential fit to data sidebands, $5000 < m(K_S^0 K_S^0) < 5230$ MeV/ c^2 , and $5420 < m(K_S^0 K_S^0) < 5600$ MeV/ c^2 into the signal region. For the normalization channel, the variation of the expected signal yield N_{sig} as a function of the BDT response threshold is determined from simulation, while the absolute normalization is set from a single fit to the data.

The figure of merit optimization is performed simultaneously with respect to the BDT classifier output and an observable based on PID information for long track candidates, where the latter observable is corrected using a resampling from data calibration samples [37] to minimize differences in data and simulation. As a last selection step, the invariant-mass windows of $m(\pi^+\pi^-)$ and $m(K^+K^-)$ are tightened to further suppress combinatorial background. Finally, multiple candidates, which occur in about 1 in 10000 of all events, are removed randomly so that each event contains only one signal candidate.

4 Fit strategy and results

For the normalization channel, the total $B^0 \rightarrow \phi K_S^0$ yield is obtained from extended unbinned maximum likelihood fits to the reconstructed B^0 mass in the range 5150 MeV/ c^2 to 5600 MeV/ c^2 , separately for each data sample and reconstruction category. The signal component is modelled by a Hypatia function with power-law tails on both sides [38], where the tail parameters are fixed to values obtained from fits to simulated samples. The mean, width and signal yield parameters are free to vary in the fit. An exponential function with a free slope parameter models the combinatorial background. To account for non- ϕ contributions to the $B^0 \rightarrow \phi K_S^0$ yield, a subsequent fit is performed to the $m(K^+K^-)$ distribution, which is background-subtracted using the $s\mathcal{P}$ lot technique [39] and where the $m(K^+K^-K_S^0)$ distribution is used as the discriminating variable. The signal ϕ component of the $m(K^+K^-)$ fit is modelled by a relativistic Breit–Wigner function [40] convolved with a Gaussian function to take into account the resolution of the detector, while the non- ϕ contributions are described by an exponential function. The slope parameter of the latter model is Gaussian-constrained to the results obtained from fits to the simulation of $f_0(980) \rightarrow K^+K^-$ decays, which is found to better describe the observed distribution than a phase-space model. The measured yields for the normalization channel are shown in the last row of Table 1. Plots of the $m(K^+K^-K_S^0)$ distributions for the Run 2 LL and LD samples are shown in Figure 1. The remaining $m(K^+K^-K_S^0)$ distributions and the $m(K^+K^-)$ distributions are shown in the Appendix.

A Hypatia function is used to model the $m(K_S^0 K_S^0)$ distribution of signal $B_s^0 \rightarrow K_S^0 K_S^0$ decays. All shape parameters are fixed to values obtained from fits to simulated samples. To account for resolution differences between simulation and data, the width is scaled by a factor—determined from the normalization channel—which takes values in the range 1.05 to 1.20 depending on the data sample. To model the $B^0 \rightarrow K_S^0 K_S^0$ signal component, the same signal shape is duplicated and shifted by the $B_s^0 - B^0$ mass difference [41]. The background component is modelled by an exponential function with a free slope parameter.

In contrast to the normalization channel, where each data category is fitted individually,

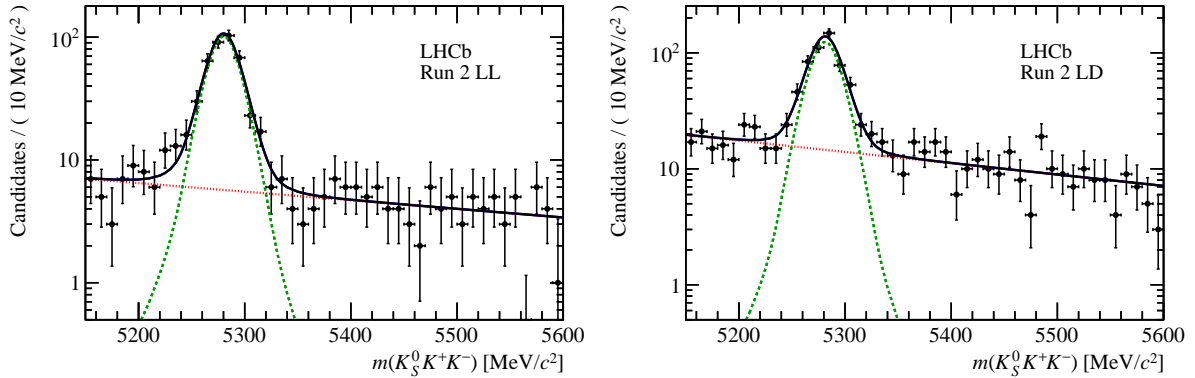


Figure 1: Fits to the invariant-mass distribution $m(K_S^0 K^+ K^-)$ of the normalization decay channel. The black curve represents the complete model, the $B^0 \rightarrow \phi K_S^0$ component is given in green (dashed), while the background component is shown in red (dotted).

a simultaneous fit to the $m(K_S^0 K_S^0)$ distribution of the four data categories (Run 1 LL, Run 1 LD, Run 2 LL, Run 2 LD) is performed in the range 5000 MeV/c² to 5600 MeV/c². Two parameters are shared across all categories in the simultaneous fit, the ratio of the $B^0 \rightarrow K_S^0 K_S^0$ and $B_s^0 \rightarrow K_S^0 K_S^0$ yields f_{B^0/B_s^0} and the branching fraction $\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0)$, which is itself related to the signal yield of each data category via the relation

$$\begin{aligned} \mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0) &= \frac{\varepsilon_{\phi K_S^0, i} f_d \mathcal{B}(\phi \rightarrow K^+ K^-) \mathcal{B}(B^0 \rightarrow \phi K_S^0)}{\varepsilon_{K_S^0 K_S^0, i} f_s \mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-) N_i(B^0 \rightarrow \phi K_S^0)} \cdot N_i(B_s^0 \rightarrow K_S^0 K_S^0) \quad (1) \\ &\equiv \alpha_i \cdot N_i(B_s^0 \rightarrow K_S^0 K_S^0), \end{aligned}$$

where the normalization constant α_i is introduced for each data category sample i . While the selection efficiencies ε and signal yields N are determined in the present analysis, external sources are used for the ratio of fragmentation fractions f_d/f_s [42, 43], and the branching fractions $\mathcal{B}(B^0 \rightarrow \phi K_S^0)$, $\mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-)$ and $\mathcal{B}(\phi \rightarrow K^+ K^-)$ [15]. To increase the robustness of the fit, the α_i constants are Gaussian constrained within their uncertainties, excluding the uncertainties from the external constants. These external uncertainties are instead applied directly to the final branching ratio measurement.

The efficiency ratio, $\varepsilon_{\phi K_S^0}/\varepsilon_{K_S^0 K_S^0}$, is determined from simulation and corrected using data control samples. This ratio is found to be approximately equal to 30 in all data samples except the Run 1 LD sample, where it is twice as large due to lower trigger efficiency for downstream tracks in this sample.

The fit results are shown in Fig. 2. The results of the simultaneous mass fit are given in Table 1, yielding a branching fraction of $\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0) = (8.3 \pm 1.6) \times 10^{-6}$, where the uncertainty is statistical only. The $B_s^0 \rightarrow K_S^0 K_S^0$ yield is around 32. The ratio of the branching fractions of the signal and normalization modes $\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0)/\mathcal{B}(B^0 \rightarrow \phi K_S^0)$ can also be calculated by removing the contribution of the world-average value of $\mathcal{B}(B^0 \rightarrow \phi K_S^0)$ from the fit result. This yields a combined branching fraction ratio $\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0)/\mathcal{B}(B^0 \rightarrow \phi K_S^0) = 2.3 \pm 0.4$, where the uncertainty is statistical only.

From the same fit, the relative fraction of $B^0 \rightarrow K_S^0 K_S^0$ decays, $f_{B^0/B_s^0} = 0.30 \pm 0.13$ is also determined. Given that the final-state particles and selections applied to the K_S^0 candidates are the same for both modes, the ratio of selection efficiencies is equal to one,

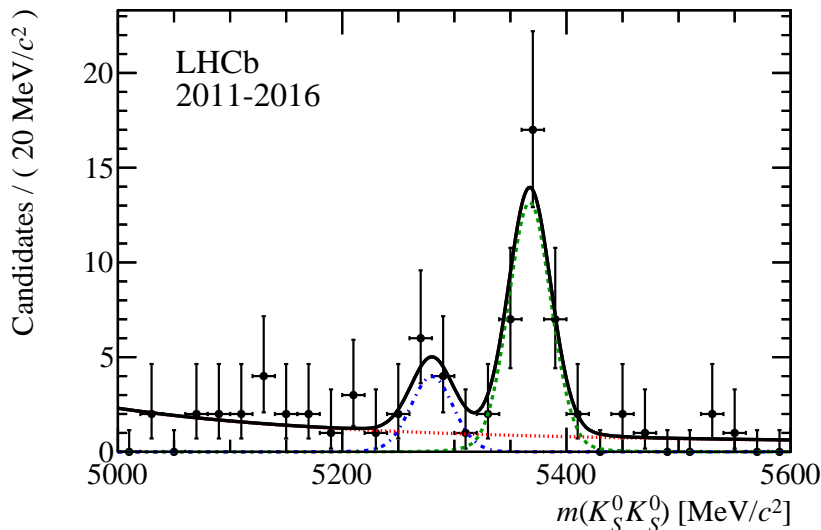


Figure 2: Combined invariant-mass distribution $m(K_S^0 K_S^0)$ of the signal decay channel. The black (solid) curve represents the complete model, the B_s^0 signal component is given in green (dashed), the smaller B^0 signal is given in blue (dash-dotted) and the background component in red (dotted).

so that f_{B^0/B_s^0} can be converted to a ratio of branching fractions by multiplying by f_s/f_d . The calculated value of $\mathcal{B}(B^0 \rightarrow K_S^0 K_S^0)/\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0)$ is $(7.5 \pm 3.1) \times 10^{-2}$, where the uncertainty is statistical only.

The significances of the $B_s^0 \rightarrow K_S^0 K_S^0$ and $B^0 \rightarrow K_S^0 K_S^0$ signal yields are estimated relative to a background-only hypothesis using Wilks' theorem [44]. The observed signal yield of 32 $B_s^0 \rightarrow K_S^0 K_S^0$ decays has a large significance of 8.6σ (6.5σ including the effect of systematic uncertainties), while the smaller $B^0 \rightarrow K_S^0 K_S^0$ signal yield has a significance of 3.5σ including systematic uncertainties.

Table 1: Results of the simultaneous fit to the invariant mass of the $K_S^0 K_S^0$ system. The fit results for \mathcal{B} and f_{B^0/B_s^0} are shared among all data categories. The given uncertainties are statistical only. The normalization constant α and the corresponding normalization channel yields N_{norm} are shown for reference.

| Parameter | Run 1 LL | Run 1 LD | Run 2 LL | Run 2 LD | Status |
|--------------------------------|-----------------|-----------------|-----------------|-----------------|---|
| $\mathcal{B} (\times 10^{-6})$ | | 8.3 ± 1.6 | | | Free |
| f_{B^0/B_s^0} | | 0.30 ± 0.13 | | | Free |
| $N_{B_s^0}$ | 4.3 ± 1.0 | 2.1 ± 0.5 | 12.8 ± 2.7 | 12.4 ± 2.7 | \mathcal{B}/α |
| N_{B^0} | 1.3 ± 0.5 | 0.63 ± 0.26 | 3.8 ± 1.5 | 3.7 ± 1.5 | $f_{B^0/B_s^0} \times \mathcal{B}/\alpha$ |
| N_{bkg} | 10.4 ± 3.5 | 3.5 ± 2.2 | 7.2 ± 3.0 | 13 ± 4 | Free |
| $\alpha (\times 10^{-6})$ | 1.90 ± 0.21 | 3.9 ± 0.5 | 0.65 ± 0.05 | 0.66 ± 0.05 | Gaussian constr. |
| N_{norm} | 179 ± 18 | 178 ± 22 | 316 ± 25 | 400 ± 31 | Included in α |

Table 2: All systematic uncertainties on the $B_s^0 \rightarrow K_S^0 K_S^0$ branching fraction, presented as relative measurements. The last row shows the combined systematic uncertainty for each data sample.

| | Run 1, LL | Run 1, LD | Run 2, LL | Run 2, LD |
|--------------------------------------|-----------|-----------|-----------|-----------|
| Systematic uncert. | | | | |
| Fit bias | 0.059 | 0.059 | 0.059 | 0.059 |
| Fit model choice | 0.022 | 0.033 | 0.015 | 0.013 |
| Fit model parameters | 0.026 | 0.026 | 0.026 | 0.026 |
| BDT | 0.023 | 0.040 | 0.014 | 0.031 |
| PID | 0.007 | 0.008 | 0.026 | 0.026 |
| Hardware trigger | 0.063 | 0.062 | 0.063 | 0.062 |
| Software trigger | 0.065 | 0.106 | 0.008 | 0.026 |
| Trigger misconfig. | — | — | 0.007 | 0.004 |
| π^\pm/K^\pm hadronic interaction | 0.005 | 0.005 | 0.005 | 0.005 |
| VELO misalignment | 0.008 | 0.008 | 0.008 | 0.008 |
| Total | 0.116 | 0.149 | 0.097 | 0.103 |

5 Systematic uncertainties

Each source of systematic uncertainty is evaluated independently and expressed as a relative uncertainty on the branching fraction of $B_s^0 \rightarrow K_S^0 K_S^0$ decays. A complete list is given in Table 2. The uncertainties are grouped into three general categories: fit and weighting uncertainties, PID uncertainties, and detector and trigger uncertainties.

Multiple different fit uncertainties are considered. Uncertainty from possible bias in the combined fit to all four data samples can be estimated using pseudoexperiments generated and fitted according to the default fit model. In each pseudoexperiment, the number of signal candidates is drawn from a Poisson distribution with a mean determined from the baseline fit result. A relative average difference between the generated and fitted branching fraction of 5.9% is determined and conservatively assigned as a systematic uncertainty. The same procedure is performed for the $B^0 \rightarrow K_S^0 K_S^0$ component, yielding a possible bias of 1.6%. To ensure a conservative approach, the 5.9% value from $B_s^0 \rightarrow K_S^0 K_S^0$ is also applied as the systematic for $B^0 \rightarrow K_S^0 K_S^0$.

Another systematic uncertainty in the fitting process arises from the specific fit model choice, which is quantified by the use of alternative probability density functions to describe the invariant-mass distributions. The reconstructed-mass shapes for B^0 and B_s^0 mesons are modelled by the sum of two Crystal Ball functions [45]. For the fit to the $m(K^+ K^-)$ distribution, the ϕ meson is modelled by a non-relativistic Breit–Wigner function. For the normalization channel, the relative yield difference when refitting the data is taken as the systematic uncertainty, while for the $B_s^0 \rightarrow K_S^0 K_S^0$ decay pseudoexperiments are used to estimate the impact of mismodeling the shape of the signal component. The systematic uncertainty due to the choice of fit model is then the sum in quadrature of these variations, yielding values of 1.3% to 3.3% depending on the data category. Another systematic uncertainty of 2.6%, evaluated with a similar procedure, is assigned due to fixing certain shape parameters to values obtained in fits to simulated samples.

Additionally, not all differences between data and simulation can be accounted for

using weights in the BDT training. As a conservative upper limit of this effect, the signal efficiency is calculated with and without weights, and the differences between these efficiencies are treated as a systematic uncertainty. This systematic uncertainty is larger by a factor of about 2 for data categories containing a downstream K_S^0 candidate than in those that contain only long K_S^0 candidates, indicating a stronger dependence of the LD channel efficiencies on the weighting.

Three sources of systematic uncertainties from PID efficiencies are considered. The effect of the finite size of the signal simulation samples is evaluated using the bootstrap method [46] for each simulation category and calculating the variance of the signal efficiency. A second systematic uncertainty is calculated by varying the model used to resample PID calibration data, and the relative difference in the signal efficiency is taken as a systematic uncertainty, though this effect is small compared to the previous source. Finally, the flight distance of the K_S^0 candidate is not considered in the resampling process, while the PID efficiency does exhibit some correlation with this variable. A systematic uncertainty is calculated by reweighting the PID distributions in bins of the K_S^0 flight distance, and calculating the relative signal efficiency on resampled simulation and resampled and reweighted simulation. The combined PID systematic uncertainty is given by summing over the three effects in quadrature, which is below 1% for the Run 1 samples and below 3% for the Run 2 samples.

Systematic uncertainties in the trigger system are divided into hardware and software trigger uncertainties. For the hardware trigger stage, the efficiency taken from simulation is compared with data calibration samples. The calibration data is used to correct the simulated efficiencies, and the resulting 6% relative difference in efficiency between the signal and normalization modes is treated as a systematic uncertainty. For the inclusive B software trigger, possible differences in efficiency between the signal and normalization channels are obtained by reweighting the $B^0 \rightarrow \phi K_S^0$ simulation to match the $B_s^0 \rightarrow K_S^0 K_S^0$ simulation and calculating the relative efficiency difference between the raw and reweighted distributions, yielding a systematic uncertainty of about 2%. An additional, larger systematic uncertainty is also included to account for the dedicated ϕ trigger requirements, which are only used for the normalization channel. Again, weighted $B^0 \rightarrow \phi K_S^0$ data are used to evaluate a relative efficiency difference between simulation and data, multiplied by the fraction of events solely triggered by the dedicated ϕ trigger requirements. The systematic uncertainty is about 5% to 10% in Run 1, but about 5 times smaller for Run 2. This is because the topological b -hadron trigger is more efficient in Run 2 so that there are far fewer events triggered only by the dedicated ϕ trigger. An additional systematic uncertainty less than 1% is assigned to account for a small known misconfiguration of the trigger during Run 2 data taking.

Two additional detector-related uncertainties are considered. A relative uncertainty of 0.5% is assigned due to the different hadronic interaction probabilities between pions and kaons in data and simulation, and a relative uncertainty of 0.8% is also introduced to account for a possible misalignment in the downstream positions of the vertex detector.

The combined systematic uncertainty is determined by using a weighted average of the total systematic uncertainty for each data category, where the weighting is based on the B_s^0 signal yield for each category, obtained from the nominal combined fit for the branching fraction. This value is then combined with the systematic uncertainties due to the $\phi \rightarrow K^+ K^-$ and $K_S^0 \rightarrow \pi^+ \pi^-$ branching fractions, to produce an overall systematic uncertainty of 10.7%. The systematic uncertainties due to $\mathcal{B}(B^0 \rightarrow \phi K_S^0)$ or f_s/f_d are

provided separately when necessary. The total systematic uncertainty in the measurement of the B^0 branching fraction is also 10.7%.

These measurements of the branching ratio are calculated using the time-integrated event yield, without taking into account $B_s^0-\bar{B}_s^0$ mixing effects. The conversion into a branching ratio that is independent of $B_s^0-\bar{B}_s^0$ mixing can be performed according to the computation given in Ref. [47], where $\mathcal{A}_{\Delta\Gamma}^f$ is calculated from the decay amplitudes of the B_s^H and B_s^L states. In this work, the simulation is generated using the average B_s^0 lifetime, corresponding to the $\mathcal{A}_{\Delta\Gamma}^f = 0$ scenario. For this scenario the mixing-corrected SM prediction of the branching ratio is equivalent to the quoted time-integrated branching ratio within uncertainties, because the impact of the scaling from $\Delta\Gamma_s/\Gamma_s = 0.135 \pm 0.008$ [15] is small.

Considering that the final state of the decay is CP -even, the relevant decay lifetime of the B_s^0 is expected to be closer to that of the B_s^L state, corresponding to a SM prediction of $\mathcal{A}_{\Delta\Gamma}^f$ close to -1 . This change in lifetime corresponds to a change in the expected efficiency of the $B_s^0 \rightarrow K_S^0 K_S^0$ reconstruction of approximately -4.5% for $\mathcal{A}_{\Delta\Gamma}^f = -1$, or 4.5% for the less-likely $\mathcal{A}_{\Delta\Gamma}^f = 1$. These scaling factors are not included in the systematic uncertainty for the time-integrated branching ratios presented below.

6 Conclusion

Data collected by the LHCb experiment in 2011–2012 and 2015–2016 was used to measure the $B_s^0 \rightarrow K_S^0 K_S^0$ branching fraction. The measured ratio of this branching fraction relative to that of the normalization channel is

$$\frac{\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0)}{\mathcal{B}(B^0 \rightarrow \phi K_S^0)} = 2.3 \pm 0.4 (\text{stat}) \pm 0.2 (\text{syst}) \pm 0.1 (f_s/f_d),$$

where the first uncertainty is statistical, the second is systematic, and the third is due to the ratio of hadronization fractions. This is compatible with the ratio $\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0)/\mathcal{B}(B^0 \rightarrow \phi K_S^0) = 2.7 \pm 0.9$ calculated from the current world average values [15].

From this measurement, the $B_s^0 \rightarrow K_S^0 K_S^0$ branching fraction is determined to be

$$\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0) = [8.3 \pm 1.6 (\text{stat}) \pm 0.9 (\text{syst}) \pm 0.8 (\text{norm}) \pm 0.3 (f_s/f_d)] \times 10^{-6},$$

where the first uncertainty is statistical, the second is systematic, and the third and fourth are due to the normalization channel branching fraction and the ratio of hadronization fractions f_s/f_d . This result is the most precise to date and is compatible with SM predictions [6–9] and the previous measurement from the Belle collaboration [14].

In the same combined fit used for the $B_s^0 \rightarrow K_S^0 K_S^0$ measurement, the fraction of $B^0 \rightarrow K_S^0 K_S^0$ decays is also determined. Using this measured fraction of yields, the branching fraction of $B^0 \rightarrow K_S^0 K_S^0$ decays measured relative to $B_s^0 \rightarrow K_S^0 K_S^0$ decays is found to be

$$\frac{\mathcal{B}(B^0 \rightarrow K_S^0 K_S^0)}{\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0)} = [7.5 \pm 3.1 (\text{stat}) \pm 0.5 (\text{syst}) \pm 0.3 (f_s/f_d)] \times 10^{-2},$$

where the first uncertainty is statistical, the second is systematic, and the third is due to the ratio of hadronization fractions. For comparison, calculating

$\mathcal{B}(B^0 \rightarrow K_S^0 K_S^0)/\mathcal{B}(B_s^0 \rightarrow K_S^0 K_S^0)$ based on world average-values [15] yields $(6.0 \pm 2.0)\%$, which is compatible with the obtained result.

The $B^0 \rightarrow K_S^0 K_S^0$ branching fraction relative to the $B^0 \rightarrow \phi K_S^0$ normalization mode is determined to be

$$\frac{\mathcal{B}(B^0 \rightarrow K_S^0 K_S^0)}{\mathcal{B}(B^0 \rightarrow \phi K_S^0)} = 0.17 \pm 0.08 \text{ (stat)} \pm 0.02 \text{ (syst)},$$

where the first uncertainty is statistical, and the second is systematic.

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Appendix: Normalization channel fits

Figure 3 shows the $m(K_S^0 K^+ K^-)$ distributions for the Run 1 LL and LD categories. The $m(K^+ K^-)$ distributions for all four data categories are shown in Fig. 4.

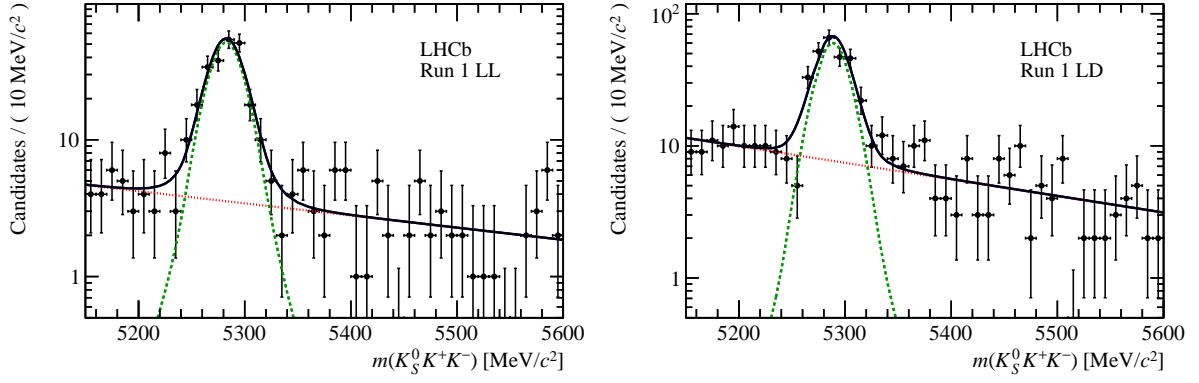


Figure 3: Fits to the invariant-mass distribution $m(K_S^0 K^+ K^-)$ of the normalization decay channel. The black curve represents the complete model, the $B^0 \rightarrow \phi K_S^0$ component is given in green (dashed), while the background component is shown in red (dotted).

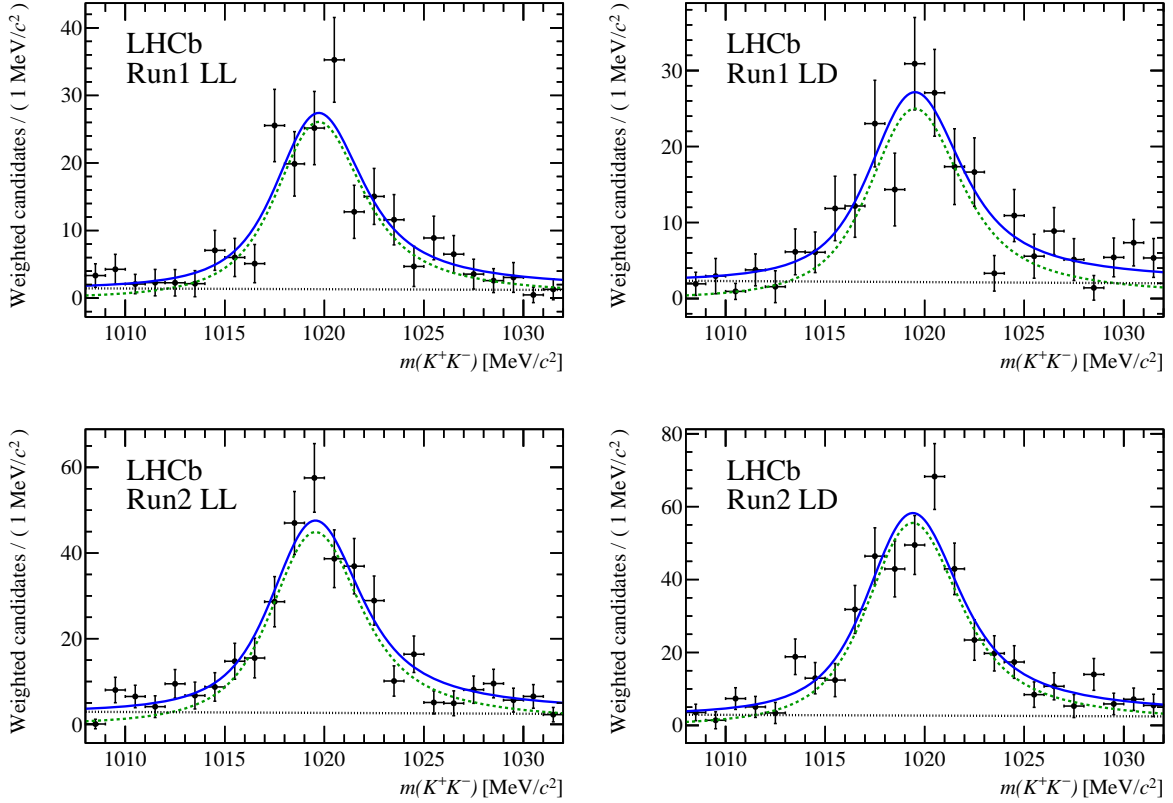


Figure 4: Fits to the invariant-mass distribution $m(K^+ K^-)$ of $B^0 \rightarrow \phi K_S^0$ data weighted using the s Plot technique. The blue curve represents the complete model, the signal ϕ component is given in green (dashed), and the background $f_0(980) \rightarrow K^+ K^-$ model is shown in black (dotted).

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