



THE EFFECT OF PRESSURE ON THE POSITIVE MUON SPIN PRECESSION  
IN IRON AND NICKEL

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ABSTRACT

We have determined the pressure dependence of the local magnetic fields at  $\mu^+$  sites to be

$$\left( \frac{\partial \ln B}{\partial P} \right)_{298 \text{ K}} = \begin{cases} -1.05(2) \times 10^{-3} / \text{kbar} & \text{for Fe} \\ +0.43(6) \times 10^{-3} / \text{kbar} & \text{for Ni} . \end{cases}$$

The dependence on temperature (also measured here) is discussed on the basis of these results.

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Dear Mr. [Name],

I have your letter of [Date] regarding [Subject].

I am sorry that I cannot give you a more definite answer at this time.

I will be glad to discuss this matter further with you if you wish.

Sincerely,  
[Name]

I have your letter of [Date] regarding [Subject].

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Sincerely,  
[Name]

The hyperfine field  $B_{\text{hf}}$  at positive muon sites in iron and nickel exhibits marked deviations from the bulk magnetization  $M$  as a function of temperature [1-3]. Similar deviations have also been found for light interstitial impurities in Fe and Ni [4,5] as well as for heavier sp-impurities at substitutional sites in Fe, Co and Ni matrices [6,7]. Such deviations can partly be attributed to volume expansion effects, i.e. the change of the lattice parameter due to thermal expansion affects  $B_{\text{hf}}(T)$  and  $M(T)$  in a different manner. The volume dependence of  $B_{\text{hf}}$  can be determined by pressure experiments. For Cd and Sn in nickel and Sn in iron the pressure dependence of  $B_{\text{hf}}$  does not follow that of the magnetization [8-10]. In connection with our efforts to understand the origin of  $B_{\text{hf}}(\mu^+)$  in magnetic metals, we have now followed the local magnetic field at muon sites in high-purity polycrystalline Fe and Ni at 298 K and at hydrostatic pressures up to 7 kbars by the muon spin precession technique. We have also measured the temperature dependence of  $B_{\text{hf}}$  below 300 K with the same high-purity Fe and Ni to confirm earlier results [1-3].

The experiments were performed in a polarized muon beam from the 600 MeV Synchro-cyclotron (SC) at CERN. A pressure cell made of copper-beryllium, with two cavities ( $\emptyset 7 \times 50$  mm) and minimum 7 mm wall thickness, was used with an oil-kerosene mixture as the pressure-transmitting medium. The pressure was generated by a 7 kbar handpump (Nova Swiss) and measured with a Heise Bourdon tube gauge, claimed by the manufacturer to have an accuracy of  $\pm 0.01$  kar. No polarizing magnetic field was used. The data were fitted to the expression

$$N(t) = N_0 \exp \left[ -t/\tau_{\mu} \right] \left[ 1 + \sum_i a_i \exp (-\lambda_i t) \cos (2\pi\nu_i t + \phi_i) \right]. \quad (1)$$

The low-temperature experiments were performed with a continuous-flow  $^4\text{He}$  cryostat. The temperature was measured with calibrated platinum and carbon resistors. The zone-refined Fe and Ni samples are described elsewhere [11]. The muon precession frequency in nickel at 298 K and ambient pressure was found to be 18.416(3) MHz, corresponding to a field at the muon of 0.13587 T in good agreement with other experiments [3,12]. For iron under the same conditions, a precession frequency of 48.665(5) MHz was found, corresponding to 0.35905 T, also in good

agreement with recent experiments [12,13]. The linewidths found at 298 K were  $\lambda_{\text{Fe}} = 0.24(4) \mu\text{s}^{-1}$ ,  $\lambda_{\text{Ni}} = 0.25(3) \mu\text{s}^{-1}$ , verifying the high purity of the samples. The nickel linewidth remains constant at this low value down to 2 K.

The measured magnetic fields at 298 K and at different pressures were fitted to a straight line (fig. 1). The slopes yield

$$\frac{\partial \ln B_{\mu}}{\partial p} = \begin{cases} -1.05(2) \times 10^{-3}/\text{kbar} & \text{for Fe} \\ +0.43(6) \times 10^{-3}/\text{kbar} & \text{for Ni} . \end{cases}$$

The total local field  $B_{\mu}$  at the muon is given by

$$B_{\mu} = B_{\text{hf}} + B_{\text{L}} + B_{\text{dip}} , \quad (2)$$

where  $B_{\text{L}}$  is the Lorentz field (298 K, Fe: 0.715 T and Ni: 0.203 T) and  $B_{\text{dip}}$  denotes the dipolar field;  $B_{\text{dip}}$  is zero for Ni because the  $\mu^{+}$  interstitial site has cubic symmetry. For Fe at room temperature,  $B_{\text{dip}}$  is considered to be averaged to zero owing to the rapid muon diffusion [14]. In order to obtain the relative change of  $B_{\text{hf}}$  with volume, the variation of  $B_{\text{L}} = (4\pi/3)M$  with volume is required, i.e. the pressure-dependence of the host magnetization  $M_0$  at  $T = 0$  as well as a change in the Curie temperature  $T_{\text{C}}$  must be considered. The change in  $T_{\text{C}}$  for Ni is:  $dT_{\text{C}}/dp = +0.32 \text{ K/kbar}$ , and for Fe  $\sim 0$  [15]. Different values on the pressure dependence of  $M_0$  at  $T = 0$  have been reported for Ni [16-18]. We use the value  $\partial \ln M_0/\partial p = -0.28 \times 10^{-3}/\text{kbar}$ , and with knowledge of the slope of  $M(T)$  at 298 K and the change in  $T_{\text{C}}$  we derive the total pressure dependence of the magnetization in Ni at 298 K to be  $\partial \ln M/\partial p = -0.20 \times 10^{-3}/\text{kbar}$ . This is also in agreement with the value at 293 K quoted by Bloch and Pauthenet [19]. For Fe we use the value  $\partial \ln M/\partial p = -0.28 \times 10^{-3}/\text{kbar}$  [16]. With the compressibilities of Fe,  $\partial \ln V/\partial p = -0.59 \times 10^{-3}/\text{kbar}$ , and of Ni,  $\partial \ln V/\partial p = -0.54 \times 10^{-3}/\text{kbar}$  [20], we deduce:

$$\frac{\partial \ln B_{\text{hf}}}{\partial \ln V} = \begin{cases} -0.92(1) & \text{for Fe} \\ +4.0 (2) & \text{for Ni} . \end{cases} \quad (3)$$

The uncertainties of  $\partial \ln M/\partial p$  and  $\partial \ln V/\partial p$  have not been included in the errors given, but we estimate that they increase them by a factor of 2 or 3.

Conventionally one writes [21]

$$B_{\text{hf}} = -\frac{8\pi}{3} \mu_{\text{B}} \eta(0) (n_0^{\uparrow} - n_0^{\downarrow}) , \quad (4)$$

where  $(n_0^\uparrow - n_0^\downarrow)$  denotes the spin density at the muon site of the unperturbed system and  $\eta(0)$  is the spin-density enhancement factor (SDEF) which accounts for the perturbation of the conduction electron polarization by presence of the muon. If we assume that  $(n_0^\uparrow - n_0^\downarrow)$  is proportional to the bulk magnetization, we obtain a contribution of 0.47 (Fe) and 0.37 (Ni) to  $\partial \ln B_{\text{hf}}/\partial \ln V$ , to which about 0.3 should be added due to the volume dependence of  $\eta(0)$  (estimated from fig. 3, ref. 21). This adds up to  $\partial \ln B_{\text{hf}}/\partial \ln V \approx +0.8$  for Fe  $\approx +0.7$  for Ni. While the Fe value agrees satisfactorily with the experimental value of +0.92, the Ni value of +4.0 cannot be explained within this approach. This discrepancy becomes even worse if it is assumed, as in Jena's theory [21], that the s-band has a very small polarization (which makes its spin density enhancement unimportant) and that most of the spin density arises from the d-band polarization (with a small SDEF [21,22]). In such a model, a strong radial dependence of the d-electron polarization would be required to explain our data. Furthermore, this model [21] cannot predict the absolute values for  $B_{\text{hf}}$  in Ni.

In Fig. 2 we present the temperature dependence, at ambient pressure, of the muon spin precession frequency, normalized to lowest temperature [Fe: 52.13(6) MHz, Ni: 20.253(3) MHz]. Using eq. (2) and assuming that  $B_{\text{hf}}(T)$  can be expressed as  $B_{\text{hf}}(T) = B_{\text{hf}}(0) A(T) M(T)/M_0$ , we calculate the deviation from the bulk magnetization  $M(T)$  [23]. The result is shown in Fig. 3. It should be pointed out that for Ni about half of the slope of 300 K can be explained by the volume dependence of  $B_{\text{hf}}$  and thermal expansion. This clearly shows the importance of information on the volume dependence of  $B_{\text{hf}}$  for interpreting the temperature dependence. Moreover, it brings the theoretical predictions by Katayama et al. [24] (shown by the solid line in Fig. 3) much closer to the experimental results. The calculations of Katayama et al. are of an *ab initio* type, using "muffin-tin" potentials. The local spin density follows from the hybridization of 1s electrons on the  $\mu^+$  sites (assumed to be octahedral) and d-electron states from nickel.

However, for Fe the volume dependence of  $B_{\text{hf}}$  is too small -- and, above all, of opposite sign -- to bridge the gap between  $B_{\text{hf}}(T)$  and  $M(T)$ . So far no calculations of the type reported in ref. [24] exist for muons in this metal.

We hope that our results will stimulate further theoretical efforts on the calculation of muon hyperfine fields, especially using cluster methods [25], which seem to be successful in explaining  $B_{\text{hf}}$  in transition metals.

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Figure captions

- Fig. 1 : Normalized local field values at different pressures P. The solid lines are results from straight line fits.
- Fig. 2 : The temperature dependence of the spin precession frequencies in Fe and Ni, normalized to lowest temperature. The solid lines represent  $M(T)$ .
- Fig. 3 : The temperature dependence of  $A(T)$  defined by  $B_{\text{hf}}(T) = B(0) A(T) M(T)/M_0$ . The theoretical prediction (solid line) is taken from ref. 24.



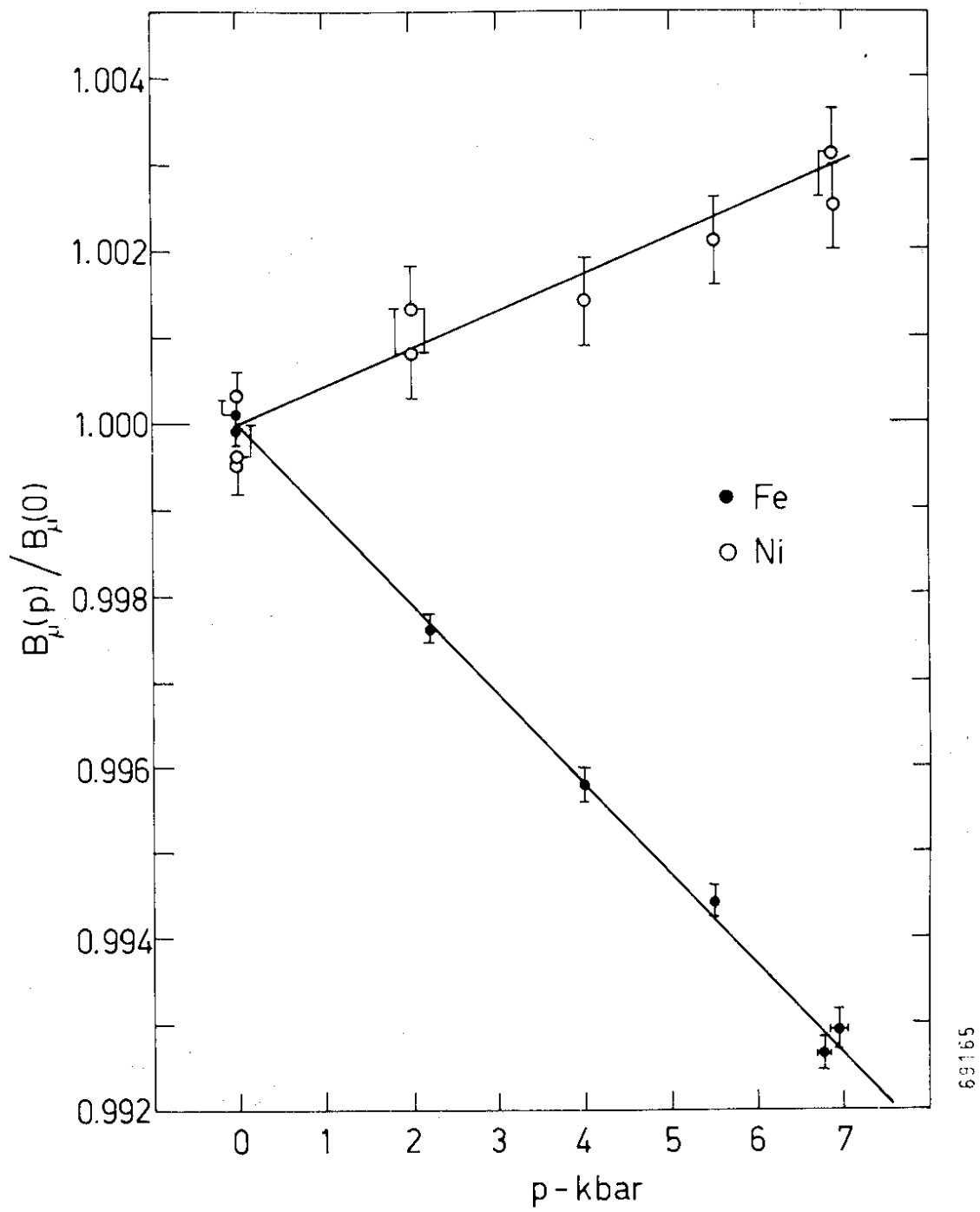


Fig. 1

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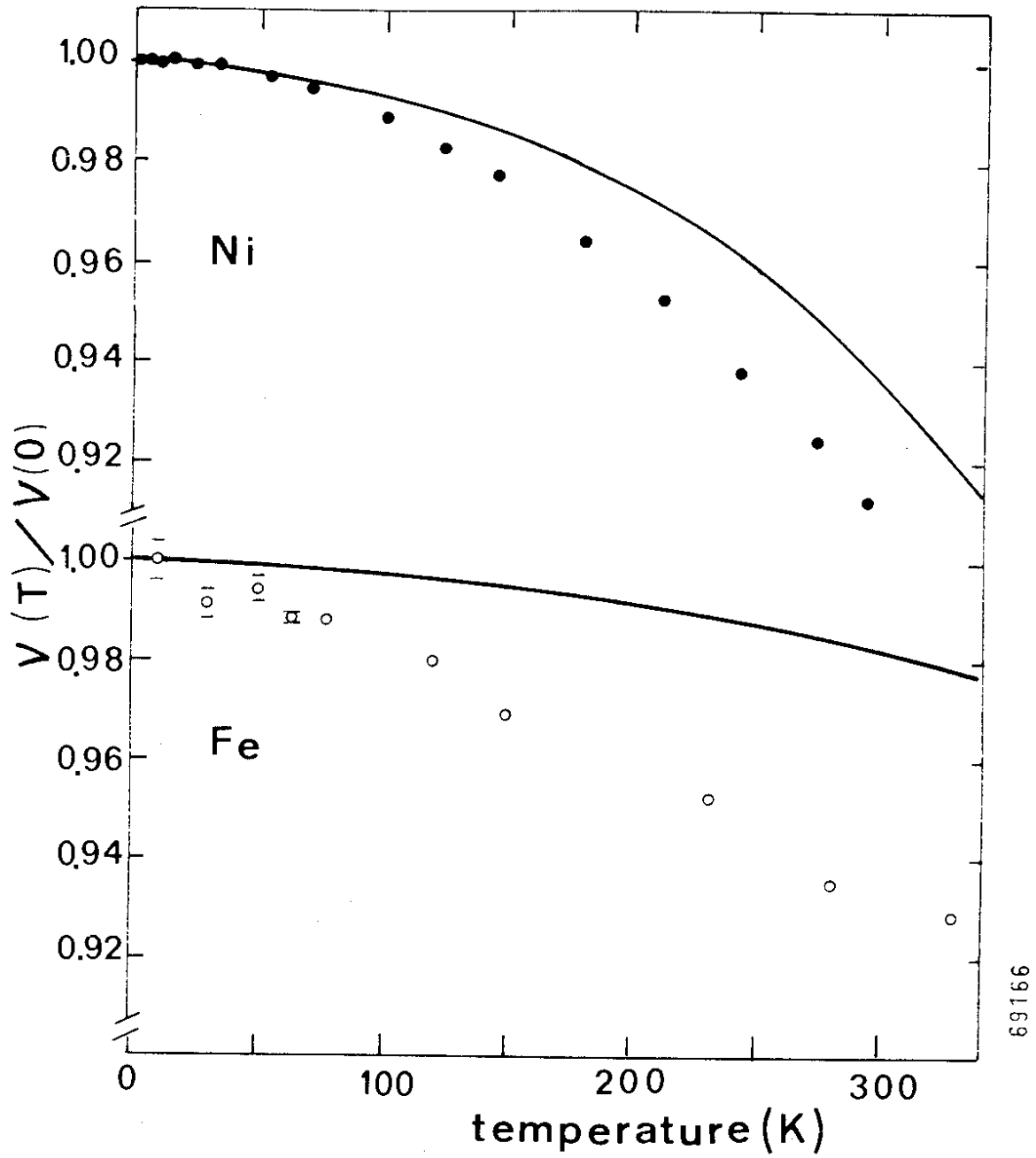


Fig. 2

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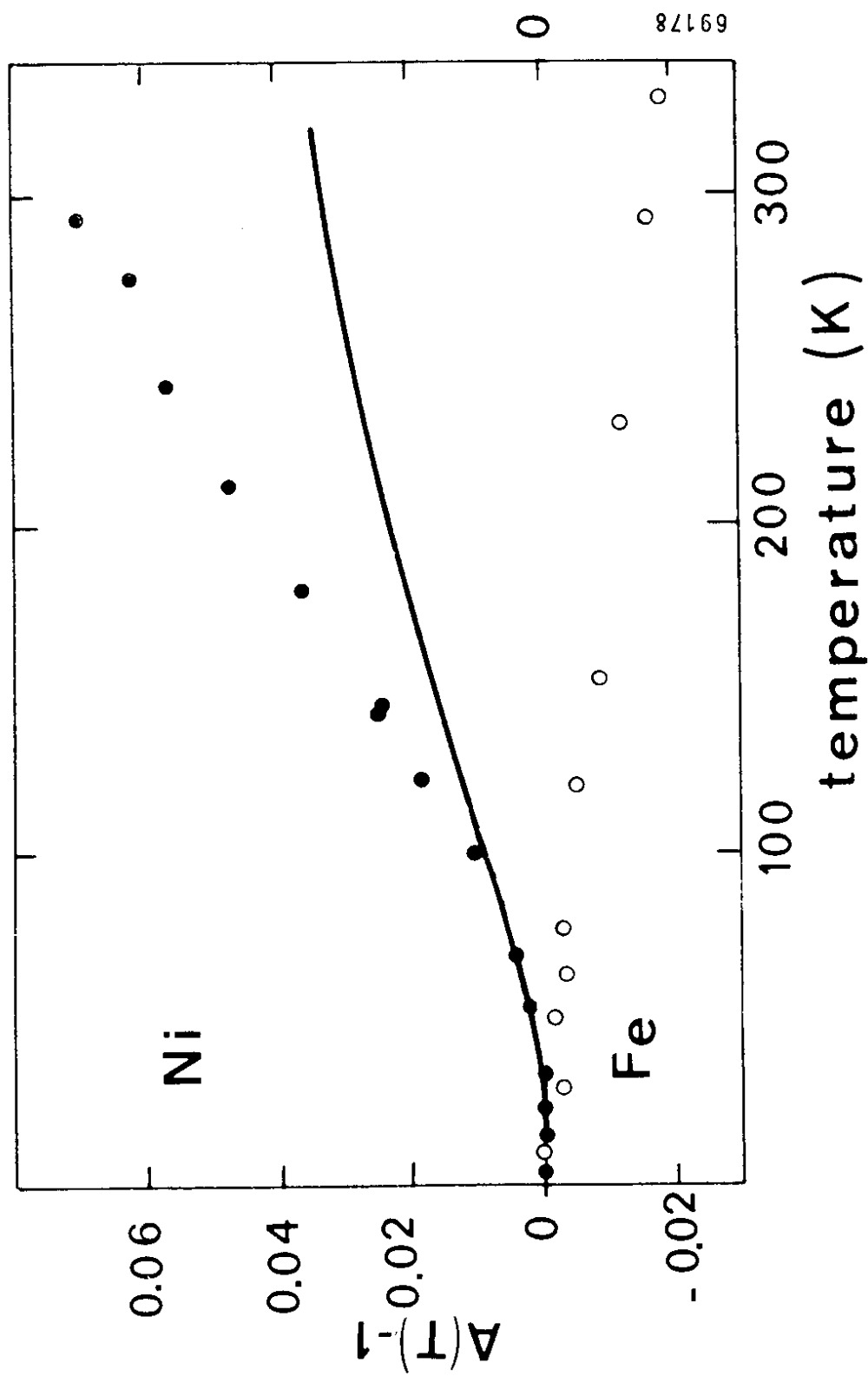


Fig. 3

