

# 1 Rare decays of flavoured mesons at the LHC

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In absence of strong, direct signs of New Physics at the LHC, rare decays of heavy flavoured hadrons constitute an ideal laboratory for indirectly exploring energies beyond those of the LHC in order to look for deviations from the Standard Model. The main results regarding flavour changing neutral current transitions obtained at the LHC are presented here, with particular emphasis put on  $b \rightarrow s$  transitions, in which tensions with the Standard Model have been observed.

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## 1. Introduction

Quarks and leptons in the Standard Model (SM) of particle physics are organized in *flavours*. Changes between flavours can only occur through the charged current weak interaction—that is, mediated by a  $W$  boson—and transitions between same-charge fermions must occur through second order, loop processes [1]. Since the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix [2, 3], which governs transitions between flavours, is found to be approximately diagonal, generation-changing processes are suppressed. As a consequence, processes involving *flavour changing neutral currents* (FCNC) are predicted to be rare within the SM.

Observables related to these decays—branching fractions,  $CP$  asymmetries, kinematic distributions, among others—can be predicted in the SM with low theoretical uncertainty. Many models of New Physics (NP) predict noticeable differences in the measured quantities, making the study of rare decays of flavoured hadrons an ideal laboratory for studying physics Beyond the Standard Model. In particular, loop-mediated processes allow indirect access to quantum corrections from degrees of freedom at larger scales and provide excellent complementarity to direct searches of new phenomena.

FCNC transitions with  $|\Delta B| = |\Delta S| = 1$  are described by a low energy effective field theory in the form of an Operator Product Expansion [4–6]:

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha}{4\pi} \sum_i \{C_i O_i + C'_i O'_i\}, \quad (1.1)$$

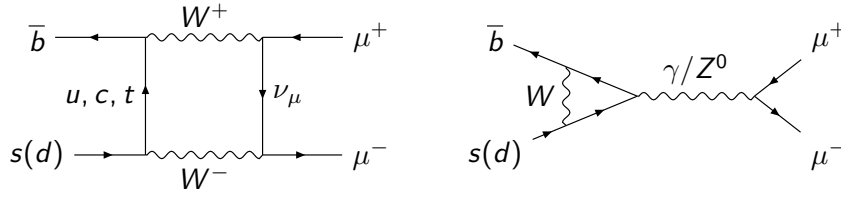
where  $G_F$  is the Fermi constant,  $V_{ij}$  are CKM matrix elements and  $\alpha_e$  is the fine structure constant. The  $O_i^{(\prime)}$  local operators take into account all possible left(right)-handed Lorentz structures and come with their corresponding Wilson coefficients  $C_i^{(\prime)}$ . The fact that the charged current interaction is left-handed implies that the Wilson coefficients corresponding to the right-handed  $O'_i$  operators are suppressed by  $\mathcal{O}(m_s/m_b)$ .

The most important operators for the study of rare  $b \rightarrow s\gamma$ ,  $b \rightarrow s\ell^+\ell^-$  and  $b \rightarrow \ell^+\ell^-$  decays<sup>1</sup> are

$$\begin{aligned} O_7^{(\prime)} &= \frac{m_b}{e} \bar{s} \sigma^{\mu\nu} P_{R(L)} b F_{\mu\nu}, \\ O_9^{(\prime)} &= \bar{s} \gamma_\mu P_{R(L)} b \bar{\ell} \gamma^\mu \ell, \\ O_{10}^{(\prime)} &= \bar{s} \gamma_\mu P_{R(L)} b \bar{\ell} \gamma^\mu \gamma_5 \ell, \\ O_S^{(\prime)} &= \bar{s} P_{R(L)} b \bar{\ell} \ell, \\ O_P^{(\prime)} &= \bar{s} P_{R(L)} b \bar{\ell} \gamma_5 \ell, \end{aligned} \quad (1.2)$$

where  $P_{L(R)}$  denotes the left(right)-handed chiral projector and  $F_{\mu\nu}$  the electromagnetic field strength tensor. Radiative  $b \rightarrow s\gamma$  transitions are controlled by the *photon penguin* operator  $O_7^{(\prime)}$ ; semileptonic  $b \rightarrow s\ell^+\ell^-$  processes receive contributions from  $O_7^{(\prime)}$  and the *electroweak penguin* operators  $O_9^{(\prime)}$  and  $O_{10}^{(\prime)}$ ; and the fully leptonic  $b \rightarrow \ell^+\ell^-$  decays are ruled by  $O_{9,10}^{(\prime)}$  and the *scalar* and *pseudoscalar penguin* operators  $O_S^{(\prime)}$  and  $O_P^{(\prime)}$ .

<sup>1</sup> $b \rightarrow d\gamma$  and  $b \rightarrow d\ell^+\ell^-$  transitions are treated analogously, but are more suppressed due to the replacement of  $V_{tb}V_{ts}^*$  by  $V_{td}V_{td}^*$  in Eq. 1.1.



**Figure 1:** Feynman diagrams of the  $B_s^0 \rightarrow \mu^+ \mu^-$  and  $B^0 \rightarrow \mu^+ \mu^-$  decays.

31 Effects from NP can be easily incorporated in Eq. 1.1 by adding an extra term for each operator

$$\mathcal{H}_{\text{eff}}^{\text{NP}} = \sum_i \frac{C_i^{\text{NP}}}{\Lambda_{\text{NP}}^2} O_i^{\text{NP}}, \quad (1.3)$$

32 where  $\Lambda_{\text{NP}}$  is the NP scale.

33 Measurements of different observables and decay modes can then be combined in *global fits*  
 34 of Wilson coefficients and used to constrain NP contributions in FCNC. Hence, the strategy in the  
 35 indirect searches for NP in rare decays is to perform many measurements, study their discrepancies  
 36 and agreements with the SM through global fits, and try to solve the puzzle: how do we explain all  
 37 these results in a single model, *i.e.*, which is the structure of the model beyond the SM?

38 The current situation in terms of rare decay results and the constraints they impose on NP are  
 39 discussed in the next sections.

## 40 2. Fully leptonic $b \rightarrow \ell^+ \ell^-$ decays

41 The dileptonic  $B_s^0 \rightarrow \mu^+ \mu^-$  and  $B^0 \rightarrow \mu^+ \mu^-$  decays are suppressed due to their loop only  
 42 diagrams, the involved CKM matrix elements and the particular helicity structure of a pseudoscalar  
 43 decaying into a pair of leptons (Fig. 1), and thus are very rare in the SM. More precisely, the  
 44 time-integrated branching fractions are predicted to be [7]

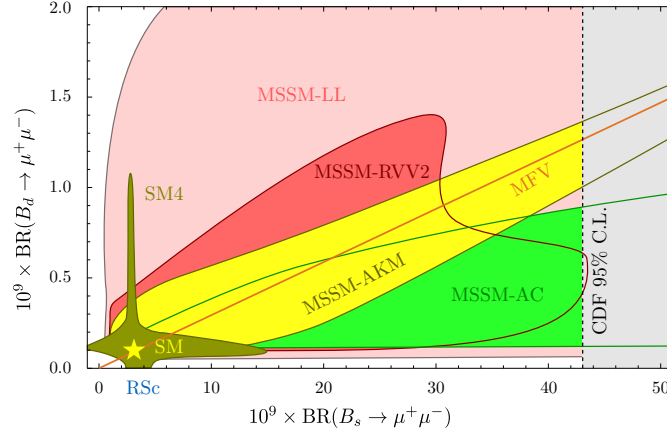
$$\begin{aligned} \mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) &= (3.66 \pm 0.23) \times 10^{-9}, \\ \mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) &= (1.06 \pm 0.09) \times 10^{-10}, \end{aligned} \quad (2.1)$$

45 where the main uncertainties come from the knowledge of the decay constants and the CKM matrix  
 46 elements. Several NP models including sizeable scalar or pseudoscalar operators can enhance the  
 47 branching fractions of one or both the  $B_s^0$  and the  $B^0$  modes [8], as shown in Fig. 2.

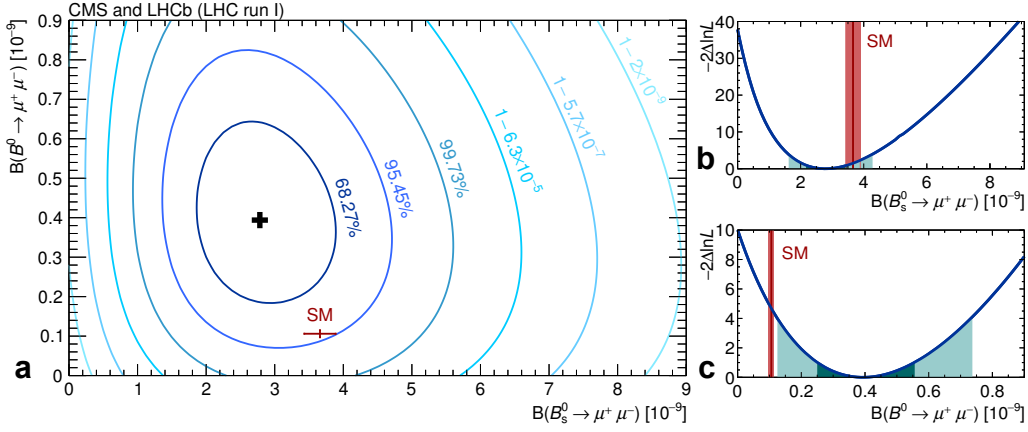
48 Culminating a story started more than thirty years ago by the CLEO collaboration [9], the  
 49 LHCb and CMS collaborations performed a combined analysis of the data collected during Run I,  
 50 and reported the first observation of  $B_s^0 \rightarrow \mu^+ \mu^-$  with a significance of  $6.2\sigma$  and an evidence for  
 51  $B^0 \rightarrow \mu^+ \mu^-$  at  $3\sigma$ . The measured branching fractions [10]

$$\begin{aligned} \mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) &= (2.8_{-0.6}^{+0.7}) \times 10^{-9}, \\ \mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) &= (3.9_{-1.4}^{+1.6}) \times 10^{-10}, \end{aligned} \quad (2.2)$$

52 are compatible with the SM at  $1.2\sigma$  and  $2.2\sigma$ , respectively, as shown in Fig. 3. Despite this fact,  
 53 these results are very important as they put strong constraints on NP scenarios [11].



**Figure 2:** Correlation between the branching fractions of  $B_s^0 \rightarrow \mu^+ \mu^-$  and  $B_d^0 \rightarrow \mu^+ \mu^-$  in several NP models [8]. The grey area was the one excluded experimentally before the LHC.



**Figure 3:** Likelihood contours in the  $\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$  vs  $\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)$  plane (a), with variations of the  $-2\Delta \ln \mathcal{L}$  test statistic for each of the modes shown in (b) and (c) [10].

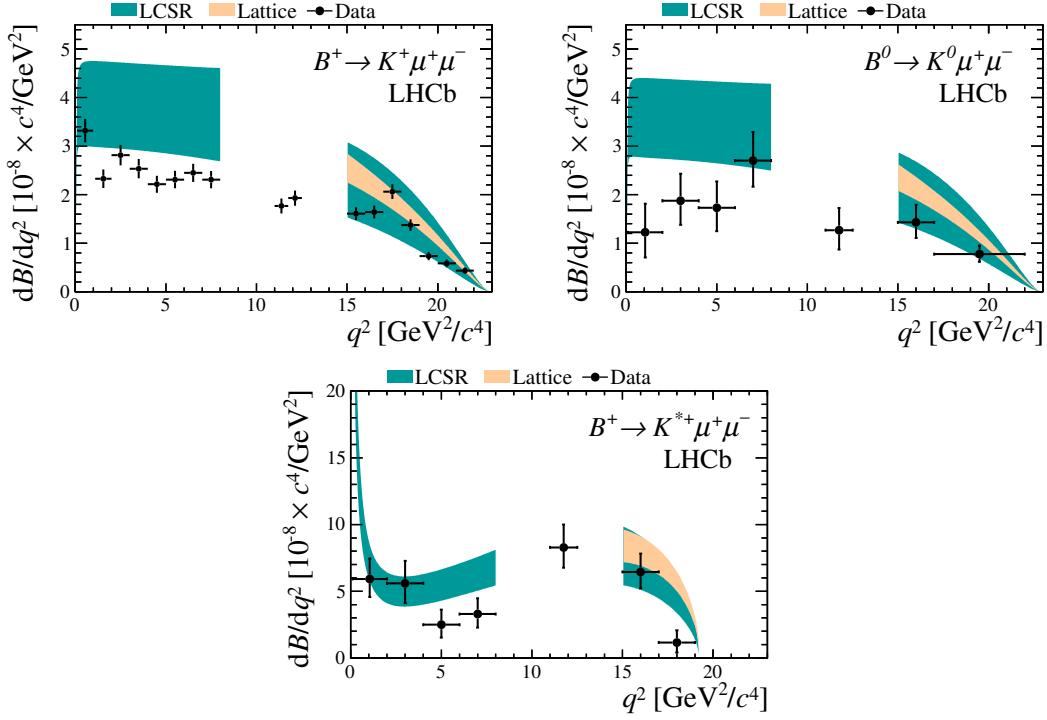
54 The ATLAS collaboration has also found compatible results with CMS and LHCb [12]:

$$\begin{aligned} \mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) &= (0.9_{-0.8}^{+1.1}) \times 10^{-9}, \\ \mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) &< 4.2 \times 10^{-10} \text{ at } 95\% \text{ C.L.} \end{aligned} \quad (2.3)$$

### 55 3. Semileptonic $b \rightarrow s(d)\ell^+\ell^-$ decays

56 Semileptonic  $b \rightarrow s(d)\ell^+\ell^-$  decays have been extensively studied at the LHC, where the signal  
57 yields of many modes are large enough for precision measurements. Results on differential branching  
58 fractions and angular distributions, as well as ratios between muonic and electronic decays, have  
59 provided many constraints on NP and have yielded interesting tensions with the SM, and will be  
60 discussed in the following.

61 **Differential branching fractions** The LHC measurements of the branching fractions of  $B \rightarrow$   
62  $K\mu^+\mu^-$  [13],  $B \rightarrow K^*\mu^+\mu^-$  [13–16],  $B_s^0 \rightarrow \phi\mu^+\mu^-$  [17] and  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  [18], performed in

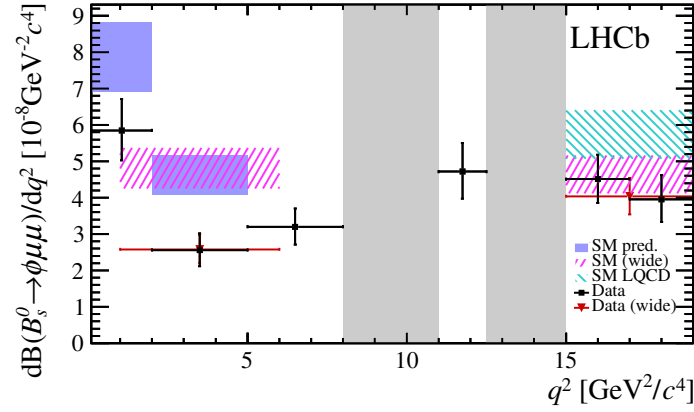


**Figure 4:** Differential branching fraction in bins of  $q^2$  of the  $B^+ \rightarrow K^+ \mu^+ \mu^-$  (top left),  $B^0 \rightarrow K^0 \mu^+ \mu^-$  (top right) and  $B^+ \rightarrow K^{*+} \mu^+ \mu^-$  (bottom) decays as measured by LHCb [13]. Theoretical predictions obtained with LCSR [19] and lattice QCD [20, 21] calculations are shown for comparison.

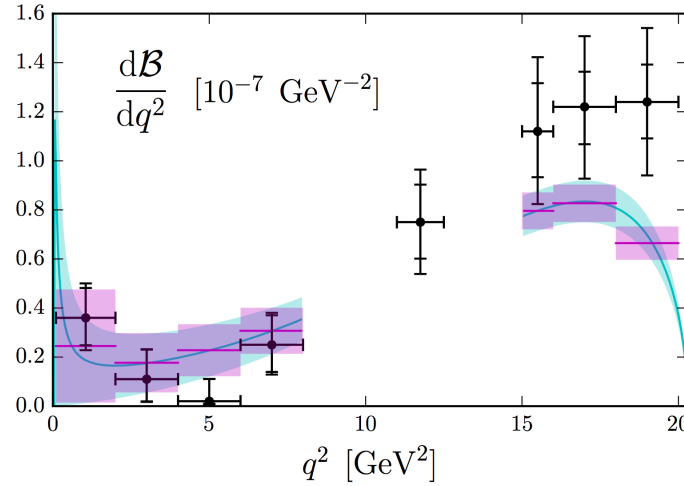
63 bins of the dilepton mass squared ( $q^2$ ), are much more precise than the corresponding theoretical  
 64 predictions, sensitive to hadronic uncertainties in the form factors. These theoretical uncertainties,  
 65 typically of the order of 30%, limit the sensitivity to NP, but are expected to improve in the future  
 66 with progress from lattice QCD.

67 While some precision results from the large datasets collected by LHCb point towards lower  
 68 values than the SM prediction in some cases, as shown in Figs. 4 and 5, the measurements are  
 69 in general compatible with the SM prediction. The branching fractions of the  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ ,  
 70 measured both by CMS [15, 16] and LHCb [14], and the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decays, affected by large  
 71 form factor uncertainties, don't show any deviations from the SM prediction, as shown in Figs. 6  
 72 and 7. The latest LHCb result on  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  [14] is the first one to include a measurement of  
 73 the  $S$ -wave component in the  $K^+ \pi^-$  system, in contrast with previous studies, which considered  
 74 it small and treated it as a systematic uncertainty. As the theory predictions are made for purely  
 75 resonant  $P$ -wave, an accurate assessment of the  $S$ -wave fraction is critical, and, as can be seen on  
 76 the left plot in Fig. 7, agreement between the measurement and the SM prediction from lattice QCD  
 77 is good.

78 As a complement to the measurement of  $b \rightarrow s \ell^+ \ell^-$  transitions,  $b \rightarrow d \ell^+ \ell^-$  decays, suppressed  
 79 by  $|V_{td}/V_{ts}|^2$ , allow to test whether NP—if any—is minimally flavour violating (MFV). The LHCb  
 80 collaboration has the  $B^+ \rightarrow \pi^+ \mu^+ \mu^-$  [26] and has found good compatibility with the SM predictions,  
 81 as can be seen in Fig. 8, with the uncertainty in the result still dominated by statistics. Further  
 82 improvements in this study, as well as observations of more  $b \rightarrow d \ell^+ \ell^-$  modes, are expected in the



**Figure 5:** Differential branching fraction in bins of  $q^2$  of the  $B_s^0 \rightarrow \phi \mu^+ \mu^-$  decay as measured by LHCb [17]. The SM prediction with LCSR [22, 23] is overlaid in purple and magenta for different  $q^2$  binning schemes, while the LQCD prediction for high- $q^2$  is showed in cyan [21].

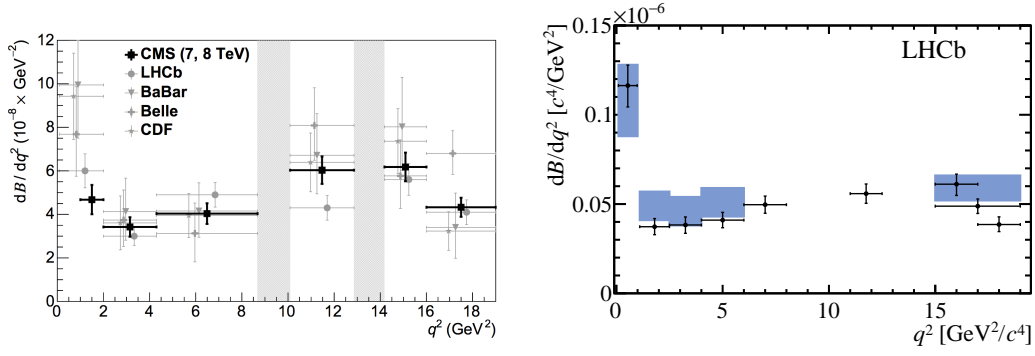


**Figure 6:** Differential branching fraction in bins of  $q^2$  of the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decay as measured by LHCb [18]. The plot, obtained from Ref. [24], shows an updated SM prediction from lattice QCD with respect to that included in Ref. [18].

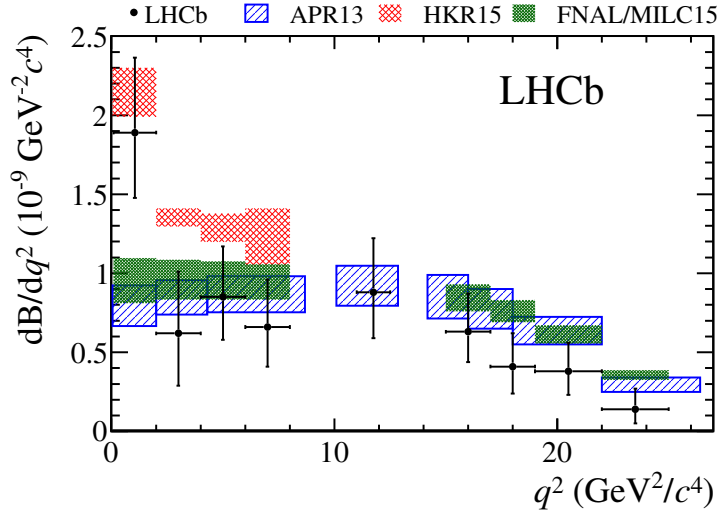
83 coming years.

84 **Angular distributions** The angular distributions of  $b \rightarrow s \ell^+ \ell^-$  decays provide a large number of  
 85 observables with different sensitivities to different types of NP. In particular, each of the observables  
 86 arising from the angular distributions—or combinations thereof—has a different dependence on the  
 87 Wilson coefficients—mainly  $C_7^{(\prime)}$ ,  $C_9^{(\prime)}$  and  $C_{10}^{(\prime)}$ —and form factors.

88 The  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  angular distribution depends on three angles: the direction of the  $\mu^+$  ( $\mu^-$ )  
 89 with respect to the  $B^0$  ( $\bar{B}^0$ ) in the dimuon rest frame ( $\theta_l$ ), the direction of the kaon with respect to  
 90 the  $B$  in the  $K\pi$  system rest frame ( $\theta_K$ ), and the angle between the dimuon plane and the  $K\pi$  system



**Figure 7:** On the left, differential branching fraction in bins of  $q^2$  of the  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  as measured by CMS, LHCb, the  $B$  factories and CDF, taken from Ref. [16]. On the right, latest differential branching fraction LHCb result in bins of  $q^2$  of the purely resonant  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  decay, after measuring the  $S$ -wave component [14]; the overlaid theory prediction is from Refs. [23, 25].

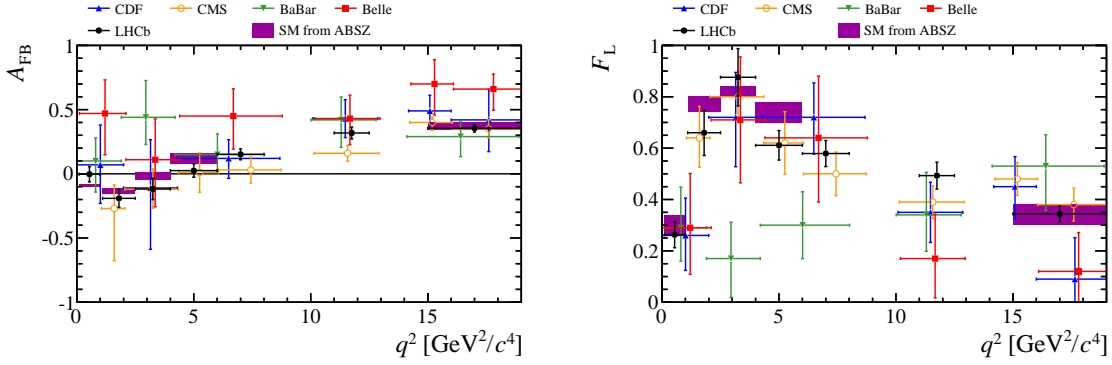


**Figure 8:** Differential branching fraction in bins of  $q^2$  of the  $B^+ \rightarrow \pi^+ \mu^+ \mu^-$  decay as measured by LHCb [26], compared with the APR13 [27], HKR15 [28] and lattice QCD FNAL/MILC15 [29] SM predictions.

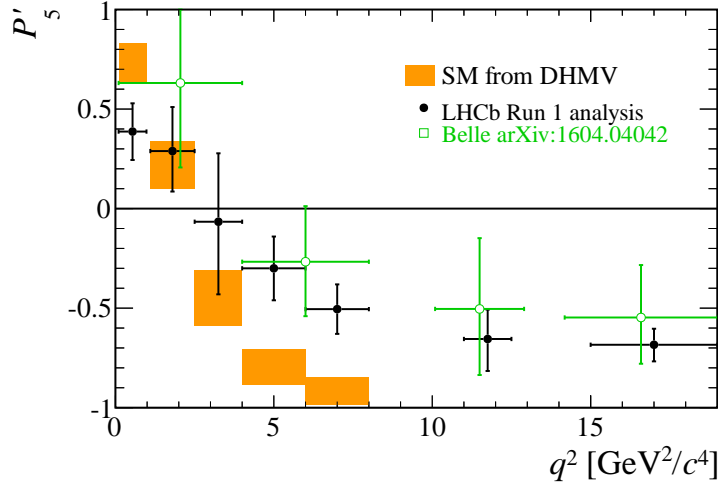
91 plane ( $\phi$ ). The  $CP$  averaged differential decay rate in terms of these angles and  $q^2$  can be written as:

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\ \left. + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\varphi \right. \\ \left. + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \varphi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \varphi \right. \\ \left. + \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \varphi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \varphi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\varphi \right], \quad (3.1)$$

92 where  $S_i$ ,  $F_L$  (fraction of longitudinal polarization of the  $K^{*0}$ ) and  $A_{FB}$  (forward-backward asymmetry



**Figure 9:** Forward-backward asymmetry of the dimuon system,  $A_{FB}$ , (left) and fraction of longitudinal polarization of the  $K^{*0}$  mesons,  $F_L$ , (right) in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  decays in bins of  $q^2$  as measured by the CDF, BaBar, Belle, CMS and LHCb collaborations, taken from Ref. [34]. The SM prediction is obtained from Ref. [23].



**Figure 10:** The optimized angular observable  $P'_5$  in bins of  $q^2$  as measured by LHCb and Belle, overlaid with the SM prediction from Ref. [36].

93 of the dilepton system) are the observables to be measured. It is possible to build theoretically  
 94 cleaner observables by combining helicity amplitudes to exploit cancellations. In particular, the  $P'_i$   
 95 set of observables [30], such as

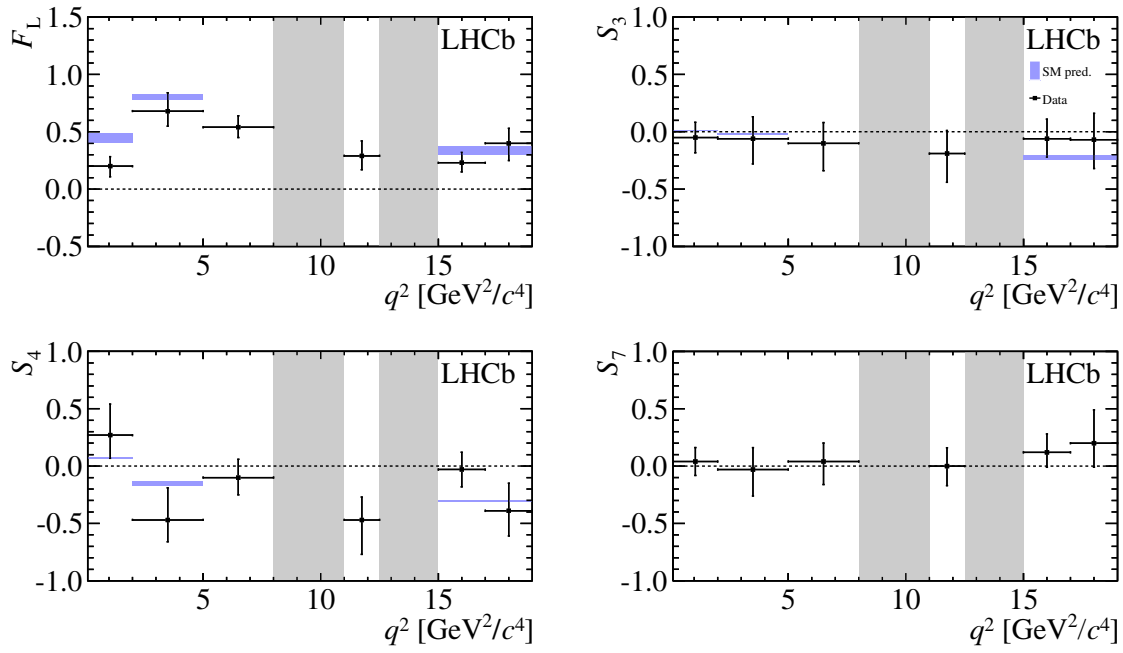
$$P'_5 = \frac{S_5}{\sqrt{F_L(1-F_L)}}, \quad (3.2)$$

96 focuses on reducing the dependence on form factors, thus reducing the theoretical uncertainty.

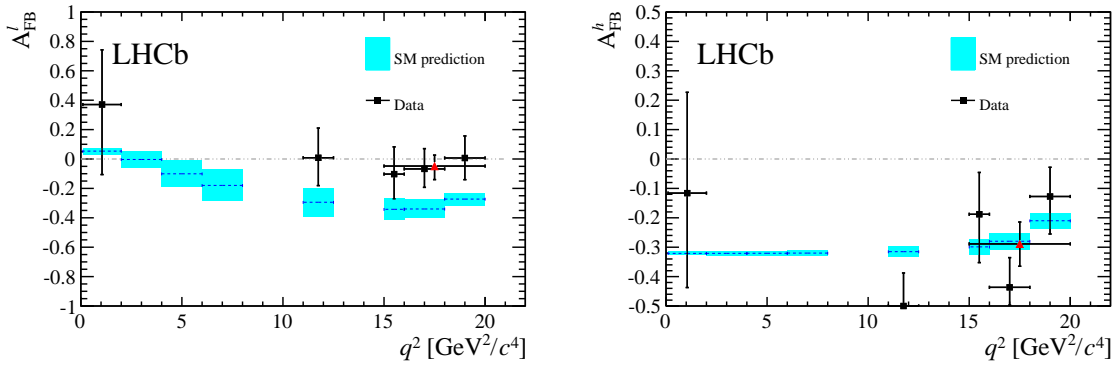
97 While the measurements of the standard  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  angular observables performed by  
 98 CDF [31], BaBar [32], Belle [33], CMS [16] and LHCb [34] have been found to be compatible with  
 99 the SM (see Fig. 9), the optimized  $P'_5$  observable, measured by LHCb and Belle [35], presents a  
 100 large local discrepancy between data and the SM prediction, shown in Fig. 10, at the level of  $3.7\sigma$ .

101 Measurements of simplified angular distributions in bins of  $q^2$  carried out by LHCb in the  
 102  $B_s^0 \rightarrow \phi \mu^+ \mu^-$  [17] and  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  [18] decays don't show large deviations from the SM, and





**Figure 11:** Fraction of longitudinal polarization of the  $K^{*0}$  mesons,  $F_L$ ,  $S_3$ ,  $S_4$  and  $S_9$  distributions in  $B_s^0 \rightarrow \phi \mu^+ \mu^-$  decays in bins of  $q^2$  as measured by LHCb [17]. The SM prediction is obtained from Refs. [22, 23].



**Figure 12:** Forward-backward asymmetry of the dimuon system,  $A_{\text{FB}}^l$ , (left) and forward-backward asymmetry of the hadron system,  $A_{\text{FB}}^h$ , (right) in  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decays in bins of  $q^2$  as measured by LHCb [18]. The SM prediction is obtained from Ref. [37].

103 can be seen in Figs. 11 and 12, respectively.

104 Additionally, the LHCb collaboration has studied the angular distribution of the  $B^0 \rightarrow K^{*0} e^+ e^-$   
 105 decay in the low- $q^2$  region [38], performing some angular transformations to reduce the number of

106 angular observables on account for the limited signal yield. The obtained results,

$$\begin{aligned}
 F_L &= 0.16 \pm 0.06 \pm 0.03, \\
 A_T^{\text{Re}} &= 0.10 \pm 0.18 \pm 0.05, \\
 A_T^{(2)} &= -0.23 \pm 0.23 \pm 0.05, \\
 A_T^{\text{Im}} &= 0.14 \pm 0.22 \pm 0.05,
 \end{aligned}
 \tag{3.3}$$

107 are compatible with the SM predictions [39,40] and help constrain the  $C_7^{(\prime)}$  Wilson coefficient thanks  
 108 to the low lepton mass.

109 **Global fits** With the wealth of measurements produced at the LHC, including some tensions with  
 110 the SM predictions, it becomes possible to gain insight on possible NP contributions to the Wilson  
 111 coefficients through the combination of these measurements, *i.e.*, performing global fits of  $b \rightarrow s$   
 112 observables. Taking into account more than eighty observables from  $b \rightarrow \ell^+ \ell^-$ ,  $b \rightarrow s(d) \ell^+ \ell^-$  and  
 113  $b \rightarrow s \gamma$  transitions, measured by six experiments, most global fits [41–44] prefer a negative NP  
 114 contribution  $C_9 \sim -1$ , with other NP parameters consistent with zero, as shown in Fig. 13. While  
 115 this destructive contribution would better accommodate the data by reducing the branching fraction  
 116 of  $b \rightarrow s(d) \mu^+ \mu^-$  decays and modifying the angular distribution of  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  to be more  
 117 consistent with the  $P_5'$  measurements, it is worth noting that these fits are still compatible with the  
 118 SM prediction at  $3 - 4.6\sigma$ .

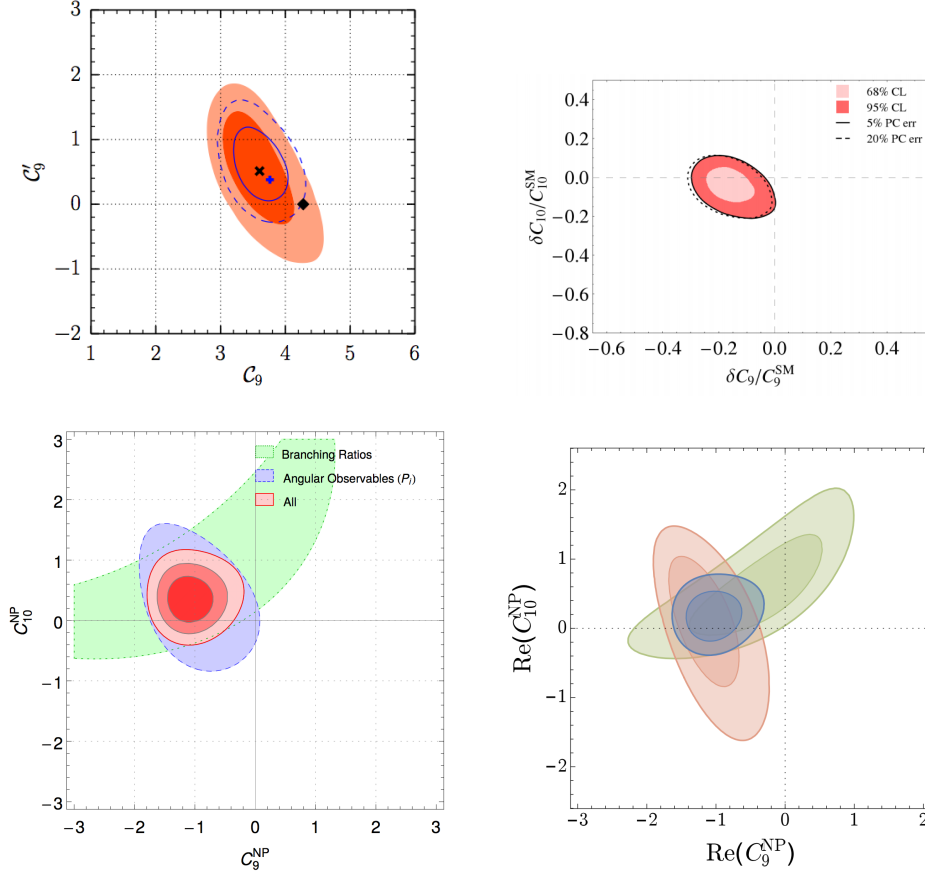
119 Further measurements  $b \rightarrow s \ell^+ \ell^-$  transitions, in particular of angular observables, with the  
 120 LHC Run II dataset, will be crucial in the clarification of the real nature of this tension—currently  
 121 one of the most significant in flavour physics.

122 **Lepton flavour universality** Another interesting tension with the SM, complementary to those  
 123 described above, arises from the studies of lepton flavour universality. In the SM, with the exception  
 124 of the Higgs boson, particles couple equally to different lepton flavours. As a consequence, ratios of  
 125 decay rates such as

$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)},
 \tag{3.4}$$

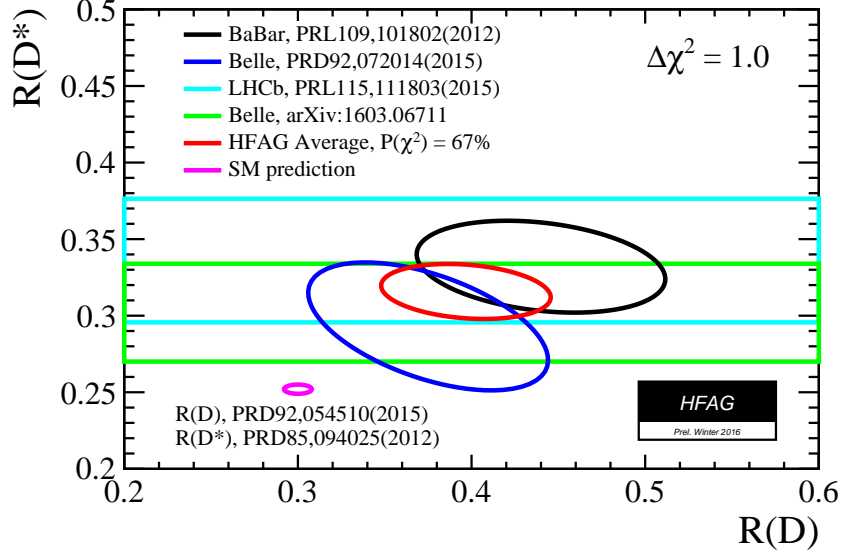
126 are expected to be very close to unity, save from very small Higgs penguin contributions and  
 127 difference in phase space due to the lepton mass. The LHCb collaboration has measured  $R_K$  in  
 128 the  $1 < q^2 < 6 \text{ GeV}^2/c^4$  range to be  $0.745_{-0.074}^{+0.090} (\text{stat}) \pm 0.036 (\text{syst})$  [45],  $2.6\sigma$  away from the SM  
 129 prediction of  $R_K = 1.0003 \pm 0.0001$  [46]. While the significance of this discrepancy is not enough  
 130 to be considered even as evidence, the combined  $4.0\sigma$  enhancement, shown in Fig. 14, of  $\tau$  with  
 131 respect to  $\mu$  in tree-level  $B^+ \rightarrow D^{(*)} \ell^+ \nu_\ell$  decays observed by BaBar, Belle and LHCb [47], has  
 132 prompted great theoretical interest in these types of measurements.

133 **Interpretation** While the results discussed so far are basically compatible with the SM picture, a  
 134 pattern of NP seems to start emerging in flavour physics, with two different sets of anomalies in  
 135  $b \rightarrow s$  transitions: angular distributions of  $b \rightarrow s \ell^+ \ell^-$  decays and lepton flavour universality violation.  
 136 These point to a preference for sizable NP in vector leptonic couples and lepton non-universality,  
 137 leaving room for the contribution of non-SM right-handed currents and, thus, a non-MFV flavour  
 138 sector.



**Figure 13:** Results from the global fits to  $b \rightarrow s$  observables: the top left plot, from Ref. [41], shows the  $C_9 - C_9'$  plane, including NP contributions, with the SM prediction represented as a black dot; on the top right, taken from Ref. [42] one can see the one- and two-sigma contours of the relative NP contributions in  $C_9$  and  $C_{10}$ , with the SM being at  $(0, 0)$ ; the bottom left plot, from Ref. [43], shows, in red, directly the contours of the value of the NP contributions in  $C_9$  and  $C_{10}$ , highlighting as well the contributions coming only from angular observables (blue) and branching fractions (green); the bottom right plot, taken from Ref. [44], shows, in blue, the contours of the real values of the NP contributions in  $C_9$  and  $C_{10}$ , also highlighting the contributions coming only from angular observables (red) and branching fractions (green).

139 Several types of models have been built to explain these hints of anomalies, including the  
 140 existence  $Z'$  bosons [54,55] or leptoquarks [56,57], as well as the gauged  $L_\tau - L_\mu$  SM extension [58,  
 141 59]. There exists, however, concern in the theory community about to which extent the long-  
 142 distance contributions from  $c\bar{c}$  resonances pollute the observables and how factorisation holds in  
 143 this case [60]; it is hard to answer those concerns from first principles, so it is necessary to use  
 144 models to try to measure the size of the  $c\bar{c}$  pollution. While this could affect the uncertainty of  
 145 the SM prediction in the case of angular observables, reducing the significance of the anomalies,  
 146 measurements such as  $R_K$  are mostly free of this type of hadronic uncertainties.



**Figure 14:** One sigma contour (red) of the combination of the BaBar (black) [48], Belle (green and dark blue) [49, 50] and LHCb (cyan) [51] results of the ratio of tauonic and muonic channels in  $B^+ \rightarrow D\ell^+\nu_\ell$  and  $B^+ \rightarrow D^*\ell^+\nu_\ell$  decays, taken from Ref. [47], with the SM prediction from Refs. [52, 53] overlaid in magenta.

#### 147 4. Other rare decays

148 **Rare charm decays** The short-distance contributions to rare  $c \rightarrow u$  transitions are very small due  
 149 to the stronger GIM suppression ( $m_b \ll m_t$ ), so rare charm decays are dominated by long-distance  
 150 contributions.

151 While the current state of measurements, shown in Fig. 15, is still not close to the SM predictions,  
 152 typically of  $< \mathcal{O}(10^{-9})$ , large improvements on the limits have been achieved at the LHC. In particu-  
 153 lar, LHCb has significantly improved the limits in the searches for the FCNC  $D^0 \rightarrow \pi^+\pi^-\mu^+\mu^-$  [61],  
 154  $D^0 \rightarrow \mu^+\mu^-$  [62] and  $D_{(s)}^+ \rightarrow \pi^+\mu^+\mu^-$  [63] decays, and the LFV  $D^0 \rightarrow e^\pm\mu^\mp$  decay [64]. Addi-  
 155 tionally, it has performed the first observation of the  $D^0 \rightarrow K^-\pi^+\mu^+\mu^-$  decay in the  $\rho$ - $\omega$  region  
 156 in  $\mu^+\mu^-$  mass [65], necessary to understand the long-distance, tree-level contributions of vector  
 157 resonances to the rare  $D \rightarrow X\mu^+\mu^-$  mode.

158 Great improvements are expected in the Run II of the LHC thanks to the improved trigger  
 159 strategy at LHCb—increasing the sample size by more than proportionally to the luminosity—with  
 160 the potential for reaching even more interesting regions in the LHCb upgrade.

161 **Rare strange decays** While the LHC is not the main player in rare kaon physics, a very competi-  
 162 tive result in the search for the  $K_s^0 \rightarrow \mu^+\mu^-$  decay was published by the LHCb collaboration using  
 163 data from 2011 [66]. The limit on the branching fraction of this decay,

$$\mathcal{B}(K_s^0 \rightarrow \mu^+\mu^-) < 9 \times 10^{-9} \text{ at } 90\% \text{ C.L.}, \quad (4.1)$$

164 is still far from the SM prediction of  $\mathcal{B}(K_s^0 \rightarrow \mu^+\mu^-) = (5.1 \pm 1.5) \times 10^{-12}$  [67], but the LHC has  
 165 the potential of reaching the most interesting region of study, in which it will be possible to assess  
 166 possible NP short-distance effects in the  $K_L^0 \rightarrow \mu^+\mu^-$  decay.

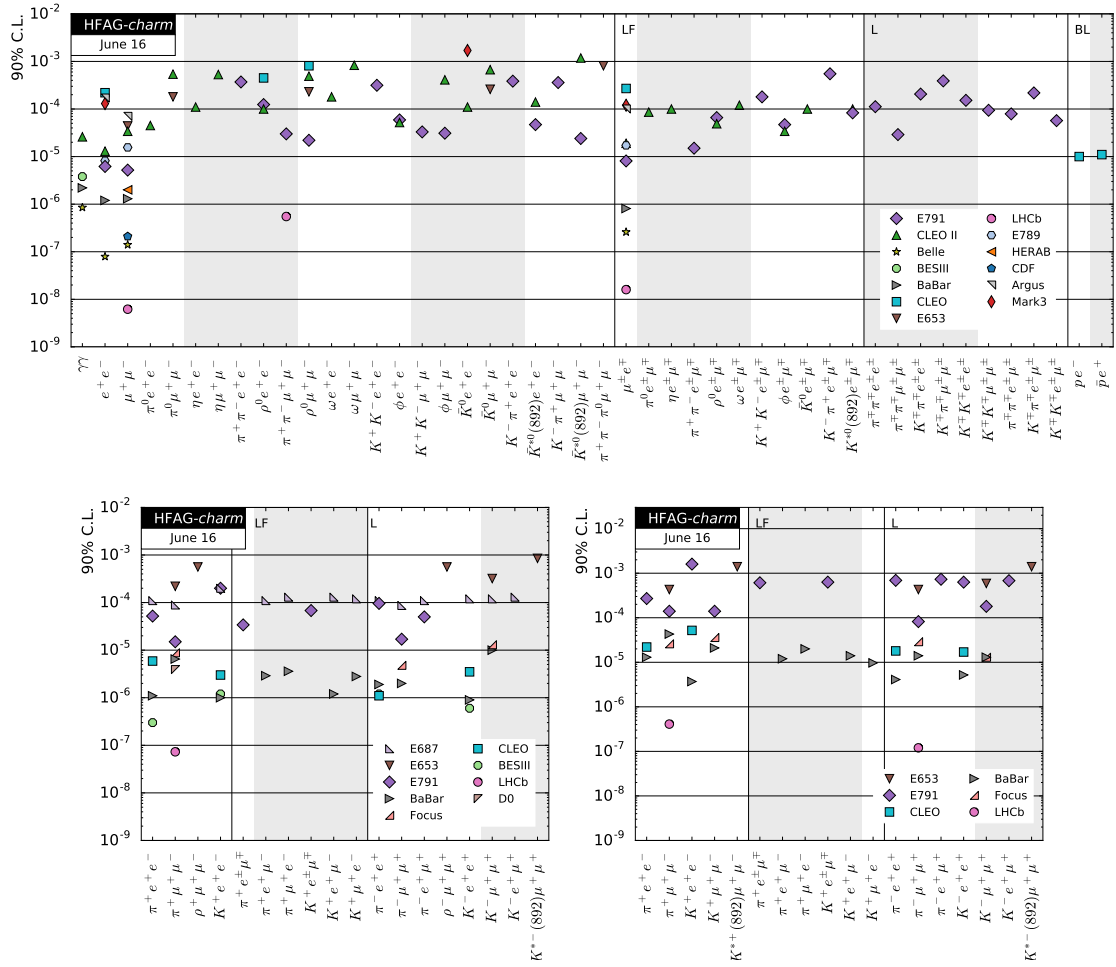
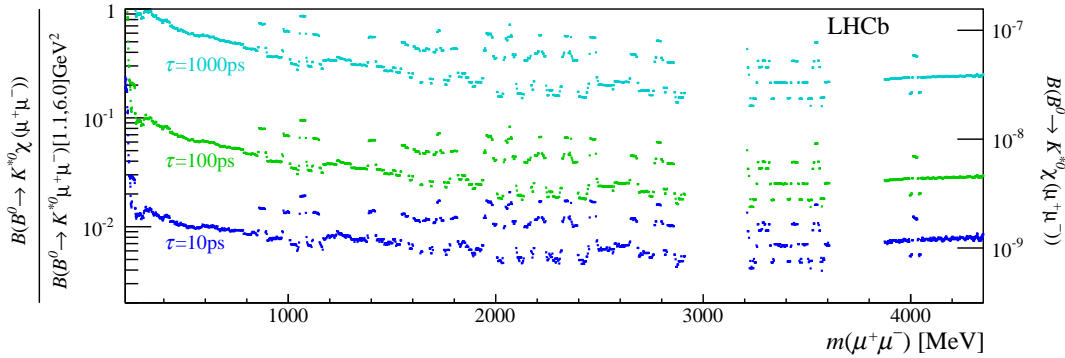


Figure 15: Status of rare charm searches for  $D^0$  (top),  $D^+$  (bottom left) and  $D_s^+$  (bottom right) mesons [47].

167 The limit  $K_s^0 \rightarrow \mu^+ \mu^-$  on shows, nonetheless, the potential of LHCb to produce significant  
 168 results in the following years—especially in its Upgrade phase—such as the study of the  $\Sigma^+ \rightarrow$   
 169  $p \mu^+ \mu^-$  decay to assess the HyperCP anomaly [68], the update of the limit  $K_s^0 \rightarrow \mu^+ \mu^-$  with the  
 170 full Run I dataset, and the exploration of further modes, including those with electrons in their final  
 171 state. These all will contribute to the exciting prospects from non-LHC experiments: NA62 took its  
 172 first data in 2015 and is currently getting ready for its 2016 run, while KOTO is expecting to reach  
 173 SM sensitivity in the search for the  $K_L^0 \rightarrow \pi^0 \nu \nu$  decay by 2018.

174 **Hidden sector** The  $b \rightarrow s$  penguin decay is also an excellent place to search for low-mass hidden  
 175 sector particles, which can mix with the Higgs boson and then decay in SM final states. The LHCb  
 176 collaboration has performed a search for hidden-sector bosons in  $B^0 \rightarrow K^{*0} \chi (\rightarrow \mu^+ \mu^-)$  decays  
 177 allowing—but not requiring—non zero lifetime of the  $\mu^+ \mu^-$  system [69]. The search at different  
 178 lifetimes, covering prompt and displaced  $\mu^+ \mu^-$  vertices and shown in Fig.16, found no significant  
 179 signal and allowed both to set model-independent limits and to constrain specific models, such as  
 180 the ones described in Refs. [70–73].



**Figure 16:** Upper limit at 95% C.L. for the  $B^0 \rightarrow K^{*0} \chi(\rightarrow \mu^+ \mu^-)$  decay as a function of the  $\mu^+ \mu^-$  mass, obtained at different lifetimes of the  $\mu^+ \mu^-$  system [69].

## 181 5. Conclusions

182 Rare flavoured decay observables place strong constraints on many NP models, allowing to  
 183 probe higher energies than direct searches due to the fact that they are forbidden at tree-level in the  
 184 SM. A large number of analyses performed using data collected during Run I of the LHC have lead  
 185 to substantial improvement in the precision of several key observables. Results like the observation  
 186 of the  $B_s^0 \rightarrow \mu^+ \mu^-$  decay or the study of angular observables in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ , while largely  
 187 consistent with the SM, have given rise to interesting tensions with the SM expectations.

188 While there is not significant NP evidence from a single measurement, global fits to rare decays  
 189 observables point to a pattern that favours the existence of NP. In this situation, it is necessary to  
 190 continue improving the precision and to add measurements, both of new, more sensitive observables,  
 191 and of new decay modes. An effort in the theory side, especially in the reduction of uncertainties  
 192 due to hadronic effects, will also be needed.

193 In a nutshell, the main goal in the next few years will be to try to confirm these tensions of  
 194 the SM, find the first evidences of NP and then study their features to determine which models are  
 195 favoured by the data.

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