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**$\bar{B}B$  INCLUSIVE CROSS-SECTION IN 320 GeV  
 $\pi^-$  URANIUM INTERACTIONS**

WA 78 Collaboration

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## ABSTRACT

The inclusive cross-section for  $B\bar{B}$  production by 320 GeV  $\pi^-$  on uranium has been measured, assuming different production models and a variable amount of  $B_0 - \bar{B}_0$  mixing. A comparison of our results with those of the NA10 Collaboration is performed. The  $J/\psi$  inclusive production cross-section has also been measured in our experiment and agrees well with existing data, thus confirming the accuracy of our overall normalization.

## 1. Introduction

The experimental study of heavy-flavour hadroproduction and decay provides a useful test of Quantum Chromodynamics (QCD) and electroweak theory. In particular, the determination of the inclusive cross-section for beauty meson production establishes the contribution of various basic QCD subprocesses to the production mechanism. The first direct evidence of beauty hadroproduction in a fixed-target experiment was the observation of the production and decay of a  $B\bar{B}$  pair in a nuclear emulsion target exposed to a 350 GeV  $\pi^-$  beam at the CERN Super Proton Synchrotron (SPS) [1]. Discrepant results were reported by two different experiments at the CERN Intersecting Storage Rings pp collider [2, 3]. More recently, the UA1 Collaboration [4] at the CERN  $p\bar{p}$  Collider, and the NA10 Collaboration [5] in a fixed-target experiment, have measured the hadroproduction of  $B\bar{B}$  pairs.

In the present paper we report the final results on inclusive  $B\bar{B}$  production cross-section obtained by the WA78 Collaboration. Data were taken at the SPS with a 320 GeV  $\pi^-$  beam on a U target. A preliminary analysis of these data has already been published [6, 7]. For the present analysis we have improved the absolute normalization of the experiment, and measured the inclusive cross-section for  $J/\psi$  production. We compare this measurement with those obtained by other experiments with  $\pi^-$  beams on different target materials and at different energies, taking into account the  $A$ -dependence and energy dependence of the  $J/\psi$  production cross-section. We find very good agreement with a cross-section value extrapolated from the existing data, thus confirming the accuracy of the normalization.

Three different  $B\bar{B}$  production models have been considered, including the production mechanism predicted by QCD [8], and the production model assumed by the NA10 Collaboration [5]. An analysis of our data using this model leads to a  $B\bar{B}$  cross-section value which is in agreement with the NA10 result. However, an experimental distribution favours the QCD-based production mechanism rather than that assumed by NA10.

Finally the dependence of  $B\bar{B}$  cross-section on the  $B_0 - \bar{B}_0$  mixing parameter ( $\chi_B$ ) has also been investigated, and an upper limit on  $\chi_B$  determined.

## 2. The WA78 detector

The WA78 detector was developed to detect muons coming from decays of  $B\bar{B}$  pairs produced by a 320 GeV  $\pi^-$  beam in a U target:

$$\begin{aligned}
\pi^- + N &\rightarrow B\bar{B} + X \\
B &\rightarrow \mu^+ + \bar{D}(\rightarrow \mu^- + X) + X \\
\bar{B} &\rightarrow \mu^- + D(\rightarrow \mu^+ + X) + X.
\end{aligned}$$

A detailed description of the apparatus has already been published [9]. It consists essentially of a dump calorimeter followed by a magnetic spectrometer. The calorimeter was designed to operate in a 320 GeV beam, at an intensity of  $\sim 6 \times 10^6$   $\pi^-$  per 2.4 s burst, with an energy resolution  $\sigma(E)/E \simeq 0.6/\sqrt{E(\text{GeV})}$ . It was constructed so that it could be easily expanded to vary the mean density  $\rho$ . This enabled us to measure the muon background [6, 7] using the standard  $1/\rho$  extrapolation method.

The spectrometer consists of a 1.5 T superconducting magnet equipped with drift and multiwire proportional chambers, which enabled us to measure the direction and momenta of the muons filtered by the calorimeter dump with a resolution  $\Delta p/p \simeq 6 \times 10^{-4}$   $p$  (GeV/c).

### 3. Trigger and event selection

Owing to the large mass difference between beauty and charm mesons, muons produced by B-meson decay (either directly or via the  $B \rightarrow D \rightarrow \mu$  decay chain) have larger transverse momentum ( $p_T$ ), and are accompanied by more energetic neutrinos than those produced by the background of charm decays. The trigger and event selection procedures were therefore designed to select events with high- $p_T$  muons and large missing energy.

The missing energy ( $E_{\text{miss}}$ ) is calculated by comparing the beam energy ( $E_{\text{beam}}$ ) with the sum of the energy deposited in the calorimeter ( $E_{\text{cal}}$ ) and the energy of the outgoing muons ( $E_\mu$ ) measured in the spectrometer:  $E_{\text{miss}} = E_{\text{beam}} - E_{\text{cal}} - \sum E_\mu$ . The total leptonic energy ( $E_{\text{lept}}$ ) and the total visible energy ( $E_{\text{vis}}$ ) are given by  $E_{\text{lept}} = E_{\text{miss}} + \sum E_\mu$  and  $E_{\text{vis}} = E_{\text{cal}} + \sum E_\mu$ .

The trigger system [9] accepted events with at least two muons in the spectrometer; one muon was required to exit from the calorimeter at a radius greater than 5 cm, to reduce the background of low- $p_T$  events. A second-level trigger required that the calorimeter energy  $E_{\text{cal}}$  be less than 280 GeV. With this trigger  $2.2 \times 10^7$  events were recorded on tape, corresponding to  $5.5 \times 10^{11}$  effective beam interactions. The final data sample analysed here contains 4356 like-sign dimuons and 1582 three-muon events. It is slightly different from that already presented in Refs. [6, 7] since additional cuts have now been applied

which improve the signal-to-background ratio by rejecting beam halo muons and hadron punch-through.

We select as  $\overline{B\overline{B}}$  candidates the like-sign dimuon events with  $E_{\text{vis}} < 300$  GeV,  $p_{\text{Ttot}} (= \sum p_{\text{T}}) > 2.7$  GeV/c, and  $E_{\text{lept}} > 100$  GeV. There are 68 such events, with an expected background of 5.2 events. The three-muon sample contains 11 candidates with  $E_{\text{vis}} < 270$  GeV and  $p_{\text{Ttot}} > 3$  GeV/c, for which the expected background is 1.1 events. The backgrounds were calculated [6, 7] by combining single-muon events taken with a special trigger, either in pairs to produce the like-sign background, or with opposite-sign events to produce the three-muon background.

The track-reconstruction efficiency has been determined by processing Monte Carlo generated events. We estimate this efficiency to be  $(85 \pm 5)\%$  for like-sign or opposite-sign dimuon events and  $(60 \pm 10)\%$  for three-muon events, with little dependence on details of the production model.

#### 4. $J/\psi$ cross-section and normalization

To verify the absolute normalization of the  $\overline{B\overline{B}}$  cross-section we have also measured the  $J/\psi$  inclusive cross-section. The comparison of this result with those already obtained by other experiments using  $\pi^-$  beams provides a useful check on our analysis procedure. For this measurement we collected a sample of  $\sim 6400$  opposite-sign dimuons with a dedicated trigger which does not require any cut on  $E_{\text{cal}}$ . This trigger was activated during one machine burst out of every twenty, so the data for  $J/\psi$  and  $\overline{B\overline{B}}$  were taken during the same experimental runs.

In Fig. 1a we show the experimental effective mass spectrum of the opposite-sign dimuon sample, fitted with a Gaussian plus an exponential distribution to extract the  $J/\psi$  contribution. To reduce the Drell-Yan background, only events with  $2.7 \leq m(\mu^+\mu^-) \leq 4$  GeV/c<sup>2</sup> have been retained. For these  $\sim 2700$  events we show in Figs. 1b and c, respectively, the  $x_{\text{F}}$  distributions of the dimuons and the  $p_{\text{T}}$  distribution of the muons. These two distributions are in quite good agreement with the Monte Carlo predictions shown on the same figures, which have been calculated using the  $x_{\text{F}}$  and  $p_{\text{T}}$  distributions reported by the NA3 Collaboration [10].

The measured inclusive cross-section for  $J/\psi$  production, in the kinematical region  $x_{\text{F}} \geq 0$ , is

$$\text{BR} \times \sigma(\pi^- + \text{U} \rightarrow J/\psi + X) = 1.52 \pm 0.17 \mu\text{b},$$

where  $\text{BR} \simeq 0.069$  is the branching ratio for the decay  $J/\psi \rightarrow \mu^+\mu^-$ . The quoted error is a quadratic combination of the statistical and systematic ones. The normalization is done

using the beam scalers and a total inelastic  $\pi^-U$  cross-section of  $1654 \pm 110$  mb [11]. To compare our value of the  $J/\psi$  inclusive cross-section with the results obtained by other experiments performed with  $\pi^-$  beams, we parametrize the  $J/\psi$  inclusive production cross-section ( $x_F \geq 0$ ) as

$$\sigma(\pi^- + A \rightarrow J/\psi + X) = \sigma_0(\sqrt{s}) \cdot A^\alpha,$$

where  $A$  is the atomic number of the target. In Fig. 2 we plot the values of  $\sigma_0$  as a function of  $\sqrt{s}$ , obtained by different experiments [12]\*), including the present one, assuming  $\alpha = 0.87$  [13]. The curve is a fit to all the points except ours, calculated (apart from a multiplicative factor) using the lowest order QCD formula [15] for  $J/\psi$  inclusive production on an isoscalar target and the partonic, scaling violating, distribution functions for the  $\pi^-$ , given by Owens [16] (set 1). This curve, extrapolated to our value of  $\sqrt{s} = 24.5$  GeV, predicts a value of  $\sigma_0 \simeq 183 \pm 5$  nb, which is in very good agreement with our experimental value of  $\sigma_0 \simeq 189 \pm 21$  nb. If we leave  $\alpha$  as a free parameter of the fit we obtain  $\alpha = 0.90 \pm 0.02$ . In this case the fitting curve extrapolated to our value of  $\sqrt{s}$  predicts  $\sigma_0 = 161 \pm 4$  nb, while our experimental value becomes  $\sigma_0 = 160 \pm 18$  nb which is still in a quite good agreement with the extrapolated one. The quoted errors on  $\sigma_0$  include the statistical and the systematic ones, combined in quadrature.

## 5. $B\bar{B}$ production and decay

A Monte Carlo study of  $B\bar{B}$  production and decay indicates that the acceptance of our experiment is largely determined by the two-dimensional  $x_F$  distribution ( $x_{F1}, x_{F2}$ ) of the  $B$  and  $\bar{B}$ , which results from the assumed production model. We have calculated the inclusive  $B\bar{B}$  cross-section using three different models:

### a ) QCD model

We use a parametrization of the lowest order QCD prediction of the differential cross-section due to Berger [17]:

$$\frac{d^3\sigma}{dx_{F1} dx_{F2} dp_T^2} = \frac{d^2\sigma}{dx_{F1} dx_{F2}} \exp\left(-\frac{p_T^2}{B}\right),$$

where  $x_{F1}$  and  $x_{F2}$  are the Feynman  $x_F$  of the  $b$  and  $\bar{b}$  quark and  $p_T$  their transverse momentum. At our energy the average  $p_T$  value is expected to be [8]  $\langle p_T \rangle \simeq 2.32$  GeV/c, which corresponds to  $B \simeq 6.9$  (GeV/c)<sup>2</sup> in the above formula. The two-dimensional

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\*) Data on hydrogen targets have not been included since the parametrization  $\sigma = \sigma_0 A^\alpha$  does not apply for  $A = 1$  [13, 14].

distribution  $d^2\sigma/dx_{F1} dx_{F2}$  is represented as a scatter plot in Fig. 3a. From this distribution (used directly to evaluate our overall acceptance for  $B\bar{B}$  events) we compute the differential cross-section for production of a single b-quark, and find it can be represented by the formula

$$\frac{d\sigma}{dx_F} \propto \exp\left[-\frac{(x_F - 0.09)^2}{A_\pi^2}\right],$$

with  $A_\pi^2 \simeq 0.3^*$ ). Smearing due to the b-quark fragmentation into physical particles has been folded in with these QCD calculations when generating the parameters of B and  $\bar{B}$  mesons.

b ) Modified QCD model

To show the sensitivity of our results to the mean value of  $x_F$ , we have also investigated a model using the same  $p_T$  distributions as in model (a), but with the  $x_F$  distribution shifted from  $\langle x_F \rangle = 0.09$  to 0.05.

c ) NA10 model

To compare our results with those obtained by the NA10 Collaboration [5], we have calculated our acceptance using the production model assumed by that experiment. According to that model, the  $B\bar{B}$  pair is the sole decay product of an intermediate mass  $M$ , which is centrally produced with a cross-section

$$\frac{d^2\sigma}{dx_F dp_T} \propto (1 - |x_F|)^3 p_T \exp(-2p_T)$$

$$\frac{d\sigma}{dM} \propto \exp[-(M - M_0)^2/(2\delta^2)], \quad (M \geq 2m_B)$$

where  $M_0$  is the mass of the  $\Upsilon'''$  resonance,  $m_B$  is the mass of the B meson, and  $\delta$  is a parameter which depends [18] on the c.m. energy  $\sqrt{s}$ . In Fig. 3b we show, for this production model, the scatter plot  $(x_{F1}, x_{F2})$  of the B and  $\bar{B}$   $x_F$ .

The quite different behaviour of the  $(x_{F1}, x_{F2})$  distributions which are compared with the relative acceptance of our apparatus in Figs. 3a and b, explain why the cross-sections obtained using the QCD or the NA10 model are significantly different, as we will see in the next section.

The B and  $\bar{B}$  decays were simulated using the Lund Monte Carlo [19]. The effective semileptonic branching ratios for B and D decay were 11.6% and 10.4% respectively, when averaged over the different flavours (u, d, s) of the mesons. The slight difference of these

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\*) In Eq. (1) of Ref. [7] the mean value  $\langle x_F \rangle$  of this distribution was erroneously reported to be 0.05 instead of 0.09.

values from those assumed in our previous analysis [6, 7] leads to an increase of the  $B\bar{B}$  cross-section of  $\sim 15\%$  with respect to that reported in Ref. [7].

## 6. Results

In Table 1 we give the  $B\bar{B}$  inclusive cross-sections on nucleon obtained for the three production models considered and for different values of the mixing parameter  $\chi_B$  [20]. A linear  $A$ -dependence of the cross-section has been assumed. Results from like-sign and three-muon samples have been combined. The normalization is done analogously to that of the  $J/\psi$  cross-section, using the beam scalers and the total inelastic  $\pi^-U$  cross-section. The cross-section value for model (a) with  $\chi_B = 0.2$  is  $\sim 55\%$  higher than that already reported in Ref. [7], which was obtained with the same assumptions. This difference is due in part ( $\sim 25\%$ ) to the new absolute normalization of our experiment, in part ( $\sim 15\%$ ) to the different effective branching ratio assumed for the semileptonic B and D decays, and in part ( $\sim 15\%$ ) to a revised version of the Monte Carlo calculations on acceptance and track reconstruction efficiency\*).

The cross-sections obtained using model (c), which have been calculated for  $\chi_B = 0$  and 0.2, are higher by a factor of  $\sim 4$  compared with that of model (a). They range between  $\sim 10$  and  $\sim 20$  nb, and are therefore compatible with the  $14_{-6}^{+7}$  nb reported by the NA10 Collaboration [5]. We conclude that both experiments are in agreement, the difference between their numerical results being due to the different production mechanism assumed in each analysis. In Fig. 4 we compare our experimental  $E_{\text{lept}}$  distribution with those expected from models (a) (QCD) and (b) (NA10). In spite of the limited statistics, we observe a better agreement with model (a). The average value of  $E_{\text{lept}}$  is 177 GeV for model (a) and 163 GeV for model (b), to be compared with  $179 \pm 10$  for the experimental data. This favours our QCD-based  $B\bar{B}$  cross-section values rather than that reported by the NA10 Collaboration [5].

In Ref. [7] an attempt was made to extract the value of the mixing parameter ( $\chi_B$ ) by comparing the cross-sections obtained from the three-muon and like-sign samples. However, using the latest values of the acceptance and taking into account the statistical

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\*) The experimental set-up has been simulated with two independent Monte Carlo calculations. Their results, which agree within  $\pm 6\%$ , have been averaged and taken with a  $\pm 10\%$  systematic error. We found that the acceptance and track reconstruction efficiency used in Ref. [7] were systematically overestimated for the three-muon sample, while those for the like-sign dimuons are practically unchanged.



and systematic uncertainties, no significant determination of  $\chi_B$  can be obtained with this method.

An estimate of  $\chi_B$  can be deduced from the distribution of the like-sign dimuon sample in the  $(p_{T\min}, p_{T\max})$  plane,  $p_{T\min}$  and  $p_{T\max}$  being respectively the minimum and maximum  $p_T$  of the two muons. In the absence of mixing these events come from a B ( $\bar{B}$ ) and a D ( $\bar{D}$ ) decay. If mixing is present, a fraction of these events come directly from the decay of the resulting BB or  $\bar{B}\bar{B}$  pair and therefore have a different  $(p_{T\min}, p_{T\max})$  distribution. A study of dimuon pairs from the three-muon beauty sample suggests that the variable  $F_T = p_{T\min} + 0.4p_{T\max}$  can be used to discriminate efficiently between mixed and unmixed events. A fit to this distribution, and the number of  $\bar{B}\bar{B}$  candidates in the three-muon sample indicates that  $\sim 10\%$  of like-sign detected events decay following  $B_0 - \bar{B}_0$  mixing. At 90% confidence level (CL) this corresponds to an upper limit of  $\chi_B \leq 0.15$ . A comparison of this value with the result on  $B_d$  mixing from  $e^+e^-$  machines cannot be performed since our data sample contains an unknown mixture of  $B_u$ ,  $B_d$ , and  $B_s$  mesons. It is in broad agreement with the upper limit of 0.12 (at 90% CL) reported by MARK II [21] and  $0.121 \pm 0.047$  reported by UA1 [22] for data samples which also contained mixtures of  $B_u$ ,  $B_d$ , and  $B_s$ . Our result is expected to depend on the  $\bar{B}\bar{B}$  production model and in particular on the assumed  $p_T$  distribution. We conclude that our data are consistent with the presence of mixed events, but do not allow us to give an accurate and model-independent value of  $\chi_B$ .

## 7. Conclusions

We have reported final results on the inclusive  $\bar{B}\bar{B}$  production cross-section measured in  $\pi^-U$  interactions at  $\sqrt{s} = 24.5$  GeV. Different  $\bar{B}\bar{B}$  production models and  $B_0 - \bar{B}_0$  mixing parameters have been considered.

With respect to our preliminary results [6, 7] several improvements in data analysis have been performed. In particular, the  $J/\psi$  inclusive cross-section has been measured in our apparatus. The very good agreement of this result with those obtained by other collaborations gives us confidence in the absolute normalization of our experiment.

A comparison with the results obtained by the NA10 Collaboration shows that the higher  $\bar{B}\bar{B}$  cross-section obtained by that experiment is very probably due to the particular production model they assumed. In spite of the limited statistics, our total leptonic energy spectrum shows a better agreement with the prediction of a QCD-based production model than with that of the NA10 model.

Finally, we compare our results [production model (a)] with the theoretical QCD predictions, which are indeterminate by a factor of  $\sim 2$  or more, owing to the choice of

b-quark mass and of evolution scale. Assuming a b-quark mass of 5 GeV the theoretical estimates range from  $\sim 1$  to  $\sim 3$  nb per nucleon in a lowest order calculation [8, 17] and from  $\sim 1.6$  to  $\sim 4.6$  nb per nucleon if next-to-leading QCD corrections are also considered [23]. We conclude that, within the experimental and theoretical uncertainties, QCD describes the main features of the  $B\bar{B}$  hadroproduction, from the present c.m. energy up to that explored at the CERN  $p\bar{p}$  Collider [4].

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**Table 1:** Inclusive  $B\bar{B}$  cross-section for different production models and  $B_0 - \bar{B}_0$  mixing parameters  $\chi_B$  (see text). In column 2 the average  $x_F$  of beauty particles is reported for the three models. The cross-sections, expressed in nb per nucleon, have been calculated assuming a linear  $A$ -dependence. The quoted errors are statistical and systematic respectively, the latter being due to uncertainties on acceptance, track reconstruction efficiency, absolute normalization, and the semileptonic branching ratio of B and D decay.

Production model	$\langle x_F \rangle$	$\chi_B$		
		0	0.1	0.2
a)	0.09	$4.8 \pm 0.6 \pm 1.5$	$3.6 \pm 0.4 \pm 1.1$	$3.1 \pm 0.4 \pm 1$
b)	0.05	$6.2 \pm 0.8 \pm 1.9$	$4.5 \pm 0.6 \pm 1.4$	$3.7 \pm 0.5 \pm 1.1$
c)	0	$18.6 \pm 2.3 \pm 5.5$	-	$11.6 \pm 1.3 \pm 3.5$

## Figure captions

Fig. 1: a): Experimental invariant mass distribution of the opposite-sign dimuons. The  $J/\psi$  signal is obtained by fitting the data with a Gaussian plus an exponential background.

b): Experimental  $x_F$  distribution of the opposite-sign dimuons.

c): Experimental  $p_T$  distribution of each muon of the opposite-sign dimuons.

In (b) and (c) the curves are Monte Carlo predictions, normalized to the data. To reduce the Drell-Yan background, only events with  $2.7 \leq m(\mu^+\mu^-) \leq 4 \text{ GeV}/c^2$  have been retained.

Fig. 2: Comparison of our present result on  $\sigma_0$  for  $J/\psi$  production (see text) with the previous ones obtained with  $\pi^-$  beams at different c.m. energies  $\sqrt{s}$ . Statistical and systematic errors, combined in quadrature, are shown. The curve is a fit to all the points except ours, calculated (apart from a multiplicative factor) using the lowest order QCD formula for  $J/\psi$  inclusive production. The quite good agreement of our results with this fit confirms the accuracy of our overall normalization.

Fig. 3: Two-dimensional distribution of the Feynman  $x_F$  of the produced beauty particles: a) in the QCD model; b) in the NA10 model. The inner (outer) solid line encloses the region where the acceptance of our experiments is greater than 50% (10%) of its maximum value.

Fig. 4: Experimental distribution of the leptonic energy ( $E_{\text{lept}}$ ) compared with the prediction of the QCD model (curve a) and NA10 model (curve b).

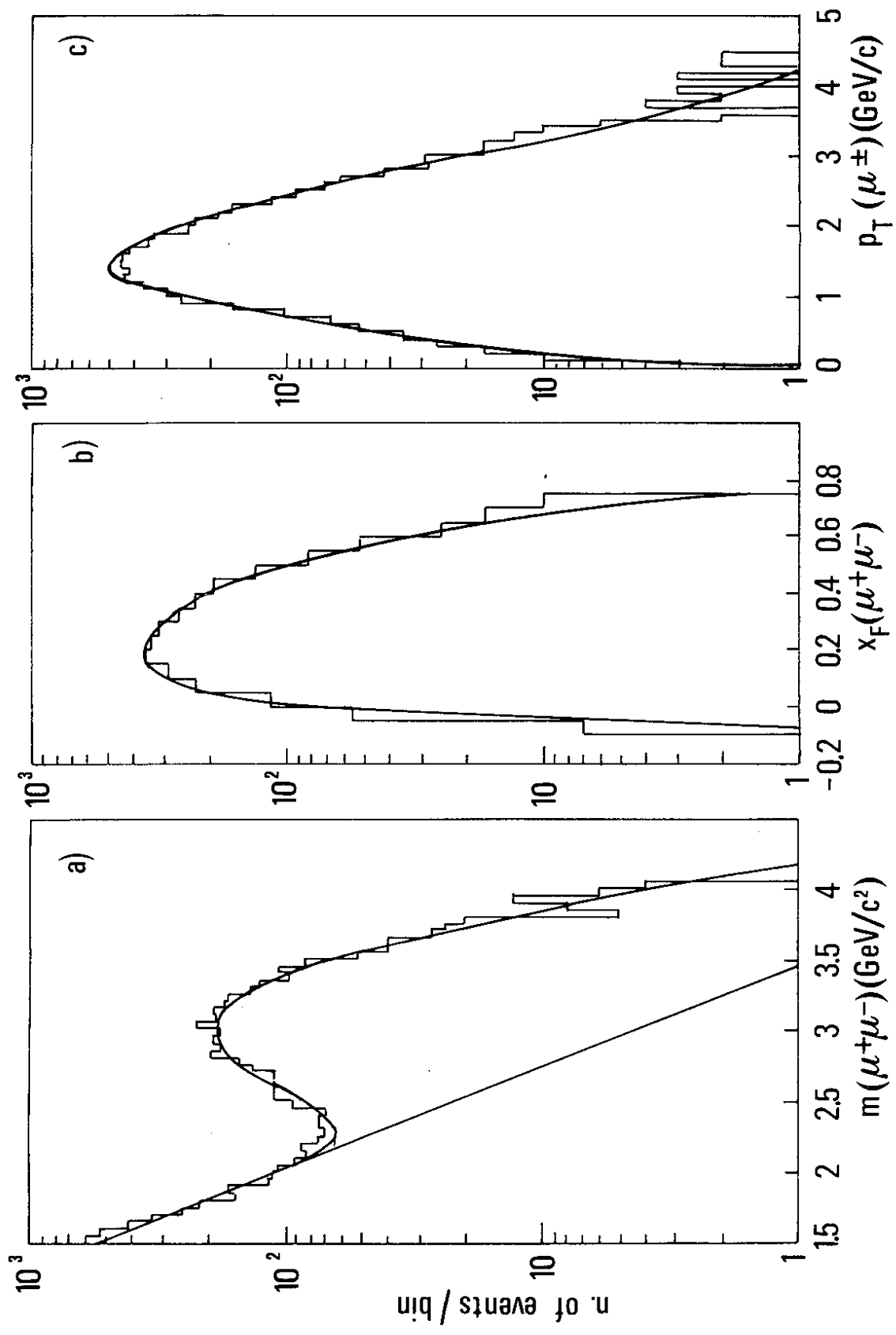


Fig. 1

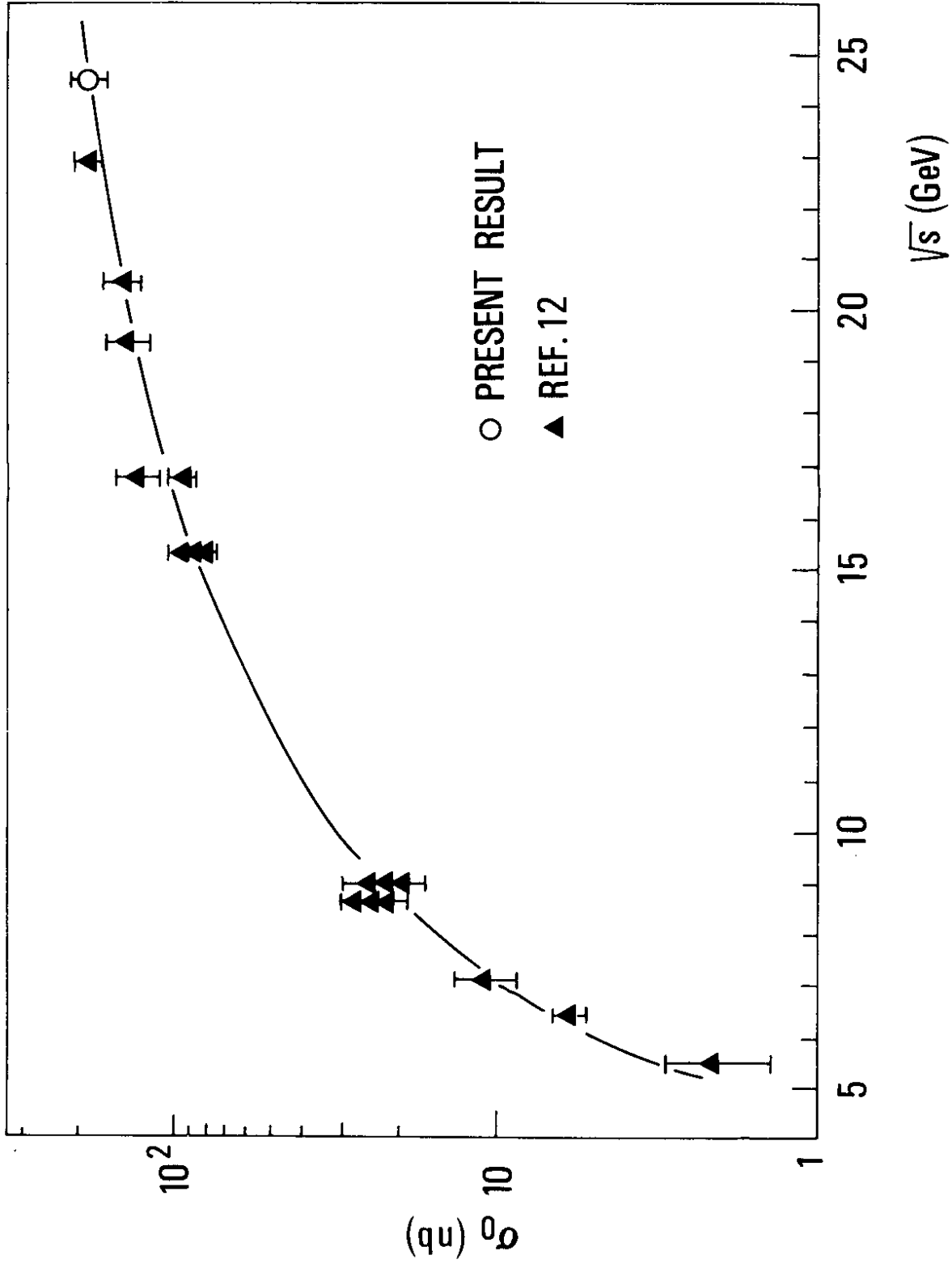


Fig. 2

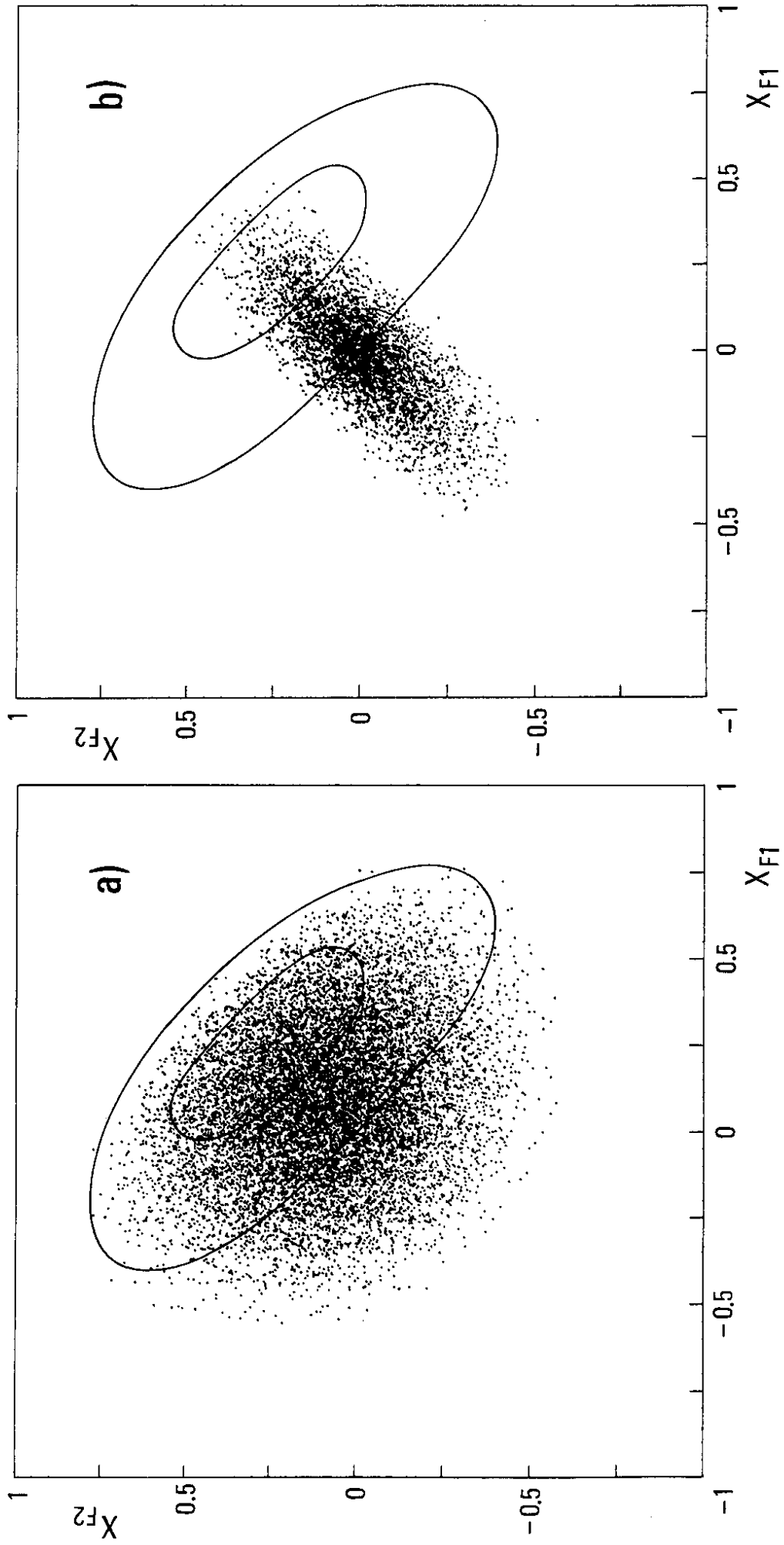


Fig. 3



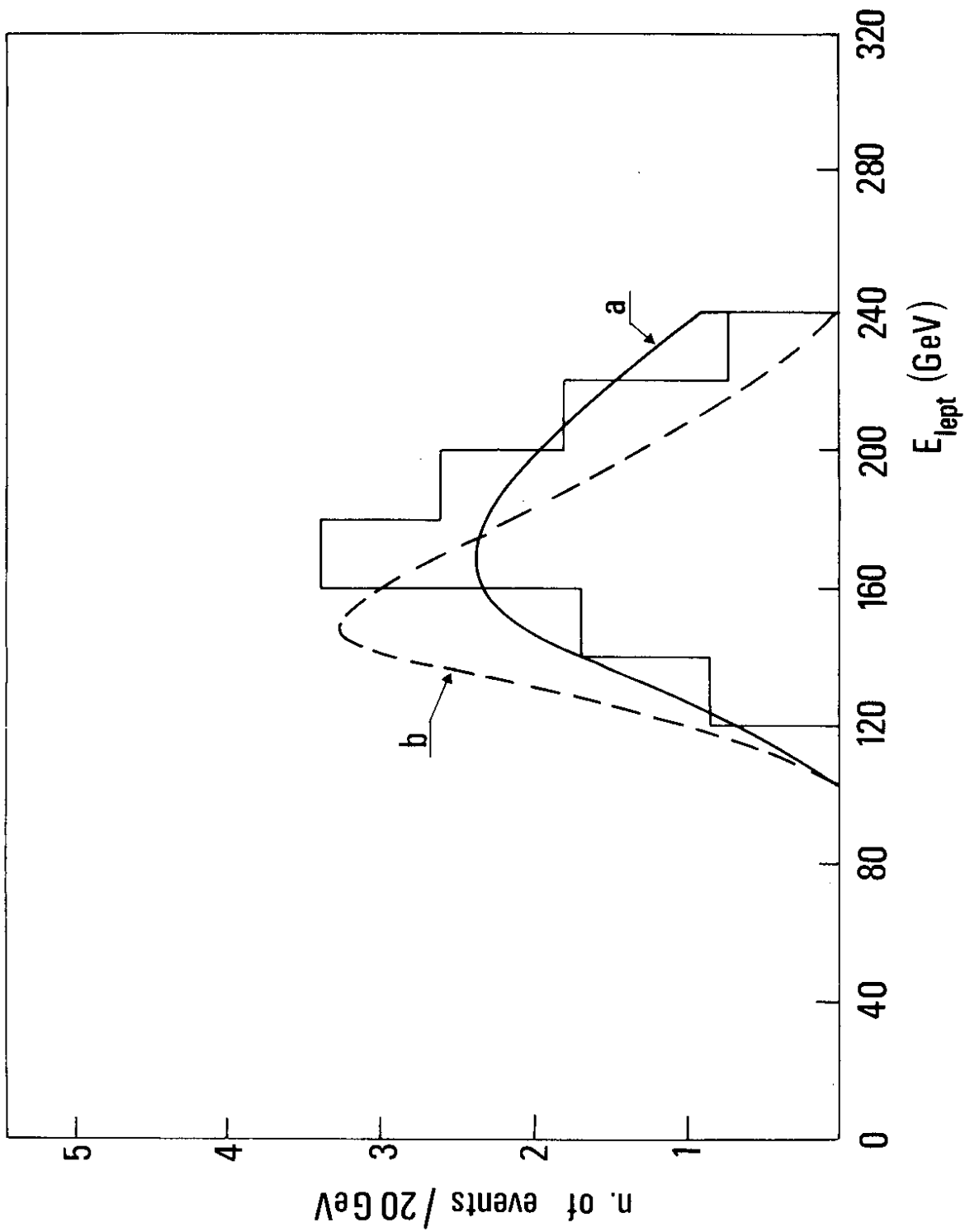


Fig. 4